
TeNPy

Release 0.7.1

TeNPy Developers

Sep 04, 2020

USER GUIDE

1	How do I get set up?	3
2	How to read the documentation	5
3	Help - I looked at the documentation, but I don't understand how ...?	7
4	I found a bug	9
5	Citing TeNPy	11
6	Acknowledgment	13
7	License	15
7.1	Installation instructions	15
7.2	Release Notes	34
7.3	Introductions	47
7.4	Literature	125
7.5	Contributing	126
7.6	Tenpy main module	131
7.7	algorithms	132
7.8	linalg	196
7.9	models	275
7.10	networks	473
7.11	tools	547
7.12	version	589
8	Indices and tables	591
	Bibliography	593
	Python Module Index	597
	Config Index	599
	Config Option Index	601
	Index	633

TeNPy (short for ‘Tensor Network Python’) is a Python library for the simulation of strongly correlated quantum systems with tensor networks.

The philosophy of this library is to get a new balance of a good readability and usability for new-comers, and at the same time powerful algorithms and fast development of new algorithms for experts. For good readability, we include an extensive documentation next to the code, both in Python doc strings and separately as *user guides*, as well as simple example codes and even toy codes, which just demonstrate various algorithms (like TEBD and DMRG) in ~100 lines per file.

HOW DO I GET SET UP?

If you have the *conda* package manager, you can install the latest released version of TeNPy with:

```
conda install --channel=conda-forge physics-tenpy
```

Further details and alternative methods can be found the file [doc/INSTALL.rst](#). The latest version of the source code can be obtained from <https://github.com/tenpy/tenpy>.

HOW TO READ THE DOCUMENTATION

The **documentation is available online** at <https://tenpy.readthedocs.io/>. The documentation is roughly split in two parts: on one hand the full “reference” containing the documentation of all functions, classes, methods, etc., and on the other hand the “user guide” containing some introductions and additional explanations.

The documentation is based on Python’s docstrings, and some additional `*.rst` files located in the folder `doc/` of the repository. All documentation is formatted as `reStructuredText`, which means it is quite readable in the source plain text, but can also be converted to other formats. If you like it simple, you can just use interactive python `help()`, Python IDEs of your choice or jupyter notebooks, or just read the source. Moreover, the documentation gets converted into HTML using `Sphinx`, and is made available online at <https://tenpy.readthedocs.io/>. The big advantages of the (online) HTML documentation are a lot of cross-links between different functions, and even a search function. If you prefer yet another format, you can try to build the documentation yourself, as described in `doc/contr/build_doc.rst`.

HELP - I LOOKED AT THE DOCUMENTATION, BUT I DON'T UNDERSTAND HOW ... ?

We have set up a **community forum** at <https://tenpy.johannes-hauschild.de/>, where you can post questions and hopefully find answers. Once you got some experience with TeNPy, you might also be able to contribute to the community and answer some questions yourself ;-) We also use this forum for official announcements, for example when we release a new version.

I FOUND A BUG

You might want to check the [github issues](#), if someone else already reported the same problem. To report a new bug, just [open a new issue](#) on github. If you already know how to fix it, you can just create a pull request :) If you are not sure whether your problem is a bug or a feature, you can also ask for help in the [TeNPy forum](#).

CITING TENPY

When you use TeNPy for a work published in an academic journal, you can cite [this paper](#) to acknowledge the work put into the development of TeNPy. (The license of TeNPy does not force you, however.) For example, you could add the sentence "Calculations were performed using the TeNPy Library (version X.X.X) \cite{tenpy} ." in the acknowledgements or in the main text.

The corresponding BibTeX Entry would be the following (the `\url{...}` requires `\usepackage{hyperref}` in the LaTeX preamble.):

```
@Article{tenpy,
  title={{Efficient numerical simulations with Tensor Networks: Tensor Network_
↪Python (TeNPy)}},
  author={Johannes Hauschild and Frank Pollmann},
  journal={SciPost Phys. Lect. Notes},
  pages={5},
  year={2018},
  publisher={SciPost},
  doi={10.21468/SciPostPhysLectNotes.5},
  url={https://scipost.org/10.21468/SciPostPhysLectNotes.5},
  archiveprefix={arXiv},
  eprint={1805.00055},
  note={Code available from \url{https://github.com/tenpy/tenpy}},
}
```


ACKNOWLEDGMENT

This work was funded by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences, Materials Sciences and Engineering Division under Contract No. DE-AC02-05-CH11231 through the Scientific Discovery through Advanced Computing (SciDAC) program (KC23DAC Topological and Correlated Matter via Tensor Networks and Quantum Monte Carlo).

LICENSE

The code is licensed under GPL-v3.0 given in the file `LICENSE` of the repository, in the online documentation readable at <https://tenpy.readthedocs.io/en/latest/install/license.html>.

7.1 Installation instructions

With the `[conda]` package manager you can install python with:

```
conda install --channel=conda-forge physics-tenpy
```

More details and tricks in *Installation with conda from conda-forge*.

If you don't have conda, but you have `[pip]`, you can:

```
pip install physics-tenpy
```

More details for this method can be found in *Installation from PyPi with pip*.

We also have a bunch of optional *Extra requirements*, which you don't have to install to use TeNPy, but you might want to.

The method with the minimal requirements is to just download the source and adjust the `PYTHONPATH`, as described in *Installation from source*. This is also the recommended way if you plan to modify parts of the source.

7.1.1 Installation with conda from conda-forge

We provide a package for the `[conda]` package manager in the *conda-forge* channel, so you can install TeNPy as:

```
conda install --channel=conda-forge physics-tenpy
```

Following the recommendation of *conda-forge*, you can also make conda-forge the default channel as follows:

```
conda config --add channels conda-forge
conda config --set channel_priority strict
```

If you have done this, you don't need to specify the `--channel=conda-forge` explicitly.

Moreover, it is actually recommended to create a separate environment. To create a conda environment with the name *tenpy*, where the TeNPy package (called *physics-tenpy*) is installed:

```
conda create --name tenpy --channel=conda-forge physics-tenpy
```

In that case, you need to activate the environment each time you want to use the package with:

```
conda activate tenpy
```

The big advantage of this approach is that it allows multiple version of software to be installed in parallel, e.g., if one of your projects requires `python>=3.8` and another one requires an old library which doesn't support that. Further info can be found in the [conda documentation](#).

7.1.2 Installation from PyPi with pip

Preparation: install requirements

If you have the `[conda]` package manager from [anaconda](#), you can just download the `environment.yml` file out of the repository and create a new environment (called `tenpy`, if you don't specify another name) for TeNPy with all the required packages:

```
conda env create -f environment.yml
conda activate tenpy
```

Further information on conda environments can be found in the [conda documentation](#). Note that installing conda also installs a version of `[pip]`.

Alternatively, if you only have `[pip]` (and not `[conda]`), install the required packages with the following command (after downloading the `requirements.txt` file from the repository):

```
pip install -r requirements.txt
```

Note: Make sure that the `pip` you call corresponds to the python version you want to use. (One way to ensure this is to use `python -m pip` instead of a simple `pip`.) Also, you might need to use the argument `--user` to install the packages to your home directory, if you don't have `sudo` rights. (Using `--user` with conda's `pip` is discouraged, though.)

Warning: It might just be a temporary problem, but I found that the `pip` version of `numpy` is incompatible with the python distribution of `anaconda`. If you have installed the `intelpython` or `anaconda` distribution, use the `conda` `packagemanager` instead of `pip` for updating the packages whenever possible!

Installing the latest stable TeNPy package

Now we are ready to install TeNPy. It should be as easy as (note the different package name - 'tenpy' was taken!)

```
pip install physics-tenpy
```

Note: If the installation fails, don't give up yet. In the minimal version, `tenpy` requires only pure Python with somewhat up-to-date NumPy and SciPy. See [Installation from source](#).

Installation of the latest version from Github

To get the latest development version from the github master branch, you can use:

```
pip install git+git://github.com/tenpy/tenpy.git
```

This should already have the latest features described in [\[latest\]](#). Disclaimer: this might sometimes be broken, although we do our best to keep it stable as well.

Installation from the downloaded source folder

Finally, if you downloaded the source and want to **modify parts of the source**, You can also install TeNPy with in development version with `--editable`:

```
cd $HOME/tenpy # after downloading the source, got to the repository
pip install --editable .
```

Uninstalling a pip-installed version

In all of the above cases, you can uninstall tenpy with:

```
pip uninstall physics-tenpy
```

7.1.3 Updating to a new version

Before you update, take a look at the [Release Notes](#), which lists the changes, fixes, and new stuff. Most importantly, it has a section on *backwards incompatible changes* (i.e., changes which may break your existing code) along with information how to fix it. Of course, we try to avoid introducing such incompatible changes, but sometimes, there's no way around them. If you skip some intermediate version(s) for the update, read also the release notes of those!

How to update depends a little bit on the way you installed TeNPy. Of course, you have always the option to just remove the TeNPy files (possibly with a `pip uninstall physics-tenpy`), and to start over with downloading and installing the newest version.

When installed with *pip*

When you installed TeNPy with [\[pip\]](#), you just need to do a

```
pip install --upgrade physics-tenpy
```

When installed from source

If you used `git clone ...` to download the repository, you can update to the newest version using [\[git\]](#). First, briefly check that you didn't change anything you need to keep with `git status`. Then, do a `git pull` to download (and possibly merge) the newest commit from the repository.

Note: If some Cython file (ending in `.pyx`) got renamed/removed (e.g., when updating from v0.3.0 to v0.4.0), you first need to remove the corresponding binary files. You can do so with the command `bash cleanup.sh`.

Furthermore, whenever one of the cython files (ending in .pyx) changed, you need to re-compile it. To do that, simply call the command `bash ./compile` again. If you are unsure whether a cython file changed, compiling again doesn't hurt.

To summarize, you need to execute the following bash commands in the repository:

```
# 0) make a backup of the whole folder
git status    # check the output whether you modified some files
git pull
bash ./cleanup.sh  # (confirm with 'y')
bash ./compile.sh
```

7.1.4 Installation from source

Minimal Requirements

This code works with a minimal requirement of pure Python ≥ 3.5 and somewhat recent versions of NumPy and SciPy.

Getting the source

The following instructions are for (some kind of) Linux, and tested on Ubuntu. However, the code itself should work on other operating systems as well (in particular MacOS and Windows).

The official repository is at <https://github.com/tenpy/tenpy.git>. To get the latest version of the code, you can clone it with [git] using the following commands:

```
git clone https://github.com/tenpy/tenpy.git $HOME/TeNPy
cd $HOME/TeNPy
```

Note: Adjust \$HOME/TeNPy to the path wherever you want to save the library.

Optionally, if you don't want to contribute, you can checkout the latest stable release:

```
git tag    # this prints the available version tags
git checkout v0.3.0 # or whatever is the latest stable version
```

Note: In case you don't have [git] installed, you can download the repository as a ZIP archive. You can find it under [releases](#), or the [latest development version](#).

Minimal installation: Including tenpy into PYTHONPATH

The python source is in the directory `tenpy/` of the repository. This folder `tenpy/` should be placed in (one of the folders of) the environment variable `PYTHONPATH`. On Linux, you can simply do this with the following line in the terminal:

```
export PYTHONPATH=$HOME/TeNPy
```

(If you have already a path in this variable, separate the paths with a colon `:`.) However, if you enter this in the terminal, it will only be temporary for the terminal session where you entered it. To make it permanently, you can add

the above line to the file `$HOME/.bashrc`. You might need to restart the terminal session or need to relogin to force a reload of the `~/.bashrc`.

Whenever the path is set, you should be able to use the library from within python:

```
>>> import tenpy
/home/username/TenPy/tenpy/tools/optimization.py:276: UserWarning: Couldn't load_
↳compiled cython code. Code will run a bit slower.
  warnings.warn("Couldn't load compiled cython code. Code will run a bit slower.")
>>> tenpy.show_config()
tenpy 0.4.0.dev0+7706003 (not compiled),
git revision 77060034a9fa64d2c7c16b4211e130cf5b6f5272 using
python 3.7.3 (default, Mar 27 2019, 22:11:17)
[GCC 7.3.0]
numpy 1.16.3, scipy 1.2.1
```

`tenpy.show_config()` prints the current version of the used TeNPy library as well as the versions of the used python, numpy and scipy libraries, which might be different on your computer. It is a good idea to save this data (given as string in `tenpy.version.version_summary` along with your data to allow to reproduce your results exactly.

If you got a similar output as above: congratulations! You can now run the codes :)

Compilation of np_conserved

At the heart of the TeNPy library is the module `tenpy.linalg.np_conserved`, which provides an Array class to exploit the conservation of abelian charges. The data model of python is not ideal for the required book-keeping, thus we have implemented the same `np_conserved` module in [Cython](#). This allows to compile (and thereby optimize) the corresponding python module, thereby speeding up the execution of the code. While this might give a significant speed-up for code with small matrix dimensions, don't expect the same speed-up in cases where most of the CPU-time is already spent in matrix multiplications (i.e. if the bond dimension of your MPS is huge).

To compile the code, you first need to install [Cython](#)

```
conda install cython          # when using anaconda, or
pip install --upgrade Cython  # when using pip
```

Moreover, you need a C++ compiler. For example, on Ubuntu you can install `sudo apt-get install build_essential`, or on Windows you can download MS Visual Studio 2015. If you use anaconda, you can also use `conda install -c conda-forge cxx-compiler`.

After that, go to the root directory of TeNPy (`$HOME/TenPy`) and simply run

```
bash ./compile.sh
```

Note that it is not required to separately download (and install) Intel MKL: the compilation just obtains the includes from numpy. In other words, if your current numpy version uses MKL (as the one provided by anaconda), the compiled TeNPy code will also use it.

After a successful compilation, the warning that TeNPy was not compiled should go away:

```
>>> import tenpy
>>> tenpy.show_config()
tenpy 0.4.0.dev0+b60bad3 (compiled from git rev.↳
↳b60bad3243b7e54f549f4f7c1f074dc55bb54ba3),
git revision b60bad3243b7e54f549f4f7c1f074dc55bb54ba3 using
python 3.7.3 (default, Mar 27 2019, 22:11:17)
```

(continues on next page)

(continued from previous page)

```
[GCC 7.3.0]
numpy 1.16.3, scipy 1.2.1
```

Note: For further optimization options, look at `tenpy.tools.optimization`.

7.1.5 Extra requirements

We have some extra requirements that you don't need to install to use TeNPy, but that you might find useful to work with. TeNPy does not import the following libraries (at least not globally), but some functions might expect arguments behaving like objects from these libraries.

Note: If you created a [conda] environment with `conda env create -f environment.yml`, all the extra requirements below should already be installed :) (However, `pip install -r requirements.txt` does not install them.)

Matplotlib

The first extra requirement is the [matplotlib] plotting library. Some functions expect a `matplotlib.axes.Axes` instance as argument to plot some data for visualization.

Intel's Math Kernel Library (MKL)

If you want to run larger simulations, we recommend the use of Intel's MKL. It ships with a Lapack library, and uses optimization for Intel CPUs. Moreover, it uses parallelization of the LAPACK/BLAS routines, which makes execution much faster. As of now, the library itself supports no other way of parallelization.

If you don't have a python version which is built against MKL, we recommend using [conda] or directly [intelpython](#). Conda has the advantage that it allows to use different environments for different projects. Both are available for Linux, Mac and Windows; note that you don't even need administrator rights to install it on linux. Simply follow the (straight-forward) instructions of the web page for the installation. After a successful installation, if you run `python` interactively, the first output line should state the python version and contain `Anaconda` or `Intel Corporation`, respectively.

If you have a working conda package manager, you can install the numpy build against mkl with:

```
conda install mkl numpy scipy
```

Note: MKL uses different threads to parallelize various BLAS and LAPACK routines. If you run the code on a cluster, make sure that you specify the number of used cores/threads correctly. By default, MKL uses all the available CPUs, which might be in stark contrast than what you required from the cluster. The easiest way to set the used threads is using the environment variable `MKL_NUM_THREADS` (or `OMP_NUM_THREADS`). For a dynamic change of the used threads, you might want to look at [process](#).

HDF5 file format support

We support exporting data to files in the [HDF5] format through the python interface of the *h5py* <<https://docs.h5py.org/en/stable/>> package, see *Saving to disk: input/output* for more information. However, that requires the installation of the HDF5 library and *h5py*.

YAML parameter files

The `tenpy.tools.params.Config` class supports reading and writing YAML files, which requires the package *pyyaml*; `pip install pyyaml`.

Tests

To run the tests, you need to install *pytest*, which you can for example do with `pip install pytest`. For information how to run the tests, see *Checking the installation*.

7.1.6 Checking the installation

The first check of whether *tenpy* is installed successfully, is to try to import it from within python:

```
>>> import tenpy
```

Note: If this raises a warning `Couldn't load compiled cython code`. Code will run a bit slower., something went wrong with the compilation of the Cython parts (or you didn't compile at all). While the code might run slower, the results should still be the same.

The function `tenpy.show_config()` prints information about the used versions of *tenpy*, *numpy* and *scipy*, as well on the fact whether the Cython parts were compiled and could be imported.

As a further check of the installation you can try to run (one of) the python files in the *examples/* subfolder; hopefully all of them should run without error.

You can also run the automated testsuite with *pytest* to make sure everything works fine. If you have *pytest* installed, you can go to the *tests* folder of the repository, and run the tests with:

```
cd tests
pytest
```

In case of errors or failures it gives a detailed traceback and possibly some output of the test. At least the stable releases should run these tests without any failures.

If you can run the examples but not the tests, check whether *pytest* actually uses the correct python version.

The test suite is also run automatically by github actions and with *travis-ci*, results can be inspected [here](#).

7.1.7 TeNPy developer team

The following people are part of the TeNPy developer team.
The full list of contributors can be obtained from the git repository with `git ↪shortlog -sn```.

```
Johannes Hauschild      tenpy@johannes-hauschild.de
Frank Pollmann
Michael P. Zaletel
Maximilian Schulz
Leon Schoonderwoerd
Kévin Hémary
Samuel Scalet
Markus Drescher
Wilhelm Kadow
Gunnar Moeller
Jakob Unfried
Yu-Chin Tzeng
```

Further, the code is based on an earlier version of the library, mainly developed by Frank Pollmann, Michael P. Zaletel and Roger S. K. Mong.

7.1.8 License

The source code documented here is published under a GPL v3 license, which we include below.

```
GNU GENERAL PUBLIC LICENSE
Version 3, 29 June 2007
```

```
Copyright (C) 2007 Free Software Foundation, Inc. <https://fsf.org/>
Everyone is permitted to copy and distribute verbatim copies
of this license document, but changing it is not allowed.
```

Preamble

The GNU General Public License is a free, copyleft license for software and other kinds of works.

The licenses for most software and other practical works are designed to take away your freedom to share and change the works. By contrast, the GNU General Public License is intended to guarantee your freedom to share and change all versions of a program--to make sure it remains free software for all its users. We, the Free Software Foundation, use the GNU General Public License for most of our software; it applies also to any other work released this way by its authors. You can apply it to your programs, too.

When we speak of free software, we are referring to freedom, not price. Our General Public Licenses are designed to make sure that you have the freedom to distribute copies of free software (and charge for them if you wish), that you receive source code or can get it if you want it, that you can change the software or use pieces of it in new free programs, and that you know you can do these things.

To protect your rights, we need to prevent others from denying you these rights or asking you to surrender the rights. Therefore, you have

(continues on next page)

(continued from previous page)

certain responsibilities if you distribute copies of the software, or if you modify it: responsibilities to respect the freedom of others.

For example, if you distribute copies of such a program, whether gratis or for a fee, you must pass on to the recipients the same freedoms that you received. You must make sure that they, too, receive or can get the source code. And you must show them these terms so they know their rights.

Developers that use the GNU GPL protect your rights with two steps: (1) assert copyright on the software, and (2) offer you this License giving you legal permission to copy, distribute and/or modify it.

For the developers' and authors' protection, the GPL clearly explains that there is no warranty for this free software. For both users' and authors' sake, the GPL requires that modified versions be marked as changed, so that their problems will not be attributed erroneously to authors of previous versions.

Some devices are designed to deny users access to install or run modified versions of the software inside them, although the manufacturer can do so. This is fundamentally incompatible with the aim of protecting users' freedom to change the software. The systematic pattern of such abuse occurs in the area of products for individuals to use, which is precisely where it is most unacceptable. Therefore, we have designed this version of the GPL to prohibit the practice for those products. If such problems arise substantially in other domains, we stand ready to extend this provision to those domains in future versions of the GPL, as needed to protect the freedom of users.

Finally, every program is threatened constantly by software patents. States should not allow patents to restrict development and use of software on general-purpose computers, but in those that do, we wish to avoid the special danger that patents applied to a free program could make it effectively proprietary. To prevent this, the GPL assures that patents cannot be used to render the program non-free.

The precise terms and conditions for copying, distribution and modification follow.

TERMS AND CONDITIONS

0. Definitions.

"This License" refers to version 3 of the GNU General Public License.

"Copyright" also means copyright-like laws that apply to other kinds of works, such as semiconductor masks.

"The Program" refers to any copyrightable work licensed under this License. Each licensee is addressed as "you". "Licensees" and "recipients" may be individuals or organizations.

To "modify" a work means to copy from or adapt all or part of the work in a fashion requiring copyright permission, other than the making of an exact copy. The resulting work is called a "modified version" of the earlier work or a work "based on" the earlier work.

(continues on next page)

(continued from previous page)

A "covered work" means either the unmodified Program or a work based on the Program.

To "propagate" a work means to do anything with it that, without permission, would make you directly or secondarily liable for infringement under applicable copyright law, except executing it on a computer or modifying a private copy. Propagation includes copying, distribution (with or without modification), making available to the public, and in some countries other activities as well.

To "convey" a work means any kind of propagation that enables other parties to make or receive copies. Mere interaction with a user through a computer network, with no transfer of a copy, is not conveying.

An interactive user interface displays "Appropriate Legal Notices" to the extent that it includes a convenient and prominently visible feature that (1) displays an appropriate copyright notice, and (2) tells the user that there is no warranty for the work (except to the extent that warranties are provided), that licensees may convey the work under this License, and how to view a copy of this License. If the interface presents a list of user commands or options, such as a menu, a prominent item in the list meets this criterion.

1. Source Code.

The "source code" for a work means the preferred form of the work for making modifications to it. "Object code" means any non-source form of a work.

A "Standard Interface" means an interface that either is an official standard defined by a recognized standards body, or, in the case of interfaces specified for a particular programming language, one that is widely used among developers working in that language.

The "System Libraries" of an executable work include anything, other than the work as a whole, that (a) is included in the normal form of packaging a Major Component, but which is not part of that Major Component, and (b) serves only to enable use of the work with that Major Component, or to implement a Standard Interface for which an implementation is available to the public in source code form. A "Major Component", in this context, means a major essential component (kernel, window system, and so on) of the specific operating system (if any) on which the executable work runs, or a compiler used to produce the work, or an object code interpreter used to run it.

The "Corresponding Source" for a work in object code form means all the source code needed to generate, install, and (for an executable work) run the object code and to modify the work, including scripts to control those activities. However, it does not include the work's System Libraries, or general-purpose tools or generally available free programs which are used unmodified in performing those activities but which are not part of the work. For example, Corresponding Source includes interface definition files associated with source files for the work, and the source code for shared libraries and dynamically linked subprograms that the work is specifically designed to require, such as by intimate data communication or control flow between those

(continues on next page)

(continued from previous page)

subprograms and other parts of the work.

The Corresponding Source need not include anything that users can regenerate automatically from other parts of the Corresponding Source.

The Corresponding Source for a work in source code form is that same work.

2. Basic Permissions.

All rights granted under this License are granted for the term of copyright on the Program, and are irrevocable provided the stated conditions are met. This License explicitly affirms your unlimited permission to run the unmodified Program. The output from running a covered work is covered by this License only if the output, given its content, constitutes a covered work. This License acknowledges your rights of fair use or other equivalent, as provided by copyright law.

You may make, run and propagate covered works that you do not convey, without conditions so long as your license otherwise remains in force. You may convey covered works to others for the sole purpose of having them make modifications exclusively for you, or provide you with facilities for running those works, provided that you comply with the terms of this License in conveying all material for which you do not control copyright. Those thus making or running the covered works for you must do so exclusively on your behalf, under your direction and control, on terms that prohibit them from making any copies of your copyrighted material outside their relationship with you.

Conveying under any other circumstances is permitted solely under the conditions stated below. Sublicensing is not allowed; section 10 makes it unnecessary.

3. Protecting Users' Legal Rights From Anti-Circumvention Law.

No covered work shall be deemed part of an effective technological measure under any applicable law fulfilling obligations under article 11 of the WIPO copyright treaty adopted on 20 December 1996, or similar laws prohibiting or restricting circumvention of such measures.

When you convey a covered work, you waive any legal power to forbid circumvention of technological measures to the extent such circumvention is effected by exercising rights under this License with respect to the covered work, and you disclaim any intention to limit operation or modification of the work as a means of enforcing, against the work's users, your or third parties' legal rights to forbid circumvention of technological measures.

4. Conveying Verbatim Copies.

You may convey verbatim copies of the Program's source code as you receive it, in any medium, provided that you conspicuously and appropriately publish on each copy an appropriate copyright notice; keep intact all notices stating that this License and any non-permissive terms added in accord with section 7 apply to the code;

(continues on next page)

(continued from previous page)

keep intact all notices of the absence of any warranty; and give all recipients a copy of this License along with the Program.

You may charge any price or no price for each copy that you convey, and you may offer support or warranty protection for a fee.

5. Conveying Modified Source Versions.

You may convey a work based on the Program, or the modifications to produce it from the Program, in the form of source code under the terms of section 4, provided that you also meet all of these conditions:

- a) The work must carry prominent notices stating that you modified it, and giving a relevant date.
- b) The work must carry prominent notices stating that it is released under this License and any conditions added under section 7. This requirement modifies the requirement in section 4 to "keep intact all notices".
- c) You must license the entire work, as a whole, under this License to anyone who comes into possession of a copy. This License will therefore apply, along with any applicable section 7 additional terms, to the whole of the work, and all its parts, regardless of how they are packaged. This License gives no permission to license the work in any other way, but it does not invalidate such permission if you have separately received it.
- d) If the work has interactive user interfaces, each must display Appropriate Legal Notices; however, if the Program has interactive interfaces that do not display Appropriate Legal Notices, your work need not make them do so.

A compilation of a covered work with other separate and independent works, which are not by their nature extensions of the covered work, and which are not combined with it such as to form a larger program, in or on a volume of a storage or distribution medium, is called an "aggregate" if the compilation and its resulting copyright are not used to limit the access or legal rights of the compilation's users beyond what the individual works permit. Inclusion of a covered work in an aggregate does not cause this License to apply to the other parts of the aggregate.

6. Conveying Non-Source Forms.

You may convey a covered work in object code form under the terms of sections 4 and 5, provided that you also convey the machine-readable Corresponding Source under the terms of this License, in one of these ways:

- a) Convey the object code in, or embodied in, a physical product (including a physical distribution medium), accompanied by the Corresponding Source fixed on a durable physical medium customarily used for software interchange.
- b) Convey the object code in, or embodied in, a physical product (including a physical distribution medium), accompanied by a

(continues on next page)

(continued from previous page)

written offer, valid for at least three years and valid for as long as you offer spare parts or customer support for that product model, to give anyone who possesses the object code either (1) a copy of the Corresponding Source for all the software in the product that is covered by this License, on a durable physical medium customarily used for software interchange, for a price no more than your reasonable cost of physically performing this conveying of source, or (2) access to copy the Corresponding Source from a network server at no charge.

c) Convey individual copies of the object code with a copy of the written offer to provide the Corresponding Source. This alternative is allowed only occasionally and noncommercially, and only if you received the object code with such an offer, in accord with subsection 6b.

d) Convey the object code by offering access from a designated place (gratis or for a charge), and offer equivalent access to the Corresponding Source in the same way through the same place at no further charge. You need not require recipients to copy the Corresponding Source along with the object code. If the place to copy the object code is a network server, the Corresponding Source may be on a different server (operated by you or a third party) that supports equivalent copying facilities, provided you maintain clear directions next to the object code saying where to find the Corresponding Source. Regardless of what server hosts the Corresponding Source, you remain obligated to ensure that it is available for as long as needed to satisfy these requirements.

e) Convey the object code using peer-to-peer transmission, provided you inform other peers where the object code and Corresponding Source of the work are being offered to the general public at no charge under subsection 6d.

A separable portion of the object code, whose source code is excluded from the Corresponding Source as a System Library, need not be included in conveying the object code work.

A "User Product" is either (1) a "consumer product", which means any tangible personal property which is normally used for personal, family, or household purposes, or (2) anything designed or sold for incorporation into a dwelling. In determining whether a product is a consumer product, doubtful cases shall be resolved in favor of coverage. For a particular product received by a particular user, "normally used" refers to a typical or common use of that class of product, regardless of the status of the particular user or of the way in which the particular user actually uses, or expects or is expected to use, the product. A product is a consumer product regardless of whether the product has substantial commercial, industrial or non-consumer uses, unless such uses represent the only significant mode of use of the product.

"Installation Information" for a User Product means any methods, procedures, authorization keys, or other information required to install and execute modified versions of a covered work in that User Product from a modified version of its Corresponding Source. The information must suffice to ensure that the continued functioning of the modified object code is in no case prevented or interfered with solely because

(continues on next page)

(continued from previous page)

modification has been made.

If you convey an object code work under this section in, or with, or specifically for use in, a User Product, and the conveying occurs as part of a transaction in which the right of possession and use of the User Product is transferred to the recipient in perpetuity or for a fixed term (regardless of how the transaction is characterized), the Corresponding Source conveyed under this section must be accompanied by the Installation Information. But this requirement does not apply if neither you nor any third party retains the ability to install modified object code on the User Product (for example, the work has been installed in ROM).

The requirement to provide Installation Information does not include a requirement to continue to provide support service, warranty, or updates for a work that has been modified or installed by the recipient, or for the User Product in which it has been modified or installed. Access to a network may be denied when the modification itself materially and adversely affects the operation of the network or violates the rules and protocols for communication across the network.

Corresponding Source conveyed, and Installation Information provided, in accord with this section must be in a format that is publicly documented (and with an implementation available to the public in source code form), and must require no special password or key for unpacking, reading or copying.

7. Additional Terms.

"Additional permissions" are terms that supplement the terms of this License by making exceptions from one or more of its conditions. Additional permissions that are applicable to the entire Program shall be treated as though they were included in this License, to the extent that they are valid under applicable law. If additional permissions apply only to part of the Program, that part may be used separately under those permissions, but the entire Program remains governed by this License without regard to the additional permissions.

When you convey a copy of a covered work, you may at your option remove any additional permissions from that copy, or from any part of it. (Additional permissions may be written to require their own removal in certain cases when you modify the work.) You may place additional permissions on material, added by you to a covered work, for which you have or can give appropriate copyright permission.

Notwithstanding any other provision of this License, for material you add to a covered work, you may (if authorized by the copyright holders of that material) supplement the terms of this License with terms:

- a) Disclaiming warranty or limiting liability differently from the terms of sections 15 and 16 of this License; or
- b) Requiring preservation of specified reasonable legal notices or author attributions in that material or in the Appropriate Legal Notices displayed by works containing it; or
- c) Prohibiting misrepresentation of the origin of that material, or

(continues on next page)

(continued from previous page)

requiring that modified versions of such material be marked in reasonable ways as different from the original version; or

d) Limiting the use for publicity purposes of names of licensors or authors of the material; or

e) Declining to grant rights under trademark law for use of some trade names, trademarks, or service marks; or

f) Requiring indemnification of licensors and authors of that material by anyone who conveys the material (or modified versions of it) with contractual assumptions of liability to the recipient, for any liability that these contractual assumptions directly impose on those licensors and authors.

All other non-permissive additional terms are considered "further restrictions" within the meaning of section 10. If the Program as you received it, or any part of it, contains a notice stating that it is governed by this License along with a term that is a further restriction, you may remove that term. If a license document contains a further restriction but permits relicensing or conveying under this License, you may add to a covered work material governed by the terms of that license document, provided that the further restriction does not survive such relicensing or conveying.

If you add terms to a covered work in accord with this section, you must place, in the relevant source files, a statement of the additional terms that apply to those files, or a notice indicating where to find the applicable terms.

Additional terms, permissive or non-permissive, may be stated in the form of a separately written license, or stated as exceptions; the above requirements apply either way.

8. Termination.

You may not propagate or modify a covered work except as expressly provided under this License. Any attempt otherwise to propagate or modify it is void, and will automatically terminate your rights under this License (including any patent licenses granted under the third paragraph of section 11).

However, if you cease all violation of this License, then your license from a particular copyright holder is reinstated (a) provisionally, unless and until the copyright holder explicitly and finally terminates your license, and (b) permanently, if the copyright holder fails to notify you of the violation by some reasonable means prior to 60 days after the cessation.

Moreover, your license from a particular copyright holder is reinstated permanently if the copyright holder notifies you of the violation by some reasonable means, this is the first time you have received notice of violation of this License (for any work) from that copyright holder, and you cure the violation prior to 30 days after your receipt of the notice.

Termination of your rights under this section does not terminate the

(continues on next page)

(continued from previous page)

licenses of parties who have received copies or rights from you under this License. If your rights have been terminated and not permanently reinstated, you do not qualify to receive new licenses for the same material under section 10.

9. Acceptance Not Required for Having Copies.

You are not required to accept this License in order to receive or run a copy of the Program. Ancillary propagation of a covered work occurring solely as a consequence of using peer-to-peer transmission to receive a copy likewise does not require acceptance. However, nothing other than this License grants you permission to propagate or modify any covered work. These actions infringe copyright if you do not accept this License. Therefore, by modifying or propagating a covered work, you indicate your acceptance of this License to do so.

10. Automatic Licensing of Downstream Recipients.

Each time you convey a covered work, the recipient automatically receives a license from the original licensors, to run, modify and propagate that work, subject to this License. You are not responsible for enforcing compliance by third parties with this License.

An "entity transaction" is a transaction transferring control of an organization, or substantially all assets of one, or subdividing an organization, or merging organizations. If propagation of a covered work results from an entity transaction, each party to that transaction who receives a copy of the work also receives whatever licenses to the work the party's predecessor in interest had or could give under the previous paragraph, plus a right to possession of the Corresponding Source of the work from the predecessor in interest, if the predecessor has it or can get it with reasonable efforts.

You may not impose any further restrictions on the exercise of the rights granted or affirmed under this License. For example, you may not impose a license fee, royalty, or other charge for exercise of rights granted under this License, and you may not initiate litigation (including a cross-claim or counterclaim in a lawsuit) alleging that any patent claim is infringed by making, using, selling, offering for sale, or importing the Program or any portion of it.

11. Patents.

A "contributor" is a copyright holder who authorizes use under this License of the Program or a work on which the Program is based. The work thus licensed is called the contributor's "contributor version".

A contributor's "essential patent claims" are all patent claims owned or controlled by the contributor, whether already acquired or hereafter acquired, that would be infringed by some manner, permitted by this License, of making, using, or selling its contributor version, but do not include claims that would be infringed only as a consequence of further modification of the contributor version. For purposes of this definition, "control" includes the right to grant patent sublicenses in a manner consistent with the requirements of this License.

(continues on next page)

(continued from previous page)

Each contributor grants you a non-exclusive, worldwide, royalty-free patent license under the contributor's essential patent claims, to make, use, sell, offer for sale, import and otherwise run, modify and propagate the contents of its contributor version.

In the following three paragraphs, a "patent license" is any express agreement or commitment, however denominated, not to enforce a patent (such as an express permission to practice a patent or covenant not to sue for patent infringement). To "grant" such a patent license to a party means to make such an agreement or commitment not to enforce a patent against the party.

If you convey a covered work, knowingly relying on a patent license, and the Corresponding Source of the work is not available for anyone to copy, free of charge and under the terms of this License, through a publicly available network server or other readily accessible means, then you must either (1) cause the Corresponding Source to be so available, or (2) arrange to deprive yourself of the benefit of the patent license for this particular work, or (3) arrange, in a manner consistent with the requirements of this License, to extend the patent license to downstream recipients. "Knowingly relying" means you have actual knowledge that, but for the patent license, your conveying the covered work in a country, or your recipient's use of the covered work in a country, would infringe one or more identifiable patents in that country that you have reason to believe are valid.

If, pursuant to or in connection with a single transaction or arrangement, you convey, or propagate by procuring conveyance of, a covered work, and grant a patent license to some of the parties receiving the covered work authorizing them to use, propagate, modify or convey a specific copy of the covered work, then the patent license you grant is automatically extended to all recipients of the covered work and works based on it.

A patent license is "discriminatory" if it does not include within the scope of its coverage, prohibits the exercise of, or is conditioned on the non-exercise of one or more of the rights that are specifically granted under this License. You may not convey a covered work if you are a party to an arrangement with a third party that is in the business of distributing software, under which you make payment to the third party based on the extent of your activity of conveying the work, and under which the third party grants, to any of the parties who would receive the covered work from you, a discriminatory patent license (a) in connection with copies of the covered work conveyed by you (or copies made from those copies), or (b) primarily for and in connection with specific products or compilations that contain the covered work, unless you entered into that arrangement, or that patent license was granted, prior to 28 March 2007.

Nothing in this License shall be construed as excluding or limiting any implied license or other defenses to infringement that may otherwise be available to you under applicable patent law.

12. No Surrender of Others' Freedom.

If conditions are imposed on you (whether by court order, agreement or otherwise) that contradict the conditions of this License, they do not

(continues on next page)

(continued from previous page)

excuse you from the conditions of this License. If you cannot convey a covered work so as to satisfy simultaneously your obligations under this License and any other pertinent obligations, then as a consequence you may not convey it at all. For example, if you agree to terms that obligate you to collect a royalty for further conveying from those to whom you convey the Program, the only way you could satisfy both those terms and this License would be to refrain entirely from conveying the Program.

13. Use with the GNU Affero General Public License.

Notwithstanding any other provision of this License, you have permission to link or combine any covered work with a work licensed under version 3 of the GNU Affero General Public License into a single combined work, and to convey the resulting work. The terms of this License will continue to apply to the part which is the covered work, but the special requirements of the GNU Affero General Public License, section 13, concerning interaction through a network will apply to the combination as such.

14. Revised Versions of this License.

The Free Software Foundation may publish revised and/or new versions of the GNU General Public License from time to time. Such new versions will be similar in spirit to the present version, but may differ in detail to address new problems or concerns.

Each version is given a distinguishing version number. If the Program specifies that a certain numbered version of the GNU General Public License "or any later version" applies to it, you have the option of following the terms and conditions either of that numbered version or of any later version published by the Free Software Foundation. If the Program does not specify a version number of the GNU General Public License, you may choose any version ever published by the Free Software Foundation.

If the Program specifies that a proxy can decide which future versions of the GNU General Public License can be used, that proxy's public statement of acceptance of a version permanently authorizes you to choose that version for the Program.

Later license versions may give you additional or different permissions. However, no additional obligations are imposed on any author or copyright holder as a result of your choosing to follow a later version.

15. Disclaimer of Warranty.

THERE IS NO WARRANTY FOR THE PROGRAM, TO THE EXTENT PERMITTED BY APPLICABLE LAW. EXCEPT WHEN OTHERWISE STATED IN WRITING THE COPYRIGHT HOLDERS AND/OR OTHER PARTIES PROVIDE THE PROGRAM "AS IS" WITHOUT WARRANTY OF ANY KIND, EITHER EXPRESSED OR IMPLIED, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE. THE ENTIRE RISK AS TO THE QUALITY AND PERFORMANCE OF THE PROGRAM IS WITH YOU. SHOULD THE PROGRAM PROVE DEFECTIVE, YOU ASSUME THE COST OF ALL NECESSARY SERVICING, REPAIR OR CORRECTION.

16. Limitation of Liability.

(continues on next page)

(continued from previous page)

IN NO EVENT UNLESS REQUIRED BY APPLICABLE LAW OR AGREED TO IN WRITING WILL ANY COPYRIGHT HOLDER, OR ANY OTHER PARTY WHO MODIFIES AND/OR CONVEYS THE PROGRAM AS PERMITTED ABOVE, BE LIABLE TO YOU FOR DAMAGES, INCLUDING ANY GENERAL, SPECIAL, INCIDENTAL OR CONSEQUENTIAL DAMAGES ARISING OUT OF THE USE OR INABILITY TO USE THE PROGRAM (INCLUDING BUT NOT LIMITED TO LOSS OF DATA OR DATA BEING RENDERED INACCURATE OR LOSSES SUSTAINED BY YOU OR THIRD PARTIES OR A FAILURE OF THE PROGRAM TO OPERATE WITH ANY OTHER PROGRAMS), EVEN IF SUCH HOLDER OR OTHER PARTY HAS BEEN ADVISED OF THE POSSIBILITY OF SUCH DAMAGES.

17. Interpretation of Sections 15 and 16.

If the disclaimer of warranty and limitation of liability provided above cannot be given local legal effect according to their terms, reviewing courts shall apply local law that most closely approximates an absolute waiver of all civil liability in connection with the Program, unless a warranty or assumption of liability accompanies a copy of the Program in return for a fee.

END OF TERMS AND CONDITIONS

How to Apply These Terms to Your New Programs

If you develop a new program, and you want it to be of the greatest possible use to the public, the best way to achieve this is to make it free software which everyone can redistribute and change under these terms.

To do so, attach the following notices to the program. It is safest to attach them to the start of each source file to most effectively state the exclusion of warranty; and each file should have at least the "copyright" line and a pointer to where the full notice is found.

```
<one line to give the program's name and a brief idea of what it does.>
Copyright (C) <year> <name of author>
```

```
This program is free software: you can redistribute it and/or modify
it under the terms of the GNU General Public License as published by
the Free Software Foundation, either version 3 of the License, or
(at your option) any later version.
```

```
This program is distributed in the hope that it will be useful,
but WITHOUT ANY WARRANTY; without even the implied warranty of
MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
GNU General Public License for more details.
```

```
You should have received a copy of the GNU General Public License
along with this program. If not, see <https://www.gnu.org/licenses/>.
```

Also add information on how to contact you by electronic and paper mail.

If the program does terminal interaction, make it output a short notice like this when it starts in an interactive mode:

```
<program> Copyright (C) <year> <name of author>
This program comes with ABSOLUTELY NO WARRANTY; for details type `show w'.
This is free software, and you are welcome to redistribute it
```

(continues on next page)

(continued from previous page)

```
under certain conditions; type `show c' for details.
```

The hypothetical commands ``show w'` and ``show c'` should show the appropriate parts of the General Public License. Of course, your program's commands might be different; for a GUI interface, you would use an "about box".

You should also get your employer (if you work as a programmer) or school, if any, to sign a "copyright disclaimer" for the program, if necessary. For more information on this, and how to apply and follow the GNU GPL, see [<https://www.gnu.org/licenses/>](https://www.gnu.org/licenses/).

The GNU General Public License does not permit incorporating your program into proprietary programs. If your program is a subroutine library, you may consider it more useful to permit linking proprietary applications with the library. If this is what you want to do, use the GNU Lesser General Public License instead of this License. But first, please read [<https://www.gnu.org/licenses/why-not-lgpl.html>](https://www.gnu.org/licenses/why-not-lgpl.html).

7.2 Release Notes

The project adheres [semantic versioning](#).

All notable changes to the project should be documented in the changelog. The most important things should be summarized in the release notes.

The changes in [\[latest\]](#) are implemented in the latest development version on github, but not yet released.

Changes compared to previous TeNPy highlights the most important changes compared to the other, previously developed (closed source) TeNPy version.

7.2.1 [latest]

Release Notes

TODO: Summarize the most important changes

Changelog

Backwards incompatible changes

- nothing yet

Added

- nothing yet

Changed

- nothing yet

Fixed

- nothing yet

7.2.2 [0.6.1] - 2020-05-18

Release Notes

This only is a follow-up release to *[0.6.0] - 2020-05-16*. It fixes a small bug in the *examples/c_tebd.py* and some roundoff problems in the tests.

It is now possible to install TeNPy with the conda package manager:

```
conda install --channel=conda-forge physics-tenpy
```

7.2.3 [0.6.0] - 2020-05-16

Release Notes

This release contains a major update of the documentation, which is now hosted by “Read the Docs” at <https://tenpy.readthedocs.io/>. Update your bookmark :-)

Apart from that, this release introduces a format how to save and load data (in particular TeNPy classes) to HDF5 files. See *Saving to disk: input/output* for more details. To use that feature, you need to **install** the h5py package (and therefore some version of the HDF5 library). This is easy with anaconda, `conda install h5py`, but might be cumbersome on your local computing cluster. (However, many university computing clusters have some version of HDF5 installed already. Check with your local sysadmin.)

Moreover, we changed how we read out parameter dictionaries - instead of the `get_parameter()` function, we have now a `Config` class which behaves like a dictionary, you can simply use `options.get(key, default)` for model parameters - as you would do for a python dictionary.

Changelog

Backwards incompatible changes

- Created a class `Config` to replace Python-native parameter dictionaries and add some useful functionality. Old code using `tenpy.tools.params.get_parameter()` and `tenpy.tools.params.unused_parameters()` still works as before, but raises a warning, and should be replaced. For example, if you defined your own models, you should replace calls `get_parameter(model_params, "key", "default_value", "ModelName")` with `model_params.get("key", "default_value")`, the latter syntax being what you would use for a normal python dictionary as well.

- Renamed the following class parameter dictionaries to simply *options* for more consistency. Old code using the class attributes should still work (since we provide property aliases), but raises warnings. Note that this affects also derived classes (for example the `TwoSiteDMRGEngine`).
 - `tenpy.algorithms.dmrp.DMRGEngine.DMRG_params` (was already renamed to *engine_params* in versin 0.5.0)
 - `tenpy.algorithms.mps_common.Sweep.engine_params`
 - `tenpy.algorithms.tebd.Engine.TEBD_params`
 - `tenpy.algorithms.tdvp.Engine.TDVP_params`
 - `tenpy.linalg.lanczos.Lanczos`
- Changed the arguments of `tenpy.models.model.MultiCouplingModel()`: We replaced the three arguments *u0*, *op0* and *other_op* with *other_ops*=[(u1, op1, dx1), (op2, u2, dx2), ...] by single, equivalent argument *ops* which should now read *ops*=[(op0, dx0, u0), (op1, dx1, u1), (op2, dx2, u2), ...], where *dx0* = [0]*lat.dim. Note the changed order inside the tuple! Old code (which specifies *opstr* and *category* as keyword argument, if at all) still works as before, but raises a warning, and should be replaced. Since `tenpy.lattice.Lattice.possible_multi_couplings()` used similar arguments, they were changed as well.
- Don't save *H_MPO_graph* as model attribute anymore - this also wasn't documented.
- Renamed the truncation parameter *symmetry_tol* to *degeneracy_tol* and make the criterion more reasonable by not checking $\log(S_i/S_j) < \log(\text{symmetry_tol})$, but simply $\log(S_i/S_j) < \text{degeneracy_tol}$. The latter makes more sense, as it is equivalent to $(S_i - S_j)/S_j < \exp(\text{degeneracy_tol}) - 1 = \text{degeneracy_tol} + \mathcal{O}(\text{degeneracy_tol}^2)$.
- Deprecated `tenpy.networks.mps.MPS.increase_L()` in favor of the newly added `tenpy.networks.mps.MPS.enlarge_mps_unit_cell()` (taking factor instead of new_L=factor*L as argument).
- `tenpy.networks.mps.MPS.correlation_function()` now auto-determines whether a Jordan-Wigner string is necessary. If any of the given operators is directly an `npc` Array, it will now raise an error; set `autoJW=False` in that case.
- Instead of "monkey-patching" *matvec* of the `tenpy.algorithms.mps_common.EffectiveH` for the case that *ortho_to_envs* is not empty, we defined a proper class `NpcLinearOperatorWrapper`, which serves as baseclass for `OrthogonalNpcLinearOperator`. The argument *ortho_to_envs* has been removed from `EffectiveH`.
- Switch order of the sites in the unit cell for the `DualSquare`, and redefine what the "default" order means. This is a huge optimization of DMRG, reducing the necessary MPS bond dimension for the ground state to the optimal 2^{L-1} on each bond.
- Deprecated the Lanczos function/class argument *orthogonal_to* of in `LanczosGroundState`. Instead, one can use the `OrthogonalNpcLinearOperator`.
- Deprecation warning for changing the default argument of *shift_ket* for non-zero *shift_bra* of the `TransferMatrix`.

Added

- `tenpy.networks.mpo.MPO.variance()` to calculate the variance of an MPO against a finite MPS.
- Classmethod `tenpy.networks.MPS.from_lat_product_state()` to initialize an MPS from a product state given in lattice coordinates (independent of the *order* of the lattice).
- argument `plus_hc` for `tenpy.models.model.CouplingModel.add_onsite()`, `tenpy.models.model.CouplingModel.add_coupling()`, and `tenpy.models.model.MultiCouplingModel.add_multi_coupling()` to simplify adding the hermitian conjugate terms.
- parameter `explicit_plus_hc` for `MPOModel`, `CouplingModel` and MPO, to reduce MPO bond dimension by not storing Hermitian conjugate terms, but computing them at runtime.
- `tenpy.models.model.CouplingModel.add_local_term()` for adding a single term to the lattice, and still handling Jordan-Wigner strings etc.
- `tenpy.networks.site.Site.get_hc_opname()` and `hc_ops` to allow getting the hermitian conjugate operator (name) of the onsite operators.
- `tenpy.tools.hdf5_io` with convenience functions for import and output with pickle, as well as an implementation allowing to save and load objects to HDF5 files in the format specified in *Saving to disk: input/output*.
- human-readable `boundary_conditions` property in `Lattice`.
- `save_hdf5` and `load_hdf5` methods to support saving/loading to HDF5 for the following classes (and their subclasses): - `ChargeInfo` - `LegCharge` - `LegPipe` - `Array` - MPS - MPO - `Lattice`
- `tenpy.networks.mps.MPSEnvironment.get_initialization_data()` for a convenient way of saving the necessary parts of the environment after an DMRG run.
- Method `enlarge_mps_unit_cell` for the following classes: - MPS - MPO - `Lattice` - `Model`, `MPOModel`, `NearestNeighborModel`
- `tenpy.tools.misc.to_iterable_of_len()` for convenience of handling arguments.
- `tenpy.models.lattice.Lattice.mps2lat_values_masked()` as generalization of `tenpy.models.lattice.Lattice.mps2lat_values()`.
- `tenpy.linalg.sparse.OrthogonalNpcLinearOperator` to orthogonalize against vectors.
- `tenpy.linalg.sparse.ShiftNpcLinearOperator` to add a constant.
- `tenpy.linalg.sparse.SumNpcLinearOperator` which serves e.g. to add the h.c. during the *matvec* (in combination with the new `tenpy.linalg.sparse.NpcLinearOperator.adjoint()`).
- `tenpy.algorithms.mps_common.make_eff_H()` to simplify implementations of `prepare_update()`.
- attribute `options` for the `Model`.
- `tenpy.networks.mps.MPS.roll_mps_unit_cell()`.

Changed

- DEFAULT DMRG parameter 'diag_method' from 'lanczos' to 'default', which is the same for large bond dimensions, but performs a full exact diagonalization if the effective Hamiltonian has small dimensions. The threshold introduced is the new DMRG parameter 'max_N_for_ED'.
- DEFAULT parameter `charge_sector=None` instead of `charge_sector=0` in `tenpy.networks.mps.MPS.overlap()` to look for eigenvalues of the transfer matrix in *all* charge sectors, and not assume that it's the 0 sector.
- Derive the following classes (and their subclasses) from the new *Hdf5Exportable* to support saving to HDF5: - *Site* - *Terms* - *OnsiteTerms* - *CouplingTerms* - *Model*, i.e., all model classes.
- Instead of just defining *to_matrix* and *adjoint* for *EffectiveH*, define the interface directly for *NpcLinearOperator*.
- Try to keep the charge block structure as far as possible for `add_charge()` and `drop_charge()`

Fixed

- Adjust the default DMRG parameter *min_sweeps* if *chi_list* is set.
- Avoid some unnecessary transpositions in MPO environments for MPS sweeps (e.g. in DMRG).
- `sort(bunch=True)` could return un-bunched Array, but still set the *bunched* flag.
- *LegPipe* did not initialize `self.bunched` correctly.
- **issue #98**: Error of calling *psi.canonical_form()* directly after disabling the DMRG mixer.
- *svd()* with `full_matrices=True` gave wrong charges.
- `tenpy.linalg.np_conserved.Array.drop_charge()` and `tenpy.lina.np_conserved.Array.drop_charge()` did not copy over labels.
- wrong pairs for the *fifth_nearest_neighbors* of the *Honeycomb*.
- Continue in `tenpy.algorithms.dmrgh.full_diag_effH()` with a warning instead of raising an Error, if the effective Hamiltonian is zero.
- `correlation_length()`: check for hermitian Flag might have raised and Error with new numpy warnings
- `correlation_function()` did not respect argument `str_on_first=False`.
- `tenpy.networks.mps.MPS.get_op()` worked unexpected for infinite *bc* with incommensurate `self.L` and `len(op_list)`.
- `tenpy.networks.mps.MPS.permute_sites()` did modify the given *perm*.
- **issue #105** Unintended side-effects using *lanczos_params.verbose* in combination with *orthogonal_to*
- **issue #108** `tenpy.linalg.sparse.FlatLinearOperator._matvec()` changes `self._charge_sector`

7.2.4 [0.5.0] - 2019-12-18

Backwards incompatible changes

- **Major** rewriting of the DMRG Engines, see [issue #39](#) and [issue #85](#) for details. The *EngineCombine* and *EngineFracture* have been combined into a single *TwoSiteDMRGEngine* with an *run* function works as before. In case you have directly used the *EngineCombine* or *EngineFracture*, you should update your code and use the *TwoSiteEngine* instead.
- Moved *init_LP* and *init_RP* method from MPS into *MPSEnvironment* and *MPOEnvironment*.

Changed

- Addition/subtraction of *Array*: check whether the both arrays have the same labels in different order, and in that case raise a warning that we will transpose in the future.
- Made *tenpy.linalg.np_conserved.Array.get_block()* public (previously *tenpy.linalg.np_conserved.Array._get_block*).
- *groundstate()* now returns a tuple (E0, psi0) instead of just psi0. Moreover, the argument *charge_sector* was added.
- Simplification in the *Lattice*: Instead of having separate arguments/attributes/functions for 'nearest_neighbors', 'next_nearest_neighbors', 'next_next_nearest_neighbors' and possibly (Honeycomb) even 'fourth_nearest_neighbors', 'fifth_nearest_neighbors', collect them in a dictionary called *pairs*. Old call structures still allowed, but deprecated.
- [issue #94](#): Array addition and *inner()* should reflect the order of the labels, if they coincided. Will change the default behaviour in the future, raising *FutureWarning* for now.
- **Default parameter** for DMRG params: increased precision by setting *P_tol_min* down to the maximum of $1.e-30$, *lanczos_params['svd_min']**2 * P_tol_to_trunc*, *lanczos_params['trunc_cut']**2 * P_tol_to_trunc* by default.

Added

- *tenpy.algorithms.mps_common* with the Sweep class and *EffectiveH* to be a *OneSiteH* or *TwoSiteH*.
- Single-Site DMRG with the *SingleSiteDMRG*.
- Example function in *examples/c_tebd.py* how to run TEBD with a model originally having next-nearest neighbors.
- *increase_L()* to allow increasing the unit cell of an MPS.
- Additional option *order='folded'* for the *Chain*.
- *tenpy.algorithms.exact_diag.ExactDiag.from_H_mpo()* wrapper as replacement for *tenpy.networks.mpo.MPO.get_full_hamiltonian()* and *tenpy.networks.mpo.MPO.get_grouped_mpo()*. The latter are now deprecated.
- Argument *max_size* to limit the matrix dimension in *ExactDiag*.
- *tenpy.linalg.sparse.FlatLinearOperator.from_guess_with_pipe()* to allow quickly converting *matvec* functions acting on multi-dimensional arrays to a *FlatLinearOperator* by combining the legs into a *LegPipe*.

- `tenpy.tools.math.speigsh()` for hermitian variant of `speigs()`
- Allow for arguments 'LA', 'SA' in `argsort()`.
- `tenpy.linalg.lanczos.lanczos_arpack()` as possible replacement of the self-implemented `lanczos` function.
- `tenpy.algorithms.dmrgh.full_diag_effH()` as another replacement of `lanczos()`.
- The new DMRG parameter 'diag_method' allows to select a method for the diagonalization of the effective Hamiltonian. See `tenpy.algorithms.dmrgh.DMRGEngine.diag()` for details.
- dtype attribute in `EffectiveH`.
- `tenpy.linalg.charges.LegCharge.get_qindex_of_charges()` to allow selecting a block of an Array from the charges.
- `tenpy.algorithms.mps_common.EffectiveH.to_matrix` to allow contracting an `EffectiveH` to a matrix, as well as metadata `tenpy.linalg.sparse.NpcLinearOperator.acts_on` and `tenpy.algorithms.mps_common.EffectiveH.N`.
- argument `only_physical_legs` in `tenpy.networks.mps.MPS.get_total_charge()`

Fixed

- `MPO.expectation_value()` did not work for finite systems.
- Calling `compute_K()` repeatedly with default parameters but on states with different `chi` would use the `chi` of the very first call for the truncation parameters.
- allow `MPSEnvironment` and `MPOEnvironment` to have MPS/MPO with different length
- `group_sites()` didn't work correctly in some situations.
- `matvec_to_array()` returned the transposed of A.
- `tenpy.networks.mps.MPS.from_full()` messed up the form of the first array.
- [issue #95](#): blowup of errors in DMRG with `update_env > 0`. Turns out to be a problem in the precision of the truncation error: `TruncationError.eps` was set to 0 if it would be smaller than machine precision. To fix it, I added `from_S()`.

7.2.5 [0.4.1] - 2019-08-14

Backwards incompatible changes

- Switch the sign of the `BoseHubbardModel` and `FermiHubbardModel` to hopping and chemical potential having negative prefactors. Of course, the same adjustment happens in the `BoseHubbardChain` and `FermiHubbardChain`.
- moved `BoseHubbardModel` and `BoseHubbardChain` as well as `FermiHubbardModel` and `FermiHubbardChain` into the new module `tenpy.models.hubbard`.
- Change arguments of `coupling_term_handle_JW()` and `multi_coupling_term_handle_JW()` to use `strength` and `sites` instead of `op_needs_JW`.
- Only accept valid identifiers as operator names in `add_op()`.

Changed

- `grid_concat()` allows for `None` entries (representing zero blocks).
- `from_full()` allows for 'segment' boundary conditions.
- `apply_local_op()` allows for n-site operators.

Added

- `max_range` attribute in MPO and *MPOGraph*.
- `is_hermitian()`
- Nearest-neighbor interaction in `BoseHubbardModel`
- `multiply_op_names()` to replace `' '.join(op_names)` and allow explicit compression/multiplication.
- `order_combine_term()` to group operators together.
- `dagger()` of MPO's (and to implement that also `flip_charges_qconj()`).
- `has_label()` to check if a label exists
- `qr_li()` and `rq_li()`
- Addition of MPOs
- 3 additional examples for chern insulators in `examples/chern_insulators/`.
- `FermionicHaldaneModel` and `BosonicHaldaneModel`.
- `from_MPOModel()` for initializing nearest-neighbor models after grouping sites.

Fixed

- [issue #36](#): long-range couplings could give `IndexError`.
- [issue #42](#): Onsite-terms in `FermiHubbardModel` were wrong for lattices with non-trivial unit cell.
- Missing a factor 0.5 in `GUE()`.
- Allow `TermList` to have terms with multiple operators acting on the same site.
- Allow MPS indices outside unit cell in `mps2lat_idx()` and `lat2mps_idx()`.
- `expectation_value()` did not work for n-site operators.

7.2.6 [0.4.0] - 2019-04-28

Backwards incompatible changes

- The argument order of `tenpy.models.lattice.Lattice` could be a tuple (priority, snake_winding) before. This is no longer valid and needs to be replaced by ("standard", snake_winding, priority).
- Moved the boundary conditions `bc_coupling` from the `tenpy.models.model.CouplingModel` into the `tenpy.models.lattice.Lattice` (as `bc`). Using the parameter `bc_coupling` will raise a `FutureWarning`, one should set the boundary conditions directly in the lattice.

- Added parameter *permute* (True by default) in `tenpy.networks.mps.MPS.from_product_state()` and `tenpy.networks.mps.MPS.from_Bflat()`. The resulting state will therefore be independent of the “conserve” parameter of the Sites - unlike before, where the meaning of the *p_state* argument might have changed.
- Generalize and rename `tenpy.networks.site.DoubleSite` to `tenpy.networks.site.GroupedSite`, to allow for an arbitrary number of sites to be grouped. Arguments *site0*, *site1*, *label0*, *label1* of the `__init__` can be replaced with [*site0*, *site1*], [*label0*, *label1*] and *op0*, *op1* of the *kronecker_product* with [*op0*, *op1*]; this will recover the functionality of the *DoubleSite*.
- Restructured callstructure of Mixer in DMRG, allowing an implementation of other mixers. To enable the mixer, set the DMRG parameter “mixer” to True or ‘DensityMatrixMixer’ instead of just ‘Mixer’.
- The interaction parameter in the `tenpy.models.bose_hubbard_chain.BoseHubbardModel` (and `tenpy.models.bose_hubbard_chain.BoseHubbardChain`) did not correspond to $U/2N(N-1)$ as claimed in the Hamiltonian, but to UN^2 . The correcting factor 1/2 and change in the chemical potential have been fixed.
- Major restructuring of `tenpy.linalg.np_conserved` and `tenpy.linalg.charges`. This should not break backwards-compatibility, but if you compiled the cython files, you **need** to remove the old binaries in the source directory. Using `bash cleanup.sh` might be helpful to do that, but also remove other files within the repository, so be careful and make a backup beforehand to be on the save side. Afterwards recompile with `bash compile.sh`.
- Changed structure of `tenpy.models.model.CouplingModel.onsite_terms` and `tenpy.models.model.CouplingModel.coupling_terms`: Each of them is now a dictionary with category strings as keys and the newly introduced `tenpy.networks.terms.OnsiteTerms` and `tenpy.networks.terms.CouplingTerms` as values.
- `tenpy.models.model.CouplingModel.calc_H_onsite()` is deprecated in favor of new methods.
- Argument *raise_op2_left* of `tenpy.models.model.CouplingModel.add_coupling()` is deprecated.

Added

- `tenpy.networks.mps.MPS.canonical_form_infinite()`.
- `tenpy.networks.mps.MPS.expectation_value_term()`, `tenpy.networks.mps.MPS.expectation_value_terms_sum()` and `tenpy.networks.mps.MPS.expectation_value_multi_sites()` for expectation values of terms.
- `tenpy.networks.mpo.MPO.expectation_value()` for an MPO.
- `tenpy.linalg.np_conserved.Array.extend()` and `tenpy.linalg.charges.LegCharge.extend()`, allowing to extend an Array with zeros.
- DMRG parameter ‘orthogonal_to’ allows to calculate excited states for finite systems.
- possibility to change the number of charges after creating LegCharges/Arrays.
- more general way to specify the order of sites in a `tenpy.models.lattice.Lattice`.
- new `tenpy.models.lattice.Triangular`, `tenpy.models.lattice.Honeycomb` and `tenpy.models.lattice.Kagome` lattice
- a way to specify nearest neighbor couplings in a *Lattice*, along with methods to count the number of nearest neighbors for sites in the bulk, and a way to plot them (*plot_coupling()* and friends)
- `tenpy.networks.mpo.MPO.from_grids()` to generate the MPO from a grid.
- `tenpy.models.model.MultiCouplingModel` for couplings involving more than 2 sites.

- request #8: Allow shift in boundary conditions of `CouplingModel`.
- Allow to use state labels in `tenpy.networks.mps.MPS.from_product_state()`.
- `tenpy.models.model.CouplingMPOModel` structuring the default initialization of most models.
- Allow to force periodic boundary conditions for finite MPS in the `CouplingMPOModel`. This is not recommended, though.
- `tenpy.models.model.NearestNeighborModel.calc_H_MPO_from_bond()` and `tenpy.models.model.MPOModel.calc_H_bond_from_MPO()` for conversion of `H_bond` into `H_MPO` and vice versa.
- `tenpy.algorithms.tebd.RandomUnitaryEvolution` for random unitary circuits
- Allow documentation links to github issues, arXiv, papers by doi and the forum with e.g. `:issue:`5``, `:arxiv:`1805.00055``, `:doi:`10.21468/SciPostPhysLectNotes.5``, `:forum:`3``
- `tenpy.models.model.CouplingModel.coupling_strength_add_ext_flux()` for adding hoppings with external flux.
- `tenpy.models.model.CouplingModel.plot_coupling_terms()` to visualize the added coupling terms.
- `tenpy.networks.terms.OnsiteTerms`, `tenpy.networks.terms.CouplingTerms`, `tenpy.networks.terms.MultiCouplingTerm` containing the of terms for the `CouplingModel` and `MultiCouplingModel`. This allowed to add the `category` argument to `add_onsite`, `add_coupling` and `add_multi_coupling`.
- `tenpy.networks.terms.TermList` as another (more human readable) representation of terms with conversion from and to the other `*Term` classes.
- `tenpy.networks.mps.MPS.init_LP()` and `tenpy.networks.mps.MPS.init_RP()` to initialize left and right parts of an Environment.
- `tenpy.networks.mpo.MPOGraph.from_terms()` and `tenpy.networks.mpo.MPOGraph.from_term_list()`.
- argument `charge_sector` in `tenpy.networks.mps.MPS.correlation_length()`.

Changed

- moved toycodes from the folder `examples/` to a new folder `toycodes/` to separate them clearly.
- **major remodelling of the internals of `tenpy.linalg.np_conserved` and `tenpy.linalg.charges`.**
 - Introduced the new module `tenpy/linalg/_npc_helper.pyx` which contains all the Cython code, and gets imported by
 - `Array` now rejects addition/subtraction with other types
 - `Array` now rejects multiplication/division with non-scalar types
 - By default, make deep copies of `npc` Arrays.
- Restructured lanczos into a class, added time evolution calculating $\exp(A*dt)|\psi_0\rangle$
- Warning for poorly conditioned Lanczos; to overcome this enable the new parameter `reortho`.
- Simplified call structure of `extend()`, and `extend()`.
- Restructured `tenpy.algorithms.dmrq`:

- `run()` is now just a wrapper around the new `run(psi, model, pars)` is roughly equivalent to `eng = EngineCombine(psi, model, pars); eng.run()`.
- Added `init_env()` and `reset_stats()` to allow a simple restart of DMRG with slightly different parameters, e.g. for tuning Hamiltonian parameters.
- Call `canonical_form()` for infinite systems if the final state is not in canonical form.
- Changed **default values** for some parameters:
 - set `trunc_params['chi_max'] = 100`. Not setting a *chi_max* at all will lead to memory problems. Disable `DMRG_params['chi_list'] = None` by default to avoid conflicting settings.
 - reduce to `mixer_params['amplitude'] = 1.e-5`. A too strong mixer screws DMRG up pretty bad.
 - increase `Lanczos_params['N_cache'] = N_max` (i.e., keep all states)
 - set `DMRG_params['P_tol_to_trunc'] = 0.05` and provide reasonable `..._min` and `..._max` values.
 - increased (default) DMRG accuracy by setting `DMRG_params['max_E_err'] = 1.e-8` and `DMRG_params['max_S_err'] = 1.e-5`.
 - don't check the (absolute) energy for convergence in Lanczos.
 - set `DMRG_params['norm_tol'] = 1.e-5` to check whether the final state is in canonical form.
- Verbosity of `get_parameter()` reduced: Print parameters only for verbosity ≥ 1 . and default values only for verbosity ≥ 2 .
- Don't print the energy during real-time TEBD evolution - it's preserved up to truncation errors.
- Renamed the *SquareLattice* class to `tenpy.models.lattice.Square` for better consistency.
- auto-determine whether Jordan-Wigner strings are necessary in `add_coupling()`.
- The way the labels of npc Arrays are stored internally changed to a simple list with None entries. There is a deprecated property setter yielding a dictionary with the labels.
- renamed *first_LP* and *last_RP* arguments of *MPSEnvironment* and *MPOEnvironment* to *init_LP* and *init_RP*.
- Testing: instead of the (outdated) `nose`, we now use `pytest` <<https://pytest.org>> for testing.

Fixed

- **issue #22: Serious bug** in `tenpy.linalg.np_conserved.inner()`: if `do_conj=True` is used with non-zero `qtotal`, it returned 0. instead of non-zero values.
- avoid error in `tenpy.networks.mps.MPS.apply_local_op()`
- Don't carry around total charge when using DMRG with a mixer
- Corrected couplings of the *FermionicHubbardChain*
- **issue #2:** memory leak in cython parts when using intelpython/anaconda
- **issue #4:** incompatible data types.
- **issue #6:** the *CouplingModel* generated wrong Couplings in some cases
- **issue #19:** Convergence of energy was slow for infinite systems with `N_sweeps_check=1`
- more reasonable traceback in case of wrong labels

- wrong dtype of `npc.Array` when adding/subtracting/... arrays of different data types
- could get wrong `H_bond` for completely decoupled chains.
- SVD could return outer indices with different axes
- `tenpy.networks.mps.MPS.overlap()` works now for MPS with different total charge (e.g. after `psi.apply_local_op(i, 'Sp')`).
- skip existing graph edges in `MPOGraph.add()` when building up terms without the strength part.

Removed

- Attribute *chinfo* of *Lattice*.

7.2.7 [0.3.0] - 2018-02-19

This is the first version published on github.

Added

- Cython modules for `np_conserved` and charges, which can optionally be compiled for speed-ups
- `tools.optimization` for dynamical optimization
- Various models.
- More predefined lattice sites.
- Example toy-codes.
- Network contractor for general networks

Changed

- Switch to python3

Removed

- Python 2 support.

7.2.8 [0.2.0] - 2017-02-24

- Compatible with python2 and python3 (using the 2to3 tool).
- Development version.
- Includes TEBD and DMRG.

7.2.9 Changes compared to previous TeNPy

This library is based on a previous (closed source) version developed mainly by Frank Pollmann, Michael P. Zaletel and Roger S. K. Mong. While almost all files are completely rewritten and not backwards compatible, the overall structure is similar. In the following, we list only the most important changes.

Global Changes

- syntax style based on PEP8. Use `$>yapf -r -i ./` to ensure consistent formatting over the whole project. Special comments `# yapf: disable` and `# yapf: enable` can be used for manual formatting of some regions in code.
- Following PEP8, we distinguish between ‘private’ functions, indicated by names starting with an underscore and to be used only within the library, and the public API. The public API should be backwards-compatible with different releases, while private functions might change at any time.
- all modules are in the folder `tenpy` to avoid name conflicts with other libraries.
- within the library, relative imports are used, e.g., `from ..tools.math import (toiterable, tonparray)` Exception: the files in `tests/` and `examples/` run as `__main__` and can’t use relative imports
Files outside of the library (and in `tests/`, `examples/`) should use absolute imports, e.g. `import tenpy.algorithms.tebd`
- renamed `tenpy/mps/` to `tenpy/networks`, since it contains various tensor networks.
- added [Site](#) describing the local physical sites by providing the physical `LegCharge` and onsite operators.

np_conserved

- pure python, no need to compile!
- in module `tenpy.linalg` instead of `algorithms/linalg`.
- moved functionality for charges to `charges`
- Introduced the classes `ChargeInfo` (basically the old `q_number`, and `mod_q`) and `LegCharge` (the old `qind`, `qconj`).
- Introduced the class `LegPipe` to replace the old `leg_pipe`. It is derived from `LegCharge` and used as a leg in the `array` class. Thus any inherited array (after `tensor_dot` etc still has all the necessary information to split the legs. (The legs are shared between different arrays, so it’s saved only once in memory)
- Enhanced indexing of the array class to support slices and 1D index arrays along certain axes
- more functions, e.g. `grid_outer()`

TEBD

- Introduced `TruncationError` for easy handling of total truncation error.
- some truncation parameters are renamed and may have a different meaning, e.g. `svd_max` -> `svd_min` has no ‘log’ in the definition.

DMRG

- separate Lanczos module in *tenpy/linalg/*. Strangely, the old version orthogonalized against the complex conjugates of *orthogonal_to* (contrary to its doc string!) (and thus calculated ‘theta_o’ as bra, not ket).
- cleaned up, provide prototypes for DMRG engine and mixer.

Tools

- added *tenpy.tools.misc*, which contains ‘random stuff’ from old *tools.math* like *to_iterable* and *to_array* (renamed to follow PEP8, documented)
- moved stuff for fitting to *tenpy.tools.fit*
- enhanced *tenpy.tools.string.vert_join()* for nice formatting
- moved (parts of) old *cluster/omp.py* to *tenpy.tools.process*
- added *tenpy.tools.params* for a simplified handling of parameter/arguments for models and/or algorithms. Similar as the old *models.model.set_var*, but use it also for algorithms. Also, it may modify the given dictionary.

7.3 Introductions

The following documents are meant as introductions to various topics relevant to TeNPy.

If you are new to TeNPy, read the [Overview](#).

7.3.1 Overview

Repository

The root directory of this git repository contains the following folders:

tenpy The actual source code of the library. Every subfolder contains an `__init__.py` file with a summary what the modules in it are good for. (This file is also necessary to mark the folder as part of the python package. Consequently, other subfolders of the git repo should not include a `__init__.py` file.)

toycode Simple toy codes completely independent of the remaining library (i.e., codes in *tenpy/*). These codes should be quite readable and intend to give a flavor of how (some of) the algorithms work.

examples Some example files demonstrating the usage and interface of the library.

doc A folder containing the documentation: the user guide is contained in the `*.rst` files. The online documentation is autogenerated from these files and the docstrings of the library. This folder contains a make file for building the documentation, run `make help` for the different options. The necessary files for the reference in *doc/* reference can be auto-generated/updated with `make src2html`.

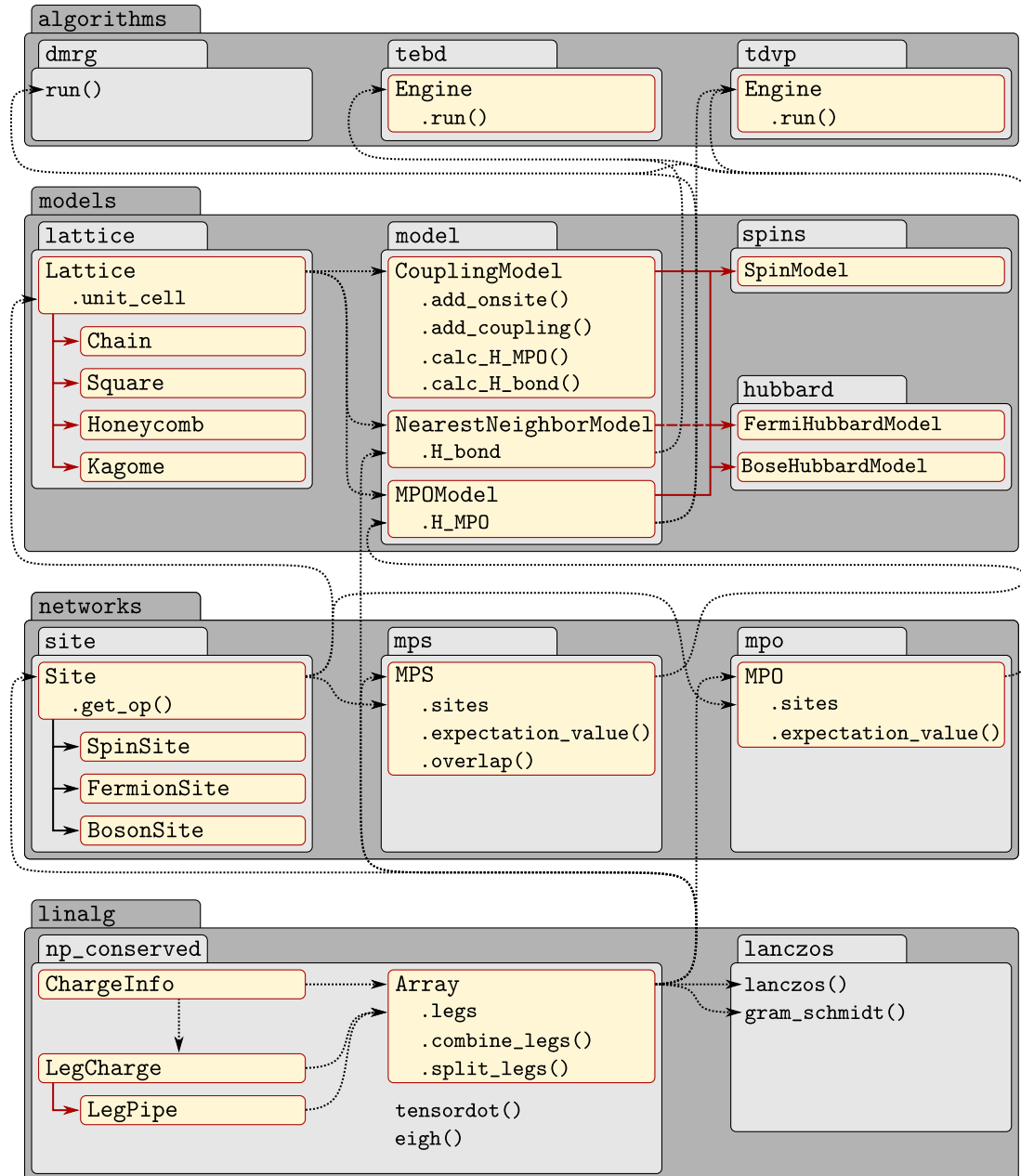
tests Contains files with test routines, to be used with *pytest*. If you are set up correctly and have *pytest* installed, you can run the test suite with `pytest` from within the *tests/* folder.

build This folder is not distributed with the code, but is generated by `setup.py` (or `compile.sh`, respectively). It contains compiled versions of the Cython files, and can be ignored (and even removed without losing functionality).

Code structure: getting started

There are several layers of abstraction in TeNPy. While there is a certain hierarchy of how the concepts build up on each other, the user can decide to utilize only some of them. A maximal flexibility is provided by an object oriented style based on classes, which can be inherited and adjusted to individual demands.

The following figure gives an overview of the most important modules, classes and functions in TeNPy. Gray backgrounds indicate (sub)modules, yellow backgrounds indicate classes. Red arrows indicate inheritance relations, dashed black arrows indicate a direct use. (The individual models might be derived from the *NearestNeighborModel* depending on the geometry of the lattice.) There is a clear hierarchy from high-level algorithms in the *tenpy.algorithms* module down to basic operations from linear algebra in the *tenpy.linalg* module.



Most basic level: linear algebra

Note: See *Charge conservation with `np_conserved`* for more information on defining charges for arrays.

The most basic layer is given by in the `linalg` module, which provides basic features of linear algebra. In particular, the `np_conserved` submodule implements an `Array` class which is used to represent the tensors. The basic interface of `np_conserved` is very similar to that of the NumPy and SciPy libraries. However, the `Array` class implements abelian charge conservation. If no charges are to be used, one can use ‘trivial’ arrays, as shown in the following example code.

```
"""Basic use of the `Array` class with trivial arrays."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

import tenpy.linalg.np_conserved as npc

M = npc.Array.from_ndarray_trivial([[0., 1.], [1., 0.]])
v = npc.Array.from_ndarray_trivial([2., 4. + 1.j])
v[0] = 3. # set individual entries like in numpy
print("|v> =", v.to_ndarray())
# |v> = [ 3.+0.j  4.+1.j]

M_v = npc.tensordot(M, v, axes=[1, 0])
print("M|v> =", M_v.to_ndarray())
# M|v> = [ 4.+1.j  3.+0.j]
print("<v|M|v> =", npc.inner(v.conj(), M_v, axes='range'))
# <v|M|v> = (24+0j)
```

The number and types of symmetries are specified in a `ChargeInfo` class. An `Array` instance represents a tensor satisfying a charge rule specifying which blocks of it are nonzero. Internally, it stores only the non-zero blocks of the tensor, along with one `LegCharge` instance for each leg, which contains the *charges* and sign *qconj* for each leg. We can combine multiple legs into a single larger `LegPipe`, which is derived from the `LegCharge` and stores all the information necessary to later split the pipe.

The following code explicitly defines the spin-1/2 S^+ , S^- , S^z operators and uses them to generate and diagonalize the two-site Hamiltonian $H = \vec{S} \cdot \vec{S}$. It prints the charge values (by default sorted ascending) and the eigenvalues of H .

```
"""Explicit definition of charges and spin-1/2 operators."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

import tenpy.linalg.np_conserved as npc

# consider spin-1/2 with Sz-conservation
chinfo = npc.ChargeInfo([1]) # just a U(1) charge
# charges for up, down state
p_leg = npc.LegCharge.from_qflat(chinfo, [[1], [-1]])
Sz = npc.Array.from_ndarray([[0.5, 0.], [0., -0.5]], [p_leg, p_leg.conj()])
Sp = npc.Array.from_ndarray([[0., 1.], [0., 0.]], [p_leg, p_leg.conj()])
Sm = npc.Array.from_ndarray([[0., 0.], [1., 0.]], [p_leg, p_leg.conj()])

Hxy = 0.5 * (npc.outer(Sp, Sm) + npc.outer(Sm, Sp))
Hz = npc.outer(Sz, Sz)
H = Hxy + Hz
# here, H has 4 legs
H.iset_leg_labels(["s1", "t1", "s2", "t2"])
H = H.combine_legs([["s1", "s2"], ["t1", "t2"]], qconj=[+1, -1])
```

(continues on next page)

(continued from previous page)

```
# here, H has 2 legs
print(H.legs[0].to_qflat().flatten())
# prints [-2  0  0  2]
E, U = npc.eigh(H) # diagonalize blocks individually
print(E)
# [ 0.25 -0.75  0.25  0.25]
```

Sites for the local Hilbert space and tensor networks

The next basic concept is that of a local Hilbert space, which is represented by a *Site* in TeNPy. This class does not only label the local states and define the charges, but also provides onsite operators. For example, the *SpinHalfSite* provides the S^+ , S^- , S^z operators under the names 'Sp', 'Sm', 'Sz', defined as *Array* instances similarly as in the code above. Since the most common sites like for example the *SpinSite* (for general spin $S=0.5, 1, 1.5, \dots$), *BosonSite* and *FermionSite* are predefined, a user of TeNPy usually does not need to define the local charges and operators explicitly. The total Hilbert space, i.e. the tensor product of the local Hilbert spaces, is then just given by a list of *Site* instances. If desired, different kinds of *Site* can be combined in that list. This list is then given to classes representing tensor networks like the MPS and MPO. The tensor network classes also use *Array* instances for the tensors of the represented network.

The following example illustrates the initialization of a spin-1/2 site, an MPS representing the Neel state, and an MPO representing the Heisenberg model by explicitly defining the W tensor.

```
"""Initialization of sites, MPS and MPO."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.networks.site import SpinHalfSite
from tenpy.networks.mps import MPS
from tenpy.networks.mpo import MPO

spin = SpinHalfSite(conserved="Sz")
print(spin.Sz.to_ndarray())
# [[ 0.5  0. ]
#   [ 0. -0.5]]

N = 6 # number of sites
sites = [spin] * N # repeat entry of list N times
pstate = ["up", "down"] * (N // 2) # Neel state
psi = MPS.from_product_state(sites, pstate, bc="finite")
print("<Sz> =", psi.expectation_value("Sz"))
# <Sz> = [ 0.5 -0.5  0.5 -0.5]
print("<Sp_i Sm_j> =", psi.correlation_function("Sp", "Sm"), sep="\n")
# <Sp_i Sm_j> =
# [[1.  0.  0.  0.  0.  0.]
#   [0.  0.  0.  0.  0.  0.]
#   [0.  0.  1.  0.  0.  0.]
#   [0.  0.  0.  0.  0.  0.]
#   [0.  0.  0.  0.  1.  0.]
#   [0.  0.  0.  0.  0.  0.]]

# define an MPO
Id, Sp, Sm, Sz = spin.Id, spin.Sp, spin.Sm, spin.Sz
J, Delta, hz = 1., 1., 0.2
W_bulk = [[Id, Sp, Sm, Sz, -hz * Sz], [None, None, None, None, 0.5 * J * Sm],
           [None, None, None, None, 0.5 * J * Sp], [None, None, None, None, J * Delta,
↪ * Sz],
```

(continues on next page)

(continued from previous page)

```

[None, None, None, None, Id]]
W_first = [W_bulk[0]] # first row
W_last = [[row[-1]] for row in W_bulk] # last column
Ws = [W_first] + [W_bulk] * (N - 2) + [W_last]
H = MPO.from_grids([spin] * N, Ws, bc='finite', IdL=0, IdR=-1)
print("<psi|H|psi> =", H.expectation_value(psi))
# <psi|H|psi> = -1.25

```

Models

Note: See [Models](#) for more information on sites and how to define and extend models on your own.

Technically, the explicit definition of an MPO is already enough to call an algorithm like DMRG in [dmrg](#). However, writing down the W tensors is cumbersome especially for more complicated models. Hence, TeNPy provides another layer of abstraction for the definition of models, which we discuss first. Different kinds of algorithms require different representations of the Hamiltonian. Therefore, the library offers to specify the model abstractly by the individual onsite terms and coupling terms of the Hamiltonian. The following example illustrates this, again for the Heisenberg model.

```

"""Definition of a model: the XXZ chain."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.networks.site import SpinSite
from tenpy.models.lattice import Chain
from tenpy.models.model import CouplingModel, NearestNeighborModel, MPOModel

class XXZChain(CouplingModel, NearestNeighborModel, MPOModel):
    def __init__(self, L=2, S=0.5, J=1., Delta=1., hz=0.):
        spin = SpinSite(S=S, conserve="Sz")
        # the lattice defines the geometry
        lattice = Chain(L, spin, bc="open", bc_MPS="finite")
        CouplingModel.__init__(self, lattice)
        # add terms of the Hamiltonian
        self.add_coupling(J * 0.5, 0, "Sp", 0, "Sm", 1) # Sp_i Sm_{i+1}
        self.add_coupling(J * 0.5, 0, "Sp", 0, "Sm", -1) # Sp_i Sm_{i-1}
        self.add_coupling(J * Delta, 0, "Sz", 0, "Sz", 1)
        # (for site dependent prefactors, the strength can be an array)
        self.add_onsite(-hz, 0, "Sz")

        # finish initialization
        # generate MPO for DMRG
        MPOModel.__init__(self, lat, self.calc_H_MPO())
        # generate H_bond for TEBD
        NearestNeighborModel.__init__(self, lat, self.calc_H_bond())

```

While this generates the same MPO as in the previous code, this example can easily be adjusted and generalized, for example to a higher dimensional lattice by just specifying a different lattice. Internally, the MPO is generated using a finite state machine picture. This allows not only to translate more complicated Hamiltonians into their corresponding MPOs, but also to automate the mapping from a higher dimensional lattice to the 1D chain along which the MPS winds. Note that this mapping introduces longer-range couplings, so the model can no longer be defined to be a [NearestNeighborModel](#) suited for TEBD if another lattice than the [Chain](#) is to be used. Of course, many

commonly studied models are also predefined. For example, the following code initializes the Heisenberg model on a kagome lattice; the spin liquid nature of the ground state of this model is highly debated in the current literature.

```
"""Initialization of the Heisenberg model on a kagome lattice."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.models.spins import SpinModel

model_params = {
    "S": 0.5, # Spin 1/2
    "lattice": "Kagome",
    "bc_MPS": "infinite",
    "bc_y": "cylinder",
    "Ly": 2, # defines cylinder circumference
    "conserve": "Sz", # use Sz conservation
    "Jx": 1.,
    "Jy": 1.,
    "Jz": 1. # Heisenberg coupling
}
model = SpinModel(model_params)
```

Algorithms

The highest level in TeNPy is given by algorithms like DMRG and TEBD. Using the previous concepts, setting up a simulation running those algorithms is a matter of just a few lines of code. The following example runs a DMRG simulation, see `dmrg`, exemplary for the transverse field Ising model at the critical point.

```
"""Call of (finite) DMRG."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFChain
from tenpy.algorithms import dmrg

N = 16 # number of sites
model = TFChain({"L": N, "J": 1., "g": 1., "bc_MPS": "finite"})
sites = model.lat.mps_sites()
psi = MPS.from_product_state(sites, ['up'] * N, "finite")
dmrg_params = {"trunc_params": {"chi_max": 100, "svd_min": 1.e-10}, "mixer": True}
info = dmrg.run(psi, model, dmrg_params)
print("E =", info['E'])
# E = -20.01638790048513
print("max. bond dimension =", max(psi.chi))
# max. bond dimension = 27
```

The switch from DMRG to `gls{iDMRG}` in TeNPy is simply accomplished by a change of the parameter `"bc_MPS"` from `"finite"` to `"infinite"`, both for the model and the state. The returned `E` is then the energy density per site. Due to the translation invariance, one can also evaluate the correlation length, here slightly away from the critical point.

```
"""Call of infinite DMRG."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFChain
from tenpy.algorithms import dmrg
```

(continues on next page)

(continued from previous page)

```

N = 2 # number of sites in unit cell
model = TFChain({"L": N, "J": 1., "g": 1.1, "bc_MPS": "infinite"})
sites = model.lat.mps_sites()
psi = MPS.from_product_state(sites, ['up'] * N, "infinite")
dmrg_params = {"trunc_params": {"chi_max": 100, "svd_min": 1.e-10}, "mixer": True}
info = dmrg.run(psi, model, dmrg_params)
print("E =", info['E'])
# E = -1.342864022725017
print("max. bond dimension =", max(psi.chi))
# max. bond dimension = 56
print("corr. length =", psi.correlation_length())
# corr. length = 4.915809146764157

```

Running time evolution with TEBD requires an additional loop, during which the desired observables have to be measured. The following code shows this directly for the infinite version of TEBD.

```

"""Call of (infinite) TEBD."""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFChain
from tenpy.algorithms import tebd

M = TFChain({"L": 2, "J": 1., "g": 1.5, "bc_MPS": "infinite"})
psi = MPS.from_product_state(M.lat.mps_sites(), [0] * 2, "infinite")
tebd_params = {
    "order": 2,
    "delta_tau_list": [0.1, 0.001, 1.e-5],
    "max_error_E": 1.e-6,
    "trunc_params": {
        "chi_max": 30,
        "svd_min": 1.e-10
    }
}
eng = tebd.Engine(psi, M, tebd_params)
eng.run_GS() # imaginary time evolution with TEBD
print("E =", sum(psi.expectation_value(M.H_bond)) / psi.L)
print("final bond dimensions: ", psi.chi)

```

7.3.2 Toy Codes

The following “toy codes” are included in the TeNPy repository in the folder `toycodes/`, we include them here in the documentation for reference. They are meant to give you a flavor of the different algorithms, while keeping the codes as readable and simple as possible. The only requirements to run them are Python 3, Numpy, and Scipy. Simply go to the folder where you downloaded them, and execute them with python.

Toycode a_mps.py

```

"""Toy code implementing a matrix product state."""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np
from scipy.linalg import svd
# if you get an error message "LinAlgError: SVD did not converge",
# uncomment the following line. (This requires TeNPy to be installed.)
# from tenpy.linalg.svd_robust import svd # (works like scipy.linalg.svd)

class SimpleMPS:
    """Simple class for a matrix product state.

    We index sites with `i` from 0 to L-1; bond `i` is left of site `i`.
    We *assume* that the state is in right-canonical form.

    Parameters
    -----
    Bs, Ss, bc:
        Same as attributes.

    Attributes
    -----
    Bs : list of np.Array[ndim=3]
        The 'matrices' in right-canonical form, one for each physical site
        (within the unit-cell for an infinite MPS).
        Each `B[i]` has legs (virtual left, physical, virtual right), in short ``vL i
    vR``
    Ss : list of np.Array[ndim=1]
        The Schmidt values at each of the bonds, ``Ss[i]`` is left of ``Bs[i]``.
    bc : 'infinite', 'finite'
        Boundary conditions.
    L : int
        Number of sites (in the unit-cell for an infinite MPS).
    nbonds : int
        Number of (non-trivial) bonds: L-1 for 'finite' boundary conditions
    """
    def __init__(self, Bs, Ss, bc='finite'):
        assert bc in ['finite', 'infinite']
        self.Bs = Bs
        self.Ss = Ss
        self.bc = bc
        self.L = len(Bs)
        self.nbonds = self.L - 1 if self.bc == 'finite' else self.L

    def copy(self):
        return SimpleMPS([B.copy() for B in self.Bs], [S.copy() for S in self.Ss],
        self.bc)

    def get_thetal(self, i):
        """Calculate effective single-site wave function on sites i in mixed
        canonical form.

        The returned array has legs ``vL, i, vR`` (as one of the Bs).
        """

```

(continues on next page)

(continued from previous page)

```

    return np.tensordot(np.diag(self.Ss[i]), self.Bs[i], [1, 0]) # vL [vL'],
↪ [vL] i vR

    def get_theta2(self, i):
        """Calculate effective two-site wave function on sites i,j=(i+1) in mixed
↪ canonical form.

        The returned array has legs ``vL, i, j, vR``.
        """
        j = (i + 1) % self.L
        return np.tensordot(self.get_theta1(i), self.Bs[j], [2, 0]) # vL i [vR],
↪ [vL] j vR

    def get_chi(self):
        """Return bond dimensions."""
        return [self.Bs[i].shape[2] for i in range(self.nbonds)]

    def site_expectation_value(self, op):
        """Calculate expectation values of a local operator at each site."""
        result = []
        for i in range(self.L):
            theta = self.get_theta1(i) # vL i vR
            op_theta = np.tensordot(op, theta, axes=[1, 1]) # i [i*], vL [i] vR
            result.append(np.tensordot(theta.conj(), op_theta, [[0, 1, 2], [1, 0,
↪ 2]]))
            # [vL*] [i*] [vR*], [i] [vL] [vR]
        return np.real_if_close(result)

    def bond_expectation_value(self, op):
        """Calculate expectation values of a local operator at each bond."""
        result = []
        for i in range(self.nbonds):
            theta = self.get_theta2(i) # vL i j vR
            op_theta = np.tensordot(op[i], theta, axes=[[2, 3], [1, 2]])
            # i j [i*] [j*], vL [i] [j] vR
            result.append(np.tensordot(theta.conj(), op_theta, [[0, 1, 2, 3], [2, 0,
↪ 1, 3]]))
            # [vL*] [i*] [j*] [vR*], [i] [j] [vL] [vR]
        return np.real_if_close(result)

    def entanglement_entropy(self):
        """Return the (von-Neumann) entanglement entropy for a bipartition at any of
↪ the bonds."""
        bonds = range(1, self.L) if self.bc == 'finite' else range(0, self.L)
        result = []
        for i in bonds:
            S = self.Ss[i].copy()
            S[S < 1.e-20] = 0. # 0*log(0) should give 0; avoid warning or NaN.
            S2 = S * S
            assert abs(np.linalg.norm(S) - 1.) < 1.e-14
            result.append(-np.sum(S2 * np.log(S2)))
        return np.array(result)

    def correlation_length(self):
        """Diagonalize transfer matrix to obtain the correlation length."""
        import scipy.sparse.linalg.eigen.arpack as arp
        assert self.bc == 'infinite' # works only in the infinite case

```

(continues on next page)

(continued from previous page)

```

    B = self.Bs[0] # vL i vR
    chi = B.shape[0]
    T = np.tensordot(B, np.conj(B), axes=[1, 1]) # vL [i] vR, vL* [i*] vR*
    T = np.transpose(T, [0, 2, 1, 3]) # vL vL* vR vR*
    for i in range(1, self.L):
        B = self.Bs[i]
        T = np.tensordot(T, B, axes=[2, 0]) # vL vL* [vR] vR*, [vL] i vR
        T = np.tensordot(T, np.conj(B), axes=[[2, 3], [0, 1]])
        # vL vL* [vR*] [i] vR, [vL*] [i*] vR*
    T = np.reshape(T, (chi**2, chi**2))
    # Obtain the 2nd largest eigenvalue
    eta = arp.eigs(T, k=2, which='LM', return_eigenvectors=False, ncv=20)
    return -self.L / np.log(np.min(np.abs(eta)))

def init_FM_MPS(L, d, bc='finite'):
    """Return a ferromagnetic MPS (= product state with all spins up)"""
    B = np.zeros([1, d, 1], np.float)
    B[0, 0, 0] = 1.
    S = np.ones([1], np.float)
    Bs = [B.copy() for i in range(L)]
    Ss = [S.copy() for i in range(L)]
    return SimpleMPS(Bs, Ss, bc)

def split_truncate_theta(theta, chi_max, eps):
    """Split and truncate a two-site wave function in mixed canonical form.

    Split a two-site wave function as follows:
        vL --(theta)-- vR      =>      vL --(A)--diag(S)--(B)-- vR
            |      |                      |      |
            i      j                      i      j

    Afterwards, truncate in the new leg (labeled ``vC``).

    Parameters
    -----
    theta : np.Array[ndim=4]
        Two-site wave function in mixed canonical form, with legs ``vL, i, j, vR``.
    chi_max : int
        Maximum number of singular values to keep
    eps : float
        Discard any singular values smaller than that.

    Returns
    -----
    A : np.Array[ndim=3]
        Left-canonical matrix on site i, with legs ``vL, i, vC``
    S : np.Array[ndim=1]
        Singular/Schmidt values.
    B : np.Array[ndim=3]
        Right-canonical matrix on site j, with legs ``vC, j, vR``
    """
    chivL, dL, dR, chivR = theta.shape
    theta = np.reshape(theta, [chivL * dL, dR * chivR])
    X, Y, Z = svd(theta, full_matrices=False)
    # truncate

```

(continues on next page)

(continued from previous page)

```

chivC = min(chi_max, np.sum(Y > eps))
piv = np.argsort(Y)[::-1][:chivC] # keep the largest `chivC` singular values
X, Y, Z = X[:, piv], Y[piv], Z[piv, :]
# renormalize
S = Y / np.linalg.norm(Y) # == Y/sqrt(sum(Y**2))
# split legs of X and Z
A = np.reshape(X, [chivL, dL, chivC])
B = np.reshape(Z, [chivC, dR, chivR])
return A, S, B

```

Toycode b_model.py

```

"""Toy code implementing the transverse-field ising model."""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np

class TFIModel:
    """Simple class generating the Hamiltonian of the transverse-field Ising model.

    The Hamiltonian reads
    .. math ::
        H = - J \sum_i \sigma^x_i \sigma^x_{i+1} - g \sum_i \sigma^z_i

    Parameters
    -----
    L : int
        Number of sites.
    J, g : float
        Coupling parameters of the above defined Hamiltonian.
    bc : 'infinite', 'finite'
        Boundary conditions.

    Attributes
    -----
    L : int
        Number of sites.
    bc : 'infinite', 'finite'
        Boundary conditions.
    sigmax, sigmay, sigmaz, id :
        Local operators, namely the Pauli matrices and identity.
    H_bonds : list of np.Array[ndim=4]
        The Hamiltonian written in terms of local 2-site operators, ``H = sum_i H_
    ↪ bonds[i]``.
        Each ``H_bonds[i]`` has (physical) legs (i out, (i+1) out, i in, (i+1) in),
        in short ``i j i* j*``.
    H_mpo : list of np.Array[ndim=4]
        The Hamiltonian written as an MPO.
        Each ``H_mpo[i]`` has legs (virtual left, virtual right, physical out,
    ↪ physical in),
        in short ``wL wR i i*``.
    """
    def __init__(self, L, J, g, bc='finite'):
        assert bc in ['finite', 'infinite']

```

(continues on next page)

(continued from previous page)

```

self.L, self.d, self.bc = L, 2, bc
self.J, self.g = J, g
self.sigmax = np.array([[0., 1.], [1., 0.]])
self.sigmay = np.array([[0., -1j], [1j, 0.]])
self.sigmaz = np.array([[1., 0.], [0., -1.]])
self.id = np.eye(2)
self.init_H_bonds()
self.init_H_mpo()

def init_H_bonds(self):
    """Initialize `H_bonds` hamiltonian.

    Called by __init__().
    """
    sx, sz, id = self.sigmax, self.sigmaz, self.id
    d = self.d
    nbonds = self.L - 1 if self.bc == 'finite' else self.L
    H_list = []
    for i in range(nbonds):
        gL = gR = 0.5 * self.g
        if self.bc == 'finite':
            if i == 0:
                gL = self.g
            if i + 1 == self.L - 1:
                gR = self.g
        H_bond = -self.J * np.kron(sx, sx) - gL * np.kron(sz, id) - gR * np.
        ↪kron(id, sz)
        # H_bond has legs ``i, j, i*, j*``
        H_list.append(np.reshape(H_bond, [d, d, d, d]))
    self.H_bonds = H_list

# (note: not required for TEBD)
def init_H_mpo(self):
    """Initialize `H_mpo` Hamiltonian.

    Called by __init__().
    """
    w_list = []
    for i in range(self.L):
        w = np.zeros((3, 3, self.d, self.d), dtype=np.float)
        w[0, 0] = w[2, 2] = self.id
        w[0, 1] = self.sigmax
        w[0, 2] = -self.g * self.sigmaz
        w[1, 2] = -self.J * self.sigmax
        w_list.append(w)
    self.H_mpo = w_list

```

Toycode c_tebd.py

```

"""Toy code implementing the time evolving block decimation (TEBD)."""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np
from scipy.linalg import expm
from a_mps import split_truncate_theta

def calc_U_bonds(H_bonds, dt):
    """Given the H_bonds, calculate ``U_bonds[i] = expm(-dt*H_bonds[i])``.

    Each local operator has legs (i out, (i+1) out, i in, (i+1) in), in short ``i j_
    ↪ i* j*``.
    Note that no imaginary 'i' is included, thus real 'dt' means 'imaginary time'
    ↪ evolution!
    """
    d = H_bonds[0].shape[0]
    U_bonds = []
    for H in H_bonds:
        H = np.reshape(H, [d * d, d * d])
        U = expm(-dt * H)
        U_bonds.append(np.reshape(U, [d, d, d, d]))
    return U_bonds

def run_TEBD(psi, U_bonds, N_steps, chi_max, eps):
    """Evolve for `N_steps` time steps with TEBD."""
    Nbonds = psi.L - 1 if psi.bc == 'finite' else psi.L
    assert len(U_bonds) == Nbonds
    for n in range(N_steps):
        for k in [0, 1]: # even, odd
            for i_bond in range(k, Nbonds, 2):
                update_bond(psi, i_bond, U_bonds[i_bond], chi_max, eps)
    # done

def update_bond(psi, i, U_bond, chi_max, eps):
    """Apply `U_bond` acting on i,j=(i+1) to `psi`."""
    j = (i + 1) % psi.L
    # construct theta matrix
    theta = psi.get_theta2(i) # vL i j vR
    # apply U
    Utheta = np.tensordot(U_bond, theta, axes=([2, 3], [1, 2])) # i j [i*] [j*], vL_
    ↪ [i] [j] vR
    Utheta = np.transpose(Utheta, [2, 0, 1, 3]) # vL i j vR
    # split and truncate
    Ai, Sj, Bj = split_truncate_theta(Utheta, chi_max, eps)
    # put back into MPS
    Gi = np.tensordot(np.diag(psi.Ss[i]**(-1)), Ai, axes=[1, 0]) # vL [vL*], [vL] i_
    ↪ vC
    psi.Bs[i] = np.tensordot(Gi, np.diag(Sj), axes=[2, 0]) # vL i [vC], [vC] vC
    psi.Ss[j] = Sj # vC
    psi.Bs[j] = Bj # vC j vR

```

(continues on next page)

(continued from previous page)

```

def example_TEBD_gs_tf_ising_finite(L, g):
    print("finite TEBD, imaginary time evolution, transverse field Ising")
    print("L={L:d}, g={g:.2f}".format(L=L, g=g))
    import a_mps
    import b_model
    M = b_model.TFIModel(L=L, J=1., g=g, bc='finite')
    psi = a_mps.init_FM_MPS(M.L, M.d, M.bc)
    for dt in [0.1, 0.01, 0.001, 1.e-4, 1.e-5]:
        U_bonds = calc_U_bonds(M.H_bonds, dt)
        run_TEBD(psi, U_bonds, N_steps=500, chi_max=30, eps=1.e-10)
        E = np.sum(psi.bond_expectation_value(M.H_bonds))
        print("dt = {dt:.5f}: E = {E:.13f}".format(dt=dt, E=E))
    print("final bond dimensions: ", psi.get_chi())
    mag_x = np.sum(psi.site_expectation_value(M.sigmax))
    mag_z = np.sum(psi.site_expectation_value(M.sigmaz))
    print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
    print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
    if L < 20: # compare to exact result
        from tfi_exact import finite_gs_energy
        E_exact = finite_gs_energy(L, 1., g)
        print("Exact diagonalization: E = {E:.13f}".format(E=E_exact))
        print("relative error: ", abs((E - E_exact) / E_exact))
    return E, psi, M

def example_TEBD_gs_tf_ising_infinite(g):
    print("infinite TEBD, imaginary time evolution, transverse field Ising")
    print("g={g:.2f}".format(g=g))
    import a_mps
    import b_model
    M = b_model.TFIModel(L=2, J=1., g=g, bc='infinite')
    psi = a_mps.init_FM_MPS(M.L, M.d, M.bc)
    for dt in [0.1, 0.01, 0.001, 1.e-4, 1.e-5]:
        U_bonds = calc_U_bonds(M.H_bonds, dt)
        run_TEBD(psi, U_bonds, N_steps=500, chi_max=30, eps=1.e-10)
        E = np.mean(psi.bond_expectation_value(M.H_bonds))
        print("dt = {dt:.5f}: E (per site) = {E:.13f}".format(dt=dt, E=E))
    print("final bond dimensions: ", psi.get_chi())
    mag_x = np.mean(psi.site_expectation_value(M.sigmax))
    mag_z = np.mean(psi.site_expectation_value(M.sigmaz))
    print("<sigma_x> = {mag_x:.5f}".format(mag_x=mag_x))
    print("<sigma_z> = {mag_z:.5f}".format(mag_z=mag_z))
    print("correlation length: ", psi.correlation_length())
    # compare to exact result
    from tfi_exact import infinite_gs_energy
    E_exact = infinite_gs_energy(1., g)
    print("Analytic result: E (per site) = {E:.13f}".format(E=E_exact))
    print("relative error: ", abs((E - E_exact) / E_exact))
    return E, psi, M

def example_TEBD_tf_ising_lightcone(L, g, tmax, dt):
    print("finite TEBD, real time evolution, transverse field Ising")
    print("L={L:d}, g={g:.2f}, tmax={tmax:.2f}, dt={dt:.3f}".format(L=L, g=g,
    ↪ tmax=tmax, dt=dt))
    # find ground state with TEBD or DMRG
    # E, psi, M = example_TEBD_gs_tf_ising_finite(L, g)

```

(continues on next page)

(continued from previous page)

```

from d_dmrg import example_DMRG_tf_ising_finite
E, psi, M = example_DMRG_tf_ising_finite(L, g)
i0 = L // 2
# apply sigmaz on site i0
SzB = np.tensordot(M.sigmaz, psi.Bs[i0], axes=[1, 1]) # i [i*], vL [i] vR
psi.Bs[i0] = np.transpose(SzB, [1, 0, 2]) # vL i vR
U_bonds = calc_U_bonds(M.H_bonds, 1.j * dt) # (imaginary dt -> realtime_
-> evolution)
S = [psi.entanglement_entropy()]
Nsteps = int(tmax / dt + 0.5)
for n in range(Nsteps):
    if abs((n * dt + 0.1) % 0.2 - 0.1) < 1.e-10:
        print("t = {t:.2f}, chi = ".format(t=n * dt), psi.get_chi())
        run_TEBD(psi, U_bonds, 1, chi_max=50, eps=1.e-10)
        S.append(psi.entanglement_entropy())
import matplotlib.pyplot as plt
plt.figure()
plt.imshow(S[:-1],
            vmin=0.,
            aspect='auto',
            interpolation='nearest',
            extent=(0, L - 1., -0.5 * dt, (Nsteps + 0.5) * dt))
plt.xlabel('site $i$')
plt.ylabel('time $t/J$')
plt.ylim(0., tmax)
plt.colorbar().set_label('entropy $$$')
filename = 'c_tebd_lightcone_{g:.2f}.pdf'.format(g=g)
plt.savefig(filename)
print("saved " + filename)

if __name__ == "__main__":
    example_TEBD_gs_tf_ising_finite(L=10, g=1.)
    print("-" * 100)
    example_TEBD_gs_tf_ising_infinite(g=1.5)
    print("-" * 100)
    example_TEBD_tf_ising_lightcone(L=20, g=1.5, tmax=3., dt=0.01)

```

Toycode d_dmrg.py

```

"""Toy code implementing the density-matrix renormalization group (DMRG)."""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np
from a_mps import split_truncate_theta
import scipy.sparse
import scipy.sparse.linalg.eigen.arpack as arp

class SimpleHeff(scipy.sparse.linalg.LinearOperator):
    """Class for the effective Hamiltonian.

    To be diagonalized in `SimpleDMRGEngine.update_bond`. Looks like this::

        .--vL*          vR*--.
    """

```

(continues on next page)

(continued from previous page)

```

/      i*      j*      /
/      /      /      /
(LP)---(W1)--(W2)----(RP)
/      /      /      /
/      i      j      /
.--vL                      vR--.

"""
def __init__(self, LP, RP, W1, W2):
    self.LP = LP # vL wL* vL*
    self.RP = RP # vR* wR* vR
    self.W1 = W1 # wL wC i i*
    self.W2 = W2 # wC wR j j*
    chi1, chi2 = LP.shape[0], RP.shape[2]
    d1, d2 = W1.shape[2], W2.shape[2]
    self.theta_shape = (chi1, d1, d2, chi2) # vL i j vR
    self.shape = (chi1 * d1 * d2 * chi2, chi1 * d1 * d2 * chi2)
    self.dtype = W1.dtype

def _matvec(self, theta):
    """Calculate |theta> = H_eff |theta>.

    This function is used by :func:scipy.sparse.linalg.eigen.arpack.eigsh` to
    ↪diagonalize
    the effective Hamiltonian with a Lanczos method, withouth generating the full
    ↪matrix."""
    x = np.reshape(theta, self.theta_shape) # vL i j vR
    x = np.tensordot(self.LP, x, axes=(2, 0)) # vL wL* [vL*], [vL] i j vR
    x = np.tensordot(x, self.W1, axes=([1, 2], [0, 3])) # vL [wL*] [i] j vR,
    ↪[wL] wC i [i*]
    x = np.tensordot(x, self.W2, axes=([3, 1], [0, 3])) # vL [j] vR [wC] i, [wC]
    ↪wR j [j*]
    x = np.tensordot(x, self.RP, axes=([1, 3], [0, 1])) # vL [vR] i [wR] j,
    ↪[vR*] [wR*] vR
    x = np.reshape(x, self.shape[0])
    return x

class SimpleDMRGEngine:
    """DMRG algorithm, implemented as class holding the necessary data.

    Parameters
    -----
    psi, model, chi_max, eps:
        See attributes

    Attributes
    -----
    psi : SimpleMPS
        The current ground-state (approximation).
    model :
        The model of which the groundstate is to be calculated.
    chi_max, eps:
        Truncation parameters, see :func:`a_mps.split_truncate_theta`.
    LPs, RPs : list of np.Array[ndim=3]
        Left and right parts ("environments") of the effective Hamiltonian.
        ``LPs[i]`` is the contraction of all parts left of site `i` in the network ``
    ↪<psi|H|psi>``,

```

(continues on next page)

(continued from previous page)

```

    and similar ``RPs[i]`` for all parts right of site `i`.
    Each ``LPs[i]`` has legs ``vL wL* vL*``, ``RPs[i]`` has legs ``vR* wR* vR``
    """
    def __init__(self, psi, model, chi_max, eps):
        assert psi.L == model.L and psi.bc == model.bc # ensure compatibility
        self.H_mpo = model.H_mpo
        self.psi = psi
        self.LPs = [None] * psi.L
        self.RPs = [None] * psi.L
        self.chi_max = chi_max
        self.eps = eps
        # initialize left and right environment
        D = self.H_mpo[0].shape[0]
        chi = psi.Bs[0].shape[0]
        LP = np.zeros([chi, D, chi], dtype=np.float) # vL wL* vL*
        RP = np.zeros([chi, D, chi], dtype=np.float) # vR* wR* vR
        LP[:, 0, :] = np.eye(chi)
        RP[:, D - 1, :] = np.eye(chi)
        self.LPs[0] = LP
        self.RPs[-1] = RP
        # initialize necessary RPs
        for i in range(psi.L - 1, 1, -1):
            self.update_RP(i)

    def sweep(self):
        # sweep from left to right
        for i in range(self.psi.nbonds - 1):
            self.update_bond(i)
        # sweep from right to left
        for i in range(self.psi.nbonds - 1, 0, -1):
            self.update_bond(i)

    def update_bond(self, i):
        j = (i + 1) % self.psi.L
        # get effective Hamiltonian
        Heff = SimpleHeff(self.LPs[i], self.RPs[j], self.H_mpo[i], self.H_mpo[j])
        # Diagonalize Heff, find ground state `theta`
        theta0 = np.reshape(self.psi.get_theta2(i), [Heff.shape[0]]) # initial guess
        e, v = arp.eigsh(Heff, k=1, which='SA', return_eigenvectors=True, v0=theta0)
        theta = np.reshape(v[:, 0], Heff.theta_shape)
        # split and truncate
        Ai, Sj, Bj = split_truncate_theta(theta, self.chi_max, self.eps)
        # put back into MPS
        Gi = np.tensordot(np.diag(self.psi.Ss[i]**(-1)), Ai, axes=[1, 0]) # vL [vL*],
        # [vL] i vC
        self.psi.Bs[i] = np.tensordot(Gi, np.diag(Sj), axes=[2, 0]) # vL i [vC],
        # [vC*] vC
        self.psi.Ss[j] = Sj # vC
        self.psi.Bs[j] = Bj # vC j vR
        self.update_LP(i)
        self.update_RP(j)

    def update_RP(self, i):
        """Calculate RP right of site `i-1` from RP right of site `i`."""
        j = (i - 1) % self.psi.L
        RP = self.RPs[i] # vR* wR* vR
        B = self.psi.Bs[i] # vL i vR

```

(continues on next page)

(continued from previous page)

```

Bc = B.conj() # vL* i* vR*
W = self.H_mpo[i] # wL wR i i*
RP = np.tensordot(B, RP, axes=[2, 0]) # vL i [vR], [vR*] wR* vR
RP = np.tensordot(RP, W, axes=[[1, 2], [3, 1]]) # vL [i] [wR*] vR, wL [wR] i
→ [i*]
RP = np.tensordot(RP, Bc, axes=[[1, 3], [2, 1]]) # vL [vR] wL [i], vL* [i*]
→ [vR*]
self.RPs[j] = RP # vL wL vL* (== vR* wR* vR on site i-1)

def update_LP(self, i):
    """Calculate LP left of site `i+1` from LP left of site `i`."""
    j = (i + 1) % self.psi.L
    LP = self.LPs[i] # vL wL vL*
    B = self.psi.Bs[i] # vL i vR
    G = np.tensordot(np.diag(self.psi.Ss[i]), B, axes=[1, 0]) # vL [vL*], [vL] i
→ vR
    A = np.tensordot(G, np.diag(self.psi.Ss[j]**-1), axes=[2, 0]) # vL i [vR],
→ [vR*] vR
    Ac = A.conj() # vL* i* vR*
    W = self.H_mpo[i] # wL wR i i*
    LP = np.tensordot(LP, A, axes=[2, 0]) # vL wL* [vL*], [vL] i vR
    LP = np.tensordot(W, LP, axes=[[0, 3], [1, 2]]) # [wL] wR i [i*], vL [wL*]
→ [i] vR
    LP = np.tensordot(Ac, LP, axes=[[0, 1], [2, 1]]) # [vL*] [i*] vR*, wR [i]
→ [vL] vR
    self.LPs[j] = LP # vR* wR vR (== vL wL* vL* on site i+1)

def example_DMRG_tf_ising_finite(L, g):
    print("finite DMRG, transverse field Ising")
    print("L={L:d}, g={g:.2f}".format(L=L, g=g))
    import a_mps
    import b_model
    M = b_model.TFIModel(L=L, J=1., g=g, bc='finite')
    psi = a_mps.init_FM_MPS(M.L, M.d, M.bc)
    eng = SimpleDMRGEngine(psi, M, chi_max=30, eps=1.e-10)
    for i in range(10):
        eng.sweep()
        E = np.sum(psi.bond_expectation_value(M.H_bonds))
        print("sweep {i:2d}: E = {E:.13f}".format(i=i + 1, E=E))
    print("final bond dimensions: ", psi.get_chi())
    mag_x = np.sum(psi.site_expectation_value(M.sigmax))
    mag_z = np.sum(psi.site_expectation_value(M.sigmaz))
    print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
    print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
    if L < 20: # compare to exact result
        from tfi_exact import finite_gs_energy
        E_exact = finite_gs_energy(L, 1., g)
        print("Exact diagonalization: E = {E:.13f}".format(E=E_exact))
        print("relative error: ", abs((E - E_exact) / E_exact))
    return E, psi, M

def example_DMRG_tf_ising_infinite(g):
    print("infinite DMRG, transverse field Ising")
    print("g={g:.2f}".format(g=g))
    import a_mps

```

(continues on next page)

(continued from previous page)

```

import b_model
M = b_model.TFIModel(L=2, J=1., g=g, bc='infinite')
psi = a_mps.init_FM_MPS(M.L, M.d, M.bc)
eng = SimpleDMRGEngine(psi, M, chi_max=20, eps=1.e-14)
for i in range(20):
    eng.sweep()
    E = np.mean(psi.bond_expectation_value(M.H_bonds))
    print("sweep {i:2d}: E (per site) = {E:.13f}".format(i=i + 1, E=E))
print("final bond dimensions: ", psi.get_chi())
mag_x = np.mean(psi.site_expectation_value(M.sigmax))
mag_z = np.mean(psi.site_expectation_value(M.sigmaz))
print("<sigma_x> = {mag_x:.5f}".format(mag_x=mag_x))
print("<sigma_z> = {mag_z:.5f}".format(mag_z=mag_z))
print("correlation length:", psi.correlation_length())
# compare to exact result
from tfi_exact import infinite_gs_energy
E_exact = infinite_gs_energy(1., g)
print("Analytic result: E (per site) = {E:.13f}".format(E=E_exact))
print("relative error: ", abs((E - E_exact) / E_exact))
return E, psi, M

if __name__ == "__main__":
    example_DMRG_tfi_ising_finite(L=10, g=1.)
    print("-" * 100)
    example_DMRG_tfi_ising_infinite(g=1.5)

```

Toycode tfi_exact.py

```

"""Provides exact ground state energies for the transverse field ising model for_
↪comparison.

The Hamiltonian reads
.. math ::
    H = - J \sum_{i} \sigma^x_i \sigma^x_{i+1} - g \sum_{i} \sigma^z_i
"""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

import numpy as np
import scipy.sparse as sparse
import scipy.sparse.linalg.eigen.arpack as arp
import warnings
import scipy.integrate

def finite_gs_energy(L, J, g):
    """For comparison: obtain ground state energy from exact diagonalization.

    Exponentially expensive in L, only works for small enough `L` <~ 20.
    """
    if L >= 20:
        warnings.warn("Large L: Exact diagonalization might take a long time!")
    # get single site operators
    sx = sparse.csr_matrix(np.array([[0., 1.], [1., 0.])))
    sz = sparse.csr_matrix(np.array([[1., 0.], [0., -1.])))

```

(continues on next page)

(continued from previous page)

```

id = sparse.csr_matrix(np.eye(2))
sx_list = [] # sx_list[i] = kron([id, id, ..., id, sx, id, .... id])
sz_list = []
for i_site in range(L):
    x_ops = [id] * L
    z_ops = [id] * L
    x_ops[i_site] = sx
    z_ops[i_site] = sz
    X = x_ops[0]
    Z = z_ops[0]
    for j in range(1, L):
        X = sparse.kron(X, x_ops[j], 'csr')
        Z = sparse.kron(Z, z_ops[j], 'csr')
    sx_list.append(X)
    sz_list.append(Z)
H_xx = sparse.csr_matrix((2**L, 2**L))
H_z = sparse.csr_matrix((2**L, 2**L))
for i in range(L - 1):
    H_xx = H_xx + sx_list[i] * sx_list[(i + 1) % L]
for i in range(L):
    H_z = H_z + sz_list[i]
H = -J * H_xx - g * H_z
E, V = arp.eigsh(H, k=1, which='SA', return_eigenvectors=True, ncv=20)
return E[0]

def infinite_gs_energy(J, g):
    """For comparison: Calculate groundstate energy density from analytic formula.

    The analytic formula stems from mapping the model to free fermions, see P. Pfeuty,
    ↪ The one-
    dimensional Ising model with a transverse field, Annals of Physics 57, p. 79
    ↪ (1970). Note that
    we use Pauli matrices compared this reference using spin-1/2 matrices and replace
    ↪ the sum_k ->
    integral dk/2pi to obtain the result in the N -> infinity limit.
    """
    def f(k, lambda_):
        return np.sqrt(1 + lambda_**2 + 2 * lambda_ * np.cos(k))

    E0_exact = -g / (J * 2. * np.pi) * scipy.integrate.quad(f, -np.pi, np.pi, args=(J,
    ↪ g, ))[0]
    return E0_exact

```

7.3.3 Example codes

The following “examples” are included in the TeNPy repository in the folder `examples/`, we include them here in the documentation for reference. These examples are meant to give an idea how to use the library and demonstrate parts of the interface. It might be helpful to compare some of them (e.g., `c_tebd.py` and `d_dmrg.py`) to the *Toy Codes*. To run these examples, you have to have TeNPy installed, see *Installation instructions*. You do not need to save the examples inside the `tenpy` folder/repository, but you can execute them from anywhere (if TeNPy is installed correctly).

Example code `a_np_conserved.py`

```

"""An example code to demonstrate the usage of :class:`~tenpy.linalg.np_conserved.
↪Array`.

This example includes the following steps:
1) create Arrays for an Neel MPS
2) create an MPO representing the nearest-neighbour AFM Heisenberg Hamiltonian
3) define 'environments' left and right
4) contract MPS and MPO to calculate the energy
5) extract two-site hamiltonian ``H2`` from the MPO
6) calculate ``exp(-1.j*dt*H2)`` by diagonalization of H2
7) apply ``exp(H2)`` to two sites of the MPS and truncate with svd

Note that this example uses only np_conserved, but no other modules.
Compare it to the example `b_mps.py`,
which does the same steps using a few predefined classes like MPS and MPO.
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import tenpy.linalg.np_conserved as npc
import numpy as np

# model parameters
Jxx, Jz = 1., 1.
L = 20
dt = 0.1
cutoff = 1.e-10
print("Jxx={Jxx}, Jz={Jz}, L={L:d}".format(Jxx=Jxx, Jz=Jz, L=L))

print("1) create Arrays for an Neel MPS")

#   vL ->--B-->- vR
#       |
#       ^
#       |
#       p

# create a ChargeInfo to specify the nature of the charge
chinfo = npc.ChargeInfo([1], ['2*Sz']) # the second argument is just a descriptive_
↪name

# create LegCharges on physical leg and even/odd bonds
p_leg = npc.LegCharge.from_qflat(chinfo, [[1], [-1]]) # charges for up, down
v_leg_even = npc.LegCharge.from_qflat(chinfo, [[0]])
v_leg_odd = npc.LegCharge.from_qflat(chinfo, [[1]])

B_even = npc.zeros([v_leg_even, v_leg_odd.conj(), p_leg],

```

(continues on next page)

(continued from previous page)

```

        labels=['vL', 'vR', 'p']) # virtual left/right, physical
B_odd = npc.zeros([v_leg_odd, v_leg_even.conj(), p_leg], labels=['vL', 'vR', 'p'])
B_even[0, 0, 0] = 1. # up
B_odd[0, 0, 1] = 1. # down

Bs = [B_even, B_odd] * (L // 2) + [B_even] * (L % 2) # (right-canonical)
Ss = [np.ones(1)] * L # Ss[i] are singular values between Bs[i-1] and Bs[i]

# Side remark:
# An MPS is expected to have non-zero entries everywhere compatible with the charges.
# In general, we recommend to use `sort_legcharge` (or `as_completely_blocked`)
# to ensure complete blocking. (But the code will also work, if you don't do it.)
# The drawback is that this might introduce permutations in the indices of single_
↪ legs,
# which you have to keep in mind when converting dense numpy arrays to and from npc.
↪ Arrays.

print("2) create an MPO representing the AFM Heisenberg Hamiltonian")

#
#      p*
#      |
#      ^
#      |
# wL ->--W-->- wR
#      |
#      ^
#      |
#      p

# create physical spin-1/2 operators Sz, S+, S-
Sz = npc.Array.from_ndarray([[0.5, 0.], [0., -0.5]], [p_leg, p_leg.conj()], labels=['p',
↪ 'p*'])
Sp = npc.Array.from_ndarray([[0., 1.], [0., 0.]], [p_leg, p_leg.conj()], labels=['p',
↪ 'p*'])
Sm = npc.Array.from_ndarray([[0., 0.], [1., 0.]], [p_leg, p_leg.conj()], labels=['p',
↪ 'p*'])
Id = npc.eye_like(Sz, labels=Sz.get_leg_labels()) # identity

mpo_leg = npc.LegCharge.from_qflat(chinfo, [[0], [2], [-2], [0], [0]])

W_grid = [[Id, Sp, Sm, Sz, None],
[None, None, None, None, 0.5 * Jxx * Sm],
[None, None, None, None, 0.5 * Jxx * Sp],
[None, None, None, None, Jz * Sz],
[None, None, None, None, Id]] # yapf:disable

W = npc.grid_outer(W_grid, [mpo_leg, mpo_leg.conj()], grid_labels=['wL', 'wR'])
# wL/wR = virtual left/right of the MPO
Ws = [W] * L

print("3) define 'environments' left and right")

# .---->- vR      vL ->----.
# |
# envL->- wR      wL ->-envR
# |
# .---->- vR*      vL*->----.

```

(continues on next page)

(continued from previous page)

```

envL = npc.zeros([W.get_leg('wL').conj(), Bs[0].get_leg('vL').conj(), Bs[0].get_leg(
    ↪ 'vL')],
                labels=['wR', 'vR', 'vR*'])
envL[0, :, :] = npc.diag(1., envL.legs[1])
envR = npc.zeros([W.get_leg('wR').conj(), Bs[-1].get_leg('vR').conj(), Bs[-1].get_leg(
    ↪ 'vR')],
                labels=['wL', 'vL', 'vL*'])
envR[-1, :, :] = npc.diag(1., envR.legs[1])

print("4) contract MPS and MPO to calculate the energy <psi|H|psi>")
contr = envL
for i in range(L):
    # contr labels: wR, vR, vR*
    contr = npc.tensordot(contr, Bs[i], axes=('vR', 'vL'))
    # wR, vR*, vR, p
    contr = npc.tensordot(contr, Ws[i], axes=(['p', 'wR'], ['p*', 'wL']))
    # vR*, vR, wR, p
    contr = npc.tensordot(contr, Bs[i].conj(), axes=(['p', 'vR*'], ['p*', 'vL*']))
    # vR, wR, vR*
    # note that the order of the legs changed, but that's no problem with labels:
    # the arrays are automatically transposed as necessary
E = npc.inner(contr, envR, axes=(['vR', 'wR', 'vR*'], ['vL', 'wL', 'vL*']))
print("E =", E)

print("5) calculate two-site hamiltonian ``H2`` from the MPO")
# label left, right physical legs with p, q
W0 = W.replace_labels(['p', 'p*'], ['p0', 'p0*'])
W1 = W.replace_labels(['p', 'p*'], ['p1', 'p1*'])
H2 = npc.tensordot(W0, W1, axes=('wR', 'wL')).itranspose(['wL', 'wR', 'p0', 'p1', 'p0*
    ↪ ', 'p1*'])
H2 = H2[0, -1] # (If H has single-site terms, it's not that simple anymore)
print("H2 labels:", H2.get_leg_labels())

print("6) calculate exp(H2) by diagonalization of H2")
# diagonalization requires to view H2 as a matrix
H2 = H2.combine_legs([( 'p0', 'p1'), ('p0*', 'p1*')], qconj=[+1, -1])
print("labels after combine_legs:", H2.get_leg_labels())
E2, U2 = npc.eigh(H2)
print("Eigenvalues of H2:", E2)
U_expE2 = U2.scale_axis(np.exp(-1.j * dt * E2), axis=1) # scale_axis ~= apply an_
    ↪ diagonal matrix
exp_H2 = npc.tensordot(U_expE2, U2.conj(), axes=(1, 1))
exp_H2.iset_leg_labels(H2.get_leg_labels())
exp_H2 = exp_H2.split_legs() # by default split all legs which are `LegPipe`
# (this restores the original labels ['p0', 'p1', 'p0*', 'p1*'] of `H2` in `exp_H2`)

print("7) apply exp(H2) to even/odd bonds of the MPS and truncate with svd")
# (this implements one time step of first order TEBD)
for even_odd in [0, 1]:
    for i in range(even_odd, L - 1, 2):
        B_L = Bs[i].scale_axis(Ss[i], 'vL').ireplace_label('p', 'p0')
        B_R = Bs[i + 1].replace_label('p', 'p1')
        theta = npc.tensordot(B_L, B_R, axes=('vR', 'vL'))
        theta = npc.tensordot(exp_H2, theta, axes=(['p0*', 'p1*'], ['p0', 'p1']))
        # view as matrix for SVD
        theta = theta.combine_legs([( 'vL', 'p0'), ('p1', 'vR')], new_axes=[0, 1],
    ↪ qconj=[+1, -1])

```

(continues on next page)

(continued from previous page)

```

    # now theta has labels '(vL.p0)', '(p1.vR)'
    U, S, V = npc.svd(theta, inner_labels=['vR', 'vL'])
    # truncate
    keep = S > cutoff
    S = S[keep]
    invsq = np.linalg.norm(S)
    Ss[i + 1] = S / invsq
    U = U.iscale_axis(S / invsq, 'vR')
    Bs[i] = U.split_legs('(vL.p0)').iscale_axis(Ss[i]**(-1), 'vL').ireplace_label(
    ↪ 'p0', 'p')
    Bs[i + 1] = V.split_legs('(p1.vR)').ireplace_label('p1', 'p')
    print("finished")

```

Example code `b_mps.py`

```

"""Simplified version of `a_np_conserved.py` making use of other classes (like MPS, ↪
    ↪MPO).

    This example includes the following steps:
    1) create Arrays for an Neel MPS
    2) create an MPO representing the nearest-neighbour AFM Heisenberg Hamiltonian
    3) define 'environments' left and right
    4) contract MPS and MPO to calculate the energy
    5) extract two-site hamiltonian ``H2`` from the MPO
    6) calculate ``exp(-1.j*dt*H2)`` by diagonalization of H2
    7) apply ``exp(H2)`` to two sites of the MPS and truncate with svd

    Note that this example performs the same steps as `a_np_conserved.py`,
    but makes use of other predefined classes except npc.
    """
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import tenpy.linalg.np_conserved as npc
import numpy as np

# some more imports
from tenpy.networks.site import SpinHalfSite
from tenpy.models.lattice import Chain
from tenpy.networks.mps import MPS
from tenpy.networks.mpo import MPO, MPOEnvironment
from tenpy.algorithms.truncation import svd_theta

# model parameters
Jxx, Jz = 1., 1.
L = 20
dt = 0.1
cutoff = 1.e-10
print("Jxx={Jxx}, Jz={Jz}, L={L:d}".format(Jxx=Jxx, Jz=Jz, L=L))

print("1) create Arrays for an Neel MPS")
site = SpinHalfSite(conserved='Sz') # predefined charges and Sp, Sm, Sz operators
p_leg = site.leg
chinfo = p_leg.chinfo
# make lattice from unit cell and create product state MPS
lat = Chain(L, site, bc_MPS='finite')

```

(continues on next page)

(continued from previous page)

```

state = ["up", "down"] * (L // 2) + ["up"] * (L % 2) # Neel state
print("state = ", state)
psi = MPS.from_product_state(lat.mps_sites(), state, lat.bc_MPS)

print("2) create an MPO representing the AFM Heisenberg Hamiltonian")

# predefined physical spin-1/2 operators Sz, S+, S-
Sz, Sp, Sm, Id = site.Sz, site.Sp, site.Sm, site.Id

mpo_leg = npc.LegCharge.from_qflat(chinfo, [[0], [2], [-2], [0], [0]])

W_grid = [[Id,   Sp,   Sm,   Sz,   None,           ],
           [None, None, None, None, 0.5 * Jxx * Sm],
           [None, None, None, None, 0.5 * Jxx * Sp],
           [None, None, None, None, Jz * Sz      ],
           [None, None, None, None, Id           ]] # yapf:disable

W = npc.grid_outer(W_grid, [mpo_leg, mpo_leg.conj()], grid_labels=['wL', 'wR'])
# wL/wR = virtual left/right of the MPO
Ws = [W] * L
Ws[0] = W[:, 1, :]
Ws[-1] = W[:, -1:]
H = MPO(psi.sites, Ws, psi.bc, IdL=0, IdR=-1)

print("3) define 'environments' left and right")

# this is automatically done during initialization of MPOEnvironment
env = MPOEnvironment(psi, H, psi)
envL = env.get_LP(0)
envR = env.get_RP(L - 1)

print("4) contract MPS and MPO to calculate the energy <psi|H|psi>")

E = env.full_contraction(L - 1)
print("E =", E)

print("5) calculate two-site hamiltonian ``H2`` from the MPO")
# label left, right physical legs with p, q
W0 = H.get_W(0).replace_labels(['p', 'p*'], ['p0', 'p0*'])
W1 = H.get_W(1).replace_labels(['p', 'p*'], ['p1', 'p1*'])
H2 = npc.tensordot(W0, W1, axes=('wR', 'wL')).itranspose(['wL', 'wR', 'p0', 'p1', 'p0*
↪', 'p1*'])
H2 = H2[H.IdL[0], H.IdR[2]] # (If H has single-site terms, it's not that simple_
↪ anymore)
print("H2 labels:", H2.get_leg_labels())

print("6) calculate exp(H2) by diagonalization of H2")
# diagonalization requires to view H2 as a matrix
H2 = H2.combine_legs([( 'p0', 'p1'), ('p0*', 'p1*')], qconj=[+1, -1])
print("labels after combine_legs:", H2.get_leg_labels())
E2, U2 = npc.eigh(H2)
print("Eigenvalues of H2:", E2)
U_expE2 = U2.scale_axis(np.exp(-1.j * dt * E2), axis=1) # scale_axis ~= apply a_
↪ diagonal matrix
exp_H2 = npc.tensordot(U_expE2, U2.conj(), axes=(1, 1))
exp_H2.iset_leg_labels(H2.get_leg_labels())
exp_H2 = exp_H2.split_legs() # by default split all legs which are `LegPipe`

```

(continues on next page)

(continued from previous page)

```

# (this restores the original labels ['p0', 'p1', 'p0*', 'p1*'] of `H2` in `exp_H2`)

# alternative way: use :func:`~tenpy.linalg.np_conserved.expm`
exp_H2_alternative = npc.expm(-1.j * dt * H2).split_legs()
assert (npc.norm(exp_H2_alternative - exp_H2) < 1.e-14)

print("7) apply exp(H2) to even/odd bonds of the MPS and truncate with svd")
# (this implements one time step of first order TEBD)
trunc_par = {'svd_min': cutoff, 'trunc_cut': None, 'verbose': 0}
for even_odd in [0, 1]:
    for i in range(even_odd, L - 1, 2):
        theta = psi.get_theta(i, 2) # handles canonical form (i.e. scaling with 'S')
        theta = npc.tensordot(exp_H2, theta, axes=([ 'p0*', 'p1*'], [ 'p0', 'p1']))
        # view as matrix for SVD
        theta = theta.combine_legs([('vL', 'p0'), ('p1', 'vR')], new_axes=[0, 1],
        ↪qconj=[+1, -1])
        # now theta has labels '(vL.p0)', '(p1.vR)'
        U, S, V, err, invsq = svd_theta(theta, trunc_par, inner_labels=['vR', 'vL'])
        psi.set_SR(i, S)
        A_L = U.split_legs('(vL.p0)').ireplace_label('p0', 'p')
        B_R = V.split_legs('(p1.vR)').ireplace_label('p1', 'p')
        psi.set_B(i, A_L, form='A') # left-canonical form
        psi.set_B(i + 1, B_R, form='B') # right-canonical form
print("finished")

```

Example code c_tebd.py

```

"""Example illustrating the use of TEBD in tenpy.

The example functions in this class do the same as the ones in `toycode/c_tebd.py`,
↪but make use
of the classes defined in tenpy.
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np

from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFChain
from tenpy.algorithms import tebd

def example_TEBD_gs_tf_ising_finite(L, g, verbose=True):
    print("finite TEBD, imaginary time evolution, transverse field Ising")
    print("L={L:d}, g={g:.2f}".format(L=L, g=g))
    model_params = dict(L=L, J=1., g=g, bc_MPS='finite', conserve=None,
    ↪verbose=verbose)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    tebd_params = {
        'order': 2,
        'delta_tau_list': [0.1, 0.01, 0.001, 1.e-4, 1.e-5],
        'N_steps': 10,
        'max_error_E': 1.e-6,
    }

```

(continues on next page)

(continued from previous page)

```

        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'verbose': verbose,
    }
    eng = tebd.Engine(psi, M, tebd_params)
    eng.run_GS()  # the main work...

    # expectation values
    E = np.sum(M.bond_energies(psi))  # M.bond_energies() works only a for_
↪NearestNeighborModel
    # alternative: directly measure E2 = np.sum(psi.expectation_value(M.H_bond[1:]))
    print("E = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    mag_x = np.sum(psi.expectation_value("Sigmax"))
    mag_z = np.sum(psi.expectation_value("Sigmaz"))
    print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
    print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
    if L < 20:  # compare to exact result
        from tfi_exact import finite_gs_energy
        E_exact = finite_gs_energy(L, 1., g)
        print("Exact diagonalization: E = {E:.13f}".format(E=E_exact))
        print("relative error: ", abs((E - E_exact) / E_exact))
    return E, psi, M

def example_TEBD_gs_tf_ising_infinite(g, verbose=True):
    print("infinite TEBD, imaginary time evolution, transverse field Ising")
    print("g={g:.2f}".format(g=g))
    model_params = dict(L=2, J=1., g=g, bc_MPS='infinite', conserve=None,
↪verbose=verbose)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    tebd_params = {
        'order': 2,
        'delta_tau_list': [0.1, 0.01, 0.001, 1.e-4, 1.e-5],
        'N_steps': 10,
        'max_error_E': 1.e-8,
        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'verbose': verbose,
    }
    eng = tebd.Engine(psi, M, tebd_params)
    eng.run_GS()  # the main work...
    E = np.mean(M.bond_energies(psi))  # M.bond_energies() works only a for_
↪NearestNeighborModel
    # alternative: directly measure E2 = np.mean(psi.expectation_value(M.H_bond))
    print("E (per site) = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    mag_x = np.mean(psi.expectation_value("Sigmax"))
    mag_z = np.mean(psi.expectation_value("Sigmaz"))
    print("<sigma_x> = {mag_x:.5f}".format(mag_x=mag_x))
    print("<sigma_z> = {mag_z:.5f}".format(mag_z=mag_z))

```

(continues on next page)

(continued from previous page)

```

print("correlation length:", psi.correlation_length())
# compare to exact result
from tfi_exact import infinite_gs_energy
E_exact = infinite_gs_energy(1., g)
print("Analytic result: E (per site) = {E:.13f}".format(E=E_exact))
print("relative error: ", abs((E - E_exact) / E_exact))
return E, psi, M

def example_TEBD_tfi_ising_lightcone(L, g, tmax, dt, verbose=True):
    print("finite TEBD, real time evolution")
    print("L={L:d}, g={g:.2f}, tmax={tmax:.2f}, dt={dt:.3f}".format(L=L, g=g,
↪tmax=tmax, dt=dt))
    # find ground state with TEBD or DMRG
    # E, psi, M = example_TEBD_gs_tfi_ising_finite(L, g)
    from d_dmrg import example_DMRG_tfi_ising_finite
    print("(run DMRG to get the groundstate)")
    E, psi, M = example_DMRG_tfi_ising_finite(L, g, verbose=False)
    print("(DMRG finished)")
    i0 = L // 2
    # apply sigma_z on site i0
    psi.apply_local_op(i0, 'Sigma_z', unitary=True)
    dt_measure = 0.05
    # tebd.Engine makes 'N_steps' steps of `dt` at once; for second order this is_
↪more efficient.
    tebd_params = {
        'order': 2,
        'dt': dt,
        'N_steps': int(dt_measure / dt + 0.5),
        'trunc_params': {
            'chi_max': 50,
            'svd_min': 1.e-10,
            'trunc_cut': None
        },
        'verbose': verbose,
    }
    eng = tebd.Engine(psi, M, tebd_params)
    S = [psi.entanglement_entropy()]
    for n in range(int(tmax / dt_measure + 0.5)):
        eng.run()
        S.append(psi.entanglement_entropy())
    import matplotlib.pyplot as plt
    plt.figure()
    plt.imshow(S[:-1],
               vmin=0.,
               aspect='auto',
               interpolation='nearest',
               extent=(0, L - 1., -0.5 * dt_measure, eng.evolved_time + 0.5 * dt_
↪measure))
    plt.xlabel('site $i$')
    plt.ylabel('time $t/J$')
    plt.ylim(0., tmax)
    plt.colorbar().set_label('entropy $$')
    filename = 'c_tebd_lightcone_{g:.2f}.pdf'.format(g=g)
    plt.savefig(filename)
    print("saved " + filename)

```

(continues on next page)

(continued from previous page)

```

def example_TEBD_gs_tf_ising_next_nearest_neighbor(L, g, Jp, verbose=True):
    from tenpy.models.spins_nnn import SpinChainNNN2
    from tenpy.models.model import NearestNeighborModel
    print("finite TEBD, imaginary time evolution, transverse field Ising next-nearest_
↪neighbor")
    print("L={L:d}, g={g:.2f}, Jp={Jp:.2f}".format(L=L, g=g, Jp=Jp))
    model_params = dict(L=L,
                        Jx=1.,
                        Jy=0.,
                        Jz=0.,
                        Jxp=Jp,
                        Jyp=0.,
                        Jzp=0.,
                        hz=g,
                        bc_MPS='finite',
                        conserve=None,
                        verbose=verbose)

    # we start with the non-grouped sites, but next-nearest neighbor interactions,
↪building the MPO
    M = SpinChainNNN2(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)

    # now we group each to sites ...
    psi.group_sites(n=2) # ... in the state
    M.group_sites(n=2) # ... and model
    # now, M has only 'nearest-neighbor' interactions with respect to the grouped_
↪sites
    # thus, we can convert the MPO into H_bond terms:
    M_nn = NearestNeighborModel.from_MPOModel(M) # hence, we can initialize H_bond_
↪from the MPO

    # now, we continue to run TEBD as before
    tebd_params = {
        'order': 2,
        'delta_tau_list': [0.1, 0.01, 0.001, 1.e-4, 1.e-5],
        'N_steps': 10,
        'max_error_E': 1.e-6,
        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'verbose': verbose,
    }
    eng = tebd.Engine(psi, M_nn, tebd_params) # use M_nn and grouped psi
    eng.run_GS() # the main work...

    # expectation values:
    E = np.sum(M_nn.bond_energies(psi)) # bond_energies() works only a for_
↪NearestNeighborModel
    print("E = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    # we can split the sites of the state again for an easier evaluation of_
↪expectation values
    psi.group_split()
    mag_x = 2. * np.sum(psi.expectation_value("Sx")) # factor of 2 for Sx vs Sigmax

```

(continues on next page)

(continued from previous page)

```

mag_z = 2. * np.sum(psi.expectation_value("Sz"))
print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
return E, psi, M

if __name__ == "__main__":
    example_TEBD_gs_tf_ising_finite(L=10, g=1.)
    print("-" * 100)
    example_TEBD_gs_tf_ising_infinite(g=1.5)
    print("-" * 100)
    example_TEBD_tf_ising_lightcone(L=20, g=1.5, tmax=3., dt=0.01)
    print("-" * 100)
    example_TEBD_gs_tf_ising_next_nearest_neighbor(L=10, g=1.0, Jp=0.1)

```

Example code d_dmrg.py

```

"""Example illustrating the use of DMRG in tenpy.

The example functions in this class do the same as the ones in `toycode/d_dmrg.py`,
but make use of the classes defined in tenpy.

.. todo ::
Docstrings?
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np

from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFICChain
from tenpy.models.spins import SpinModel
from tenpy.algorithms import dmrg

def example_DMRG_tf_ising_finite(L, g, verbose=True):
    print("finite DMRG, transverse field Ising model")
    print("L={L:d}, g={g:.2f}".format(L=L, g=g))
    model_params = dict(L=L, J=1., g=g, bc_MPS='finite', conserve=None,
↳ verbose=verbose)
    M = TFICChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    dmrg_params = {
        'mixer': None, # setting this to True helps to escape local minima
        'max_E_err': 1.e-10,
        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'verbose': verbose,
        'combine': True
    }
    info = dmrg.run(psi, M, dmrg_params) # the main work...
    E = info['E']

```

(continues on next page)

(continued from previous page)

```

print("E = {E:.13f}".format(E=E))
print("final bond dimensions: ", psi.chi)
mag_x = np.sum(psi.expectation_value("Sigmax"))
mag_z = np.sum(psi.expectation_value("Sigmaz"))
print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
if L < 20: # compare to exact result
    from tfi_exact import finite_gs_energy
    E_exact = finite_gs_energy(L, 1., g)
    print("Exact diagonalization: E = {E:.13f}".format(E=E_exact))
    print("relative error: ", abs((E - E_exact) / E_exact))
return E, psi, M

def example_1site_DMRG_tf_ising_finite(L, g, verbose=True):
    print("single-site finite DMRG, transverse field Ising model")
    print("L={L:d}, g={g:.2f}".format(L=L, g=g))
    model_params = dict(L=L, J=1., g=g, bc_MPS='finite', conserve=None,
↳ verbose=verbose)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    dmrgh_params = {
        'mixer': True, # setting this to True is essential for the 1-site algorithm,
↳ to work.
        'max_E_err': 1.e-10,
        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'verbose': verbose,
        'combine': False,
        'active_sites': 1 # specifies single-site
    }
    info = dmrgh.run(psi, M, dmrgh_params)
    E = info['E']
    print("E = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    mag_x = np.sum(psi.expectation_value("Sigmax"))
    mag_z = np.sum(psi.expectation_value("Sigmaz"))
    print("magnetization in X = {mag_x:.5f}".format(mag_x=mag_x))
    print("magnetization in Z = {mag_z:.5f}".format(mag_z=mag_z))
    if L < 20: # compare to exact result
        from tfi_exact import finite_gs_energy
        E_exact = finite_gs_energy(L, 1., g)
        print("Exact diagonalization: E = {E:.13f}".format(E=E_exact))
        print("relative error: ", abs((E - E_exact) / E_exact))
    return E, psi, M

def example_DMRG_tf_ising_infinite(g, verbose=True):
    print("infinite DMRG, transverse field Ising model")
    print("g={g:.2f}".format(g=g))
    model_params = dict(L=2, J=1., g=g, bc_MPS='infinite', conserve=None,
↳ verbose=verbose)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites

```

(continues on next page)

(continued from previous page)

```

psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
dmrg_params = {
    'mixer': True, # setting this to True helps to escape local minima
    'trunc_params': {
        'chi_max': 30,
        'svd_min': 1.e-10
    },
    'max_E_err': 1.e-10,
    'verbose': verbose,
}
# Sometimes, we want to call a 'DMRG engine' explicitly
eng = dmrg.TwoSiteDMRGEngine(psi, M, dmrg_params)
E, psi = eng.run() # equivalent to dmrg.run() up to the return parameters.
print("E = {E:.13f}".format(E=E))
print("final bond dimensions: ", psi.chi)
mag_x = np.mean(psi.expectation_value("Sigmax"))
mag_z = np.mean(psi.expectation_value("Sigmaz"))
print("<sigma_x> = {mag_x:.5f}".format(mag_x=mag_x))
print("<sigma_z> = {mag_z:.5f}".format(mag_z=mag_z))
print("correlation length:", psi.correlation_length())
# compare to exact result
from tfi_exact import infinite_gs_energy
E_exact = infinite_gs_energy(1., g)
print("Analytic result: E (per site) = {E:.13f}".format(E=E_exact))
print("relative error: ", abs((E - E_exact) / E_exact))
return E, psi, M

def example_1site_DMRG_tf_ising_infinite(g, verbose=True):
    print("single-site infinite DMRG, transverse field Ising model")
    print("g={g:.2f}".format(g=g))
    model_params = dict(L=2, J=1., g=g, bc_MPS='infinite', conserve=None,
    verbose=verbose)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    dmrg_params = {
        'mixer': True, # setting this to True is essential for the 1-site algorithm
        'trunc_params': {
            'chi_max': 30,
            'svd_min': 1.e-10
        },
        'max_E_err': 1.e-10,
        'verbose': verbose,
        'combine': True
    }
    eng = dmrg.SingleSiteDMRGEngine(psi, M, dmrg_params)
    E, psi = eng.run() # equivalent to dmrg.run() up to the return parameters.
    print("E = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    mag_x = np.mean(psi.expectation_value("Sigmax"))
    mag_z = np.mean(psi.expectation_value("Sigmaz"))
    print("<sigma_x> = {mag_x:.5f}".format(mag_x=mag_x))
    print("<sigma_z> = {mag_z:.5f}".format(mag_z=mag_z))
    print("correlation length:", psi.correlation_length())
    # compare to exact result

```

(continues on next page)

(continued from previous page)

```

from tfi_exact import infinite_gs_energy
E_exact = infinite_gs_energy(1., g)
print("Analytic result: E (per site) = {E:.13f}".format(E=E_exact))
print("relative error: ", abs((E - E_exact) / E_exact))

def example_DMRG_heisenberg_xxz_infinite(Jz, conserve='best', verbose=True):
    print("infinite DMRG, Heisenberg XXZ chain")
    print("Jz={Jz:.2f}, conserve={conserve!r}".format(Jz=Jz, conserve=conserve))
    model_params = dict(
        L=2,
        S=0.5, # spin 1/2
        Jx=1.,
        Jy=1.,
        Jz=Jz, # couplings
        bc_MPS='infinite',
        conserve=conserve,
        verbose=verbose)
    M = SpinModel(model_params)
    product_state = ["up", "down"] # initial Neel state
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    dmrgh_params = {
        'mixer': True, # setting this to True helps to escape local minima
        'trunc_params': {
            'chi_max': 100,
            'svd_min': 1.e-10,
        },
        'max_E_err': 1.e-10,
        'verbose': verbose,
    }
    info = dmrgh.run(psi, M, dmrgh_params)
    E = info['E']
    print("E = {E:.13f}".format(E=E))
    print("final bond dimensions: ", psi.chi)
    Sz = psi.expectation_value("Sz") # Sz instead of Sigma z: spin-1/2 operators!
    mag_z = np.mean(Sz)
    print("<S_z> = [{Sz0:.5f}, {Sz1:.5f}]; mean = {mag_z:.5f}".format(Sz0=Sz[0],
                                                                    Sz1=Sz[1],
                                                                    mag_z=mag_z))

    # note: it's clear that mean(<Sz>) is 0: the model has Sz conservation!
    print("correlation length:", psi.correlation_length())
    corrs = psi.correlation_function("Sz", "Sz", sites1=range(10))
    print("correlations <Sz_i Sz_j> =")
    print(corrs)
    return E, psi, M

if __name__ == "__main__":
    example_DMRG_tfi_ising_finite(L=10, g=1., verbose=True)
    print("-" * 100)
    example_1site_DMRG_tfi_ising_finite(L=10, g=1., verbose=True)
    print("-" * 100)
    example_DMRG_tfi_ising_infinite(g=1.5, verbose=True)
    print("-" * 100)
    example_1site_DMRG_tfi_ising_infinite(g=1.5, verbose=True)
    print("-" * 100)
    example_DMRG_heisenberg_xxz_infinite(Jz=1.5)

```

Example code `e_tdvp.py`

```

"""Example illustrating the use of TDVP in tenpy.

As of now, we have TDVP only for finite systems. The call structure is quite similar
↳to TEBD. A
difference is that we can run one-site TDVP or two-site TDVP. In the former, the bond
↳dimension can
not grow; the latter allows to grow the bond dimension and hence requires a
↳truncation.
"""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3
import numpy as np
import tenpy.linalg.np_conserved as npc
import tenpy.models.spins
import tenpy.networks.mps as mps
import tenpy.networks.site as site
from tenpy.algorithms import tdvp
from tenpy.networks.mps import MPS
import copy

def run_out_of_equilibrium():
    L = 10
    chi = 5
    delta_t = 0.1
    model_params = {
        'L': L,
        'S': 0.5,
        'conserve': 'Sz',
        'Jz': 1.0,
        'Jy': 1.0,
        'Jx': 1.0,
        'hx': 0.0,
        'hy': 0.0,
        'hz': 0.0,
        'muJ': 0.0,
        'bc_MPS': 'finite',
    }

    heisenberg = tenpy.models.spins.SpinChain(model_params)
    product_state = ["up"] * (L // 2) + ["down"] * (L - L // 2)
    # starting from a domain-wall product state which is not an eigenstate of the
    ↳Heisenberg model
    psi = MPS.from_product_state(heisenberg.lat.mps_sites(),
                                product_state,
                                bc=heisenberg.lat.bc_MPS,
                                form='B')

    tdvp_params = {
        'start_time': 0,
        'dt': delta_t,
        'trunc_params': {
            'chi_max': chi,
            'svd_min': 1.e-10,
            'trunc_cut': None
        }
    }

```

(continues on next page)

(continued from previous page)

```

}
tdvp_engine = tdvp.Engine(psi, heisenberg, tdvp_params)
times = []
S_mid = []
for i in range(30):
    tdvp_engine.run_two_sites(N_steps=1)
    times.append(tdvp_engine.evolved_time)
    S_mid.append(psi.entanglement_entropy(bonds=[L // 2])[0])
for i in range(30):
    tdvp_engine.run_one_site(N_steps=1)
    #psi_2=copy.deepcopy(psi)
    #psi_2.canonical_form()
    times.append(tdvp_engine.evolved_time)
    S_mid.append(psi.entanglement_entropy(bonds=[L // 2])[0])
import matplotlib.pyplot as plt
plt.figure()
plt.plot(times, S_mid)
plt.xlabel('t')
plt.ylabel('S')
plt.axvline(x=3.1, color='red')
plt.text(0.0, 0.0000015, "Two sites update")
plt.text(3.1, 0.0000015, "One site update")
plt.show()

if __name__ == "__main__":
    run_out_of_equilibrium()

```

Example code `tfi_exact.py`

```

"""Provides exact ground state energies for the transverse field ising model for_
↪comparison.

The Hamiltonian reads
.. math ::
    H = - J \sum_{i} \sigma^x_i \sigma^x_{i+1} - g \sum_{i} \sigma^z_i
"""
# Copyright 2019-2020 TeNPy Developers, GNU GPLv3

import numpy as np
import scipy.sparse as sparse
import scipy.sparse.linalg.eigen.arpack as arp
import warnings
import scipy.integrate

def finite_gs_energy(L, J, g):
    """For comparison: obtain ground state energy from exact diagonalization.

    Exponentially expensive in L, only works for small enough `L` <~ 20.
    """
    if L >= 20:
        warnings.warn("Large L: Exact diagonalization might take a long time!")
    # get single site operators
    sx = sparse.csr_matrix(np.array([[0., 1.], [1., 0.])))

```

(continues on next page)

(continued from previous page)

```

sz = sparse.csr_matrix(np.array([[1., 0.], [0., -1.]])
id = sparse.csr_matrix(np.eye(2))
sx_list = [] # sx_list[i] = kron([id, id, ..., id, sx, id, .... id])
sz_list = []
for i_site in range(L):
    x_ops = [id] * L
    z_ops = [id] * L
    x_ops[i_site] = sx
    z_ops[i_site] = sz
    X = x_ops[0]
    Z = z_ops[0]
    for j in range(1, L):
        X = sparse.kron(X, x_ops[j], 'csr')
        Z = sparse.kron(Z, z_ops[j], 'csr')
    sx_list.append(X)
    sz_list.append(Z)
H_xx = sparse.csr_matrix((2**L, 2**L))
H_z = sparse.csr_matrix((2**L, 2**L))
for i in range(L - 1):
    H_xx = H_xx + sx_list[i] * sx_list[(i + 1) % L]
for i in range(L):
    H_z = H_z + sz_list[i]
H = -J * H_xx - g * H_z
E, V = arp.eigsh(H, k=1, which='SA', return_eigenvectors=True, ncv=20)
return E[0]

def infinite_gs_energy(J, g):
    """For comparison: Calculate groundstate energy density from analytic formula.

    The analytic formula stems from mapping the model to free fermions, see P. Pfeuty,
    ↪ The one-
    dimensional Ising model with a transverse field, Annals of Physics 57, p. 79
    ↪ (1970). Note that
    we use Pauli matrices compared this reference using spin-1/2 matrices and replace
    ↪ the sum_k ->
    integral dk/2pi to obtain the result in the N -> infinity limit.
    """
    def f(k, lambda_):
        return np.sqrt(1 + lambda_**2 + 2 * lambda_ * np.cos(k))

    E0_exact = -g / (J * 2. * np.pi) * scipy.integrate.quad(f, -np.pi, np.pi, args=(J,
    ↪ g, ))[0]
    return E0_exact

```

Example code purication.py

Example code z_exact_diag.py

```

"""A simple example comparing DMRG output with full diagonalization (ED).

Sorry that this is not well documented! ED is meant to be used for debugging only ;)
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

```

(continues on next page)

(continued from previous page)

```

import tenpy.linalg.np_conserved as npc
from tenpy.models.xxz_chain import XXZChain
from tenpy.networks.mps import MPS

from tenpy.algorithms.exact_diag import ExactDiag
from tenpy.algorithms import dmrg

def example_exact_diagonalization(L, Jz):
    xxz_pars = dict(L=L, Jxx=1., Jz=Jz, hz=0.0, bc_MPS='finite')
    M = XXZChain(xxz_pars)

    product_state = ["up", "down"] * (xxz_pars['L'] // 2) # this selects a charge_
    ↪ sector!
    psi_DMRG = MPS.from_product_state(M.lat.mps_sites(), product_state)
    charge_sector = psi_DMRG.get_total_charge(True) # ED charge sector should match

    ED = ExactDiag(M, charge_sector=charge_sector, max_size=2.e6)
    ED.build_full_H_from_mpo()
    # ED.build_full_H_from_bonds() # whatever you prefer
    print("start diagonalization")
    ED.full_diagonalization() # the expensive part for large L
    E0_ED, psi_ED = ED.groundstate() # return the ground state
    print("psi_ED =", psi_ED)

    print("run DMRG")
    dmrg.run(psi_DMRG, M, {'verbose': 0}) # modifies psi_DMRG in place!
    # first way to compare ED with DMRG: convert MPS to ED vector
    psi_DMRG_full = ED.mps_to_full(psi_DMRG)
    print("psi_DMRG_full =", psi_DMRG_full)
    ov = npc.inner(psi_ED, psi_DMRG_full, axes='range', do_conj=True)
    print("<psi_ED|psi_DMRG_full> =", ov)
    assert (abs(abs(ov) - 1.) < 1.e-13)

    # second way: convert ED vector to MPS
    psi_ED_mps = ED.full_to_mps(psi_ED)
    ov2 = psi_ED_mps.overlap(psi_DMRG)
    print("<psi_ED_mps|psi_DMRG> =", ov2)
    assert (abs(abs(ov2) - 1.) < 1.e-13)
    assert (abs(ov - ov2) < 1.e-13)
    # -> advantage: expectation_value etc. of MPS are available!
    print("<Sz> =", psi_ED_mps.expectation_value('Sz'))

if __name__ == "__main__":
    example_exact_diagonalization(10, 1.)

```

Advanced examples

The following “advanced examples” are included in the TeNPy repository in the folder `examples/advanced`, we include them here in the documentation for reference. These “advanced examples” go beyond the basic usage of the algorithm, but can give you an idea for certain tasks. It’s a somewhat random collection, feel free to suggest further examples.

Advanced example `xxz_corr_length.py`

```

"""Calculate the correleation legnth of the transerse field Ising model for various_
↪h_z.

This example uses DMRG to find the ground state of the transverse field Ising model_
↪when tuning
through the phase transition by changing the field `hz`. It uses
:meth:`~tenpy.networks.mps.MPS.correlation_length` to extract the correlation length_
↪of the ground
state, and plots it vs. hz in the end.
"""
# Copyright 2018–2020 TeNPy Developers, GNU GPLv3

import numpy as np

from tenpy.models.spins import SpinChain
from tenpy.networks.mps import MPS
from tenpy.algorithms import dmrg
import matplotlib.pyplot as plt

def run(Jzs):
    L = 2
    model_params = dict(L=L, Jx=1., Jy=1., Jz=Jzs[0], bc_MPS='infinite', conserve='Sz'
    ↪, verbose=0)
    chi = 300
    dmrg_params = {
        'trunc_params': {
            'chi_max': chi,
            'svd_min': 1.e-10,
            'trunc_cut': None
        },
        'update_env': 20,
        'start_env': 20,
        'max_E_err': 0.0001,
        'max_S_err': 0.0001,
        'verbose': 1,
        'mixer': False
    }

    M = SpinChain(model_params)
    psi = MPS.from_product_state(M.lat.mps_sites(), (["up", "down"] * L)[:L], M.lat.
    ↪bc_MPS)

    engine = dmrg.TwoSiteDMRGEngine(psi, M, dmrg_params)
    np.set_printoptions(linewidth=120)
    corr_length = []
    for Jz in Jzs:

```

(continues on next page)

(continued from previous page)

```

print("-" * 80)
print("Jz =", Jz)
print("-" * 80)
model_params['Jz'] = Jz
M = SpinChain(model_params)
engine.init_env(model=M) # (re)initialize DMRG environment with new model
# this uses the result from the previous DMRG as first initial guess
engine.run()
# psi is modified by engine.run() and now represents the ground state for the
↪current `Jz`.
corr_length.append(psi.correlation_length(tol_ev0=1.e-3))
print("corr. length", corr_length[-1])
print("<Sz>", psi.expectation_value('Sz'))
dmrg_params['start_env'] = 0 # (some of) the parameters are read out again
corr_length = np.array(corr_length)
results = {
    'model_params': model_params,
    'dmrg_params': dmrg_params,
    'Jzs': Jzs,
    'corr_length': corr_length,
    'eval_transfermatrix': np.exp(-1. / corr_length)
}
return results

def plot(results, filename):
    corr_length = results['corr_length']
    Jzs = results['Jzs']
    plt.plot(Jzs, np.exp(-1. / corr_length))
    plt.xlabel(r'$J_z/J_x$')
    plt.ylabel(r'$t = \exp(-\frac{1}{\xi})$')
    plt.savefig(filename)
    print("saved to " + filename)

if __name__ == "__main__":
    filename = 'xxz_corrlength.pkl'
    import pickle
    import os.path
    if not os.path.exists(filename):
        results = run(list(np.arange(4.0, 1.5, -0.25)) + list(np.arange(1.5, 0.8, -0.
↪05)))
        with open(filename, 'wb') as f:
            pickle.dump(results, f)
    else:
        print("just load the data")
        with open(filename, 'rb') as f:
            results = pickle.load(f)
    plot(results, filename[:-4] + '.pdf')

```

Advanced example central_charge_ising.py

```

"""Example to extract the central charge from the entanglement scaling.

This example code evaluate the central charge of the transverse field Ising model_
↳using IDMRG.
The expected value for the central charge  $c = 1/2$ . The code always recycle the_
↳environment from
the previous simulation, which can be seen at the "age".
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np
import tenpy
import time
from tenpy.networks.mps import MPS
from tenpy.models.tf_ising import TFChain
from tenpy.algorithms import dmrg

def example_DMRG_tf_ising_infinite_S_xi_scaling(g):
    model_params = dict(L=2, J=1., g=g, bc_MPS='infinite', conserve='best', verbose=0)
    M = TFChain(model_params)
    product_state = ["up"] * M.lat.N_sites
    psi = MPS.from_product_state(M.lat.mps_sites(), product_state, bc=M.lat.bc_MPS)
    dmrg_params = {
        'start_env': 10,
        'mixer': False,
        # 'mixer_params': {'amplitude': 1.e-3, 'decay': 5., 'disable_after': 50},
        'trunc_params': {
            'chi_max': 5,
            'svd_min': 1.e-10
        },
        'max_E_err': 1.e-9,
        'max_S_err': 1.e-6,
        'update_env': 0,
        'verbose': 0
    }

    chi_list = np.arange(7, 31, 2)
    s_list = []
    xi_list = []
    eng = dmrg.TwoSiteDMRGEngine(psi, M, dmrg_params)

    for chi in chi_list:

        t0 = time.time()
        eng.reset_stats(
            ) # necessary if you for example have a fixed number of sweeps, if you don't_
        ↳set this you option your simulation stops after initial number of sweeps!
        eng.trunc_params['chi_max'] = chi
        ## DMRG Calculation ##
        print("Start IDMRG CALCULATION")
        eng.run()
        eng.options['mixer'] = None
        psi.canonical_form()

```

(continues on next page)

(continued from previous page)

```

    ## Calculating bond entropy and correlation length ##
    s_list.append(np.mean(psi.entanglement_entropy()))
    xi_list.append(psi.correlation_length())

    print(chi,
          time.time() - t0,
          np.mean(psi.expectation_value(M.H_bond)),
          s_list[-1],
          xi_list[-1],
          flush=True)
    tenpy.tools.optimization.optimize(3) # quite some speedup for small chi

    print("SETTING NEW BOND DIMENSION")

    return s_list, xi_list

def fit_plot_central_charge(s_list, xi_list, filename):
    """Plot routine in order to determine the central charge."""
    import matplotlib.pyplot as plt
    from scipy.optimize import curve_fit

    def fitFunc(Xi, c, a):
        return (c / 6) * np.log(Xi) + a

    Xi = np.array(xi_list)
    S = np.array(s_list)
    LXi = np.log(Xi) # Logarithm of the correlation length xi

    fitParams, fitCovariances = curve_fit(fitFunc, Xi, S)

    # Plot fitting parameter and covariances
    print('c =', fitParams[0], 'a =', fitParams[1])
    print('Covariance Matrix', fitCovariances)

    # plot the data as blue circles
    plt.errorbar(LXi,
                 S,
                 fmt='o',
                 c='blue',
                 ms=5.5,
                 markerfacecolor='white',
                 markeredgecolor='blue',
                 markeredgewidth=1.4)

    # plot the fitted line
    plt.plot(LXi,
             fitFunc(Xi, fitParams[0], fitParams[1]),
             linewidth=1.5,
             c='black',
             label='fit c={c:.2f}'.format(c=fitParams[0]))

    plt.xlabel(r'$\log\{\}\backslash xi_{\chi}$', fontsize=16)
    plt.ylabel(r'$S$', fontsize=16)
    plt.legend(loc='lower right', borderaxespad=0., fancybox=True, shadow=True,
    ↪ fontsize=16)
    plt.savefig(filename)

```

(continues on next page)

(continued from previous page)

```

if __name__ == "__main__":
    s_list, xi_list = example_DMRG_tf_ising_infinite_S_xi_scaling(g=1)
    fit_plot_central_charge(s_list, xi_list, "central_charge_ising.pdf")

```

Advanced example `mpo_exponential_decay.py`

```

"""Demonstration of the mpo.MPO.from_grids method.

We construct a MPO model for a spin 1/2 Heisenberg chain with an infinite number of
2-sites interactions, with strength that decays exponentially with the distance
↪ between the sites.

Because of the infinite number of couplings it is not possible to construct the MPO
↪ from a
coupling model. However the tensors that form the MPO have a surprisingly simple
form (see the grid below).

We run the iDMRG algorithm to find the ground state and energy density of the
system in the thermodynamic limit.
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np
import tenpy.linalg.np_conserved as npc

from tenpy.networks.mpo import MPO
from tenpy.networks.mps import MPS
from tenpy.networks.site import SpinHalfSite
from tenpy.models.model import MPOModel
from tenpy.models.lattice import Chain
from tenpy.algorithms import dmrg
from tenpy.tools.params import asConfig

class ExponentiallyDecayingHeisenberg(MPOModel):
    r"""Spin-1/2 Heisenberg Chain with exponentially decaying interactions.

    The Hamiltonian reads:

    .. math ::

        H = \sum_i \sum_{j>i} \exp(-\frac{|j-i-1|}{\mathtt{xi}}) (
            \mathtt{Jxx}/2 (S^{+}_{-i} S^{-}_{-j} + S^{-}_{-i} S^{+}_{-j})
            + \mathtt{Jz} S^z_{-i} S^z_{-j}
            - \sum_i \mathtt{hz} S^z_{-i}

    All parameters are collected in a single dictionary `model_params`.

    Parameters
    -----
    L : int
        Length of the chain.
    Jxx, Jz, hz, xi: float

```

(continues on next page)

(continued from previous page)

```

    Coupling parameters as defined for the Hamiltonian above.
bc_MPS : {'finite' | 'infinte'}
    MPS boundary conditions.
conserve : 'Sz' | 'parity' | None
    What should be conserved. See :class:`~tenpy.networks.Site.SpinHalfSite`.
"""
def __init__(self, model_params):
    # model parameters
    model_params = asConfig(model_params, "ExponentiallyDecayingHeisenberg")
    L = model_params.get('L', 2)
    xi = model_params.get('xi', 0.5)
    Jxx = model_params.get('Jxx', 1.)
    Jz = model_params.get('Jz', 1.5)
    hz = model_params.get('hz', 0.)
    conserve = model_params.get('conserve', 'Sz')
    if xi == 0.:
        g = 0.
    elif xi == np.inf:
        g = 1.
    else:
        g = np.exp(-1 / (xi))

    # Define the sites and the lattice, which in this case is a simple uniform_
    chain
    # of spin 1/2 sites
    site = SpinHalfSite(conserve=conserve)
    lat = Chain(L, site, bc_MPS='infinite', bc='periodic')

    # The operators that appear in the Hamiltonian. Standard spin operators are
    # already defined for the spin 1/2 site, but it is also possible to add new
    # operators using the add_op method
    Sz, Sp, Sm, Id = site.Sz, site.Sp, site.Sm, site.Id

    # yapf:disable
    # The grid (list of lists) that defines the MPO. It is possible to define the
    # operators in the grid in the following ways:
    # 1) NPC arrays, defined above:
    grid = [[Id, Sp, Sm, Sz, -hz*Sz ],
            [None, g*Id, None, None, 0.5*Jxx*Sm],
            [None, None, g*Id, None, 0.5*Jxx*Sp],
            [None, None, None, g*Id, Jz*Sz ],
            [None, None, None, None, Id ] ]

    # 2) In the form [("OpName", strength)], where "OpName" is the name of the
    # operator (e.g. "Sm" for Sm) and "strength" is a number that multiplies it.
    grid = [[("Id", 1)], [("Sp", 1)], [("Sm", 1)], [("Sz", 1)], [("Sz", -hz) ] ,
            [None , [("Id", g)], None , None , [("Sm", 0.5*Jxx)] ],
            [None , None , [("Id", g)], None , [("Sp", 0.5*Jxx)] ],
            [None , None , None , [("Id", g)], [("Sz", Jz) ] ],
            [None , None , None , None , [("Id", 1) ] ] ]

    # 3) It is also possible to write a single "OpName", equivalent to
    # [("OpName", 1)].
    grid = [{"Id" , "Sp" , "Sm" , "Sz" , [("Sz", -hz) ] },
            [None , [("Id", g)], None , None , [("Sm", 0.5*Jxx)] ],
            [None , None , [("Id", g)], None , [("Sp", 0.5*Jxx)] ],
            [None , None , None , [("Id", g)], [("Sz", Jz) ] ],
            [None , None , None , None , "Id" ] ]

    # yapf:enable

```

(continues on next page)

(continued from previous page)

```

        grids = [grid] * L

        # Generate the MPO from the grid. Note that it is not necessary to specify
        # the physical legs and their charges, since the from_grids method can extract
        # this information from the position of the operators inside the grid.
        H = MPO.from_grids(lat.mps_sites(), grids, bc='infinite', IdL=0, IdR=-1)
        MPOModel.__init__(self, lat, H)

def example_run_dmrg():
    """Use iDMRG to extract information about the ground state of the system."""
    model_params = dict(L=2, Jxx=1, Jz=1.5, xi=0.8, verbose=1)
    model = ExponentiallyDecayingHeisenberg(model_params)
    psi = MPS.from_product_state(model.lat.mps_sites(), ["up", "down"], bc='infinite')
    dmrg_params = {
        'mixer': True,
        'chi_list': {
            0: 100
        },
        'trunc_params': {
            'svd_min': 1.e-10
        },
        'verbose': 1
    }
    results = dmrg.run(psi, model, dmrg_params)
    print("Energy per site: ", results['E'])
    print("<Sz>: ", psi.expectation_value('Sz'))

if __name__ == "__main__":
    example_run_dmrg()

```

7.3.4 Charge conservation with np_conserved

The basic idea is quickly summarized: By inspecting the Hamiltonian, you can identify symmetries, which correspond to conserved quantities, called **charges**. These charges divide the tensors into different sectors. This can be used to infer for example a block-diagonal structure of certain matrices, which in turn speeds up SVD or diagonalization a lot. Even for more general (non-square-matrix) tensors, charge conservation imposes restrictions which blocks of a tensor can be non-zero. Only those blocks need to be saved, which ultimately (= for large enough arrays) leads to a speedup of many routines, e.g., `tensor.dot`.

This introduction covers our implementation of charges; explaining mathematical details of the underlying symmetry is beyond its scope. We refer you to the corresponding chapter in our [\[TeNPyNotes\]](#) for a more general introduction of the idea (also stating the “charge rule” introduced below). Ref. [\[Singh2009\]](#) explains why it works from a mathematical point of view, [\[Singh2010\]](#) has the focus on a $U(1)$ symmetry and might be easier to read.

Notations

Lets fix the notation of certain terms for this introduction and the doc-strings in `np_conserved`. This might be helpful if you know the basics from a different context. If you're new to the subject, keep reading even if you don't understand each detail, and come back to this section when you encounter the corresponding terms again.

A `Array` is a multi-dimensional array representing a **tensor** with the entries:

$$T_{a_0, a_1, \dots, a_{rank-1}} \quad \text{with} \quad a_i \in \{0, \dots, n_i - 1\}$$

Each **leg** a_i corresponds the a vector space of dimension n_i .

An **index** of a leg is a particular value $a_i \in \{0, \dots, n_i - 1\}$.

The **rank** is the number of legs, the **shape** is (n_0, \dots, n_{rank-1}) .

We restrict ourselves to abelian charges with entries in \mathbb{Z} or in \mathbb{Z}_m . The nature of a charge is specified by m ; we set $m = 1$ for charges corresponding to \mathbb{Z} . The number of charges is referred to as **qnumber** as a short hand, and the collection of m for each charge is called **qmod**. The qnumber, qmod and possibly descriptive names of the charges are saved in an instance of `ChargeInfo`.

To each index of each leg, a value of the charge(s) is associated. A **charge block** is a contiguous slice corresponding to the same charge(s) of the leg. A **qindex** is an index in the list of charge blocks for a certain leg. A **charge sector** is for given charge(s) the set of all qindices of that charge(s). A leg is **blocked** if all charge sectors map one-to-one to qindices. Finally, a leg is **sorted**, if the charges are sorted lexicographically. Note that a *sorted* leg is always *blocked*. We can also speak of the complete array to be **blocked by charges** or **legcharge-sorted**, which means that all of its legs are blocked or sorted, respectively. The charge data for a single leg is collected in the class `LegCharge`. A `LegCharge` has also a flag **qconj**, which tells whether the charges point *inward* (+1) or *outward* (-1). What that means, is explained later in *Which entries of the npc Array can be non-zero?*.

For completeness, let us also summarize also the internal structure of an `Array` here: The array saves only non-zero **blocks**, collected as a list of `np.array` in `self._data`. The qindices necessary to map these blocks to the original leg indices are collected in `self._qdata`. An array is said to be **qdata-sorted** if its `self._qdata` is lexicographically sorted. More details on this follow *later*. However, note that you usually shouldn't access `_qdata` and `_data` directly - this is only necessary from within *tensordot*, *svd*, etc. Also, an array has a **total charge**, defining which entries can be non-zero - details in *Which entries of the npc Array can be non-zero?*.

Finally, a **leg pipe** (implemented in `LegPipe`) is used to formally combine multiple legs into one leg. Again, more details follow *later*.

Physical Example

For concreteness, you can think of the Hamiltonian $H = -t \sum_{\langle i,j \rangle} (c_i^\dagger c_j + H.c.) + U n_i n_j$ with $n_i = c_i^\dagger c_i$. This Hamiltonian has the global $U(1)$ gauge symmetry $c_i \rightarrow c_i e^{i\phi}$. The corresponding charge is the total number of particles $N = \sum_i n_i$. You would then introduce one charge with $m = 1$.

Note that the total charge is a sum of local terms, living on single sites. Thus, you can infer the charge of a single physical site: it's just the value $q_i = n_i \in \mathbb{N}$ for each of the states.

Note that you can only assign integer charges. Consider for example the spin 1/2 Heisenberg chain. Here, you can naturally identify the magnetization $S^z = \sum_i S_i^z$ as the conserved quantity, with values $S_i^z = \pm \frac{1}{2}$. Obviously, if S^z is conserved, then so is $2S^z$, so you can use the charges $q_i = 2S_i^z \in \{-1, +1\}$ for the *down* and *up* states, respectively. Alternatively, you can also use a shift and define $q_i = S_i^z + \frac{1}{2} \in \{0, 1\}$.

As another example, consider BCS like terms $\sum_k (c_k^\dagger c_{-k}^\dagger + H.c.)$. These terms break the total particle conservation, but they preserve the total parity, i.e., N

In the above examples, we had only a single charge conserved at a time, but you might be lucky and have multiple conserved quantities, e.g. if you have two chains coupled only by interactions. TeNPy is designed to handle the general

case of multiple charges. When giving examples, we will restrict to one charge, but everything generalizes to multiple charges.

The different formats for LegCharge

As mentioned above, we assign charges to each index of each leg of a tensor. This can be done in three formats: **qflat**, as **qind** and as **qdict**. Let me explain them with examples, for simplicity considering only a single charge (the most inner array has one entry for each charge).

qflat form: simply a list of charges for each index. An example:

```
qflat = [[-2], [-1], [-1], [0], [0], [0], [0], [3], [3]]
```

This tells you that the leg has size 9, the charges for are $[-2], [-1], [-1], \dots, [3]$ for the indices 0, 1, 2, 3, ..., 8. You can identify four *charge blocks* `slice(0, 1)`, `slice(1, 3)`, `slice(3, 7)`, `slice(7, 9)` in this example, which have charges $[-2], [-1], [0], [3]$. In other words, the indices 1, 2 (which are in `slice(1, 3)`) have the same charge value $[-1]$. A *qindex* would just enumerate these blocks as 0, 1, 2, 3.

qind form: a 1D array *slices* and a 2D array *charges*. This is a more compact version than the *qflat* form: the *slices* give a partition of the indices and the *charges* give the charge values. The same example as above would simply be:

```
slices = [0, 1, 3, 7, 9]
charges = [[-2], [-1], [0], [3]]
```

Note that *slices* includes 0 as first entry and the number of indices (here 9) as last entries. Thus it has len `block_number + 1`, where `block_number` (given by *block_number*) is the number of charge blocks in the leg, i.e. a *qindex* runs from 0 to `block_number-1`. On the other hand, the 2D array *charges* has shape `(block_number, qnumber)`, where `qnumber` is the number of charges (given by *qnumber*).

In that way, the *qind* form maps an *qindex*, say `qi`, to the indices `slice(slices[qi], slices[qi+1])` and the charge(s) `charges[qi]`.

qdict form: a dictionary in the other direction than qind, taking charge tuples to slices. Again for the same example:

```
{(-2,): slice(0, 1),
 (-1,): slice(1, 3),
 (0,): slice(3, 7),
 (3,): slice(7, 9)}
```

Since the keys of a dictionary are unique, this form is only possible if the leg is *completely blocked*.

The *LegCharge* saves the charge data of a leg internally in *qind* form, directly in the attribute *slices* and *charges*. However, it also provides convenient functions for conversion between from and to the *qflat* and *qdict* form.

The above example was nice since all charges were sorted and the charge blocks were ‘as large as possible’. This is however not required.

The following example is also a valid *qind* form:

```
slices = [0, 1, 3, 5, 7, 9]
charges = [[-2], [-1], [0], [0], [3]]
```

This leads to the *same qflat* form as the above examples, thus representing the same charges on the leg indices. However, regarding our Arrays, this is quite different, since it divides the leg into 5 (instead of previously 4) charge blocks. We say the latter example is *not bunched*, while the former one is *bunched*.

To make the different notions of *sorted* and *bunched* clearer, consider the following (valid) examples:

charges	bunched	sorted	blocked
<code>[[-2], [-1], [0], [1], [3]]</code>	True	True	True
<code>[[-2], [-1], [0], [0], [3]]</code>	False	True	False
<code>[[-2], [0], [-1], [1], [3]]</code>	True	False	True
<code>[[-2], [0], [-1], [0], [3]]</code>	True	False	False

If a leg is *bunched* and *sorted*, it is automatically *blocked* (but not vice versa). See also [below](#) for further comments on that.

Which entries of the npc Array can be non-zero?

The reason for the speedup with `np_conserved` lies in the fact that it saves only the blocks ‘compatible’ with the charges. But how is this ‘compatible’ defined?

Assume you have a tensor, call it T , and the *LegCharge* for all of its legs, say a, b, c, \dots

Remember that the *LegCharge* associates to each index of the leg a charge value (for each of the charges, if $qnumber > 1$). Let `a.to_qflat()[ia]` denote the charge(s) of index ia for leg a , and similar for other legs.

In addition, the *LegCharge* has a flag `qconj`. This flag **qconj** is only a sign, saved as +1 or -1, specifying whether the charges point ‘inward’ (+1, default) or ‘outward’ (-1) of the tensor.

Then, the **total charge of an entry** `T[ia, ib, ic, ...]` of the tensor is defined as:

```
qtotal[ia, ib, ic, ...] = a.to_qflat()[ia] * a.qconj + b.to_qflat()[ib] * b.qconj + c.  
→to_qflat()[ic] * c.qconj + ... modulo qmod
```

The rule which entries of the a *Array* can be non-zero (i.e., are ‘compatible’ with the charges), is then very simple:

Rule for non-zero entries

An entry `ia, ib, ic, ...` of a *Array* can only be non-zero, if `qtotal[ia, ib, ic, ...]` matches the *unique* `qtotal` attribute of the class.

In other words, there is a **single total charge** `.qtotal` attribute of a *Array*. All indices `ia, ib, ic, ...` for which the above defined `qtotal[ia, ib, ic, ...]` matches this *total charge*, are said to be **compatible with the charges** and can be non-zero. All other indices are **incompatible with the charges** and must be zero.

In case of multiple charges, $qnumber > 1$, is a straight-forward generalization: an entry can only be non-zero if it is *compatible* with each of the defined charges.

The pesky qconj - contraction as an example

Why did we introduce the `qconj` flag? Remember it’s just a sign telling whether the charge points inward or outward. So what’s the reasoning?

The short answer is, that *LegCharges* actually live on bonds (i.e., legs which are to be contracted) rather than individual tensors. Thus, it is convenient to share the *LegCharges* between different legs and even tensors, and just adjust the sign of the charges with `qconj`.

As an example, consider the contraction of two tensors, $C_{ia,ic} = \sum_{ib} A_{ia,ib} B_{ib,ic}$. For simplicity, say that the total charge of all three tensors is zero. What are the implications of the above rule for non-zero entries? Or rather, how can

we ensure that C complies with the above rule? An entry $C[ia, ic]$ will only be non-zero, if there is an ib such that both $A[ia, ib]$ and $B[ib, ic]$ are non-zero, i.e., both of the following equations are fulfilled:

```
A.qtotal == A.legs[0].to_qflat()[ia] * A.legs[0].qconj + A.legs[1].to_qflat()[ib] * A.
↳legs[1].qconj modulo qmod
B.qtotal == B.legs[0].to_qflat()[ib] * B.legs[0].qconj + B.legs[1].to_qflat()[ic] * B.
↳legs[1].qconj modulo qmod
```

($A.legs[0]$ is the *LegCharge* saving the charges of the first leg (with index ia) of A .)

For the uncontracted legs, we just keep the charges as they are:

```
C.legs = [A.legs[0], B.legs[1]]
```

It is then straight-forward to check, that the rule is fulfilled for C , if the following condition is met:

```
A.qtotal + B.qtotal - C.qtotal == A.legs[1].to_qflat()[ib] A.b.qconj + B.legs[0].to_
↳qflat()[ib] B.b.qconj modulo qmod
```

The easiest way to meet this condition is (1) to require that $A.b$ and $B.b$ share the *same* charges $b.to_qflat()$, but have opposite *qconj*, and (2) to define $C.qtotal = A.qtotal + B.qtotal$. This justifies the introduction of *qconj*: when you define the tensors, you have to define the *LegCharge* for the b only once, say for $A.legs[1]$. For $B.legs[0]$ you simply use $A.legs[1].conj()$ which creates a copy of the *LegCharge* with shared *slices* and *charges*, but opposite *qconj*. As a more impressive example, all ‘physical’ legs of an MPS can usually share the same *LegCharge* (up to different *qconj* if the local Hilbert space is the same). This leads to the following convention:

Convention

When an npc algorithm makes tensors which share a bond (either with the input tensors, as for `tensordot`, or amongst the output tensors, as for `SVD`), the algorithm is free, but not required, to use the **same** *LegCharge* for the tensors sharing the bond, *without* making a copy. Thus, if you want to modify a *LegCharge*, you **must** make a copy first (e.g. by using methods of *LegCharge* for what you want to achieve).

Assigning charges to non-physical legs

From the above physical examples, it should be clear how you assign charges to physical legs. But what about other legs, e.g. the virtual bond of an MPS (or an MPO)?

The charge of these bonds must be derived by using the ‘rule for non-zero entries’, as far as they are not arbitrary. As a concrete example, consider an MPS on just two spin 1/2 sites:

```
|
|  x->- | A | ->-y->- | B | ->-z
|          ^           ^
|          |p          |p
```

The two legs p are the physical legs and share the same charge, as they both describe the same local Hilbert space. For better distinction, let me label the indices of them by $\uparrow = 0$ and $\downarrow = 1$. As noted above, we can associate the charges 1 ($p = \uparrow$) and -1 ($p = \downarrow$), respectively, so we define:

```
chinfo = npc.ChargeInfo([1], ['2*Sz'])
p = npc.LegCharge.from_qflat(chinfo, [1, -1], qconj=+1)
```

For the `qconj` signs, we stick to the convention used in our MPS code and indicated by the arrows in above ‘picture’: physical legs are incoming (`qconj=+1`), and from left to right on the virtual bonds. This is achieved by using `[p, x, y.conj()]` as *legs* for A, and `[p, y, z.conj()]` for B, with the default `qconj=+1` for all `p, x, y, z: y.conj()` has the same charges as `y`, but opposite `qconj=-1`.

The legs `x` and `z` of an $L=2$ MPS, are ‘dummy’ legs with just one index 0. The charge on one of them, as well as the total charge of both A and B is arbitrary (i.e., a gauge freedom), so we make a simple choice: total charge 0 on both arrays, as well as for $x=0$, `x = npc.LegCharge.from_qflat(chinfo, [0], qconj=+1)`.

The charges on the bonds `y` and `z` then depend on the state the MPS represents. Here, we consider a singlet $\psi = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)/\sqrt{2}$ as a simple example. A possible MPS representation is given by:

```
A[up, :, :] = [[1/2.**0.5, 0]]      B[up, :, :] = [[0], [-1]]
A[down, :, :] = [[0, 1/2.**0.5]]    B[down, :, :] = [[1], [0]]
```

There are two non-zero entries in A, for the indices $(a, x, y) = (\uparrow, 0, 0)$ and $(\downarrow, 0, 1)$. For $(a, x, y) = (\uparrow, 0, 0)$, we want:

```
A.qtotal = 0 = p.to_qflat()[up] * p.qconj + x.to_qflat()[0] * x.qconj + y.conj().to_
↪qflat()[0] * y.conj().qconj
              = 1                * (+1)      + 0                * (+1)      + y.conj().to_
↪qflat()[0] * (-1)
```

This fixes the charge of $y=0$ to 1. A similar calculation for $(a, x, y) = (\downarrow, 0, 1)$ yields the charge -1 for $y=1$. We have thus all the charges of the leg `y` and can define `y = npc.LegCharge.from_qflat(chinfo, [1, -1], qconj=+1)`.

Now take a look at the entries of B. For the non-zero entry $(b, y, z) = (\uparrow, 1, 0)$, we want:

```
B.qtotal = 0 = p.to_qflat()[up] * p.qconj + y.to_qflat()[1] * y.qconj + z.conj().to_
↪qflat()[0] * z.conj().qconj
              = 1                * (+1)      + (-1)                * (+1)      + z.conj().to_
↪qflat()[0] * (-1)
```

This implies the charge 0 for $z=0$, thus `z = npc.LegCharge.from_qflat(chinfo, [0], qconj=+1)`. Finally, note that the rule for $(b, y, z) = (\downarrow, 0, 0)$ is automatically fulfilled! This is an implication of the fact that the singlet has a well defined value for $S_a^z + S_b^z$. For other states without fixed magnetization (e.g., $|\uparrow\uparrow\rangle + |\downarrow\downarrow\rangle$) this would not be the case, and we could not use charge conservation.

As an exercise, you can calculate the charge of `z` in the case that `A.qtotal=5, B.qtotal = -1` and charge 2 for `x=0`. The result is -2.

Note: This section is meant to be a pedagogical introduction. In your program, you can use the functions `detect_legcharge()` (which does exactly what’s described above) or `detect_qtotal()` (if you know all `LegCharges`, but not `qtotal`).

Array creation

Making an new `Array` requires both the tensor entries (data) and charge data.

The default initialization `a = Array(...)` creates an empty `Array`, where all entries are zero (equivalent to `zeros()`). (Non-zero) data can be provided either as a dense `np.array` to `from_ndarray()`, or by providing a numpy function such as `np.random`, `np.ones` etc. to `from_func()`.

In both cases, the charge data is provided by one `ChargeInfo`, and a `LegCharge` instance for each of the legs.

Note: The charge data instances are not copied, in order to allow it to be shared between different `Arrays`. Consequently, you *must* make copies of the charge data, if you manipulate it directly. (However, methods like `sort()` do that for you.)

Of course, a new `Array` can also created using the charge data from existing `Arrays`, for examples with `zeros_like()` or creating a (deep or shallow) `copy()`. Further, there are the higher level functions like `tensordot()` or `svd()`, which also return new `Arrays`.

Further, new `Arrays` are created by the various functions like `tensordot` or `svd` in `np_conserved`.

Complete blocking of Charges

While the code was designed in such a way that each charge sector has a different charge, the code should still run correctly if multiple charge sectors (for different `qindex`) correspond to the same charge. In this sense `Array` can act like a sparse array class to selectively store subblocks. Algorithms which need a full blocking should state that explicitly in their doc-strings. (Some functions (like `svd` and `eigh`) require complete blocking internally, but if necessary they just work on a temporary copy returned by `as_completely_blocked()`).

If you expect the tensor to be dense subject to charge constraints (as for MPS), it will be most efficient to fully block by charge, so that work is done on large chunks.

However, if you expect the tensor to be sparser than required by charge (as for an MPO), it may be convenient not to completely block, which forces smaller matrices to be stored, and hence many zeroes to be dropped. Nevertheless, the algorithms were not designed with this in mind, so it is not recommended in general. (If you want to use it, run a benchmark to check whether it is really faster!)

If you haven't created the array yet, you can call `sort()` (with `bunch=True`) on each `LegCharge` which you want to block. This sorts by charges and thus induces a permutation of the indices, which is also returned as an 1D array `perm`. For consistency, you have to apply this permutation to your flat data as well.

Alternatively, you can simply call `sort_legcharge()` on an existing `Array`. It calls `sort()` internally on the specified legs and performs the necessary permutations directly to (a copy of) `self`. Yet, you should keep in mind, that the axes are permuted afterwards.

Internal Storage schema of npc Arrays

The actual data of the tensor is stored in `_data`. Rather than keeping a single `np.array` (which would have many zeros in it), we store only the non-zero sub blocks. So `_data` is a python list of `np.array`'s. The order in which they are stored in the list is not physically meaningful, and so not guaranteed (more on this later). So to figure out where the sub block sits in the tensor, we need the `_qdata` structure (on top of the `LegCharges` in `legs`).

Consider a rank 3 tensor `T`, with the first leg like:

```
legs[0].slices = np.array([0, 1, 4, ...])
legs[0].charges = np.array([[ -2], [1], ...])
```

Each row of *charges* gives the charges for a *charge block* of the leg, with the actual indices of the total tensor determined by the *slices*. The *qindex* simply enumerates the charge blocks of a leg. Picking a *qindex* (and thus a *charge block*) from each leg, we have a subblock of the tensor.

For each (non-zero) subblock of the tensor, we put a (numpy) ndarray entry in the `_data` list. Since each subblock of the tensor is specified by *rank* *qindices*, we put a corresponding entry in `_qdata`, which is a 2D array of shape `(#stored_blocks, rank)`. Each row corresponds to a non-zero subblock, and there are rank columns giving the corresponding *qindex* for each leg.

Example: for a rank 3 tensor we might have:

```
T._data = [t1, t2, t3, t4, ...]
T._qdata = np.array([[3, 2, 1],
                    [1, 1, 1],
                    [4, 2, 2],
                    [2, 1, 2],
                    ...])
```

The third subblock has an ndarray `t3`, and *qindices* `[4 2 2]` for the three legs.

- To find the position of `t3` in the actual tensor you can use `get_slice()`:

```
T.legs[0].get_slice(4), T.legs[1].get_slice(2), T.legs[2].get_slice(2)
```

The function `leg.get_charges(qi)` simply returns `slice(leg.slices[qi], leg.slices[qi+1])`

- To find the charges of `t3`, we can use `get_charge()`:

```
T.legs[0].get_charge(2), T.legs[1].get_charge(2), T.legs[2].get_charge(2)
```

The function `leg.get_charge(qi)` simply returns `leg.charges[qi]*leg.qconj`.

Note: Outside of *np_conserved*, you should use the API to access the entries. If you really need to iterate over all blocks of an Array `T`, try for `(block, blockslices, charges, qindices)` in `T: do_something()`.

The order in which the blocks stored in `_data/_qdata` is arbitrary (although of course `_data` and `_qdata` must be in correspondence). However, for many purposes it is useful to sort them according to some convention. So we include a flag `._qdata_sorted` to the array. So, if sorted (with `isort_qdata()`), the `_qdata` example above goes to

```
_qdata = np.array([[1, 1, 1],
                  [3, 2, 1],
                  [2, 1, 2],
                  [4, 2, 2],
                  ...])
```

Note that *np.lexsort* chooses the right-most column to be the dominant key, a convention we follow throughout.

If `_qdata_sorted == True`, `_qdata` and `_data` are guaranteed to be lexsorted. If `_qdata_sorted == False`, there is no guarantee. If an algorithm modifies `_qdata`, it **must** set `_qdata_sorted = False` (unless it guarantees it is still sorted). The routine `sort_qdata()` brings the data to sorted form.

Indexing of an Array

Although it is usually not necessary to access single entries of an `Array`, you can of course do that. In the simplest case, this is something like `A[0, 2, 1]` for a rank-3 `Array` `A`. However, accessing single entries is quite slow and usually not recommended. For small `Arrays`, it may be convenient to convert them back to flat numpy arrays with `to_ndarray()`.

On top of that very basic indexing, `Array` supports slicing and some kind of advanced indexing, which is however different from the one of numpy arrays (described [here](#)). Unlike numpy arrays, our `Array` class does not broadcast existing index arrays – this would be terribly slow. Also, `np.newaxis` is not supported, since inserting new axes requires additional information for the charges.

Instead, we allow just indexing of the legs independent of each other, of the form `A[i0, i1, ...]`. If all indices `i0, i1, ...` are integers, the single corresponding entry (of type `dtype`) is returned.

However, the individual ‘indices’ `i0` for the individual legs can also be one of what is described in the following list. In that case, a new `Array` with less data (specified by the indices) is returned.

The ‘indices’ can be:

- an `int`: fix the index of that axis, return array with one less dimension. See also `take_slice()`.
- a `slice(None)` or `::`: keep the complete axis
- an `Ellipsis` or `...`: shorthand for `slice(None)` for missing axes to fix the len
- an 1D bool `ndarray` mask: apply a mask to that axis, see `iproject()`.
- a `slice(start, stop, step)` or `start:stop:step`: keep only the indices specified by the slice. This is also implemented with `iproject`.
- an 1D int `ndarray` mask: keep only the indices specified by the array. This is also implemented with `iproject`.

For slices and 1D arrays, additional permutations may be performed with the help of `permute()`.

If the number of indices is less than `rank`, the remaining axes remain free, so for a rank 4 `Array` `A`, `A[i0, i1] == A[i0, i1, ..., :]`.

Note that indexing always **copies** the data – even if `int` contains just slices, in which case numpy would return a view. However, assigning with `A[:, [3, 5], 3] = B` should work as you would expect.

Warning: Due to numpy’s advanced indexing, for 1D integer arrays `a0` and `a1` the following holds

```
A[a0, a1].to_ndarray() == A.to_ndarray()[np.ix_(a0, a1)] != A.to_ndarray()[a0, a1]
```

For a combination of slices and arrays, things get more complicated with numpy’s advanced indexing. In that case, a simple `np.ix_(...)` doesn’t help any more to emulate our version of indexing.

Introduction to combine_legs, split_legs and LegPipes

Often, it is necessary to “combine” multiple legs into one: for example to perform a SVD, a tensor needs to be viewed as a matrix. For a flat array, this can be done with `np.reshape`, e.g., if `A` has shape `(10, 3, 7)` then `B = np.reshape(A, (30, 7))` will result in a (view of the) array with one less dimension, but a “larger” first leg. By default (`order='C'`), this results in

```
B[i*3 + j, k] == A[i, j, k] for i in range(10) for j in range(3) for k in range(7)
```

While for a `np.array`, also a reshaping `(10, 3, 7) -> (2, 21, 5)` would be allowed, it does not make sense physically. The only sensible “reshape” operation on an `Array` are

- 1) to **combine** multiple legs into one **leg pipe** (*LegPipe*) with `combine_legs()`, or
- 2) to **split** a pipe of previously combined legs with `split_legs()`.

Each leg has a Hilbert space, and a representation of the symmetry on that Hilbert space. Combining legs corresponds to the tensor product operation, and for abelian groups, the corresponding “fusion” of the representation is the simple addition of charge.

Fusion is not a lossless process, so if we ever want to split the combined leg, we need some additional data to tell us how to reverse the tensor product. This data is saved in the class *LegPipe*, derived from the *LegCharge* and used as new *leg*. Details of the information contained in a *LegPipe* are given in the class doc string.

The rough usage idea is as follows:

- 1) You can call `combine_legs()` without supplying any *LegPipes*, `combine_legs` will then make them for you. Nevertheless, if you plan to perform the combination over and over again on sets of legs you know to be identical [with same charges etc, up to an overall -1 in *qconj* on all incoming and outgoing Legs] you might make a *LegPipe* anyway to save on the overhead of computing it each time.
- 2) In any way, the resulting Array will have a *LegPipe* as a *LegCharge* on the combined leg. Thus, it – and all tensors inheriting the leg (e.g. the results of *svd*, *tensordot* etc.) – will have the information how to split the *LegPipe* back to the original legs.
- 3) Once you performed the necessary operations, you can call `split_legs()`. This uses the information saved in the *LegPipe* to split the legs, recovering the original legs.

For a *LegPipe*, `conj()` changes *qconj* for the outgoing pipe *and* the incoming legs. If you need a *LegPipe* with the same incoming *qconj*, use `outer_conj()`.

Leg labeling

It’s convenient to name the legs of a tensor: for instance, we can name legs 0, 1, 2 to be 'a', 'b', 'c': T_{i_a, i_b, i_c} . That way we don’t have to remember the ordering! Under *tensordot*, we can then call

```
U = npc.tensordot(S, T, axes = [ [...], ['b'] ] )
```

without having to remember where exactly 'b' is. Obviously U should then inherit the name of its legs from the uncontracted legs of *S* and *T*. So here is how it works:

- Labels can *only* be strings. The labels should not include the characters . or ?. Internally, the labels are stored as dict `a.labels = {label: leg_position, ...}`. Not all legs need a label.
- To set the labels, call

```
A.set_labels(['a', 'b', None, 'c', ... ])
```

which will set up the labeling `{'a': 0, 'b': 1, 'c': 3 ...}`.

- (Where implemented) the specification of axes can use either the labels **or** the index positions. For instance, the call `tensordot(A, B, [['a', 2, 'c'], [...]])` will interpret 'a' and 'c' as labels (calling `get_leg_indices()` to find their positions using the dict) and 2 as ‘the 2nd leg’. That’s why we require labels to be strings!
- **Labels will be intelligently inherited through the various operations of *np_conserved*.**
 - Under *transpose*, labels are permuted.
 - Under *tensordot*, labels are inherited from uncontracted legs. If there is a collision, both labels are dropped.

- Under *combine_legs*, labels get concatenated with a `.` delimiter and surrounded by brackets. Example: let `a.labels = {'a': 1, 'b': 2, 'c': 3}`. Then if `b = a.combine_legs([[0, 1], [2]])`, it will have `b.labels = {'(a.b)': 0, '(c)': 1}`. If some sub-leg of a combined leg isn't named, then a `'?#'` label is inserted (with `#` the leg index), e.g., `'a.?0.c'`.
- Under *split_legs*, the labels are split using the delimiters (and the `'?#'` are dropped).
- Under *conj*, *iconj*: take `'a' → 'a*'`, `'a*' → 'a'`, and `'(a.(b*.c))' → '(a*. (b.c*))'`
- Under *svd*, the outer labels are inherited, and inner labels can be optionally passed.
- Under *pinv*, the labels are transposed.

See also

- The module `tenpy.linalg.np_conserved` should contain all the API needed from the point of view of the algorithms. It contains the fundamental `Array` class and functions for working with them (creating and manipulating).
- The module `tenpy.linalg.charges` contains implementations for the charge structure, for example the classes `ChargeInfo`, `LegCharge`, and `LegPipe`. As noted above, the 'public' API is imported to (and accessible from) `np_conserved`.

A full example code for spin-1/2

Below follows a full example demonstrating the creation and contraction of Arrays. (It's the file `a_np_conserved.py` in the examples folder of the tenpy source.)

```
"""An example code to demonstrate the usage of :class:`~tenpy.linalg.np_conserved.
↪Array`.

This example includes the following steps:
1) create Arrays for an Neel MPS
2) create an MPO representing the nearest-neighbour AFM Heisenberg Hamiltonian
3) define 'environments' left and right
4) contract MPS and MPO to calculate the energy
5) extract two-site hamiltonian ``H2`` from the MPO
6) calculate ``exp(-1.j*dt*H2)`` by diagonalization of H2
7) apply ``exp(H2)`` to two sites of the MPS and truncate with svd

Note that this example uses only np_conserved, but no other modules.
Compare it to the example `b_mps.py`,
which does the same steps using a few predefined classes like MPS and MPO.
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import tenpy.linalg.np_conserved as npc
import numpy as np

# model parameters
Jxx, Jz = 1., 1.
L = 20
dt = 0.1
cutoff = 1.e-10
print("Jxx={Jxx}, Jz={Jz}, L={L:d}".format(Jxx=Jxx, Jz=Jz, L=L))
```

(continues on next page)

(continued from previous page)

```

print("1) create Arrays for an Neel MPS")

#   vL --B--> vR
#       |
#       ^
#       |
#       p

# create a ChargeInfo to specify the nature of the charge
chinfo = npc.ChargeInfo([1], ['2*Sz']) # the second argument is just a descriptive_
↳name

# create LegCharges on physical leg and even/odd bonds
p_leg = npc.LegCharge.from_qflat(chinfo, [[1], [-1]]) # charges for up, down
v_leg_even = npc.LegCharge.from_qflat(chinfo, [[0]])
v_leg_odd = npc.LegCharge.from_qflat(chinfo, [[1]])

B_even = npc.zeros([v_leg_even, v_leg_odd.conj(), p_leg],
                    labels=['vL', 'vR', 'p']) # virtual left/right, physical
B_odd = npc.zeros([v_leg_odd, v_leg_even.conj(), p_leg], labels=['vL', 'vR', 'p'])
B_even[0, 0, 0] = 1. # up
B_odd[0, 0, 1] = 1. # down

Bs = [B_even, B_odd] * (L // 2) + [B_even] * (L % 2) # (right-canonical)
Ss = [np.ones(1)] * L # Ss[i] are singular values between Bs[i-1] and Bs[i]

# Side remark:
# An MPS is expected to have non-zero entries everywhere compatible with the charges.
# In general, we recommend to use `sort_legcharge` (or `as_completely_blocked`)
# to ensure complete blocking. (But the code will also work, if you don't do it.)
# The drawback is that this might introduce permutations in the indices of single_
↳legs,
# which you have to keep in mind when converting dense numpy arrays to and from npc.
↳Arrays.

print("2) create an MPO representing the AFM Heisenberg Hamiltonian")

#       p*
#       |
#       ^
#       |
#   wL --W--> wR
#       |
#       ^
#       |
#       p

# create physical spin-1/2 operators Sz, S+, S-
Sz = npc.Array.from_ndarray([[0.5, 0.], [0., -0.5]], [p_leg, p_leg.conj()], labels=['p',
↳', 'p*'])
Sp = npc.Array.from_ndarray([[0., 1.], [0., 0.]], [p_leg, p_leg.conj()], labels=['p',
↳'p*'])
Sm = npc.Array.from_ndarray([[0., 0.], [1., 0.]], [p_leg, p_leg.conj()], labels=['p',
↳'p*'])
Id = npc.eye_like(Sz, labels=Sz.get_leg_labels()) # identity

```

(continues on next page)

(continued from previous page)

```

mpo_leg = npc.LegCharge.from_qflat(chinfo, [[0], [2], [-2], [0], [0]])

W_grid = [[Id,   Sp,   Sm,   Sz,   None,   ],
           [None, None, None, None, 0.5 * Jxx * Sm],
           [None, None, None, None, 0.5 * Jxx * Sp],
           [None, None, None, None, Jz * Sz      ],
           [None, None, None, None, Id          ]] # yapf:disable

W = npc.grid_outter(W_grid, [mpo_leg, mpo_leg.conj()], grid_labels=['wL', 'wR'])
# wL/wR = virtual left/right of the MPO
Ws = [W] * L

print("3) define 'environments' left and right")

# .---->- vR      vL ->----.
# |                                     |
# envL->- wR      wL ->-envR
# |                                     |
# .---->- vR*     vL*->----.

envL = npc.zeros([W.get_leg('wL').conj(), Bs[0].get_leg('vL').conj(), Bs[0].get_leg(
    ↪ 'vL')],
                 labels=['wR', 'vR', 'vR*'])
envL[0, :, :] = npc.diag(1., envL.legs[1])
envR = npc.zeros([W.get_leg('wR').conj(), Bs[-1].get_leg('vR').conj(), Bs[-1].get_leg(
    ↪ 'vR')],
                 labels=['wL', 'vL', 'vL*'])
envR[-1, :, :] = npc.diag(1., envR.legs[1])

print("4) contract MPS and MPO to calculate the energy <psi|H|psi>")
contr = envL
for i in range(L):
    # contr labels: wR, vR, vR*
    contr = npc.tensordot(contr, Bs[i], axes=('vR', 'vL'))
    # wR, vR*, vR, p
    contr = npc.tensordot(contr, Ws[i], axes=(['p', 'wR'], ['p*', 'wL']))
    # vR*, vR, wR, p
    contr = npc.tensordot(contr, Bs[i].conj(), axes=(['p', 'vR*'], ['p*', 'vL*']))
    # vR, wR, vR*
    # note that the order of the legs changed, but that's no problem with labels:
    # the arrays are automatically transposed as necessary
E = npc.inner(contr, envR, axes=(['vR', 'wR', 'vR*'], ['vL', 'wL', 'vL*']))
print("E =", E)

print("5) calculate two-site hamiltonian ``H2`` from the MPO")
# label left, right physical legs with p, q
W0 = W.replace_labels(['p', 'p*'], ['p0', 'p0*'])
W1 = W.replace_labels(['p', 'p*'], ['p1', 'p1*'])
H2 = npc.tensordot(W0, W1, axes=('wR', 'wL')).itranspose(['wL', 'wR', 'p0', 'p1', 'p0*
    ↪', 'p1*'])
H2 = H2[0, -1] # (If H has single-site terms, it's not that simple anymore)
print("H2 labels:", H2.get_leg_labels())

print("6) calculate exp(H2) by diagonalization of H2")
# diagonalization requires to view H2 as a matrix
H2 = H2.combine_legs([('p0', 'p1'), ('p0*', 'p1*')], qconj=[+1, -1])
print("labels after combine_legs:", H2.get_leg_labels())

```

(continues on next page)

(continued from previous page)

```

E2, U2 = npc.eigh(H2)
print("Eigenvalues of H2:", E2)
U_expE2 = U2.scale_axis(np.exp(-1.j * dt * E2), axis=1) # scale_axis ~= apply an_
↳diagonal matrix
exp_H2 = npc.tensordot(U_expE2, U2.conj(), axes=(1, 1))
exp_H2.iset_leg_labels(H2.get_leg_labels())
exp_H2 = exp_H2.split_legs() # by default split all legs which are `LegPipe`
# (this restores the original labels ['p0', 'p1', 'p0*', 'p1*'] of `H2` in `exp_H2`)

print("7) apply exp(H2) to even/odd bonds of the MPS and truncate with svd")
# (this implements one time step of first order TEBD)
for even_odd in [0, 1]:
    for i in range(even_odd, L - 1, 2):
        B_L = Bs[i].scale_axis(Ss[i], 'vL').ireplace_label('p', 'p0')
        B_R = Bs[i + 1].replace_label('p', 'p1')
        theta = npc.tensordot(B_L, B_R, axes=('vR', 'vL'))
        theta = npc.tensordot(exp_H2, theta, axes=(['p0*', 'p1*'], ['p0', 'p1']))
        # view as matrix for SVD
        theta = theta.combine_legs([( 'vL', 'p0'), ('p1', 'vR')], new_axes=[0, 1],
↳qconj=[+1, -1])
        # now theta has labels '(vL.p0)', '(p1.vR)'
        U, S, V = npc.svd(theta, inner_labels=['vR', 'vL'])
        # truncate
        keep = S > cutoff
        S = S[keep]
        invsq = np.linalg.norm(S)
        Ss[i + 1] = S / invsq
        U = U.iscale_axis(S / invsq, 'vR')
        Bs[i] = U.split_legs('(vL.p0)').iscale_axis(Ss[i]**(-1), 'vL').ireplace_label(
↳'p0', 'p')
        Bs[i + 1] = V.split_legs('(p1.vR)').ireplace_label('p1', 'p')
print("finished")

```

7.3.5 Models

What is a model?

Abstractly, a **model** stands for some physical (quantum) system to be described. For tensor networks algorithms, the model is usually specified as a Hamiltonian written in terms of second quantization. For example, let us consider a spin-1/2 Heisenberg model described by the Hamiltonian

$$H = J \sum_i S_i^x S_{i+1}^x + S_i^y S_{i+1}^y + S_i^z S_{i+1}^z$$

Note that a few things are defined more or less implicitly.

- The local Hilbert space: it consists of Spin-1/2 degrees of freedom with the usual spin-1/2 operators S^x, S^y, S^z .
- The geometric (lattice) structure: above, we spoke of a 1D “chain”.
- The boundary conditions: do we have open or periodic boundary conditions? The “chain” suggests open boundaries, which are in most cases preferable for MPS-based methods.
- The range of i : How many sites do we consider (for a 2D system: in each direction)?

Obviously, these things need to be specified in TeNPy in one way or another, if we want to define a model.

Ultimately, our goal is to run some algorithm. However, different algorithm requires the model and Hamiltonian to be specified in different forms. We have one class for each such required form. For example `dmrg` requires an `MPOModel`, which contains the Hamiltonian written as an MPO. So a new model class suitable for DMRG should have this general structure:

```
class MyNewModel(MPOModel):
    def __init__(self, model_params):
        lattice = somehow_generate_lattice(model_params)
        H_MPO = somehow_generate_MPO(lattice, model_params)
        # initialize MPOModel
        MPOModel.__init__(self, lattice, H_MPO)
```

On the other hand, if we want to evolve a state with `tebd` we need a `NearestNeighborModel`, in which the Hamiltonian is written in terms of two-site bond-terms to allow a Suzuki-Trotter decomposition of the time-evolution operator:

```
class MyNewModel2(NearestNeighborModel):
    """General strucutre for a model suitable for TEBD."""
    def __init__(self, model_params):
        lattice = somehow_generate_lattice(model_params)
        H_bond = somehow_generate_H_bond(lattice, model_params)
        # initialize MPOModel
        NearestNeighborModel.__init__(self, lattice, H_bond)
```

Of course, the difficult part in these examples is to generate the `H_MPO` and `H_bond` in the required form. If you want to write it down by hand, you can of course do that. But it can be quite tedious to write every model multiple times, just because we need different representations of the same Hamiltonian. Luckily, there is a way out in TeNPy: the `CouplingModel`. Before we describe this class, let's discuss the background of the `Site` and `Site` class.

The Hilbert space

The **local Hilbert** space is represented by a `Site` (read its doc-string!). In particular, the `Site` contains the local `LegCharge` and hence the meaning of each basis state needs to be defined. Beside that, the site contains the local operators - those give the real meaning to the local basis. Having the local operators in the site is very convenient, because it makes them available by name for example when you want to calculate expectation values. The most common sites (e.g. for spins, spin-less or spin-full fermions, or bosons) are predefined in the module `tenpy.networks.site`, but if necessary you can easily extend them by adding further local operators or completely write your own subclasses of `Site`.

The full Hilbert space is a tensor product of the local Hilbert space on each site.

Note: The `LegCharge` of all involved sites need to have a common `ChargeInfo` in order to allow the contraction of tensors acting on the various sites. This can be ensured with the function `multi_sites_combine_charges()`.

An example where `multi_sites_combine_charges()` is needed would be a coupling of different types of sites, e.g., when a tight binding chain of fermions is coupled to some local spin degrees of freedom. Another use case of this function would be a model with a $U(1)$ symmetry involving only half the sites, say $\sum_{i=0}^{L/2} n_{2i}$.

Note: If you don't know about the charges and `np_conserved` yet, but want to get started with models right away, you can set `conserve=None` in the existing sites or use `leg = tenpy.linalg.np_conserved.LegCharge.from_trivial(d)` for an implementation of your custom site, where `d` is the dimension of the local Hilbert space. Alternatively, you can find some introduction to the charges in the [Charge conservation with np_conserved](#).

The geometry : lattice class

The geometry is usually given by some kind of **lattice** structure how the sites are arranged, e.g. implicitly with the sum over nearest neighbours $\sum_{\langle i,j \rangle}$. In TeNPy, this is specified by a `Lattice` class, which contains a unit cell of a few `Site` which are shifted periodically by its basis vectors to form a regular lattice. Again, we have pre-defined some basic lattices like a `Chain`, two chains coupled as a `Ladder` or 2D lattices like the `Square`, `Honeycomb` and `Kagome` lattices; but you are also free to define your own generalizations.

MPS based algorithms like DMRG always work on purely 1D systems. Even if our model “lives” on a 2D lattice, these algorithms require to map it onto a 1D chain (probably at the cost of longer-range interactions). This mapping is also done by the lattice by defining the **order** (`order`) of the sites.

Note: Further details on the lattice geometry can be found in [Details on the lattice geometry](#).

The CouplingModel: general structure

The `CouplingModel` provides a general, quite abstract way to specify a Hamiltonian of two-site couplings on a given lattice. Once initialized, its methods `add_onsite()` and `add_coupling()` allow to add onsite and coupling terms repeated over the different unit cells of the lattice. In that way, it basically allows a straight-forward translation of the Hamiltonian given as a math formula $H = \sum_i A_i B_{i+dx} + \dots$ with onsite operators A, B, \dots into a model class.

The general structure for a new model based on the `CouplingModel` is then:

```
class MyNewModel3(CouplingModel, MPOModel, NearestNeighborModel):
    def __init__(self, ...):
        ... # follow the basic steps explained below
```

In the initialization method `__init__(self, ...)` of this class you can then follow these basic steps:

0. Read out the parameters.
1. Given the parameters, determine the charges to be conserved. Initialize the `LegCharge` of the local sites accordingly.
2. Define (additional) local operators needed.
3. Initialize the needed `Site`.

Note: Using pre-defined sites like the `SpinHalfSite` is recommended and can replace steps 1-3.

4. Initialize the lattice (or if you got the lattice as a parameter, set the sites in the unit cell).
5. Initialize the `CouplingModel` with `CouplingModel.__init__(self, lat)`.
6. Use `add_onsite()` and `add_coupling()` to add all terms of the Hamiltonian. Here, the `pairs` of the lattice can come in handy, for example:

```
self.add_onsite(-np.asarray(h), 0, 'Sz')
for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
    self.add_coupling(0.5*J, u1, 'Sp', u2, 'Sm', dx, plus_hc=True)
    self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

Note: The method `add_coupling()` adds the coupling only in one direction, i.e. not switching i and j in a $\sum_{\langle i,j \rangle}$. If you have terms like $c_i^\dagger c_j$ or $S_i^+ S_j^-$ in your Hamiltonian, you *need* to add it in both directions to

get a Hermitian Hamiltonian! The easiest way to do that is to use the *plus_hc* option of `add_onsite()` and `add_coupling()`, as we did for the $J/2(S_i^+ S_j^- + h.c.)$ terms of the Heisenberg model above. Alternatively, you can add the hermitian conjugate terms explicitly, see the examples in `add_coupling()` for more details.

Note that the *strength* arguments of these functions can be (numpy) arrays for site-dependent couplings. If you need to add or multiply some parameters of the model for the *strength* of certain terms, it is recommended use `np.asarray` beforehand – in that way lists will also work fine.

7. Finally, if you derived from the `MPOModel`, you can call `calc_H_MPO()` to build the MPO and use it for the initialization as `MPOModel.__init__(self, lat, self.calc_H_MPO())`.
8. Similarly, if you derived from the `NearestNeighborModel`, you can call `calc_H_bond()` to initialize it as `NearestNeighborModel.__init__(self, lat, self.calc_H_bond())`. Calling `self.calc_H_bond()` will fail for models which are not nearest-neighbors (with respect to the MPS ordering), so you should only subclass the `NearestNeighborModel` if the lattice is a simple `Chain`.

The `CouplingModel` works for Hamiltonians which are a sum of terms involving at most two sites. The generalization `MultiCouplingModel` can be used for Hamiltonians with coupling terms acting on more than 2 sites at once. Follow the exact same steps in the initialization, and just use the `add_multi_coupling()` instead or in addition to the `add_coupling()`. A prototypical example is the exactly solvable `ToricCode`.

The code of the module `tenpy.models.xxz_chain` is included below as an illustrative example how to implement a Model. The implementation of the `XXZChain` directly follows the steps outline above. The `XXZChain2` implements the very same model, but based on the `CouplingMPOModel` explained in the next section.

```
"""Prototypical example of a 1D quantum model: the spin-1/2 XXZ chain.

The XXZ chain is contained in the more general :class:`~tenpy.models.spins.SpinChain`;
→ the idea of
this module is more to serve as a pedagogical example for a model.
"""
# Copyright 2018–2020 TeNPy Developers, GNU GPLv3

import numpy as np

from .lattice import Site, Chain
from .model import CouplingModel, NearestNeighborModel, MPOModel, CouplingMPOModel
from ..linalg import np_conserved as npc
from ..tools.params import asConfig
from ..networks.site import SpinHalfSite # if you want to use the predefined site

__all__ = ['XXZChain', 'XXZChain2']

class XXZChain(CouplingModel, NearestNeighborModel, MPOModel):
    r"""Spin-1/2 XXZ chain with Sz conservation.

    The Hamiltonian reads:

    .. math ::
        H = \sum_i \mathtt{Jxx}/2 (S^{+}_i S^{-}_{i+1} + S^{-}_i S^{+}_{i+1})
            + \mathtt{Jz} S^z_i S^z_{i+1} \setminus\setminus
            - \sum_i \mathtt{hz} S^z_i

    All parameters are collected in a single dictionary `model_params`, which
    is turned into a :class:`~tenpy.tools.params.Config` object.

    Parameters
```

(continues on next page)

(continued from previous page)

```

-----
model_params : :class:`~tenpy.tools.params.Config`
    Parameters for the model. See :cfg:config:`XXZChain` below.

Options
-----
.. cfg:config :: XXZChain
    :include: CouplingMPOModel

    L : int
        Length of the chain.
    Jxx, Jz, hz : float | array
        Coupling as defined for the Hamiltonian above.
    bc_MPS : {'finite' | 'infinite'}
        MPS boundary conditions. Coupling boundary conditions are chosen_
↪appropriately.

    """
    def __init__(self, model_params):
        # 0) read out/set default parameters
        model_params = asConfig(model_params, "XXZChain")
        L = model_params.get('L', 2)
        Jxx = model_params.get('Jxx', 1.)
        Jz = model_params.get('Jz', 1.)
        hz = model_params.get('hz', 0.)
        bc_MPS = model_params.get('bc_MPS', 'finite')
        # 1-3):
        USE_PREDEFINED_SITE = False
        if not USE_PREDEFINED_SITE:
            # 1) charges of the physical leg. The only time that we actually define_
↪charges!
            leg = npc.LegCharge.from_qflat(npc.ChargeInfo([1], ['2*Sz']), [1, -1])
            # 2) onsite operators
            Sp = [[0., 1.], [0., 0.]]
            Sm = [[0., 0.], [1., 0.]]
            Sz = [[0.5, 0.], [0., -0.5]]
            # (Can't define Sx and Sy as onsite operators: they are incompatible with_
↪Sz charges.)
            # 3) local physical site
            site = Site(leg, ['up', 'down'], Sp=Sp, Sm=Sm, Sz=Sz)
        else:
            # there is a site for spin-1/2 defined in TeNPy, so just we can just use_
↪it
            # replacing steps 1-3)
            site = SpinHalfSite(conserved='Sz')
        # 4) lattice
        bc = 'periodic' if bc_MPS == 'infinite' else 'open'
        lat = Chain(L, site, bc=bc, bc_MPS=bc_MPS)
        # 5) initialize CouplingModel
        CouplingModel.__init__(self, lat)
        # 6) add terms of the Hamiltonian
        # (u is always 0 as we have only one site in the unit cell)
        self.add_onsite(-hz, 0, 'Sz')
        self.add_coupling(Jxx * 0.5, 0, 'Sp', 0, 'Sm', 1, plus_hc=True)
        # instead of plus_hc=True, we could explicitly add the h.c. term with:
        self.add_coupling(Jz, 0, 'Sz', 0, 'Sz', 1)
        # 7) initialize H_MPO

```

(continues on next page)

(continued from previous page)

```

MPOModel.__init__(self, lat, self.calc_H_MPO())
# 8) initialize H_bond (the order of 7/8 doesn't matter)
NearestNeighborModel.__init__(self, lat, self.calc_H_bond())

class XXZChain2(CouplingMPOModel, NearestNeighborModel):
    """Another implementation of the Spin-1/2 XXZ chain with Sz conservation.

    This implementation takes the same parameters as the :class:`XXZChain`, but is_
    ↪implemented
    based on the :class:`~tenpy.models.model.CouplingMPOModel`.

    Parameters
    -----
    model_params : dict | :class:`~tenpy.tools.params.Config`
        See :cfg:config:`XXZChain`
    """
    def __init__(self, model_params):
        model_params = asConfig(model_params, "XXZChain2")
        model_params.setdefault('lattice', "Chain")
        CouplingMPOModel.__init__(self, model_params)

    def init_sites(self, model_params):
        return SpinHalfSite(conserved='Sz') # use predefined Site

    def init_terms(self, model_params):
        # read out parameters
        Jxx = model_params.get('Jxx', 1.)
        Jz = model_params.get('Jz', 1.)
        hz = model_params.get('hz', 0.)
        # add terms
        for u in range(len(self.lat.unit_cell)):
            self.add_onsite(-hz, u, 'Sz')
        for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
            self.add_coupling(Jxx * 0.5, u1, 'Sp', u2, 'Sm', dx, plus_hc=True)
            self.add_coupling(Jz, u1, 'Sz', u2, 'Sz', dx)

```

The easy easy way: the CouplingMPOModel

Since many of the basic steps above are always the same, we don't need to repeat them all the time. So we have yet another class helping to structure the initialization of models: the CouplingMPOModel. The general structure of this class is like this:

```

class CouplingMPOModel(CouplingModel, MPOModel):
    def __init__(self, model_param):
        # ... follows the basic steps 1-8 using the methods
        lat = self.init_lattice(self, model_param) # for step 4
        # ...
        self.init_terms(self, model_param) # for step 6
        # ...

    def init_sites(self, model_param):
        # You should overwrite this

    def init_lattice(self, model_param):

```

(continues on next page)

(continued from previous page)

```

    sites = self.init_sites(self, model_param) # for steps 1-3
    # initialize an arbitrary pre-defined lattice
    # using model_params['lattice']

    def init_terms(self, model_param):
        # does nothing.
        # You should overwrite this

```

The `XXZChain2` included above illustrates, how it can be used. You need to implement steps 1-3) by overwriting the method `init_sites()` Step 4) is performed in the method `init_lattice()`, which initializes arbitrary 1D or 2D lattices; by default a simple 1D chain. If your model only works for specific lattices, you can overwrite this method in your own class. Step 6) should be done by overwriting the method `init_terms()`. Steps 5,7,8 and calls to the `init_...` methods for the other steps are done automatically if you just call the `CouplingMPOModel.__init__(self, model_param)`.

The `XXZChain` and `XXZChain2` work only with the `Chain` as lattice, since they are derived from the `NearestNeighborModel`. This allows to use them for TEBD in 1D (yeah!), but we can't get the MPO for DMRG on a e.g. a *Square* lattice cylinder - although it's intuitively clear, what the Hamiltonian there should be: just put the nearest-neighbor coupling on each bond of the 2D lattice.

It's not possible to generalize a `NearestNeighborModel` to an arbitrary lattice where it's no longer nearest Neighbors in the MPS sense, but we can go the other way around: first write the model on an arbitrary 2D lattice and then restrict it to a 1D chain to make it a `NearestNeighborModel`.

Let me illustrate this with another standard example model: the transverse field Ising model, implemented in the module `tenpy.models.tf_ising` included below. The `TFIModel` works for arbitrary 1D or 2D lattices. The `TFIChain` is then taking the exact same model making a `NearestNeighborModel`, which only works for the 1D chain.

```

"""Prototypical example of a quantum model: the transverse field Ising model.

Like the :class:`~tenpy.models.xxz_chain.XXZChain`, the transverse field ising chain
:class:`~TFIChain` is contained in the more general :class:`~tenpy.models.spins.
↪SpinChain`;
the idea is more to serve as a pedagogical example for a 'model'.

We choose the field along z to allow to conserve the parity, if desired.
"""
# Copyright 2018-2020 TeNPy Developers, GNU GPLv3

import numpy as np

from .model import CouplingMPOModel, NearestNeighborModel
from ..tools.params import asConfig
from ..networks.site import SpinHalfSite

__all__ = ['TFIModel', 'TFIChain']

class TFIModel(CouplingMPOModel):
    """Transverse field Ising model on a general lattice.

    The Hamiltonian reads:

    .. math ::
        H = - \sum_{\langle i,j \rangle, i < j} J \sigma^x_i \sigma^x_j

```

(continues on next page)

(continued from previous page)

```

- \sum_{i} \mathtt{g} \sigma^z_i

Here,  $\langle i, j \rangle$  denotes nearest neighbor pairs, each pair
↪ appearing
exactly once.
All parameters are collected in a single dictionary `model_params`, which
is turned into a tenpy.tools.params.Config object.

Parameters
-----
model_params : tenpy.tools.params.Config
    Parameters for the model. See tenpy.config.TFIModel below.

Options
-----
.. tenpy.config.TFIModel
   include: CouplingMPOModel

   conserve : None | 'parity'
       What should be conserved. See tenpy.networks.Site.SpinHalfSite.
   J, g : float | array
       Coupling as defined for the Hamiltonian above.

"""
def init_sites(self, model_params):
    conserve = model_params.get('conserve', 'parity')
    assert conserve != 'Sz'
    if conserve == 'best':
        conserve = 'parity'
    if self.verbose >= 1.:
        print(self.name + ": set conserve to", conserve)
    site = SpinHalfSite(conserve=conserve)
    return site

def init_terms(self, model_params):
    J = np.asarray(model_params.get('J', 1.))
    g = np.asarray(model_params.get('g', 1.))
    for u in range(len(self.lat.unit_cell)):
        self.add_onsite(-g, u, 'Sigmaz')
    for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
        self.add_coupling(-J, u1, 'Sigmax', u2, 'Sigmax', dx)
    # done

class TFChain(TFIModel, NearestNeighborModel):
    """The TFIModel on a Chain, suitable for TEBD.

    See the TFIModel for the documentation of parameters.
    """
    def __init__(self, model_params):
        model_params = asConfig(model_params, self.__class__.__name__)
        model_params.setdefault('lattice', "Chain")
        CouplingMPOModel.__init__(self, model_params)

```

Automation of Hermitian conjugation

As most physical Hamiltonians are Hermitian, these Hamiltonians are fully determined when only half of the mutually conjugate terms is defined. For example, a simple Hamiltonian:

$$H = \sum_{\langle i,j \rangle, i < j} -J(c_i^\dagger c_j + c_j^\dagger c_i)$$

is fully determined by the term $c_i^\dagger c_j$ if we demand that Hermitian conjugates are included automatically. In TeNPy, whenever you add a coupling using `add_on_site()`, `add_coupling()`, or `add_multi_coupling()`, you can use the optional argument `plus_hc` to automatically create and add the Hermitian conjugate of that coupling term - as shown above.

Additionally, in an MPO, explicitly adding both a non-Hermitian term and its conjugate increases the bond dimension of the MPO, which increases the memory requirements of the `MPOEnvironment`. Instead of adding the conjugate terms explicitly, you can set a flag `explicit_plus_hc` in the `MPOCouplingModel` parameters, which will ensure two things:

1. The model and the MPO will only store half the terms of each Hermitian conjugate pair added, but the flag `explicit_plus_hc` indicates that they *represent self + h.c.*. In the example above, only the term $c_i^\dagger c_j$ would be saved.
2. At runtime during DMRG, the Hermitian conjugate of the (now non-Hermitian) MPO will be computed and applied along with the MPO, so that the effective Hamiltonian is still Hermitian.

Note: The model flag `explicit_plus_hc` should be used in conjunction with the flag `plus_hc` in `add_coupling()` or `add_multi_coupling()`. If `plus_hc` is `False` while `explicit_plus_hc` is `True` the MPO bond dimension will not be reduced, but you will still pay the additional computational cost of computing the Hermitian conjugate at runtime.

Thus, we end up with several use cases, depending on your preferences. Consider the `FermionModel`. If you do not care about the MPO bond dimension, and want to add Hermitian conjugate terms manually, you would set `model_par['explicit_plus_hc'] = False` and write:

```
self.add_coupling(-J, u1, 'Cd', u2, 'C', dx)
self.add_coupling(np.conj(-J), u2, 'Cd', u1, 'C', -dx)
```

If you wanted to save the trouble of the extra line of code (but still did not care about MPO bond dimension), you would keep the `model_par`, but instead write:

```
self.add_coupling(-J, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Finally, if you wanted a reduction in MPO bond dimension, you would need to set `model_par['explicit_plus_hc'] = True`, and write:

```
self.add_coupling(-J, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Some random remarks on models

- Needless to say that we have also various predefined models under `tenpy.models`.
- Of course, an MPO is all you need to initialize a `MPOModel` to be used for DMRG; you don't have to use the `CouplingModel` or `CouplingMPOModel`. For example an exponentially decaying long-range interactions are not supported by the coupling model but straight-forward to include to an MPO, as demonstrated in the example `examples/mpo_exponentially_decaying.py`.
- If the model of your interest contains Fermions, you should read the *Fermions and the Jordan-Wigner transformation*.
- We suggest writing the model to take a single parameter dictionary for the initialization, as the `CouplingMPOModel` does. The `CouplingMPOModel` converts the dictionary to a dict-like `Config` with some additional features before passing it on to the `init_lattice`, `init_site`, ... methods. It is recommended to read out providing default values with `model_params.get("key", default_value)`, see `get()`.
- When you write a model and want to include a test that it can be at least constructed, take a look at `tests/test_model.py`.

7.3.6 Details on the lattice geometry

The `Lattice` class defines the geometry of the system. In the basic form, it represents a unit cell of a few sites repeated in one or multiple directions. Moreover, it maps this higher-dimensional geometry to a one-dimensional chain for MPS-based algorithms.

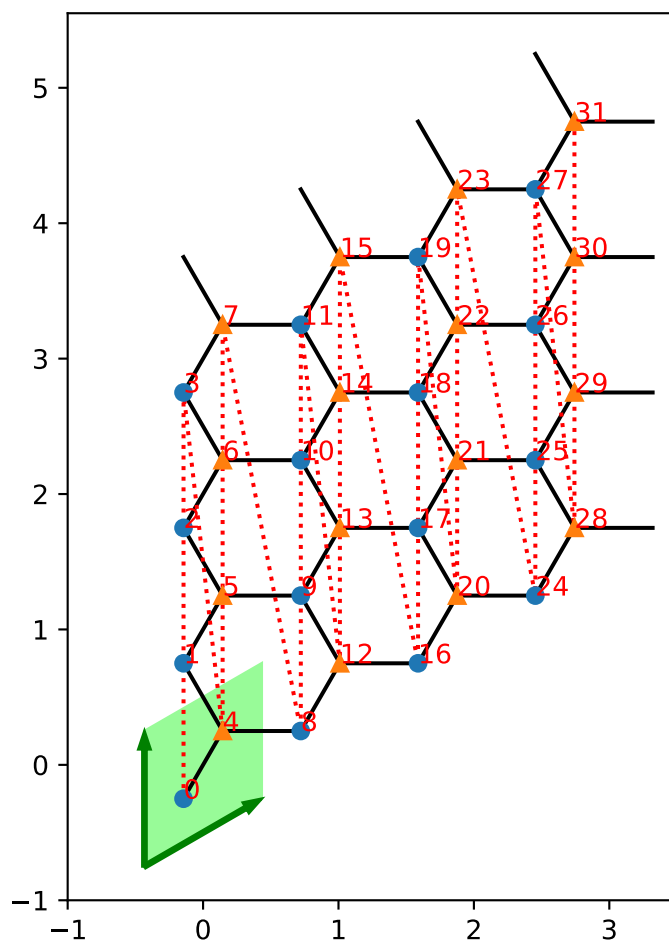
Visualization

A plot of the lattice can greatly help to understand which sites are connected by what couplings. The methods `plot_*` of the `Lattice` can do a good job for a quick illustration. Let's look at the Honeycomb lattice as an example.

```
import matplotlib.pyplot as plt
from tenpy.models import lattice

plt.figure(figsize=(5, 6))
ax = plt.gca()
lat = lattice.Honeycomb(Lx=4, Ly=4, sites=None, bc='periodic')
lat.plot_coupling(ax)
lat.plot_order(ax, linestyle=':')
lat.plot_sites(ax)
lat.plot_basis(ax, origin=-0.5*(lat.basis[0] + lat.basis[1]))
ax.set_aspect('equal')
ax.set_xlim(-1)
ax.set_ylim(-1)
plt.show()
```

In this case, the unit cell (shaded green) consists of two sites, which for the purpose of plotting we just set to `sites=None`; in general you should specify instances of `Site` for that. The unit cell gets repeated in the directions given by the lattice basis (green arrows at the unit cell boundary). Hence, we can label each site by a **lattice index** (x, y, u) in this case, where x in `range(Lx)`, y in `range(Ly)` specify the translation of the unit cell and u in `range(len(unit_cell))`, here u in `[0, 1]`, specifies the index within the unit cell.



How an MPS winds through the lattice: the *order*

For MPS-based algorithms, we need to map a 2D lattice like the one above to a 1D chain. The red, dashed line in the plot indicates how an MPS winds through the 2D lattice. The **MPS index** i is a simple enumeration of the sites along this line, shown as numbers next to the sites in the plot. The methods `mps2lat_idx()` and `lat2mps_idx()` map indices of the MPS to and from indices of the lattice.

The MPS class itself is (mostly) agnostic of the underlying geometry. For example, `expectation_value()` will return a 1D array of the expectation value on each site indexed by the MPS index i . If you have a two-dimensional lattice, you can use `mps2lat_values()` to map this result to a 2D array index by the lattice indices.

A suitable order is critical for the efficiency of MPS-based algorithms. On one hand, different orderings can lead to different MPO bond-dimensions, with direct impact on the complexity scaling. On the other hand, it influences how much entanglement needs to go through each bonds of the underlying MPS, e.g., the ground state to be found in DMRG, and therefore influences the required MPS bond dimensions. For the latter reason, the “optimal” ordering can not be known a priori and might even depend on your coupling parameters (and the phase you are in). In the end, you can just try different orderings and see which one works best.

The simplest way to *change* the order is to use a non-default value for the initialization parameter *order* of the `Lattice` class. This gets passed on to `ordering()`, which you can override in a custom lattice class to define new possible orderings. Alternatively, you can go the most general way and simply set the attribute *order* to be a 2D numpy array with lattice indices as rows, in the order you want.

```
import matplotlib.pyplot as plt
from tenpy.models import lattice

Lx, Ly = 3, 3
fig, axes = plt.subplots(2, 2, figsize=(7, 8))

lat1 = lattice.Honeycomb(Lx, Ly, sites=None, bc='periodic') # default order
lat2 = lattice.Honeycomb(Lx, Ly, sites=None, bc='periodic',
                        order="Cstyle") # first method to change order
# alternative: directly set "Cstyle" order
lat3 = lattice.Honeycomb(Lx, Ly, sites=None, bc='periodic')
lat3.order = lat2.ordering("Cstyle") # now equivalent to lat2

# general: can apply arbitrary permutation to the order
lat4 = lattice.Honeycomb(Lx, Ly, sites=None, bc='periodic',
                        order="Cstyle")

old_order = lat4.order
permutation = []
for i in range(0, len(old_order), 2):
    permutation.append(i+1)
    permutation.append(i)
lat4.order = old_order[permutation, :]

for lat, label, ax in zip([lat1, lat2, lat3, lat4],
                        ["order='default'",
                         "order='Cstyle'",
                         "order='Cstyle'",
                         "custom permutation"],
                        axes.flatten()):
    lat.plot_coupling(ax)
    lat.plot_sites(ax)
    lat.plot_order(ax, linestyle=':', linewidth=2.)
    ax.set_aspect('equal')
    ax.set_title('order = ' + repr(label))
```

(continues on next page)

(continued from previous page)

```
plt.show()
```

Boundary conditions

The `Lattice` defines the **boundary conditions** `bc` in each direction. It can be one of the usual 'open' or 'periodic' in each direction.

On top of that, there is the `bc_MPS` boundary condition of the MPS, one of 'finite', 'segment', 'infinite'. For an 'infinite' MPS, the whole lattice is repeated in the direction of the *first* basis vector of the lattice. For `bc_MPS='infinite'`, the first direction should always be 'periodic', but you *can* also define a lattice with `bc_MPS='finite'`, `bc=['periodic', 'periodic']` for a finite system on the torus. This is discouraged, though, because the ground state MPS will require the *squared* bond dimension for the *same* precision in this case!

For two (or higher) dimensional lattices, e.g. for DMRG on an infinite cylinder, you can also specify an integer *shift* instead of just saying 'periodic': Rolling the 2D lattice up into a cylinder, you have a degree of freedom which sites to connect. This is illustrated in the figure below for a *Square* lattice with `bc=['periodic', shift]` for `shift` in `[-1, 0, 1]` (different columns). In the first row, the orange markers indicate a pair of identified sites (see `plot_bc_shift()`). The dashed orange line indicates the direction of the cylinder axis. The line where the cylinder is “cut open” therefore winds around the cylinder for a non-zero *shift*. (A similar thing happens even for `shift=0` for more complicated lattices with non-orthogonal basis.) In the second row, we directly draw lines between all sites connected by nearest-neighbor couplings, as they appear in the MPO.

Irregular Lattices

The `IrregularLattice` allows to add or remove sites from/to an existing regular lattice. The doc-string of `IrregularLattice` contains several examples, let us consider another one here, where we use the `IrregularLattice` to “fix” the boundary of the Honeycomb lattice: when we use "open" boundary conditions for a finite system, there are two sites (on the lower left, and upper right), which are not included into any hexagonal. The following example shows how to remove them from the system:

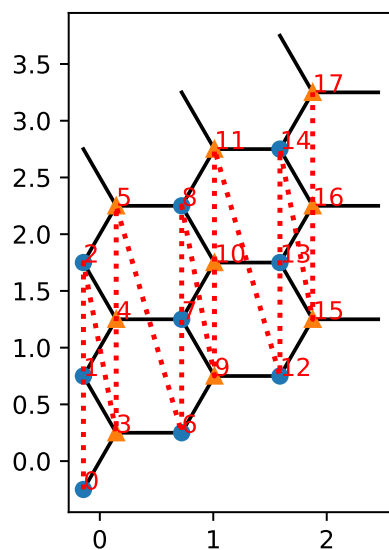
```
import matplotlib.pyplot as plt
from tenpy.models import lattice

Lx, Ly = 3, 3
fig, axes = plt.subplots(1, 2, True, True, figsize=(6, 4))

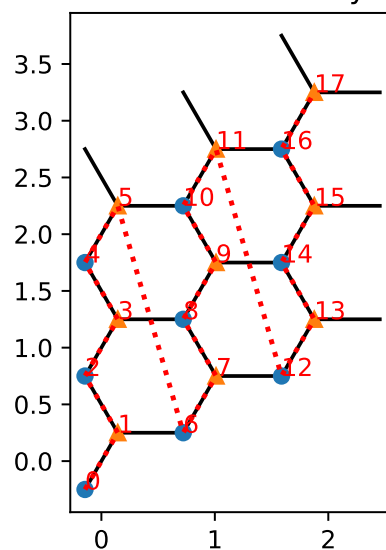
reg_lat = lattice.Honeycomb(Lx=Lx, Ly=Ly, sites=None, bc='open')
irr_lat = lattice.IrregularLattice(reg_lat, remove=[[0, 0, 0], [-1, -1, 1]])
for lat, label, ax in zip([reg_lat, irr_lat],
                          ["regular", "irregular"],
                          axes.flatten()):
    lat.plot_coupling(ax)
    lat.plot_order(ax, linestyle=':')
    lat.plot_sites(ax)
    ax.set_aspect('equal')
    ax.set_title(label)

plt.show()
```

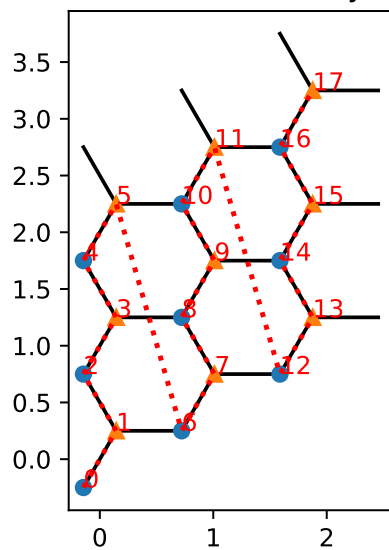
order = "order='default'"



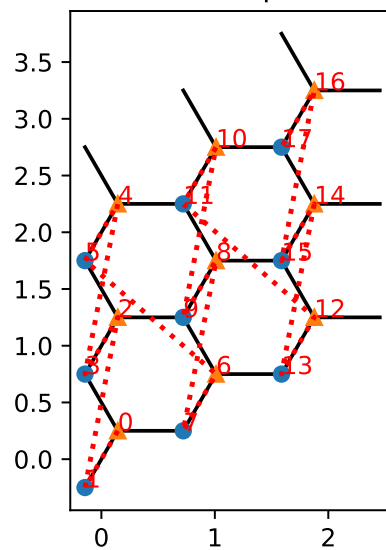
order = "order='Cstyle'"

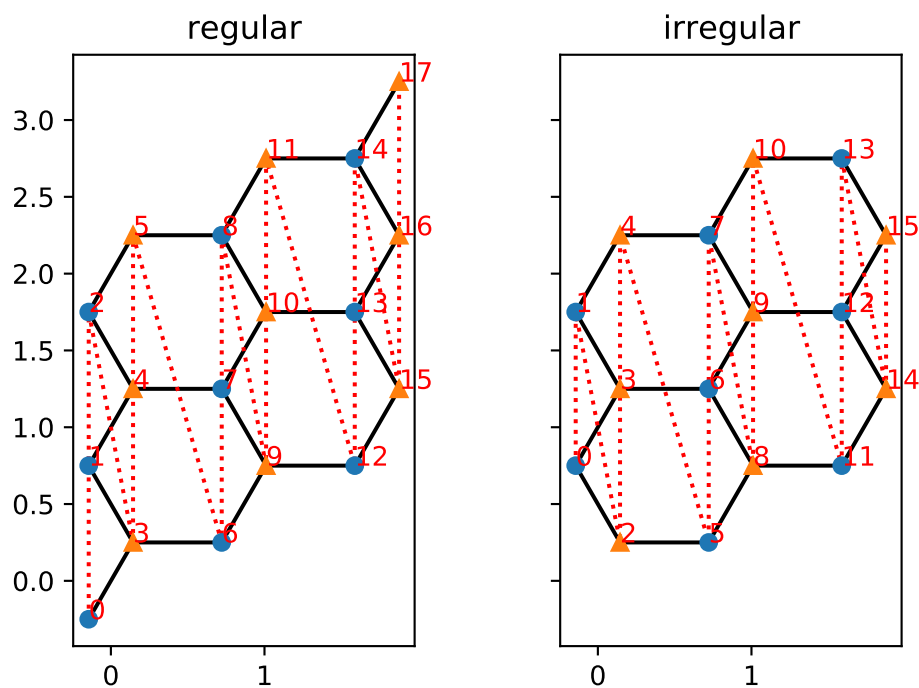
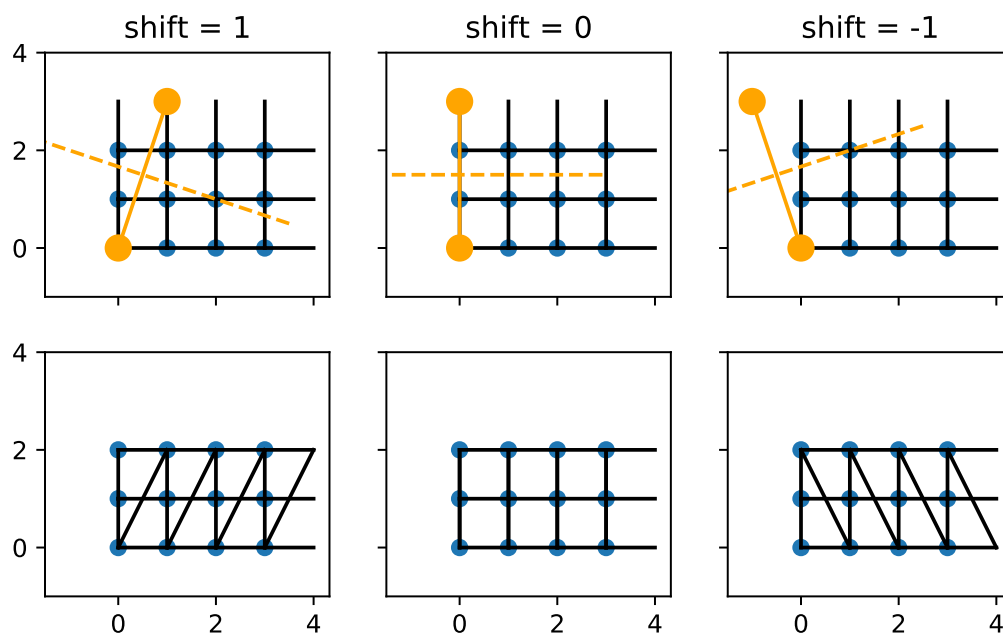


order = "order='Cstyle'"



order = 'custom permutation'





7.3.7 Fermions and the Jordan-Wigner transformation

The [Jordan-Wigner transformation](#) maps fermionic creation- and annihilation operators to (bosonic) spin-operators.

Spinless fermions in 1D

Let's start by explicitly writing down the transformation. With the Pauli matrices $\sigma_j^{x,y,z}$ and $\sigma_j^\pm = (\sigma_j^x \pm i\sigma_j^y)/2$ on each site, we can map

$$\begin{aligned} n_j &\leftrightarrow (\sigma_j^z + 1)/2 \\ c_j &\leftrightarrow (-1)^{\sum_{l<j} n_l} \sigma_j^- \\ c_j^\dagger &\leftrightarrow (-1)^{\sum_{l<j} n_l} \sigma_j^+ \end{aligned}$$

The n_l in the second and third row are defined in terms of Pauli matrices according to the first row. We do not interpret the Pauli matrices as spin-1/2; they have nothing to do with the spin in the spin-full case. If you really want to interpret them physically, you might better think of them as hard-core bosons ($b_j = \sigma_j^-, b_j^\dagger = \sigma_j^+$), with a spin of the fermions mapping to a spin of the hard-core bosons.

Note that this transformation maps the fermionic operators c_j and c_j^\dagger to *global* operators; although they carry an index j indicating a site, they actually act on all sites $1 \leq j$! Thus, clearly the operators `C` and `Cd` defined in the [FermionSite](#) do *not* directly correspond to c_j and c_j^\dagger . The part $(-1)^{\sum_{l<j} n_l}$ is called Jordan-Wigner string and in the [FermionSite](#) is given by the local operator $JW := (-1)^{n_l}$ acting all sites $1 \leq j$. Since this is important, let me stress it again:

Warning: The fermionic operator c_j (and similar c_j^\dagger) maps to a *global* operator consisting of the Jordan-Wigner string built by the local operator `JW` on sites $1 \leq j$ *and* the local operator `C` (or `Cd`, respectively) on site j .

On the sites itself, the onsite operators `C` and `Cd` in the [FermionSite](#) fulfill the correct anti-commutation relation, without the need to include `JW` strings. The `JW` string is necessary to ensure the anti-commutation for operators acting on different sites.

Written in terms of *onsite* operators defined in the [FermionSite](#), with the i -th entry in the list acting on site i , the relations are thus:

```
["JW", ..., "JW", "C", "Id", ..., "Id"] # for the annihilation operator
["JW", ..., "JW", "Cd", "Id", ..., "Id"] # for the creation operator
```

Note that "JW" squares to the identity, "JW JW" == "Id", which is the reason that the Jordan-wigner string completely cancels in $n_j = c_j^\dagger c_j$. In the above notation, this can be written as:

```
["JW", ..., "JW", "Cd", "Id", ..., "Id"] * ["JW", ..., "JW", "C", "Id", ..., "Id"]
== ["JW JW", ..., "JW JW", "Cd C", "Id Id", ..., "Id Id"] # by definition of
↪ the tensorproduct
== ["Id", ..., "Id", "N", "Id", ..., "Id"] # by definition of
↪ the local operators
# ("X Y" stands for the local operators X and Y applied on the same site. We assume
↪ that the "Cd" and "C" on the first line act on the same site.)
```

For a pair of operators acting on different sites, `JW` strings have to be included for every site between the operators. For example, taking $i < j$, $c_i^\dagger c_j \leftrightarrow \sigma_i^+ (-1)^{\sum_{i<=l<j} n_l} \sigma_j^-$. More explicitly, for $j = i+2$ we get:

```
["JW", ..., "JW", "Cd", "Id", "Id", "Id", ..., "Id"] * ["JW", ..., "JW", "JW", "JW",
↪ "C", "Id", ..., "Id"]
== ["JW JW", ..., "JW JW", "Cd JW", "Id JW", "Id C", ..., "Id"]
== ["Id", ..., "Id", "Cd JW", "JW", "C", ..., "Id"]
```

In other words, the Jordan-Wigner string appears only in the range $i \leq l < j$, i.e. between the two sites *and* on the smaller/left one of them. (You can easily generalize this rule to cases with more than two c or c^\dagger .)

This last line (as well as the last line of the previous example) can be rewritten by changing the order of the operators $Cd JW$ to $"JW Cd" == - "Cd"$. (This is valid because either site i is occupied, yielding a minus sign from the JW , or it is empty, yielding a 0 from the Cd .)

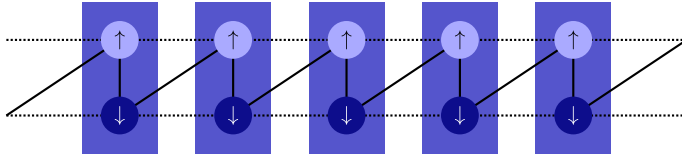
This is also the case for $j < i$, say $j = i-2$: $c_i^\dagger c_j \leftrightarrow (-1)^{\sum_{j <= l < i} n_l} \sigma_i^+ \sigma_j^-$. As shown in the following, the JW again appears on the left site, but this time acting *after* C :

```
["JW", ..., "JW", "JW", "JW", "Cd", "Id", ..., "Id"] * ["JW", ..., "JW", "C", "Id",
↪ "Id", "Id", ..., "Id"]
== ["JW JW", ..., "JW JW", "JW C", "JW", "Cd Id", ..., "Id"]
== ["Id", ..., "Id", "JW C", "JW", "Cd", ..., "Id"]
```

Higher dimensions

For an MPO or MPS, you always have to define an ordering of all your sites. This ordering effectivly maps the higher-dimensional lattice to a 1D chain, usually at the expense of long-range hopping/interactions. With this mapping, the Jordan-Wigner transformation generalizes to higher dimensions in a straight-forward way.

Spinful fermions



As illustrated in the above picture, you can think of spin-1/2 fermions on a chain as spinless fermions living on a ladder (and analogous mappings for higher dimensional lattices). Each rung (a blue box in the picture) forms a *SpinHalfFermionSite* which is composed of two *FermionSite* (the circles in the picture) for spin-up and spin-down. The mapping of the spin-1/2 fermions onto the ladder induces an ordering of the spins, as the final result must again be a one-dimensional chain, now containing both spin species. The solid line indicates the convention for the ordering, the dashed lines indicate spin-preserving hopping $c_{s,i}^\dagger c_{s,i+1} + h.c.$ and visualize the ladder structure. More generally, each species of fermions appearing in your model gets a separate label, and its Jordan-Wigner string includes the signs $(-1)^{n_l}$ of *all* species of fermions to the ‘left’ of it (in the sense of the ordering indicated by the solid line in the picture).

In the case of spin-1/2 fermions labeled by \uparrow and \downarrow on each *site*, the complete mapping is given (where j and l are indices of the *FermionSite*):

$$\begin{aligned}
 n_{\uparrow,j} &\leftrightarrow (\sigma_{\uparrow,j}^z + 1)/2 \\
 n_{\downarrow,j} &\leftrightarrow (\sigma_{\downarrow,j}^z + 1)/2 \\
 c_{\uparrow,j} &\leftrightarrow (-1)^{\sum_{l < j} n_{\uparrow,l} + n_{\downarrow,l}} \sigma_{\uparrow,j}^- \\
 c_{\uparrow,j}^\dagger &\leftrightarrow (-1)^{\sum_{l < j} n_{\uparrow,l} + n_{\downarrow,l}} \sigma_{\uparrow,j}^+ \\
 c_{\downarrow,j} &\leftrightarrow (-1)^{\sum_{l < j} n_{\uparrow,l} + n_{\downarrow,l}} (-1)^{n_{\uparrow,j}} \sigma_{\downarrow,j}^- \\
 c_{\downarrow,j}^\dagger &\leftrightarrow (-1)^{\sum_{l < j} n_{\uparrow,l} + n_{\downarrow,l}} (-1)^{n_{\uparrow,j}} \sigma_{\downarrow,j}^+
 \end{aligned}$$

In each of the above mappings the operators on the right hand sides commute; we can rewrite $(-1)^{\sum_{l < j} n_{\uparrow,l} + n_{\downarrow,l}} = \prod_{l < j} (-1)^{n_{\uparrow,l}} (-1)^{n_{\downarrow,l}}$, which resembles the actual structure in the code more closely. The parts of the operator acting in the same box of the picture, i.e. which have the same index j or l , are the ‘onsite’ operators in the `SpinHalfFermionSite`: for example JW on site j is given by $(-1)^{n_{\uparrow,j}} (-1)^{n_{\downarrow,j}}$, Cu is just the $\sigma_{\uparrow,j}^-$, Cdu is $\sigma_{\uparrow,j}^+$, Cd is $(-1)^{n_{\uparrow,j}} \sigma_{\downarrow,j}^-$, and Cdd is $(-1)^{n_{\uparrow,j}} \sigma_{\downarrow,j}^+$. Note the asymmetry regarding the spin in the definition of the onsite operators: the spin-down operators include Jordan-Wigner signs for the spin-up fermions on the same site. This asymmetry stems from the ordering convention introduced by the solid line in the picture, according to which the spin-up site is “left” of the spin-down site. With the above definition, the operators within the same `SpinHalfFermionSite` fulfill the expected commutation relations, for example `"Cu Cdd" == - "Cdd Cu"`, but again the JW on sites left of the operator pair is crucial to get the correct commutation relations globally.

Warning: Again, the fermionic operators $c_{\downarrow,j}, c_{\downarrow,j}^\dagger, c_{\uparrow,j}, c_{\uparrow,j}^\dagger$ correspond to *global* operators consisting of the Jordan-Wigner string built by the local operator JW on sites $1 < j$ and the local operators `'Cu'`, `'Cdu'`, `'Cd'`, `'Cdd'` on site j .

Written explicitly in terms of onsite operators defined in the `FermionSite`, with the j -th entry entry in the list acting on site j , the relations are:

```
[ "JW", ..., "JW", "Cu", "Id", ..., "Id"]    # for the annihilation operator spin-up
[ "JW", ..., "JW", "Cd", "Id", ..., "Id"]    # for the annihilation operator spin-down
[ "JW", ..., "JW", "Cdu", "Id", ..., "Id"]   # for the creation operator spin-up
[ "JW", ..., "JW", "Cdd", "Id", ..., "Id"]   # for the creation operator spin-down
```

As you can see, the asymmetry regarding the spins in the definition of the local onsite operators `"Cu"`, `"Cd"`, `"Cdu"`, `"Cdd"` lead to a symmetric definition in the global sense. If you look at the definitions very closely, you can see that in terms like `["Id", "Cd JW", "JW", "Cd"]` the Jordan-Wigner sign $(-1)^{n_{\uparrow,2}}$ appears twice (namely once in the definition of `"Cd"` and once in the `"JW"` on site 2) and could in principle be canceled, however in favor of a simplified handling in the code we do not recommend you to cancel it. Similar, within a spinless `FermionSite`, one can simplify `"Cd JW" == "Cd"` and `"JW C" == "C"`, but these relations do *not* hold in the `SpinHalfSite`, and for consistency we recommend to explicitly keep the `"JW"` operator string even in nearest-neighbor models where it is not strictly necessary.

How to handle Jordan-Wigner strings in practice

There are only a few pitfalls where you have to keep the mapping in mind: When **building a model**, you map the physical fermionic operators to the usual spin/bosonic operators. The algorithms don’t care about the mapping, they just use the given Hamiltonian, be it given as MPO for DMRG or as nearest neighbor couplings for TEBD. Only when you do a **measurement** (e.g. by calculating an expectation value or a correlation function), you have to reverse this mapping. Be aware that in certain cases, e.g. when calculating the entanglement entropy on a certain bond, you cannot reverse this mapping (in a straightforward way), and thus your results might depend on how you defined the Jordan-Wigner string.

Whatever you do, you should first think about if (and how much of) the Jordan-Wigner string cancels. For example for many of the onsite operators (like the particle number operator N or the spin operators in the `SpinHalfFermionSite`) the Jordan-Wigner string cancels completely and you can just ignore it both in onsite-terms and couplings. In case of two operators acting on different sites, you typically have a Jordan-Wigner string inbetween (e.g. for the $c_i^\dagger c_j$ examples described above and below) or no Jordan-Wigner strings at all (e.g. for density-density interactions $n_i n_j$). In fact, the case that the Jordan Wigner string on the left of the first non-trivial operator does not cancel is currently not supported for models and expectation values, as it usually doesn’t appear in practice. For terms involving more operators, things tend to get more complicated, e.g. $c_i^\dagger c_j^\dagger c_k c_l$ with $i < j < k < l$ requires a Jordan-Wigner string on sites m with $i \leq m < j$ or $k \leq m < l$, but not for $j < m < k$.

Note: TeNPy keeps track of which onsite operators need a Jordan-Wigner string in the `Site` class, specifically in `need_JW_string` and `op_needs_JW()`. Hence, when you define custom sites or add extra operators to the sites, make sure that `op_needs_JW()` returns the expected results.

When **building a model** the Jordan-Wigner strings need to be taken into account. If you just specify the `H_MPO` or `H_bond`, it is *your* responsibility to use the correct mapping. However, if you use the `add_coupling()` method of the `CouplingModel`, (or the generalization `add_multi_coupling()` for more than 2 operators), TeNPy can use the information from the `Site` class to *automatically add Jordan-Wigner* strings as needed. Indeed, with the default argument `op_string=None`, `add_coupling` will automatically check whether the operators need Jordan-Wigner strings and correspondingly set `op_string='JW'`, `str_on_first=True`, if necessary. For `add_multi_coupling`, you can't even explicitly specify the correct Jordan-Wigner strings, but you **must use** `op_string=None`, from which it will automatically determine where Jordan-Wigner strings are needed.

Obviously, you should be careful about the convention which of the operators is applied first (in a physical sense as an operator acting on a state), as this corresponds to a sign of the prefactor. Read the doc-strings of `add_coupling()` `add_multi_coupling()` for details.

As a concrete example, let us specify a hopping $\sum_i (c_i^\dagger c_{i+1} + h.c.) = \sum_i (c_i^\dagger c_{i+1} + c_i^\dagger c_{i-1})$ in a 1D chain of `FermionSite` with `add_coupling()`. The recommended way is just:

```
add_coupling(strength, 0, 'Cd', 0, 'C', 1, plus_hc=True)
```

If you want to specify both the Jordan-Wigner string and the h.c. term explicitly, you can use:

```
add_coupling(strength, 0, 'Cd', 0, 'C', 1, op_string='JW', str_on_first=True)
add_coupling(strength, 0, 'Cd', 0, 'C', -1, op_string='JW', str_on_first=True)
```

Slightly more complicated, to specify the hopping $\sum_{\langle i,j \rangle, s} (c_{s,i}^\dagger c_{s,j} + h.c.)$ in the Fermi-Hubbard model on a 2D square lattice, we could use:

```
for (dx, dy) in [(1, 0), (0, 1)]:
    add_coupling(strength, 0, 'Cdu', 0, 'Cu', (dx, dy), plus_hc=True) # spin up
    add_coupling(strength, 0, 'Cdd', 0, 'Cd', (dx, dy), plus_hc=True) # spin down

# or without `plus_hc`
for (dx, dy) in [(1, 0), (-1, 0), (0, 1), (0, -1)]: # include -dx !
    add_coupling(strength, 0, 'Cdu', 0, 'Cu', (dx, dy)) # spin up
    add_coupling(strength, 0, 'Cdd', 0, 'Cd', (dx, dy)) # spin down

# or specifying the 'JW' string explicitly
for (dx, dy) in [(1, 0), (-1, 0), (0, 1), (0, -1)]:
    add_coupling(strength, 0, 'Cdu', 0, 'Cu', (dx, dy), 'JW', True) # spin up
    add_coupling(strength, 0, 'Cdd', 0, 'Cd', (dx, dy), 'JW', True) # spin down
```

The most important functions for doing **measurements** are probably `expectation_value()` and `correlation_function()`. Again, if all the Jordan-Wigner strings cancel, you don't have to worry about them at all, e.g. for many onsite operators or correlation functions involving only number operators. If you build multi-site operators to be measured by `expectation_value`, take care to include the Jordan-Wigner string correctly.

Some MPS methods like `correlation_function()`, `expectation_value_term()` and `expectation_value_terms_sum()` automatically add Jordan-Wigner strings (at least with default arguments). Other more low-level functions like `expectation_value_multi_sites()` don't do it. Hence, you should always watch out during measurements, if the function used needs special treatment for Jordan-Wigner strings.

7.3.8 Saving to disk: input/output

Using pickle

A simple and pythonic way to store data of TeNPy arrays is to use `pickle` from the Python standard library. Pickle allows to store (almost) arbitrary python objects, and the `Array` is no exception (and neither are other TeNPy classes).

Say that you have run DMRG to get a ground state *psi* as an MPS. With pickle, you can save it to disk as follows:

```
import pickle
with open('my_psi_file.pkl', 'wb') as f:
    pickle.dump(psi, f)
```

Here, the `with ... :` structure ensures that the file gets closed after the pickle dump, and the `'wb'` indicates the file opening mode “write binary”. Reading the data from disk is as easy as `'rb'` for reading binary):

```
with open('my_psi_file.pkl', 'rb') as f:
    psi = pickle.load(f)
```

Note: It is a good (scientific) practice to include meta-data to the file, like the parameters you used to generate that state. Instead of just the *psi*, you can simply store a dictionary containing *psi* and other data, e.g., `data = {'psi': psi, 'dmrg_params': dmrg_params, 'model_params': model_params}`. This can *save you a lot of pain*, when you come back looking at the files a few month later and forgot what you’ve done to generate them!

In some cases, compression can significantly reduce the space needed to save the data. This can for example be done with `gzip` (as well in the Python standard library). However, be warned that it might cause longer loading and saving times, i.e. it comes at the penalty of more CPU usage for the input/output. In Python, this requires only small adjustments:

```
import pickle
import gzip

# to save:
with gzip.open('my_data_file.pkl', 'wb') as f:
    pickle.dump(data, f)
# and to load:
with gzip.open('my_data_file.pkl', 'rb') as f:
    data = pickle.load(data, f)
```

Using HDF5 with h5py

While `pickle` is great for simple input/output of python objects, it also has disadvantages. The probably most dramatic one is the limited portability: saving data on one PC and loading it on another one might fail! Even exporting data from Python 2 to load them in Python 3 on the same machine can give quite some troubles. Moreover, pickle requires to load the whole file at once, which might be unnecessary if you only need part of the data, or even lead to memory problems if you have more data on disk than fits into RAM.

Hence, we support saving to `HDF5` files as an alternative. The `h5py` package provides a dictionary-like interface for the file/group objects with numpy-like data sets, and is quite easy to use. If you don’t know about `HDF5`, read the [quickstart](#) of the `h5py` documentation (and this guide).

The implementation can be found in the `tenpy.tools.hdf5_io` module with the `Hdf5Saver` and `Hdf5Loader` classes and the wrapper functions `save_to_hdf5()`, `load_from_hdf5()`.

The usage is very similar to pickle:

```
import h5py
from tenpy.tools import hdf5_io

data = {"psi": psi, # e.g. an MPS
        "model": my_model,
        "parameters": {"L": 6, "g": 1.3}}

with h5py.File("file.h5", 'w') as f:
    hdf5_io.save_to_hdf5(f, data)
# ...
with h5py.File("file.h5", 'r') as f:
    data = hdf5_io.load_from_hdf5(f)
    # or for partial reading:
    pars = hdf5_io.load_from_hdf5(f, "/parameters")
```

Note: The [hickle](#) package imitates the pickle functionality while saving the data to HDF5 files. However, since it aims to be close to pickle, it results in a more complicated data structure than we want here.

Note: To use the export/import features to HDF5, you need to install the [h5py](#) python package (and hence some version of the HDF5 library).

Data format specification for saving to HDF5

This section motivates and defines the format how we save data of TeNPy-defined classes. The goal is to have the `save_to_hdf5()` function for saving sufficiently simple enough python objects (supported by the format) to disk in an HDF5 file, such that they can be reconstructed with the `load_from_hdf5()` function, as outlined in the example code above.

Guidelines of the format:

0. Store enough data such that `load_from_hdf5()` can reconstruct a copy of the object (provided that the save did not fail with an error).
1. Objects of a type supported by the HDF5 datasets (with the [h5py](#) interface) should be directly stored as [h5py Dataset](#). Such objects are for example numpy arrays (of non-object *dtype*), scalars and strings.
2. Allow to save (nested) python lists, tuples and dictionaries with values (and keys) which can be saved.
3. Allow user-defined classes to implement a well-defined interface which allows to save instances of that class, hence extending what data can be saved. An instance of a class supporting the interface gets saved as an [HDF5 Group](#). Class attributes are stored as entries of the group, metadata like the type should be stored in HDF5 attributes, see [attributes](#).
4. Simple and intuitive, human-readable structure for the HDF5 paths. For example, saving a simple dictionary `{ 'a': np.arange(10), 'b': 123.45 }` should result in an HDF5 file with just the two data sets `/a` and `/b`.
5. Allow loading only a subset of the data by specifying the *path* of the HDF5 group to be loaded. For the above example, specifying the path `/b` should result in loading the float `123.45`, not the array.
6. Avoid unnecessary copies if the same python object is referenced by different names, e.g, for the data `{ 'c': large_obj, 'd': large_obj }` with two references to the same *large_obj*, save it only once and use HDF5 hard-links such that `/c` and `/d` are the same HDF5 dataset/group. Also avoid the copies during the

loading, i.e., the loaded dictionary should again have two references to a single object *large_obj*. This is also necessary to allow saving and loading of objects with cyclic references.

7. Loading a dataset should be (fairly) secure and not execute arbitrary python code (even if the dataset was manipulated), as it is the case for pickle.

Disclaimer: I'm not an security expert, so I can't guarantee that... Also, loading a HDF5 file can import other python modules, so importing a manipulated file is not secure if you downloaded a malicious python file as well.

The full format specification is given by the what the code in `hdf5_io` does... Since this is not trivial to understand, let me summarize it here:

- Following 1), simple scalars, strings and numpy arrays are saved as `Dataset`. Other objects are saved as a HDF5 `Group`, with the actual data being saved as group members (as sub-groups and sub-datasets) or as attributes (for metadata or simple data).
- The type of the object is stored in the HDF5 attribute `'type'`, which is one of the global `REPR_*` variables in `tenpy.tools.hdf5_io`. The type determines the format for saving/loading of builtin types (list, ...)
- Userdefined classes which should be possible to export/import need to implement the methods `save_hdf5` and `from_hdf5` as specified in `Hdf5Exportable`. When saving such a class, the attribute `'type'` is automatically set to `'instance'`, and the class name and module are saved under the attributes `'module'` and `'class'`. During loading, this information is used to automatically import the module, get the class and call the classmethod `from_hdf5` for reconstruction. This can only work if the class definition already exists, i.e., you can only save class instances, not classes itself.
- For most (python) classes, simply subclassing `Hdf5Exportable` should work to make the class exportable. The latter saves the contents of `__dict__`, with the extra attribute `'format'` specifying whether the dictionary is “simple” (see below.).
- The `None` object is saved as a group with the attribute `'type'` being `'None'` and no subgroups.
- For iterables (list, tuple and set), we simple enumerate the entries and save entries as group members under the names `'0'`, `'1'`, `'2'`, ..., and a maximum `'len'` attribute.
- The format for dictionaries depends on whether all keys are “simple”, which we define as being strings which are valid path names in HDF5, see `valid_hdf5_path_component()`. Following 4), the keys of a simple dictionary are directly used as names for group members, and the values being whatever object the group member represents.
- Partial loading along 5) is possible by directly specifying the subgroup or the path to `load_from_hdf5()`.
- Guideline 6) is ensured as much as possible. However, there is a bug/exception: tuples with cyclic references are not re-constructed correctly; the inner objects will be lists instead of tuples (but with the same object entries).

Finally, we have to mention that many TeNPy classes are `Hdf5Exportable`. In particular, the `Array` supports this. To see what the exact format for those classes is, look at the `save_hdf5` and `from_hdf5` methods of those classes.

Note: There can be multiple possible output formats for the same object. The dictionary – with the format for simple keys or general keys – is such an example, but userdefined classes can use the same technique in their `from_hdf5` method. The user might also explicitly choose a “lossy” output format (e.g. “flat” for np_conserved Arrays and LegCharges).

Tip: The above format specification is quite general and not bound to TeNPy. Feel free to use it in your own projects ;-) To separate the development, versions and issues of the format clearly from TeNPy, we maintain the code for it in a separate git repository, https://github.com/tenpy/hdf5_io

7.4 Literature

This is a (by far non-exhaustive) list of some references for the various ideas behind the code. They can be cited from the python doc-strings using the format `[Author####]_`. Within each category, we sort the references by year and author.

7.4.1 TeNPy related sources

[TeNPyNotes] are lecture notes, meant as an introduction to tensor networks (focusing on MPS), and introduced TeNPy to the scientific community by giving examples how to call the algorithms in TeNPy. [TeNPySource] is the location of the source code, and the place where you can report bugs. [TeNPyDoc] is where the location is hosted online. [TeNPyForum] is the place where you can ask questions and look for help, when you are stuck with implementing something.

7.4.2 General reading

[Schollwoeck2011] is an extensive introduction to MPS, DMRG and TEBD with lots of details on the implementations, and a classic read, although a bit lengthy. Our [TeNPyNotes] are a shorter summary of the important concepts, similar as [Orus2014]. [Hubig2019] is a very good, recent review focusing on time evolution with MPS. The lecture notes of [Eisert2013] explain the area law as motivation for tensor networks very well. PEPS are for example reviewed in [Verstraete2009], [Eisert2013] and [Orus2014]. [Stoudenmire2011] reviews the use of DMRG for 2D systems. [Cirac2009] discusses the different groups of tensor network states.

7.4.3 Algorithm developments

[White1992] is the invention of DMRG, which started everything. [Vidal2004] introduced TEBD. [White2005] and [Hubig2015] solved problems for single-site DMRG. [McCulloch2008] was a huge step forward to solve convergence problems for infinite DMRG. [Singh2009], [Singh2010] explain how to incorporate Symmetries. [Haegeman2011] introduced TDVP, again explained more accessible in [Haegeman2016]. [Zaletel2015] is another standard method for time-evolution with long-range Hamiltonians. [Karrasch2013] gives some tricks to do finite-temperature simulations (DMRG), which is a bit extended in [Hauschild2018]. [Vidal2007] introduced MERA.

7.4.4 Related theory

The following are referenced from somewhere in the algorithms.

7.4.5 Software-related

The following are not physics-related, but are good to know if you want to work with TeNPy (or more generally Python).

7.5 Contributing

There are lots of things where you can help, even if you don't want to dig deep into the source code. You are welcome to do any of the following things, all of them are very helpful!

- Report bugs and problems, such that they can be fixed.
- Implement new models.
- Update and extend the documentation.
- Give feedback on how you like TeNPy and what you would like to see improved.
- Help fixing bugs.
- Help fixing minor issues.
- Extend the functionality by implementing new functions, methods, and algorithms.

The code is maintained in a git repository, the official repository is on [github](#). Even if you're not yet on the developer team, you can still submit pull requests on github. If you're unsure how or what to do, you can ask for help in the [\[TeNPyForum\]](#). If you want to become a member of the developer team, just ask ;-)

Thank You!

7.5.1 Coding Guidelines

To keep consistency, we ask you to comply with the following guidelines for contributions. However, these are just guidelines - it still helps if you contribute something, even if doesn't follow these rules ;-)

- Use a code style based on **PEP 8**. The git repo includes a config file `.style.yapf` for the python package `yapf`. `yapf` is a tool to auto-format code, e.g., by the command `yapf -i some/file` (-i for "in place"). We run `yapf` on a regular basis on the github master branch. If your branch diverged, it might help to run `yapf` before merging.

Note: Since no tool is perfect, you can format some regions of code manually and enclose them with the special comments `# yapf: disable` and `# yapf: enable`.

- Every function/class/module should be documented by its doc-string, see **PEP 257**. We auto-format the doc-strings with `docformatter` on a regular basis.

Additional documentation for the user guide is in the folder `doc/`.

The documentation uses *reStructuredText*. If you are new to *reStructuredText*, read this [introduction](#). We use the *numpy* style for doc-strings (with the [napoleon](#) extension to sphinx). You can read about them in these [Instructions for the doc strings](#). In addition, you can take a look at the following [example file](#). Helpful hints on top of that:

```
r""<- this r makes me a raw string, thus '\' has no special meaning.
Otherwise you would need to escape backslashes, e.g. in math formulas.

You can include cross references to classes, methods, functions, modules like
:class:`~tenpy.linalg.np_conserved.Array`, :meth:`~tenpy.linalg.np_conserved.
↪Array.to_ndarray`,
:func:`~tenpy.tools.math.toiterable`, :mod:`~tenpy.linalg.np_conserved`.
The ~ in the beginning makes only the last part of the name appear in the_
↪generated documentation.
Documents of the userguide can be referenced with :doc:`~intro_npc` even from_
↪inside the doc-strings.
```

(continues on next page)

(continued from previous page)

```

You can also cross-link to other documentations, e.g. :class:`numpy.ndarray`,
↪:func`scipy.linalg.svd` and :mod: will work.

Moreover, you can link to github issues, arXiv papers, dois, and topics in the
↪community forum with
e.g. :issue:`5`, :arxiv:`1805.00055`, :doi:`10.1000/1` and :forum:`3`.

Write inline formulas as :math:`H |\Psi\rangle = E |\Psi\rangle` or displayed
↪equations as
.. math ::


$$e^{i\pi} + 1 = 0$$


In doc-strings, math can only be used in the Notes section.
To refer to variables within math, use `\mathtt{varname}`.

.. todo ::

    This block can describe things which need to be done and is automatically
↪included in a section of :doc:`todo`.
"""

```

- Use relative imports within TeNPy. Example:

```
from ..linalg import np_conserved as npc
```

- Use the python package `pytest` for testing. Run it simply with `pytest` in `tests/`. You should make sure that all tests run through, before you `git push` back into the public repo. Long-running tests are marked with the attribute `slow`; for a quick check you can also run `pytest -m "not slow"`.

We have set up github actions to automatically run the tests.

- Reversely, if you write new functions, please also include suitable tests!
- During development, you might introduce `# TODO` comments. But also try to remove them again later! If you're not 100% sure that you will remove it soon, please add a doc-string with a `.. todo ::` block, such that we can keep track of it.

Unfinished functions should raise `NotImplementedError()`.

- Summarize the changes you have made in the Changelog under [\[latest\]](#).
- If you want to try out new things in temporary files: any folder named `playground` is ignored by `git`.
- If you add a new toycode or example: add a reference to include it in the documentation.
- We've created a sphinx extensions for [documenting config-option dictionaries](#). If a class takes a dictionary of options, we usually call it `options`, convert it to a `Config` at the very beginning of the `__init__` with `asConfig()`, save it as `self.options`, and document it in the class doc-string with a `.. cfg:config ::` directive. The name of the `config` should usually be the class-name (if that is sufficiently unique), or for algorithms directly the common name of the algorithm, e.g. "DMRG"; use the same name for the use the same name for the documentation of the `.. cfg:config ::` directive as for the `Config` class instance. Attributes which are simply read-out options should be documented by just referencing the options with the `:cfg:option:`configname.optionname`` role.

7.5.2 Bulding the documentation

You can use [Sphinx](#) to generate the full documentation in various formats (including HTML or PDF) yourself, as described in the following. First, install the extra requirements, i.e., [Sphinx](#), with:

```
pip install -r doc/requirements.txt
```

Note: Plotting the inheritance graphs also requires [Graphviz](#). If you have *conda*, installing it requires just `conda install graphviz`.

Afterwards, simply go to the folder `doc/` and run the following command:

```
make html
```

This should generate the html documentation in the folder `doc/sphinx_build/html`. Open this folder (or to be precise: the file `index.html` in it) in your webbrowser and enjoy this and other documentation beautifully rendered, with cross links, math formulas and even a search function. Other output formats are available as other make targets, e.g., `make latexpdf`.

Note: Building the documentation with sphinx requires loading the modules. The `conf.py` adjusts the python path to include the *tenpy* from root directory of the repository.

7.5.3 To-Do list

You can check <https://github.com/tenpy/tenpy/issues> for things to be done.

The following list is auto-generated by sphinx, extracting `.. todo ::` blocks from doc-strings of the code.

Todo: Write UserGuide!!!

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/algorithms/dmrg.py:docstring of tenpy.algorithms.dmrg`, line 30.)

Todo: Rebuild TDVP engine as subclasses of sweep.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/algorithms/mps_common.py:docstring of tenpy.algorithms.mps_common`, line 21.)

Todo:

- **implement or wrap `netcon.m`, a function to find optimal contractionn sequences** ([arXiv:1304.6112](#))
 - improve helpfulness of Warnings
 - `_do_trace`: trace over all pairs of legs at once. need the corresponding `npc` function first.
-

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/algorithms/network_contractor.py:docstring of tenpy.algorithms.network_contractor`, line 10.)

Todo: This is still a beta version, use with care. The interface might still change.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/algorithms/tdvp.py:docs` of `tenpy.algorithms.tdvp`, line 12.)

Todo: long-term: Much of the code is similar as in DMRG. To avoid too much duplicated code, we should have a general way to sweep through an MPS and updated one or two sites, used in both cases.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/algorithms/tdvp.py:docs` of `tenpy.algorithms.tdvp`, line 16.)

Todo: add further terms (e.g. $c^\dagger c^\dagger + \text{h.c.}$) to the Hamiltonian.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/fermions_spinless.py:docs` of `tenpy.models.fermions_spinless`, line 3.)

Todo: WARNING: These models are still under development and not yet tested for correctness. Use at your own risk! Replicate known results to confirm models work correctly. Long term: implement different lattices. Long term: implement variable hopping strengths J_x, J_y .

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/hofstadter.py:docs` of `tenpy.models.hofstadter`, line 3.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.Honeycomb.mps2lat_values`, line 53.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.IrregularLattice.mps2lat_values`, line 53.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.Kagome.mps2lat_values`, line 53.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.Ladder.mps2lat_values`, line 53.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.Lattice.mps2lat_values`, line 53.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/lattice.py:docs` of `tenpy.models.lattice.TrivialLattice.mps2lat_values`, line 53.)

Todo: implement MPO for time evolution...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/model.py:docs` of `tenpy.models.model.MPOModel`, line 7.)

Todo: make sure this function is used for expectation values...

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/models/toric_code.py:docs` of `tenpy.models.toric_code.DualSquare.mps2lat_values`, line 53.)

Todo: This is a naive, expensive implementation contracting the full network. Try to follow [arXiv:1711.01104](#) for a better estimate; would that even work in the infinite limit?

(The *original entry* is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/networks/mpo.py:docs` of `tenpy.networks.mpo.MPO.variance`, line 5.)

Todo: might be useful to add a “cleanup” function which removes operators cancelling each other and/or unused states. Or better use a ‘compress’ of the MPO?

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/networks/mpo.py:docs` of `tenpy.networks.mpo.MPOGraph`, line 17.)

Todo: Make more general: it should be possible to specify states as strings.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/networks/mps.py:docs` of `tenpy.networks.mps.build_initial_state`, line 14.)

Todo: One can also look at the canonical ensembles by defining the conserved quantities differently, see Barthel (2016), [arXiv:1607.01696](#) for details. Idea: usual charges on p , trivial charges on q ; fix total charge to desired value. I think it should suffice to implement another *from_infiniteT*.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/networks/purification.py:docs` of `tenpy.networks.purification_mps`, line 106.)

Todo: Check if Jordan-Wigner strings for 4x4 operators are correct.

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/networks/site.py:docs` of `tenpy.networks.site.SpinHalfFermionSite`, line 61.)

Todo: For memory caching with big MPO environments, we need a Hdf5Cacher clearing the memo's every now and then (triggered by what?).

(The [original entry](#) is located in `/home/docs/checkouts/readthedocs.org/user_builds/tenpy/checkouts/v0.7.1/tenpy/tools/hdf5_io.py:docst of tenpy.tools.hdf5_io, line 60.`)

7.6 Tenpy main module

- full name: `tenpy`
- parent module: `tenpy`
- type: module

Submodules

<code>algorithms</code>	A collection of algorithms such as TEBD and DMRG.
<code>linalg</code>	Linear-algebra tools for tensor networks.
<code>models</code>	Definition of the various models.
<code>networks</code>	Definitions of tensor networks like MPS and MPO.
<code>tools</code>	A collection of tools: mostly short yet quite useful functions.
<code>version</code>	Access to version of this library.

Module description

TeNPy - a Python library for Tensor Network Algorithms

TeNPy is a library for algorithms working with tensor networks, e.g., matrix product states and -operators, designed to study the physics of strongly correlated quantum systems. The code is intended to be accessible for newcomers and yet powerful enough for day-to-day research.

```
tenpy.__version__ = '0.7.1'
    hard-coded version string
```

```
tenpy.__full_version__ = '0.7.1'
    full version from git description, and numpy/scipy/python versions
```

```
tenpy.show_config()
    Print information about the version of tenpy and used libraries.
```

The information printed is `tenpy.version.version_summary`.

Submodules

<i>algorithms</i>	A collection of algorithms such as TEBD and DMRG.
<i>linalg</i>	Linear-algebra tools for tensor networks.
<i>models</i>	Definition of the various models.
<i>networks</i>	Definitions of tensor networks like MPS and MPO.
<i>tools</i>	A collection of tools: mostly short yet quite useful functions.
<i>version</i>	Access to version of this library.

7.7 algorithms

- full name: `tenpy.algorithms`
- parent module: *tenpy*
- type: module

Module description

A collection of algorithms such as TEBD and DMRG.

Submodules

<i>truncation</i>	Truncation of Schmidt values.
<i>tebd</i>	Time evolving block decimation (TEBD).
<i>mps_common</i>	‘Sweep’ algorithm and effective Hamiltonians.
<i>dmrg</i>	Density Matrix Renormalization Group (DMRG).
<i>tdvp</i>	Time Dependant Variational Principle (TDVP) with MPS (finite version only).
<i>purification</i>	Algorithms for using Purification.
<i>mpo_evolution</i>	Time evolution using the WI or WII approximation of the time evolution operator.
<i>network_contractor</i>	Network Contractor.
<i>exact_diag</i>	Full diagonalization (ED) of the Hamiltonian.

7.7.1 truncation

- full name: `tenpy.algorithms.truncation`
- parent module: *tenpy.algorithms*
- type: module

Classes

TruncationError

TruncationError([eps, ov])

Class representing a truncation error.

TruncationError

- full name: `tenpy.algorithms.truncation.TruncationError`
- parent module: `tenpy.algorithms.truncation`
- type: class

Inheritance Diagram

TruncationError

Methods

<code>TruncationError.__init__([eps, ov])</code>	Initialize self.
<code>TruncationError.copy()</code>	Return a copy of self.
<code>TruncationError.from_S(S_discarded[, norm_old])</code>	Construct TruncationError from discarded singular values.
<code>TruncationError.from_norm(norm_new[, norm_old])</code>	Construct TruncationError from norm after and before the truncation.

Class Attributes and Properties

`TruncationError.ov_err`

Error $1 - \text{ov}$ of the overlap with the correct state.

class `tenpy.algorithms.truncation.TruncationError` (*eps*=0.0, *ov*=1.0)

Bases: `object`

Class representing a truncation error.

The default initialization represents “no truncation”.

Warning: For imaginary time evolution, this is *not* the error you are interested in!

Parameters *ov* (*eps*,) – See below.

eps

The total sum of all discarded Schmidt values squared. Note that if you keep singular values up to $1.e-14$ (= a bit more than machine precision for 64bit floats), *eps* is on the order of $1.e-28$ (due to the square)!

Type `float`

ov

A lower bound for the overlap $|\langle \psi_{\text{trunc}} | \psi_{\text{correct}} \rangle|^2$ (assuming normalization of both states). This is probably the quantity you are actually interested in. Takes into account the factor 2 explained in the section on Errors in the *TEBD Wikipedia article* <https://en.wikipedia.org/wiki/Time-evolving_block_decimation>.

Type `float`

Examples

```
>>> TE = TruncationError()
>>> TE += tebd.time_evolution(...) # add `eps`, multiply `ov`
```

copy()

Return a copy of self.

classmethod from_norm (*norm_new*, *norm_old*=1.0)

Construct TruncationError from norm after and before the truncation.

Parameters

- **norm_new** (*float*) – Norm of Schmidt values kept, $\sqrt{\sum_{a \text{ kept}} \lambda_a^2}$ (before re-normalization).
- **norm_old** (*float*) – Norm of all Schmidt values before truncation, $\sqrt{\sum_a \lambda_a^2}$.

classmethod from_S (*S_discarded*, *norm_old*=None)

Construct TruncationError from discarded singular values.

Parameters

- **S_discarded** (*1D numpy array*) – The singular values discarded.
- **norm_old** (*float*) – Norm of all Schmidt values before truncation, $\sqrt{\sum_a \lambda_a^2}$. Default (None) is 1.

property `ov_err`

Error $1 - \text{ov}$ of the overlap with the correct state.

Functions

<code>svd_theta(theta, trunc_par[, qtotal_LR, ...])</code>	Performs SVD of a matrix <i>theta</i> (= the wavefunction) and truncates it.
<code>truncate(S, options)</code>	Given a Schmidt spectrum <i>S</i> , determine which values to keep.

svd_theta

- full name: `tenpy.algorithms.truncation.svd_theta`
- parent module: `tenpy.algorithms.truncation`
- type: function

`tenpy.algorithms.truncation.svd_theta(theta, trunc_par, qtotal_LR=[None, None], inner_labels=['vR', 'vL'])`

Performs SVD of a matrix *theta* (= the wavefunction) and truncates it.

Perform a singular value decomposition (SVD) with `svd()` and truncates with `truncate()`. The result is an approximation `theta ~= tensordot(U.scale_axis(S*renormalization, 1), VH, axes=1)`

Parameters

- **theta** (`Array`, shape (M, N)) – The matrix, on which the singular value decomposition (SVD) is performed. Usually, *theta* represents the wavefunction, such that the SVD is a Schmidt decomposition.
- **trunc_par** (`dict`) – truncation parameters as described in `truncate()`.
- **qtotal_LR** (`(charges, charges)`) – The total charges for the returned *U* and *VH*.
- **inner_labels** (`(string, string)`) – Labels for the *U* and *VH* on the newly-created bond.

Returns

- **U** (`Array`) – Matrix with left singular vectors as columns. Shape (M, M) or (M, K) depending on *full_matrices*.
- **S** (`1D ndarray`) – The singular values of the array. If no *cutoff* is given, it has length $\min(M, N)$. Normalized to `np.linalg.norm(S)==1`.
- **VH** (`Array`) – Matrix with right singular vectors as rows. Shape (N, N) or (K, N) depending on *full_matrices*.
- **err** (`TruncationError`) – The truncation error introduced.
- **renormalization** (`float`) – Factor, by which *S* was renormalized.

Module description

Truncation of Schmidt values.

Often, it is necessary to truncate the number of states on a virtual bond of an MPS, keeping only the state with the largest Schmidt values. The function `truncate()` picks exactly those from a given Schmidt spectrum λ_a , depending on some parameters explained in the doc-string of the function.

Further, we provide `TruncationError` for a simple way to keep track of the total truncation error.

The SVD on a virtual bond of an MPS actually gives a Schmidt decomposition $|\psi\rangle = \sum_a \lambda_a |L_a\rangle |R_a\rangle$ where $|L_a\rangle$ and $|R_a\rangle$ form orthonormal bases of the parts left and right of the virtual bond. Let us assume that the state is properly normalized, $\langle\psi|\psi\rangle = \sum_a \lambda_a^2 = 1$. Assume that the singular values are ordered descending, and that we keep the first χ_c of the initially χ Schmidt values.

Then we decompose the untruncated state as $|\psi\rangle = \sqrt{1-\epsilon} |\psi_{tr}\rangle + \sqrt{\epsilon} |\psi_{tr}^\perp\rangle$ where $|\psi_{tr}\rangle = \frac{1}{\sqrt{1-\epsilon}} \sum_{a < \chi_c} \lambda_a |L_a\rangle |R_a\rangle$ is the truncated state kept (normalized to 1), $|\psi_{tr}^\perp\rangle = \frac{1}{\sqrt{\epsilon}} \sum_{a \geq \chi_c} \lambda_a |L_a\rangle |R_a\rangle$ is the discarded part (orthogonal to the kept part) and the *truncation error of a single truncation* is defined as $\epsilon = 1 - |\langle\psi|\psi_{tr}\rangle|^2 = \sum_{a \geq \chi_c} \lambda_a^2$.

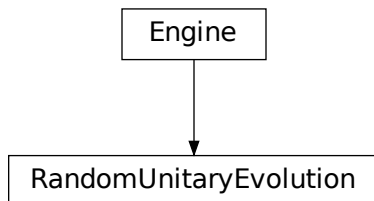
Warning: For imaginary time evolution (e.g. with TEBD), you try to project out the ground state. Then, looking at the truncation error defined in this module does *not* give you any information how good the found state coincides with the actual ground state! (Instead, the returned truncation error depends on the overlap with the initial state, which is arbitrary > 0)

Warning: This module takes only track of the errors coming from the truncation of Schmidt values. There might be other sources of error as well, for example TEBD has also an discretisation error depending on the chosen time step.

7.7.2 tebd

- full name: `tenpy.algorithms.tebd`
- parent module: `tenpy.algorithms`
- type: module

Classes



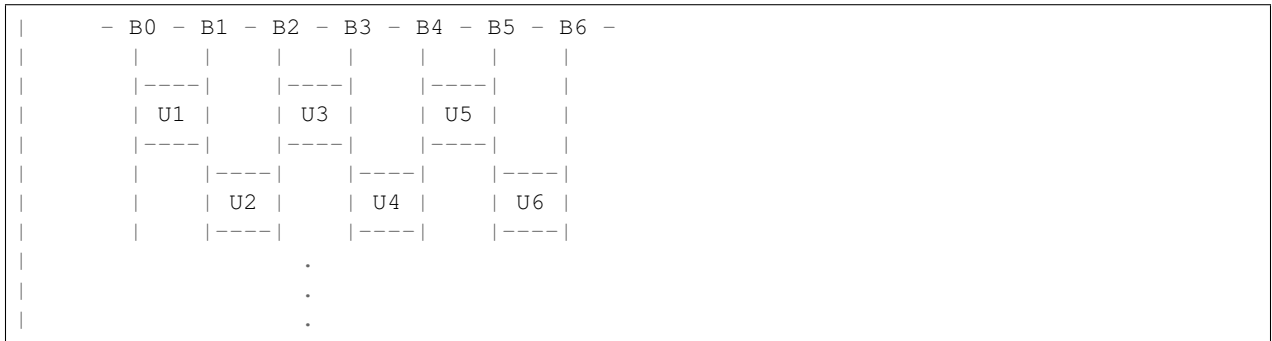
<code>Engine(psi, model, options)</code>	Time Evolving Block Decimation (TEBD) algorithm.
<code>RandomUnitaryEvolution(psi, options)</code>	Evolution of an MPS with random two-site unitaries in a TEBD-like fashion.

Module description

Time evolving block decimation (TEBD).

The TEBD algorithm (proposed in [Vidal2004]) uses a trotter decomposition of the Hamiltonian to perform a time evolution of an MPS. It works only for nearest-neighbor hamiltonians (in tenpy given by a `NearestNeighborModel`), which can be written as $H = H^{even} + H^{odd}$, such that H^{even} contains the terms on even bonds (and similar H^{odd} the terms on odd bonds). In the simplest case, we apply first $U = \exp(-i * dt * H^{even})$, then $U = \exp(-i * dt * H^{odd})$ for each time step dt . This is correct up to errors of $O(dt^2)$, but to evolve until a time T , we need T/dt steps, so in total it is only correct up to error of $O(T * dt)$. Similarly, there are higher order schemata (in dt) (for more details see `Engine.update()`).

Remember, that bond i is between sites $(i-1, i)$, so for a finite MPS it looks like:



After each application of a U_i , the MPS needs to be truncated - otherwise the bond dimension chi would grow indefinitely. A bound for the error introduced by the truncation is returned.

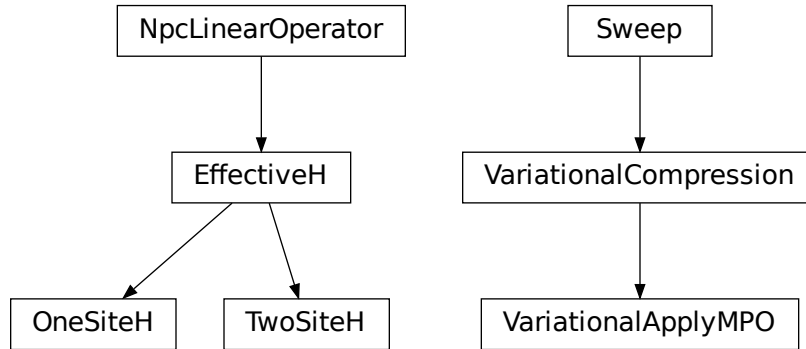
If one chooses imaginary dt , the exponential projects (for sufficiently long ‘time’ evolution) onto the ground state of the Hamiltonian.

Note: The application of DMRG is typically much more efficient than imaginary TEBD! Yet, imaginary TEBD might be usefull for cross-checks and testing.

7.7.3 mps_common

- full name: `tenpy.algorithms.mps_common`
- parent module: `tenpy.algorithms`
- type: module

Classes

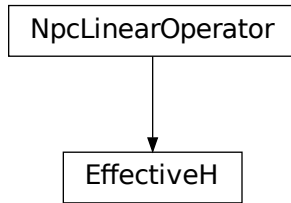


<code>EffectiveH(env, i0[, combine, move_right])</code>	Prototype class for local effective Hamiltonians used in sweep algorithms.
<code>OneSiteH(env, i0[, combine, move_right])</code>	Class defining the one-site effective Hamiltonian for Lanczos.
<code>Sweep(psi, model, options)</code>	Prototype class for a ‘sweeping’ algorithm.
<code>TwoSiteH(env, i0[, combine, move_right])</code>	Class defining the two-site effective Hamiltonian for Lanczos.
<code>VariationalApplyMPO(psi, U_MPO, options)</code>	Variational compression for applying an MPO to an MPS (in place).
<code>VariationalCompression(psi, options)</code>	Variational compression of an MPS (in place).

EffectiveH

- full name: `tenpy.algorithms.mps_common.EffectiveH`
- parent module: `tenpy.algorithms.mps_common`
- type: class

Inheritance Diagram



Methods

<code>EffectiveH.__init__(env, i0[, combine, ...])</code>	Initialize self.
<code>EffectiveH.adjoint()</code>	Return the hermitian conjugate of <i>self</i>
<code>EffectiveH.combine_theta(theta)</code>	Combine the legs of <i>theta</i> , such that it fits to how we combined the legs of <i>self</i> .
<code>EffectiveH.matvec(vec)</code>	Calculate the action of the operator on a vector <i>vec</i> .
<code>EffectiveH.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

<code>EffectiveH.acts_on</code>
<code>EffectiveH.length</code>

class `tenpy.algorithms.mps_common.EffectiveH` (*env*, *i0*, *combine=False*, *move_right=True*)
 Bases: `tenpy.linalg.sparse.NpcLinearOperator`

Prototype class for local effective Hamiltonians used in sweep algorithms.

As an example, the local effective Hamiltonian for a two-site (DMRG) algorithm looks like:



where H0 and H1 are MPO tensors.

Parameters

- **env** (*MPOEnvironment*) – Environment for contraction $\langle \text{psi} | H | \text{psi} \rangle$.
- **i0** (*int*) – Index of the active site if *length*=1, or of the left-most active site if *length*>1.
- **combine** (*bool*, *optional*) – Whether to combine legs into pipes as far as possible. This reduces the overhead of calculating charge combinations in the contractions.

- **move_right** (*bool*, *optional*) – Whether the sweeping algorithm that calls for an *EffectiveH* is moving to the right.

length

Number of (MPS) sites the effective hamiltonian covers. NB: Class attribute.

Type `int`

dtype

The data type of the involved arrays.

Type `np.dtype`

N

Contracting *self* with `as_matrix()` will result in an $N \times N$ matrix .

Type `int`

acts_on

Labels of the state on which *self* acts. NB: class attribute. Overwritten by normal attribute, if *combine*.

Type list of str

combine

Whether to combine legs into pipes as far as possible. This reduces the overhead of calculating charge combinations in the contractions.

Type `bool`

move_right

Whether the sweeping algorithm that calls for an *EffectiveH* is moving to the right.

Type `bool`

combine_theta (*theta*)

Combine the legs of *theta*, such that it fits to how we combined the legs of *self*.

Parameters **theta** (`Array`) – Wave function to apply the effective Hamiltonian to, with uncombined legs.

Returns **theta** – Wave function with labels as given by *self.acts_on*.

Return type `Array`

adjoint ()

Return the hermitian conjugate of *self*

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

matvec (*vec*)

Calculate the action of the operator on a vector *vec*.

Note that we don't require *vec* to be one-dimensional. However, for square operators we require that the result of *matvec* has the same legs (in the same order) as *vec* such that they can be added. Note that this excludes a non-trivial *qtotal* for square operators.

to_matrix ()

Contract *self* to a matrix.

If *self* represents an operator with very small shape, e.g. because the MPS bond dimension is very small, an algorithm might choose to contract *self* to a single tensor.

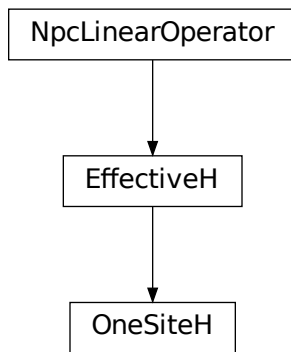
Returns **matrix** – Contraction of the represented operator.

Return type `Array`

OneSiteH

- full name: `tenpy.algorithms.mps_common.OneSiteH`
- parent module: `tenpy.algorithms.mps_common`
- type: class

Inheritance Diagram



Methods

<code>OneSiteH.__init__(env, i0[, combine, move_right])</code>	Initialize self.
<code>OneSiteH.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>OneSiteH.combine_Heff()</code>	Combine LP and RP with W to form LHeff and RHeff, depending on the direction.
<code>OneSiteH.combine_theta(theta)</code>	Combine the legs of <i>theta</i> , such that it fits to how we combined the legs of <i>self</i> .
<code>OneSiteH.matvec(theta)</code>	Apply the effective Hamiltonian to <i>theta</i> .
<code>OneSiteH.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

<code>OneSiteH.acts_on</code>
<code>OneSiteH.length</code>

class `tenpy.algorithms.mps_common.OneSiteH` (*env*, *i0*, *combine=False*, *move_right=True*)

Bases: `tenpy.algorithms.mps_common.EffectiveH`

Class defining the one-site effective Hamiltonian for Lanczos.

The effective one-site Hamiltonian looks like this:



If *combine* is True, we define either *LHeff* as contraction of *LP* with *W* (in the case *move_right* is True) or *RHeff* as contraction of *RP* and *W*.

Parameters

- **env** (*MPOEnvironment*) – Environment for contraction $\langle \text{psi} | H | \text{psi} \rangle$.
- **i0** (*int*) – Index of the active site if length=1, or of the left-most active site if length>1.
- **combine** (*bool*) – Whether to combine legs into pipes. This combines the virtual and physical leg for the left site (when moving right) or right side (when moving left) into pipes. This reduces the overhead of calculating charge combinations in the contractions, but one *matvec()* is formally more expensive, $O(2d^3\chi^3D)$. Is originally from the w-site method; unclear if it works well for 1 site.
- **move_right** (*bool*) – Whether the the sweep is moving right or left for the next update.

length

Number of (MPS) sites the effective hamiltonian covers.

Type *int*

acts_on

Labels of the state on which *self* acts. NB: class attribute. Overwritten by normal attribute, if *combine*.

Type list of str

combine, move_right

See above.

Type *bool*

LHeff, RHeff

Only set if *combine*, and only one of them depending on *move_right*. If *move_right* was True, *LHeff* is set with labels ' (vR*.p0) ', 'wR', ' (vR.p0*) ' for bra, MPO, ket; otherwise *RHeff* is set with labels ' (p0*.vL) ', 'wL', ' (p0, vL*) '

Type *Array*

LP, W0, RP

Tensors making up the network of *self*.

Type *Array*

matvec(theta)

Apply the effective Hamiltonian to *theta*.

Parameters *theta* (*Array*) – Labels: vL, p0, vR if *combine*=False, (vL.p0), vR or vL, (p0.vR) if True (depending on the direction of movement)

Returns Product of *theta* and the effective Hamiltonian.

Return type *theta* *Array*

combine_Heff()

Combine LP and RP with W to form LHeff and RHeff, depending on the direction.

In a move to the right, we need LHeff. In a move to the left, we need RHeff. Both contain the same W.

combine_theta (*theta*)

Combine the legs of *theta*, such that it fits to how we combined the legs of *self*.

Parameters *theta* (*Array*) – Wave function with labels 'vL', 'p0', 'p1', 'vR'

Returns *theta* – Wave function with labels 'vL', 'p0', 'p1', 'vR'

Return type *Array*

to_matrix ()

Contract *self* to a matrix.

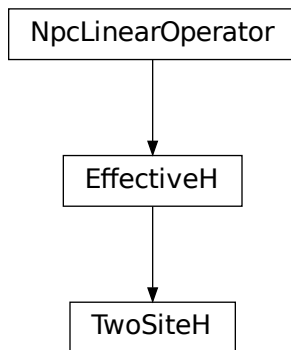
adjoint ()

Return the hermitian conjugate of *self*.

TwoSiteH

- full name: `tenpy.algorithms.mps_common.TwoSiteH`
- parent module: `tenpy.algorithms.mps_common`
- type: class

Inheritance Diagram



Methods

<code>TwoSiteH.__init__(env, i0[, combine, move_right])</code>	Initialize self.
<code>TwoSiteH.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>TwoSiteH.combine_Heff()</code>	Combine LP and RP with W to form LHeff and RHeff.
<code>TwoSiteH.combine_theta(theta)</code>	Combine the legs of <i>theta</i> , such that it fits to how we combined the legs of <i>self</i> .
<code>TwoSiteH.matvec(theta)</code>	Apply the effective Hamiltonian to <i>theta</i> .
<code>TwoSiteH.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

`TwoSiteH.acts_on`

`TwoSiteH.length`

class `tenpy.algorithms.mps_common.TwoSiteH` (*env*, *i0*, *combine=False*, *move_right=True*)

Bases: `tenpy.algorithms.mps_common.EffectiveH`

Class defining the two-site effective Hamiltonian for Lanczos.

The effective two-site Hamiltonian looks like this:



If *combine* is True, we define *LHeff* and *RHeff*, which are the contractions of *LP* with *W0*, and *RP* with *W1*, respectively.

Parameters

- **env** (*MPOEnvironment*) – Environment for contraction $\langle \text{psi} | H | \text{psi} \rangle$.
- **i0** (*int*) – Index of the active site if *length*=1, or of the left-most active site if *length*>1.
- **combine** (*bool*) – Whether to combine legs into pipes. This combines the virtual and physical leg for the left site (when moving right) or right site (when moving left) into pipes. This reduces the overhead of calculating charge combinations in the contractions, but one *matvec()* is formally more expensive, $O(2d^3\chi^3D)$.
- **move_right** (*bool*) – Whether the the sweep is moving right or left for the next update.

combine

Whether to combine legs into pipes. This combines the virtual and physical leg for the left site and right site into pipes. This reduces the overhead of calculating charge combinations in the contractions, but one *matvec()* is formally more expensive, $O(2d^3\chi^3D)$.

Type *bool*

length

Number of (MPS) sites the effective hamiltonian covers.

Type *int*

acts_on

Labels of the state on which *self* acts. NB: class attribute. Overwritten by normal attribute, if *combine*.

Type list of str

LHeff

Left part of the effective Hamiltonian. Labels ' (vR*.p0) ', ' wR ', ' (vR.p0*) ' for bra, MPO, ket.

Type *Array*

RHeff

Right part of the effective Hamiltonian. Labels ' (p1*.vL) ', ' wL ', ' (p1.vL*) ' for ket, MPO, bra.

Type *Array*

LP, W0, W1, RP
Tensors making up the network of *self*.

Type *Array*

matvec (*theta*)
Apply the effective Hamiltonian to *theta*.

Parameters *theta* (*Array*) – Labels: *vL*, *p0*, *p1*, *vR* if *combine=False*, (*vL.p0*), (*p1.vR*) if *True*

Returns Product of *theta* and the effective Hamiltonian.

Return type *theta Array*

combine_Heff ()
Combine LP and RP with W to form LHeff and RHeff.

Combine LP with W0 and RP with W1 to get the effective parts of the Hamiltonian with piped legs.

combine_theta (*theta*)
Combine the legs of *theta*, such that it fits to how we combined the legs of *self*.

Parameters *theta* (*Array*) – Wave function with labels '*vL*', '*p0*', '*p1*', '*vR*'

Returns *theta* – Wave function with labels '*vL*', '*p0*', '*p1*', '*vR*'

Return type *Array*

to_matrix ()
Contract *self* to a matrix.

adjoint ()
Return the hermitian conjugate of *self*.

Module description

‘Sweep’ algorithm and effective Hamiltonians.

Many MPS-based algorithms use a ‘sweep’ structure, wherein local updates are performed on the MPS tensors sequentially, first from left to right, then from right to left. This procedure is common to DMRG, TDVP, sequential time evolution, etc.

Another common feature of these algorithms is the use of an effective local Hamiltonian to perform the local updates. The most prominent example of this is probably DMRG, where the local MPS object is optimized with respect to the rest of the MPS-MPO-MPS network, the latter forming the effective Hamiltonian.

The `Sweep` class attempts to generalize as many aspects of ‘sweeping’ algorithms as possible. `EffectiveH` and its subclasses implement the effective Hamiltonians mentioned above. Currently, effective Hamiltonians for 1-site and 2-site optimization are implemented.

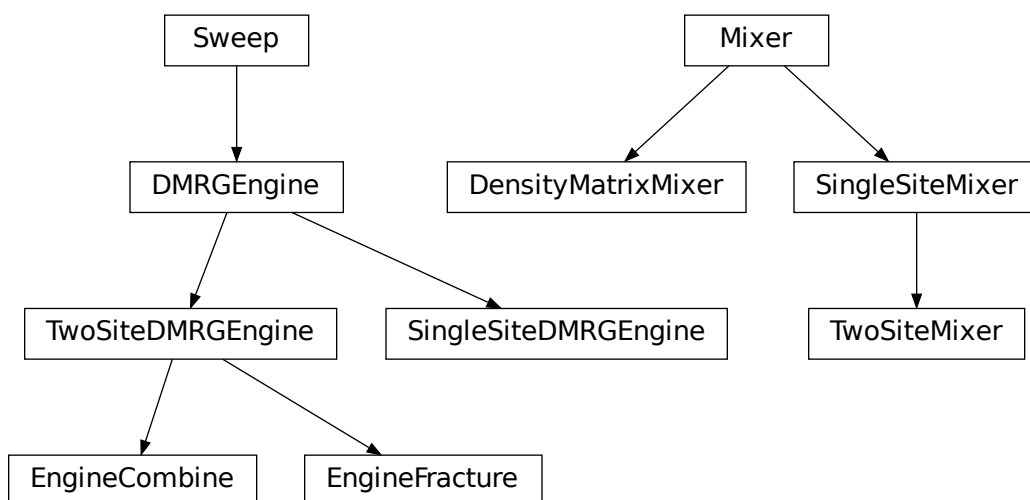
The `VariationalCompression` and `VariationalApplyMPO` implemented here also directly use the `Sweep` class.

Todo: Rebuild TDVP engine as subclasses of `sweep`.

7.7.4 dmrg

- full name: `tenpy.algorithms.dmrg`
- parent module: `tenpy.algorithms`
- type: module

Classes

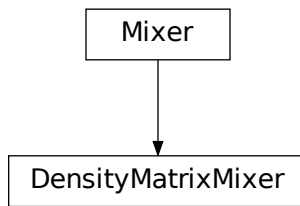


<code>DMRGEngine(psi, model, options)</code>	DMRG base class. 'Engine' for the DMRG algorithm.
<code>DensityMatrixMixer(options)</code>	Mixer based on density matrices.
<code>EngineCombine(psi, model, DMRG_params)</code>	Engine which combines legs into pipes as far as possible.
<code>EngineFracture(psi, model, DMRG_params)</code>	Engine which keeps the legs separate.
<code>Mixer(options)</code>	Base class of a general Mixer.
<code>SingleSiteDMRGEngine(psi, model, options)</code>	'Engine' for the single-site DMRG algorithm.
<code>SingleSiteMixer(options)</code>	Mixer for single-site DMRG.
<code>TwoSiteDMRGEngine(psi, model, options)</code>	'Engine' for the two-site DMRG algorithm.
<code>TwoSiteMixer(options)</code>	Mixer for two-site DMRG.

DensityMatrixMixer

- full name: `tenpy.algorithms.dmrp.DensityMatrixMixer`
- parent module: `tenpy.algorithms.dmrp`
- type: class

Inheritance Diagram



Methods

<code>DensityMatrixMixer.__init__(options)</code>	Initialize self.
<code>DensityMatrixMixer.get_xL(wL_leg, Id_L, Id_R)</code>	Generate the coupling of the MPO legs for the reduced density matrix.
<code>DensityMatrixMixer.get_xR(wR_leg, Id_L, Id_R)</code>	Generate the coupling of the MPO legs for the reduced density matrix.
<code>DensityMatrixMixer.mix_rho_L(engine, theta, ...)</code>	Calculated mixed reduced density matrix for left site.
<code>DensityMatrixMixer.mix_rho_R(engine, theta, ...)</code>	Calculated mixed reduced density matrix for left site.
<code>DensityMatrixMixer.perturb_svd(engine, ...)</code>	Mix extra terms to theta and perform an SVD.
<code>DensityMatrixMixer.update_amplitude(sweeps)</code>	Update the amplitude, possibly disable the mixer.

class `tenpy.algorithms.dmrp.DensityMatrixMixer` (*options*)

Bases: `tenpy.algorithms.dmrp.Mixer`

Mixer based on density matrices.

This mixer constructs density matrices as described in the original paper [White2005].

perturb_svd (*engine, theta, i0, update_LP, update_RP*)

Mix extra terms to theta and perform an SVD.

We calculate the left and right reduced density using the mixer (which might include applications of H). These density matrices are diagonalized and truncated such that we effectively perform a svd for the case `mixer.amplitude=0`.

Parameters

- **engine** (`SingleSiteDMRGEngine` | `TwoSiteDMRGEngine`) – The DMRG engine calling the mixer.
- **theta** (`Array`) – The optimized wave function, prepared for svd.
- **i0** (`int`) – Site index; *theta* lives on *i0*, *i0*+1.
- **update_LP** (`bool`) – Whether to calculate the next `env.LP[i0+1]`.
- **update_RP** (`bool`) – Whether to calculate the next `env.RP[i0]`.

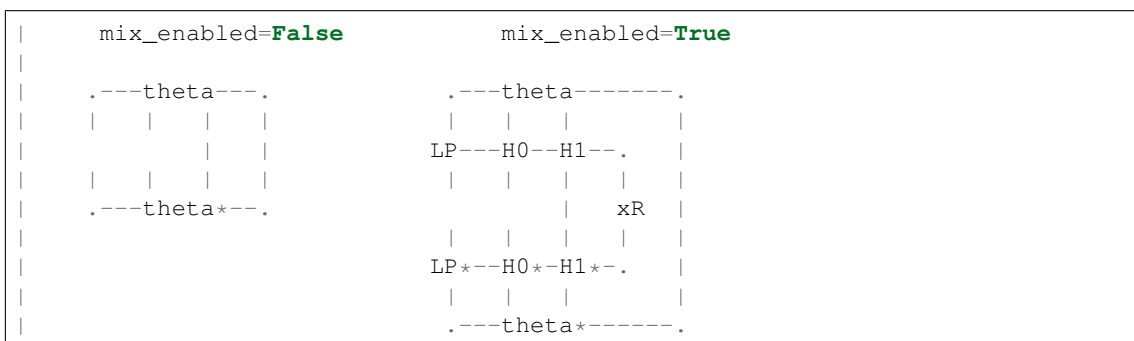
Returns

- **U** (`Array`) – Left-canonical part of *theta*. Labels '`vL.p0`', '`vR`'.
- **S** (`1D ndarray` | `2D Array`) – Without mixer just the singular values of the array; with mixer it might be a general matrix; see comment above.
- **VH** (`Array`) – Right-canonical part of *theta*. Labels '`vL`', '`p1.vR`'.
- **err** (`TruncationError`) – The truncation error introduced.

mix_rho_L (*engine*, *theta*, *i0*, *mix_enabled*)

Calculated mixed reduced density matrix for left site.

Pictorially:



Parameters

- **engine** (`Engine`) – The DMRG engine calling the mixer.
- **theta** (`Array`) – Ground state of the effective Hamiltonian, prepared for svd.
- **i0** (`int`) – Site index; *theta* lives on *i0*, *i0*+1.
- **mix_enabled** (`bool`) – Whether we should perturb the density matrix.

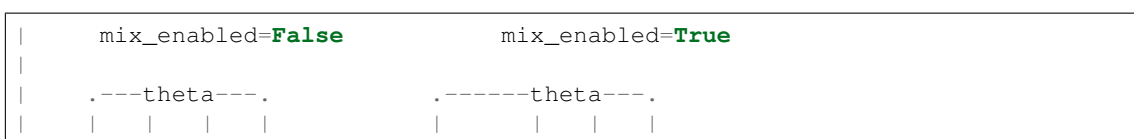
Returns rho_L – A (hermitian) square array with labels '`vL.p0`', '`vL*.p0*`',
Mainly the reduced density matrix of the left part, but with some additional mixing.

Return type `Array`

mix_rho_R (*engine*, *theta*, *i0*, *mix_enabled*)

Calculated mixed reduced density matrix for left site.

Pictorially:



(continues on next page)

					.	--H0--H1--RP
	.	--theta*--.			wL	
					.	--H0*-H1*-RP*
					.-----theta*--.	

- **engine** (`Engine`) – The DMRG engine calling the mixer.
- **theta** (`Array`) – Ground state of the effective Hamiltonian, prepared for svd.
- **i0** (`int`) – Site index; *theta* lives on `i0`, `i0+1`.
- **mix_enabled** (`bool`) – Whether we should perturb the density matrix.

Return type *Array*

Generate the coupling of the MPO legs for the reduced density matrix.

- **wR_leg** (*LegCharge*) – LegCharge to be connected to.
- **IdL** (int | None) – Index within the leg for which the MPO has only identities to the left.
- **IdR** (int | None) – Index within the leg for which the MPO has only identities to the right.

- **mixed_xR** (*Array*) – Connection of the MPOs on the right for the reduced density matrix *rhoL*. Labels ('wL', 'wL*').
- **add_separate_Id** (*bool*) – If Id_L is None, we can't include the identity into *mixed_xR*, so it has to be added directly in *mix_rho_L()*.

Generate the coupling of the MPO legs for the reduced density matrix.

- **wL_leg** (*LegCharge*) – LegCharge to be connected to.
- **Id_L** (int | None) – Index within the leg for which the MPO has only identities to the left.
- **Id_R** (int | None) – Index within the leg for which the MPO has only identities to the right.

- **mixed_xL** (*Array*) – Connection of the MPOs on the left for the reduced density matrix ρ_R . Labels ('wR', 'wR*').
- **add_separate_Id** (*bool*) – If Id_R is None, we can't include the identity into *mixed_xL*, so it has to be added directly in *mix_rho_R()*.

Update the amplitude, possibly disable the mixer.

Parameters `sweeps` (*int*) – The number of performed sweeps, to check if we need to disable the mixer.

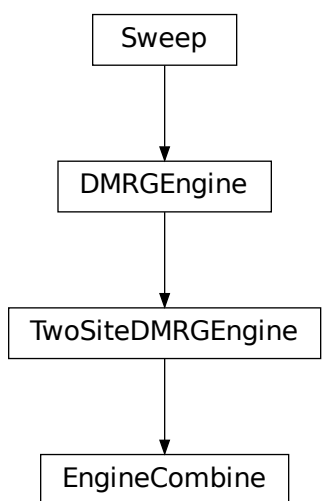
Returns `mixer` – Returns *self* if we should continue mixing, or `None`, if the mixer should be disabled.

Return type `Mixer` | `None`

EngineCombine

- full name: `tenpy.algorithms.dmrp.EngineCombine`
- parent module: `tenpy.algorithms.dmrp`
- type: class

Inheritance Diagram



Methods

<code>EngineCombine.__init__(psi, DMRG_params)</code>	<code>model,</code>	Initialize self.
<code>EngineCombine.diag(theta_guess)</code>		Diagonalize the effective Hamiltonian represented by self.
<code>EngineCombine.environment_sweeps(N_sweeps)</code>		Perform <i>N_sweeps</i> sweeps without optimization to update the environment.
<code>EngineCombine.get_sweep_schedule()</code>		Define the schedule of the sweep.
<code>EngineCombine.init_env([model])</code>		(Re-)initialize the environment.

continues on next page

Table 18 – continued from previous page

<code>EngineCombine.make_eff_H()</code>	Create new instance of <code>self.EffectiveH</code> at <code>self.i0</code> and set it to <code>self.eff_H</code> .
<code>EngineCombine.mixed_svd(theta)</code>	Get (truncated) B from the new theta (as returned by <code>diag</code>).
<code>EngineCombine.mixer_activate()</code>	Set <code>self.mixer</code> to the class specified by <code>options['mixer']</code> .
<code>EngineCombine.mixer_cleanup()</code>	Cleanup the effects of a mixer.
<code>EngineCombine.plot_sweep_stats([axes, ...])</code>	Plot <code>sweep_stats</code> to display the convergence with the sweeps.
<code>EngineCombine.plot_update_stats(axes[, ...])</code>	Plot <code>update_stats</code> to display the convergence during the sweeps.
<code>EngineCombine.post_update_local(update_data)</code>	Perform post-update actions.
<code>EngineCombine.prepare_svd(theta)</code>	Transform theta into matrix for <code>svd</code> .
<code>EngineCombine.prepare_update()</code>	Prepare <code>self</code> for calling <code>update_local()</code> on sites $(i0, i0+1)$.
<code>EngineCombine.reset_stats()</code>	Reset the statistics, useful if you want to start a new sweep run.
<code>EngineCombine.run()</code>	Run the DMRG simulation to find the ground state.
<code>EngineCombine.set_B(U, S, VH)</code>	Update the MPS with the U , S , VH returned by <code>self.mixed_svd</code> .
<code>EngineCombine.sweep([optimize, meas_E_trunc])</code>	One 'sweep' of a the algorithm.
<code>EngineCombine.update_LP(U)</code>	Update left part of the environment.
<code>EngineCombine.update_RP(VH)</code>	Update right part of the environment.
<code>EngineCombine.update_local(theta[, ...])</code>	Perform bond-update on the sites $(i0, i0+1)$.

Class Attributes and Properties

<code>EngineCombine.DMRG_params</code>
<code>EngineCombine.engine_params</code>

class `tenpy.algorithms.dmrq.EngineCombine` (*psi*, *model*, *DMRG_params*)

Bases: `tenpy.algorithms.dmrq.TwoSiteDMRGEngine`

Engine which combines legs into pipes as far as possible.

This engine combines the virtual and physical leg for the left site and right site into pipes. This reduces the overhead of calculating charge combinations in the contractions, but one `matvec()` is formally more expensive, $O(2d^3\chi^3D)$.

Deprecated since version 0.5.0: Directly use the `TwoSiteDMRGEngine` with the DMRG parameter `combine=True`.

EffectiveH

alias of `tenpy.algorithms.mps_common.TwoSiteH`

diag (*theta_guess*)

Diagonalize the effective Hamiltonian represented by `self`.

option `DMRGEngine.max_N_for_ED: int`

Maximum matrix dimension of the effective hamiltonian up to which the 'default' `diag_method` uses ED instead of Lanczos.

option `DMRGEngine.diag_method: str`

One of the folloing strings:

- ‘**default**’ Same as ‘`lanczos`’ for large bond dimensions, but if the total dimension of the effective Hamiltonian does not exceed the DMRG parameter ‘`max_N_for_ED`’ it uses ‘`ED_block`’.
- ‘**lanczos**’ `lanczos()` Default, the Lanczos implementation in TeNPy.
- ‘**arpack**’ `lanczos_arpack()` Based on `scipy.linalg.sparse.eigsh()`. Slower than ‘`lanczos`’, since it needs to convert the `npc` arrays to `numpy` arrays during *each* matvec, and possibly does many more iterations.
- ‘**ED_block**’ `full_diag_effH()` Contract the effective Hamiltonian to a (large!) matrix and diagonalize the block in the charge sector of the initial state. Preserves the charge sector of the explicitly conserved charges. However, if you don’t preserve a charge explicitly, it can break it. For example if you use a `SpinChain({'conserve': 'parity'})`, it could change the total “Sz”, but not the parity of ‘Sz’.
- ‘**ED_all**’ `full_diag_effH()` Contract the effective Hamiltonian to a (large!) matrix and diagonalize it completely. Allows to change the charge sector *even for explicitly conserved charges*. For example if you use a `SpinChain({'conserve': 'Sz'})`, it **can** change the total “Sz”.

Parameters `theta_guess` (`Array`) – Initial guess for the ground state of the effective Hamiltonian.

Returns

- **E0** (`float`) – Energy of the found ground state.
- **theta** (`Array`) – Ground state of the effective Hamiltonian.
- **N** (`int`) – Number of Lanczos iterations used. -1 if unknown.
- **ov_change** (`float`) – Change in the wave function $1. - \text{abs}(\langle \text{theta_guess} | \text{theta_diag} \rangle)$

environment_sweeps (`N_sweeps`)

Perform `N_sweeps` sweeps without optimization to update the environment.

Parameters `N_sweeps` (`int`) – Number of sweeps to run without optimization

get_sweep_schedule ()

Define the schedule of the sweep.

One ‘sweep’ is a full sequence from the leftmost site to the right and back. Only those *LP* and *RP* that can be used later should be updated.

Returns `schedule` – Schedule for the sweep. Each entry is `(i0, move_right, (update_LP, update_RP))`, where `i0` is the leftmost of the `self.EffectiveH.length` sites to be updated in `update_local()`, `move_right` indicates whether the next `i0` in the schedule is right (`True`) of the current one, and `update_LP`, `update_RP` indicate whether it is necessary to update the *LP* and *RP*. The latter are chosen such that the environment is growing for infinite systems, but we only keep the minimal number of environment tensors in memory.

Return type iterable of (`int`, `bool`, (`bool`, `bool`))

init_env (`model=None`)

(Re-)initialize the environment.

This function is useful to (re-)start a Sweep with a slightly different model or different (engine) parameters. Note that we assume that we still have the same *psi*. Calls `reset_stats()`.

Parameters `model` (`MPOModel`) – The model representing the Hamiltonian for which we want to find the ground state. If `None`, keep the model used before.

Options

Deprecated since version 0.6.0: Options *LP*, *LP_age*, *RP* and *RP_age* are now collected in a dictionary *init_env_data* with different keys *init_LP*, *init_RP*, *age_LP*, *age_RP*

option `Sweep.init_env_data:` `dict`
 Dictionary as returned by `self.env.get_initialization_data()` from `get_initialization_data()`.

option `Sweep.orthogonal_to:` `list of MPSEnvironment`
 List of other matrix product states to orthogonalize against. Works only for finite systems. This parameter can be used to find (a few) excited states as follows. First, run DMRG to find the ground state and then run DMRG again while orthogonalizing against the ground state, which yields the first excited state (in the same symmetry sector), and so on.

option `Sweep.start_env:` `int`
 Number of sweeps to be performed without optimization to update the environment.

Raises `ValueError` – If the engine is re-initialized with a new model, which legs are incompatible with those of the old model.

make_eff_H()
 Create new instance of `self.EffectiveH` at `self.i0` and set it to `self.eff_H`.

mixed_svd(theta)
 Get (truncated) *B* from the new *theta* (as returned by `diag`).

The goal is to split *theta* and truncate it:

	--	theta	--	==>	--	U	--	S	--	VH	-

Without a mixer, this is done by a simple svd and truncation of Schmidt values.

With a mixer, the state is perturbed before the SVD. The details of the perturbation are defined by the `Mixer` class.

Note that the returned *S* is a general (not diagonal) matrix, with labels '*vL*', '*vR*'.

Parameters `theta (Array)` – The optimized wave function, prepared for svd.

Returns

- `U (Array)` – Left-canonical part of *theta*. Labels '*(vL.p0)*', '*vR*'.
- `S (1D ndarray | 2D Array)` – Without mixer just the singular values of the array; with mixer it might be a general matrix with labels '*vL*', '*vR*'; see comment above.
- `VH (Array)` – Right-canonical part of *theta*. Labels '*vL*', '*(p1.vR)*'.
- `err (TruncationError)` – The truncation error introduced.

mixer_activate()
 Set `self.mixer` to the class specified by `options['mixer']`.

option `TwoSiteDMRGEngine.mixer:` `str | class | bool`
 Chooses the `Mixer` to be used. A string stands for one of the mixers defined in this module, a class is used as custom mixer. Default (`None`) uses no mixer, `True` uses `DensityMatrixMixer` for the 2-site case and `SingleSiteMixer` for the 1-site case.

option `TwoSiteDMRGEngine.mixer_params:` `dict`
 Mixer parameters as described in `Mixer`.

mixer_cleanup()

Cleanup the effects of a mixer.

A `sweep()` with an enabled Mixer leaves the MPS `psi` with 2D arrays in `S`. To recover the original form, this function simply performs one sweep with disabled mixer.

plot_sweep_stats (*axes=None, xaxis='time', yaxis='E', y_exact=None, **kwargs*)

Plot `sweep_stats` to display the convergence with the sweeps.

Parameters

- **axes** (`matplotlib.axes.Axes`) – The axes to plot into. Defaults to `matplotlib.pyplot.gca()`
- **yaxis** (*xaxis*,) – Key of `sweep_stats` to be used for the x-axis and y-axis of the plots.
- **y_exact** (*float*) – Exact value for the quantity on the y-axis for comparison. If given, plot `abs((y-y_exact)/y_exact)` on a log-scale yaxis.
- ****kwargs** – Further keyword arguments given to `axes.plot(...)`.

plot_update_stats (*axes, xaxis='time', yaxis='E', y_exact=None, **kwargs*)

Plot `update_stats` to display the convergence during the sweeps.

Parameters

- **axes** (`matplotlib.axes.Axes`) – The axes to plot into. Defaults to `matplotlib.pyplot.gca()`
- **xaxis** ('N_updates' | 'sweep' | keys of `update_stats`) – Key of `update_stats` to be used for the x-axis of the plots. 'N_updates' is just enumerating the number of bond updates, and 'sweep' corresponds to the sweep number (including environment sweeps).
- **yaxis** ('E' | keys of `update_stats`) – Key of `update_stats` to be used for the y-axis of the plots. For 'E', use the energy (per site for infinite systems).
- **y_exact** (*float*) – Exact value for the quantity on the y-axis for comparison. If given, plot `abs((y-y_exact)/y_exact)` on a log-scale yaxis.
- ****kwargs** – Further keyword arguments given to `axes.plot(...)`.

post_update_local (*update_data*)

Perform post-update actions.

Compute truncation energy, remove *LP/RP* that are no longer needed and collect statistics.

Parameters `update_data` (*dict*) – What was returned by `update_local()`.

prepare_svd (*theta*)

Transform `theta` into matrix for svd.

prepare_update ()

Prepare *self* for calling `update_local()` on sites (`i0`, `i0+1`).

Returns `theta` – Current best guess for the ground state, which is to be optimized. Labels 'vL', 'p0', 'vR', 'p1'.

Return type `Array`

reset_stats ()

Reset the statistics, useful if you want to start a new sweep run.

option `DMRGEngine.chi_list: dict | None`

A dictionary to gradually increase the `chi_max` parameter of `trunc_params`. The key defines starting from which sweep `chi_max` is set to the value, e.g. `{0: 50, 20: 100}` uses `chi_max=50` for the first 20 sweeps and `chi_max=100` afterwards. Overwrites `trunc_params['chi_list']`. By default (None) this feature is disabled.

option `DMRGEngine.sweep_0: int`

The number of sweeps already performed. (Useful for re-start).

run()

Run the DMRG simulation to find the ground state.

Returns

- **E** (*float*) – The energy of the resulting ground state MPS.
- **psi** (MPS) – The MPS representing the ground state after the simulation, i.e. just a reference to `psi`.

Options

option `DMRGEngine.diag_method: str`

Method to be used for diagonalization, default 'default'. For possible arguments see `DMRGEngine.diag()`.

option `DMRGEngine.E_tol_to_trunc: float`

It's reasonable to choose the Lanczos convergence criteria '`E_tol`' not many magnitudes lower than the current truncation error. Therefore, if `E_tol_to_trunc` is not None, we update `E_tol` of `lanczos_params` to `max_E_trunc * E_tol_to_trunc`, restricted to the interval `[E_tol_min, E_tol_max]`, where `max_E_trunc` is the maximal energy difference due to truncation right after each Lanczos optimization during the sweeps.

option `DMRGEngine.E_tol_max: float`

See `E_tol_to_trunc`

option `DMRGEngine.E_tol_min: float`

See `E_tol_to_trunc`

option `DMRGEngine.max_E_err: float`

Convergence if the change of the energy in each step satisfies $-\Delta E / \max(|E|, 1) < \max_E_err$. Note that this is also satisfied if $\Delta E > 0$, i.e., if the energy increases (due to truncation).

option `DMRGEngine.max_hours: float`

If the DMRG took longer (measured in wall-clock time), 'shelve' the simulation, i.e. stop and return with the flag `shelve=True`.

option `DMRGEngine.max_S_err: float`

Convergence if the relative change of the entropy in each step satisfies $|\Delta S|/S < \max_S_err$

option `DMRGEngine.max_sweeps: int`

Maximum number of sweeps to be performed.

option `DMRGEngine.min_sweeps: int`

Minimum number of sweeps to be performed. Defaults to `1.5 * N_sweeps_check`.

option `DMRGEngine.N_sweeps_check: int`

Number of sweeps to perform between checking convergence criteria and giving a status update.

option `DMRGEngine.norm_tol: float`

After the DMRG run, update the environment with at most `norm_tol_iter` sweeps until `np.linalg.norm(psi.norm_err()) < norm_tol`.

option `DMRGEngine.norm_tol_iter: float`

Perform at most `norm_tol_iter * update_env` sweeps to converge the norm error below `norm_tol`. If the state is not converged after that, call `canonical_form()` instead.

option `DMRGEngine.P_tol_to_trunc: float`

It's reasonable to choose the Lanczos convergence criteria '`P_tol`' not many magnitudes lower than the current truncation error. Therefore, if `P_tol_to_trunc` is not `None`, we update `P_tol` of `lanczos_params` to `max_trunc_err * P_tol_to_trunc`, restricted to the interval `[P_tol_min, P_tol_max]`, where `max_trunc_err` is the maximal truncation error (discarded weight of the Schmidt values) due to truncation right after each Lanczos optimization during the sweeps.

option `DMRGEngine.P_tol_max: float`

See `P_tol_to_trunc`

option `DMRGEngine.P_tol_min: float`

See `P_tol_to_trunc`

option `DMRGEngine.update_env: int`

Number of sweeps without bond optimization to update the environment for infinite boundary conditions, performed every `N_sweeps_check` sweeps.

set_B (`U, S, VH`)

Update the MPS with the `U`, `S`, `VH` returned by `self.mixed_svd`.

Parameters

- **VH** (`U,`) – Left and Right-canonical matrices as returned by the SVD.
- **S** (1D array | 2D *Array*) – The middle part returned by the SVD, `theta = U S VH`. Without a mixer just the singular values, with enabled *mixer* a 2D array.

sweep (`optimize=True, meas_E_trunc=False`)

One 'sweep' of a the algorithm.

Iterate over the bond which is optimized, to the right and then back to the left to the starting point.

Parameters

- **optimize** (`bool, optional`) – Whether we actually optimize to find the ground state of the effective Hamiltonian. (If `False`, just update the environments).
- **meas_E_trunc** (`bool, optional`) – Whether to measure truncation energies.

Returns

- **max_trunc_err** (`float`) – Maximal truncation error introduced.
- **max_E_trunc** (`None | float`) – `None` if `meas_E_trunc` is `False`, else the maximal change of the energy due to the truncation.

update_LP (`U`)

Update left part of the environment.

We always update the environment at site `i0 + 1`: this environment then contains the site where we just performed a local update (when sweeping right).

Parameters **U** (*Array*) – The `U` as returned by the SVD, with combined legs, labels '`vL`', '`p0`', '`vR`'.

update_RP (*VH*)

Update right part of the environment.

We always update the environment at site *i0*: this environment then contains the site where we just performed a local update (when sweeping left).

Parameters *VH* (*Array*) – The *VH* as returned by SVD, with combined legs, labels '*vL*', '*(vR.p1)*'.

update_local (*theta*, *optimize=True*, *meas_E_trunc=False*)

Perform bond-update on the sites (*i0*, *i0+1*).

Parameters

- **theta** (*Array*) – Initial guess for the ground state of the effective Hamiltonian.
- **optimize** (*bool*) – Whether we actually optimize to find the ground state of the effective Hamiltonian. (If False, just update the environments).
- **meas_E_trunc** (*bool*) – Whether to measure the energy after truncation.

Returns

update_data – Data computed during the local update, as described in the following:

E0 [float] Total energy, obtained *before* truncation (if *optimize=True*), or *after* truncation (if *optimize=False*) (but never None).

N [int] Dimension of the Krylov space used for optimization in the lanczos algorithm. 0 if *optimize=False*.

age [int] Current size of the DMRG simulation: number of physical sites involved into the contraction.

U, VH: Array *U* and *VH* returned by *mixed_svd()*.

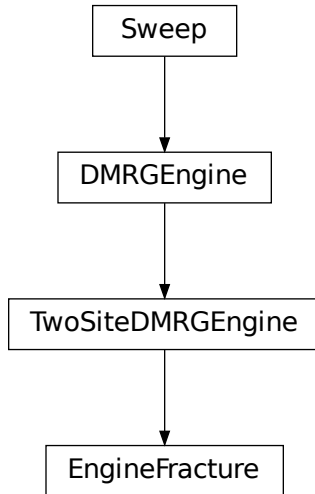
ov_change: float Change in the wave function $1 - \text{abs}(\langle \text{theta_guess} | \text{theta} \rangle)$ induced by *diag()*, *not* including the truncation!

Return type dict

EngineFracture

- full name: `tenpy.algorithms.dmrq.EngineFracture`
- parent module: `tenpy.algorithms.dmrq`
- type: class

Inheritance Diagram



Methods

<code>EngineFracture.__init__(psi, DMRG_params)</code>	<code>model,</code>	Initialize self.
<code>EngineFracture.diag(theta_guess)</code>		Diagonalize the effective Hamiltonian represented by self.
<code>EngineFracture.environment_sweeps(N_sweeps)</code>		Perform N_sweeps sweeps without optimization to update the environment.
<code>EngineFracture.get_sweep_schedule()</code>		Define the schedule of the sweep.
<code>EngineFracture.init_env([model])</code>		(Re-)initialize the environment.
<code>EngineFracture.make_eff_H()</code>		Create new instance of <code>self.EffectiveH</code> at <code>self.i0</code> and set it to <code>self.eff_H</code> .
<code>EngineFracture.mixed_svd(theta)</code>		Get (truncated) B from the new theta (as returned by diag).
<code>EngineFracture.mixer_activate()</code>		Set <code>self.mixer</code> to the class specified by <code>options['mixer']</code> .
<code>EngineFracture.mixer_cleanup()</code>		Cleanup the effects of a mixer.
<code>EngineFracture.plot_sweep_stats([axes, ...])</code>		Plot <code>sweep_stats</code> to display the convergence with the sweeps.
<code>EngineFracture.plot_update_stats(axes[, ...])</code>		Plot <code>update_stats</code> to display the convergence during the sweeps.
<code>EngineFracture.post_update_local(update_data)</code>		Perform post-update actions.
<code>EngineFracture.prepare_svd(theta)</code>		Transform theta into matrix for svd.
<code>EngineFracture.prepare_update()</code>		Prepare <code>self</code> for calling <code>update_local()</code> on sites $(i0, i0+1)$.

continues on next page

Table 20 – continued from previous page

<code>EngineFracture.reset_stats()</code>	Reset the statistics, useful if you want to start a new sweep run.
<code>EngineFracture.run()</code>	Run the DMRG simulation to find the ground state.
<code>EngineFracture.set_B(U, S, VH)</code>	Update the MPS with the U, S, VH returned by <i>self.mixed_svd</i> .
<code>EngineFracture.sweep([optimize, meas_E_trunc])</code>	One ‘sweep’ of a the algorithm.
<code>EngineFracture.update_LP(U)</code>	Update left part of the environment.
<code>EngineFracture.update_RP(VH)</code>	Update right part of the environment.
<code>EngineFracture.update_local(theta[,...])</code>	Perform bond-update on the sites (i0, i0+1).

Class Attributes and Properties

<code>EngineFracture.DMRG_params</code>
<code>EngineFracture.engine_params</code>

class `tenpy.algorithms.dmrq.EngineFracture` (*psi, model, DMRG_params*)

Bases: `tenpy.algorithms.dmrq.TwoSiteDMRGEngine`

Engine which keeps the legs separate.

Due to a different contraction order in `matvec()`, this engine might be faster than `EngineCombine`, at least for large physical dimensions and if the MPO is sparse. One `matvec()` is $O(2\chi^3 d^2 W + 2\chi^2 d^3 W^2)$.

Deprecated since version 0.5.0: Directly use the `TwoSiteDMRGEngine` with the DMRG parameter `combine=False`.

EffectiveH

alias of `tenpy.algorithms.mps_common.TwoSiteH`

diag (*theta_guess*)

Diagonalize the effective Hamiltonian represented by self.

option `DMRGEngine.max_N_for_ED: int`

Maximum matrix dimension of the effective hamiltonian up to which the 'default' *diag_method* uses ED instead of Lanczos.

option `DMRGEngine.diag_method: str`

One of the folloing strings:

‘default’ Same as ‘lanczos’ for large bond dimensions, but if the total dimension of the effective Hamiltonian does not exceed the DMRG parameter ‘max_N_for_ED’ it uses ‘ED_block’.

‘lanczos’ `lanczos()` Default, the Lanczos implementation in TeNPy.

‘arpack’ `lanczos_arpack()` Based on `scipy.linalg.sparse.eigsh()`. Slower than ‘lanczos’, since it needs to convert the npc arrays to numpy arrays during *each* matvec, and possibly does many more iterations.

‘ED_block’ `full_diag_effH()` Contract the effective Hamiltonian to a (large!) matrix and diagonalize the block in the charge sector of the initial state. Preserves the charge sector of the explicitly conserved charges. However, if you don’t preserve a charge explicitly, it can break it. For example if you use a `SpinChain({'conserve': 'parity'})`, it could change the total “Sz”, but not the parity of “Sz”.

‘ED_all’ `full_diag_effH()` Contract the effective Hamiltonian to a (large!) matrix and diagonalize it completely. Allows to change the charge sector *even for explicitly conserved charges*. For example if you use a `SpinChain({'conserve': 'Sz'})`, it **can** change the total “Sz”.

Parameters `theta_guess` (*Array*) – Initial guess for the ground state of the effective Hamiltonian.

Returns

- `E0` (*float*) – Energy of the found ground state.
- `theta` (*Array*) – Ground state of the effective Hamiltonian.
- `N` (*int*) – Number of Lanczos iterations used. `-1` if unknown.
- `ov_change` (*float*) – Change in the wave function $1 - \text{abs}(\langle \text{theta_guess} | \text{theta_diag} \rangle)$

environment_sweeps (*N_sweeps*)

Perform *N_sweeps* sweeps without optimization to update the environment.

Parameters `N_sweeps` (*int*) – Number of sweeps to run without optimization

get_sweep_schedule ()

Define the schedule of the sweep.

One ‘sweep’ is a full sequence from the leftmost site to the right and back. Only those *LP* and *RP* that can be used later should be updated.

Returns `schedule` – Schedule for the sweep. Each entry is `(i0, move_right, (update_LP, update_RP))`, where *i0* is the leftmost of the `self.EffectiveH.length` sites to be updated in `update_local()`, *move_right* indicates whether the next *i0* in the schedule is right (*True*) of the current one, and *update_LP*, *update_RP* indicate whether it is necessary to update the *LP* and *RP*. The latter are chosen such that the environment is growing for infinite systems, but we only keep the minimal number of environment tensors in memory.

Return type iterable of (*int*, *bool*, (*bool*, *bool*))

init_env (*model=None*)

(Re-)initialize the environment.

This function is useful to (re-)start a Sweep with a slightly different model or different (engine) parameters. Note that we assume that we still have the same *psi*. Calls `reset_stats()`.

Parameters `model` (*MPOModel*) – The model representing the Hamiltonian for which we want to find the ground state. If *None*, keep the model used before.

Options

Deprecated since version 0.6.0: Options *LP*, *LP_age*, *RP* and *RP_age* are now collected in a dictionary `init_env_data` with different keys `init_LP`, `init_RP`, `age_LP`, `age_RP`

option `Sweep.init_env_data:` *dict*

Dictionary as returned by `self.env.get_initialization_data()` from `get_initialization_data()`.

option `Sweep.orthogonal_to:` *list of MPSEnvironment*

List of other matrix product states to orthogonalize against. Works only for finite systems. This parameter can be used to find (a few) excited states as follows. First, run DMRG to find the ground state and then run DMRG again while orthogonalizing against the ground state, which yields the first excited state (in the same symmetry sector), and so on.

option `Sweep.start_env:` *int*

Number of sweeps to be performed without optimization to update the environment.

Raises `ValueError` – If the engine is re-initialized with a new model, which legs are incompatible with those of the old model.

`make_eff_H()`

Create new instance of *self.EffectiveH* at *self.i0* and set it to *self.eff_H*.

`mixed_svd(theta)`

Get (truncated) *B* from the new *theta* (as returned by *diag*).

The goal is to split *theta* and truncate it:

	--	theta	--	=>	--	U	--	S	--	VH	-

Without a mixer, this is done by a simple svd and truncation of Schmidt values.

With a mixer, the state is perturbed before the SVD. The details of the perturbation are defined by the *Mixer* class.

Note that the returned *S* is a general (not diagonal) matrix, with labels '*vL*', '*vR*'.

Parameters *theta* (*Array*) – The optimized wave function, prepared for svd.

Returns

- ***U* (*Array*)** – Left-canonical part of *theta*. Labels '*(vL.p0)*', '*vR*'.
- ***S* (*1D ndarray* | *2D Array*)** – Without mixer just the singular values of the array; with mixer it might be a general matrix with labels '*vL*', '*vR*'; see comment above.
- ***VH* (*Array*)** – Right-canonical part of *theta*. Labels '*vL*', '*(p1.vR)*'.
- ***err* (*TruncationError*)** – The truncation error introduced.

`mixer_activate()`

Set *self.mixer* to the class specified by *options['mixer']*.

`option TwoSiteDMRGEngine.mixer: str | class | bool`

Chooses the *Mixer* to be used. A string stands for one of the mixers defined in this module, a class is used as custom mixer. Default (*None*) uses no mixer, *True* uses *DensityMatrixMixer* for the 2-site case and *SingleSiteMixer* for the 1-site case.

`option TwoSiteDMRGEngine.mixer_params: dict`

Mixer parameters as described in *Mixer*.

`mixer_cleanup()`

Cleanup the effects of a mixer.

A *sweep()* with an enabled *Mixer* leaves the MPS *psi* with 2D arrays in *S*. To recover the original form, this function simply performs one sweep with disabled mixer.

`plot_sweep_stats` (*axes=None*, *xaxis='time'*, *yaxis='E'*, *y_exact=None*, *kwargs*)**

Plot *sweep_stats* to display the convergence with the sweeps.

Parameters

- ***axes* (*matplotlib.axes.Axes*)** – The axes to plot into. Defaults to *matplotlib.pyplot.gca()*
- ***yaxis* (*xaxis,*)** – Key of *sweep_stats* to be used for the x-axis and y-axis of the plots.
- ***y_exact* (*float*)** – Exact value for the quantity on the y-axis for comparison. If given, plot *abs((y-y_exact)/y_exact)* on a log-scale yaxis.

- ****kwargs** – Further keyword arguments given to `axes.plot(...)`.

plot_update_stats (*axes*, *xaxis*='time', *yaxis*='E', *y_exact*=None, ****kwargs**)

Plot `update_stats` to display the convergence during the sweeps.

Parameters

- **axes** (`matplotlib.axes.Axes`) – The axes to plot into. Defaults to `matplotlib.pyplot.gca()`
- **xaxis** ('N_updates' | 'sweep' | keys of `update_stats`) – Key of `update_stats` to be used for the x-axis of the plots. 'N_updates' is just enumerating the number of bond updates, and 'sweep' corresponds to the sweep number (including environment sweeps).
- **yaxis** ('E' | keys of `update_stats`) – Key of `update_stats` to be used for the y-axis of the plots. For 'E', use the energy (per site for infinite systems).
- **y_exact** (*float*) – Exact value for the quantity on the y-axis for comparison. If given, plot `abs((y-y_exact)/y_exact)` on a log-scale yaxis.
- ****kwargs** – Further keyword arguments given to `axes.plot(...)`.

post_update_local (*update_data*)

Perform post-update actions.

Compute truncation energy, remove *LP/RP* that are no longer needed and collect statistics.

Parameters `update_data` (*dict*) – What was returned by `update_local()`.

prepare_svd (*theta*)

Transform *theta* into matrix for svd.

prepare_update ()

Prepare *self* for calling `update_local()` on sites (*i0*, *i0+1*).

Returns *theta* – Current best guess for the ground state, which is to be optimized. Labels 'vL', 'p0', 'vR', 'p1'.

Return type *Array*

reset_stats ()

Reset the statistics, useful if you want to start a new sweep run.

option `DMRGEngine.chi_list`: *dict* | None

A dictionary to gradually increase the *chi_max* parameter of *trunc_params*. The key defines starting from which sweep *chi_max* is set to the value, e.g. {0: 50, 20: 100} uses *chi_max*=50 for the first 20 sweeps and *chi_max*=100 afterwards. Overwrites *trunc_params['chi_list']*. By default (None) this feature is disabled.

option `DMRGEngine.sweep_0`: *int*

The number of sweeps already performed. (Useful for re-start).

run ()

Run the DMRG simulation to find the ground state.

Returns

- **E** (*float*) – The energy of the resulting ground state MPS.
- **psi** (MPS) – The MPS representing the ground state after the simulation, i.e. just a reference to `psi`.

Options

option `DMRGEngine.diag_method:` **str**

Method to be used for diagonalization, default 'default'. For possible arguments see `DMRGEngine.diag()`.

option `DMRGEngine.E_tol_to_trunc:` **float**

It's reasonable to choose the Lanczos convergence criteria '`E_tol`' not many magnitudes lower than the current truncation error. Therefore, if `E_tol_to_trunc` is not `None`, we update `E_tol` of `lanczos_params` to `max_E_trunc * E_tol_to_trunc`, restricted to the interval `[E_tol_min, E_tol_max]`, where `max_E_trunc` is the maximal energy difference due to truncation right after each Lanczos optimization during the sweeps.

option `DMRGEngine.E_tol_max:` **float**

See `E_tol_to_trunc`

option `DMRGEngine.E_tol_min:` **float**

See `E_tol_to_trunc`

option `DMRGEngine.max_E_err:` **float**

Convergence if the change of the energy in each step satisfies $-\Delta E / \max(|E|, 1) < \max_E_err$. Note that this is also satisfied if $\Delta E > 0$, i.e., if the energy increases (due to truncation).

option `DMRGEngine.max_hours:` **float**

If the DMRG took longer (measured in wall-clock time), 'shelve' the simulation, i.e. stop and return with the flag `shelve=True`.

option `DMRGEngine.max_S_err:` **float**

Convergence if the relative change of the entropy in each step satisfies $|\Delta S|/S < \max_S_err$

option `DMRGEngine.max_sweeps:` **int**

Maximum number of sweeps to be performed.

option `DMRGEngine.min_sweeps:` **int**

Minimum number of sweeps to be performed. Defaults to `1.5 * N_sweeps_check`.

option `DMRGEngine.N_sweeps_check:` **int**

Number of sweeps to perform between checking convergence criteria and giving a status update.

option `DMRGEngine.norm_tol:` **float**

After the DMRG run, update the environment with at most `norm_tol_iter` sweeps until `np.linalg.norm(psi.norm_err()) < norm_tol`.

option `DMRGEngine.norm_tol_iter:` **float**

Perform at most `norm_tol_iter * update_env` sweeps to converge the norm error below `norm_tol`. If the state is not converged after that, call `canonical_form()` instead.

option `DMRGEngine.P_tol_to_trunc:` **float**

It's reasonable to choose the Lanczos convergence criteria '`P_tol`' not many magnitudes lower than the current truncation error. Therefore, if `P_tol_to_trunc` is not `None`, we update `P_tol` of `lanczos_params` to `max_trunc_err * P_tol_to_trunc`, restricted to the interval `[P_tol_min, P_tol_max]`, where `max_trunc_err` is the maximal truncation error (discarded weight of the Schmidt values) due to truncation right after each Lanczos optimization during the sweeps.

option `DMRGEngine.P_tol_max:` **float**

See `P_tol_to_trunc`

option `DMRGEngine.P_tol_min:` **float**

See `P_tol_to_trunc`

option `DMRGEngine.update_env: int`

Number of sweeps without bond optimization to update the environment for infinite boundary conditions, performed every $N_{\text{sweeps_check}}$ sweeps.

set_B (U, S, VH)

Update the MPS with the U, S, VH returned by `self.mixed_svd`.

Parameters

- **VH** (U, S) – Left and Right-canonical matrices as returned by the SVD.
- **S** (1D array | 2D *Array*) – The middle part returned by the SVD, $\text{theta} = U S VH$. Without a mixer just the singular values, with enabled *mixer* a 2D array.

sweep (*optimize=True, meas_E_trunc=False*)

One ‘sweep’ of the algorithm.

Iterate over the bond which is optimized, to the right and then back to the left to the starting point.

Parameters

- **optimize** (*bool, optional*) – Whether we actually optimize to find the ground state of the effective Hamiltonian. (If False, just update the environments).
- **meas_E_trunc** (*bool, optional*) – Whether to measure truncation energies.

Returns

- **max_trunc_err** (*float*) – Maximal truncation error introduced.
- **max_E_trunc** (*None | float*) – None if `meas_E_trunc` is False, else the maximal change of the energy due to the truncation.

update_LP (U)

Update left part of the environment.

We always update the environment at site $i0 + 1$: this environment then contains the site where we just performed a local update (when sweeping right).

Parameters **U** (*Array*) – The U as returned by the SVD, with combined legs, labels ‘vL’, ‘p0’, ‘vR’.

update_RP (VH)

Update right part of the environment.

We always update the environment at site $i0$: this environment then contains the site where we just performed a local update (when sweeping left).

Parameters **VH** (*Array*) – The VH as returned by SVD, with combined legs, labels ‘vL’, ‘(vR.p1)’.

update_local (*theta, optimize=True, meas_E_trunc=False*)

Perform bond-update on the sites ($i0, i0+1$).

Parameters

- **theta** (*Array*) – Initial guess for the ground state of the effective Hamiltonian.
- **optimize** (*bool*) – Whether we actually optimize to find the ground state of the effective Hamiltonian. (If False, just update the environments).
- **meas_E_trunc** (*bool*) – Whether to measure the energy after truncation.

Returns

update_data – Data computed during the local update, as described in the following:

E0 [float] Total energy, obtained *before* truncation (if `optimize=True`), or *after* truncation (if `optimize=False`) (but never `None`).

N [int] Dimension of the Krylov space used for optimization in the lanczos algorithm. 0 if `optimize=False`.

age [int] Current size of the DMRG simulation: number of physical sites involved into the contraction.

U, VH: **Array** *U* and *VH* returned by `mixed_svd()`.

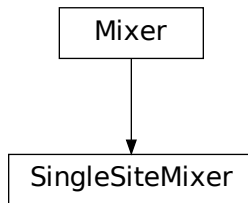
ov_change: **float** Change in the wave function $1 - \text{abs}(\langle \text{theta_guess} | \text{theta} \rangle)$ induced by `diag()`, *not* including the truncation!

Return type `dict`

SingleSiteMixer

- full name: `tenpy.algorithms.dmrp.SingleSiteMixer`
- parent module: `tenpy.algorithms.dmrp`
- type: class

Inheritance Diagram



Methods

<code>SingleSiteMixer.__init__(options)</code>	Initialize self.
<code>SingleSiteMixer.perturb_svd(engine, theta, ...)</code>	Mix extra terms to theta and perform an SVD.
<code>SingleSiteMixer.subspace_expand(engine, ...)</code>	Expand the MPS subspace, to allow the bond dimension to increase.
<code>SingleSiteMixer.update_amplitude(sweeps)</code>	Update the amplitude, possibly disable the mixer.

class `tenpy.algorithms.dmrp.SingleSiteMixer(options)`

Bases: `tenpy.algorithms.dmrp.Mixer`

Mixer for single-site DMRG.

Performs a subspace expansion following [Hubig2015].

perturb_svd (*engine*, *theta*, *i0*, *move_right*, *next_B*)

Mix extra terms to *theta* and perform an SVD.

We calculate the left and right reduced density matrix using the mixer (which might include applications of H). These density matrices are diagonalized and truncated such that we effectively perform a svd for the case `mixer.amplitude=0`.

Parameters

- **engine** (*Engine*) – The DMRG engine calling the mixer.
- **theta** (*Array*) – The optimized wave function, prepared for svd.
- **i0** (*int*) – The site index where *theta* lives.
- **move_right** (*bool*) – Whether we move to the right (`True`) or left (`False`).
- **next_B** (*Array*) – The subspace expansion requires to change the tensor on the next site as well. If *move_right*, it should correspond to `engine.psi.get_B(i0+1, form='B')`. If not *move_right*, it should correspond to `engine.psi.get_B(i0-1, form='A')`.

Returns

- **U** (*Array*) – Left-canonical part of `tensordot(theta, next_B)`. Labels ' (vL.p0) ', 'vR'.
- **S** (*1D ndarray*) – (Perturbed) singular values on the new bond (between *theta* and *next_B*).
- **VH** (*Array*) – Right-canonical part of `tensordot(theta, next_B)`. Labels 'vL', ' (p1.vR) '.
- **err** (*TruncationError*) – The truncation error introduced.

subspace_expand (*engine*, *theta*, *i0*, *move_right*, *next_B*)

Expand the MPS subspace, to allow the bond dimension to increase.

This is the subspace expansion following [Hubig2015].

Parameters

- **engine** (*SingleSiteDMRGEngine* | *TwoSiteDMRGEngine*) – ‘Engine’ for the DMRG algorithm
- **theta** (*Array*) – Optimized guess for the ground state of the effective local Hamiltonian.
- **i0** (*int*) – Site index at which the local update has taken place.
- **move_right** (*bool*) – Whether the next *i0* of the sweep will be right or left of the current one.
- **next_B** (*Array*) – The subspace expansion requires to change the tensor on the next site as well. If *move_right*, it should correspond to `engine.psi.get_B(i0+1, form='B')`. If not *move_right*, it should correspond to `engine.psi.get_B(i0-1, form='A')`.

Returns

- *theta* – Local MPS tensor at site *i0* after subspace expansion.
- *next_B* – MPS tensor at site *i0+1* or *i0-1* (depending on sweep direction) after subspace expansion.

update_amplitude (*sweeps*)

Update the amplitude, possibly disable the mixer.

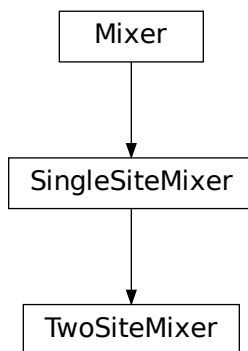
Parameters *sweeps* (*int*) – The number of performed sweeps, to check if we need to disable the mixer.

Returns *mixer* – Returns *self* if we should continue mixing, or *None*, if the mixer should be disabled.

Return type *Mixer* | *None*

TwoSiteMixer

- full name: `tenpy.algorithms.dmrp.TwoSiteMixer`
- parent module: `tenpy.algorithms.dmrp`
- type: class

Inheritance Diagram**Methods**

<code>TwoSiteMixer.__init__(options)</code>	Initialize self.
<code>TwoSiteMixer.perturb_svd(engine, theta, i0, ...)</code>	Mix extra terms to theta and perform an SVD.
<code>TwoSiteMixer.subspace_expand(engine, theta, ...)</code>	Expand the MPS subspace, to allow the bond dimension to increase.
<code>TwoSiteMixer.update_amplitude(sweeps)</code>	Update the amplitude, possibly disable the mixer.

class `tenpy.algorithms.dmrp.TwoSiteMixer` (*options*)

Bases: `tenpy.algorithms.dmrp.SingleSiteMixer`

Mixer for two-site DMRG.

This is the two-site version of the mixer described in [Hubig2015]. Equivalent to the `DensityMatrixMixer`, but never construct the full density matrix.

perturb_svd (*engine*, *theta*, *i0*, *move_right*)

Mix extra terms to *theta* and perform an SVD.

Parameters

- **engine** (`Engine`) – The DMRG engine calling the mixer.
- **theta** (`Array`) – The optimized wave function, prepared for svd.
- **i0** (`int`) – Site index; *theta* lives on *i0*, *i0*+1.
- **update_LP** (`bool`) – Whether to calculate the next `env.LP[i0+1]`.
- **update_RP** (`bool`) – Whether to calculate the next `env.RP[i0]`.

Returns

- **U** (`Array`) – Left-canonical part of *theta*. Labels '`vL.p0`', '`vR`'.
- **S** (`1D ndarray` | `2D Array`) – Without mixer just the singular values of the array; with mixer it might be a general matrix; see comment above.
- **VH** (`Array`) – Right-canonical part of *theta*. Labels '`vL`', '`vR.p1`'.
- **err** (`TruncationError`) – The truncation error introduced.

subspace_expand (*engine*, *theta*, *i0*, *move_right*, *next_B*)

Expand the MPS subspace, to allow the bond dimension to increase.

This is the subspace expansion following [Hubig2015].

Parameters

- **engine** (`SingleSiteDMRGEngine` | `TwoSiteDMRGEngine`) – ‘Engine’ for the DMRG algorithm
- **theta** (`Array`) – Optimized guess for the ground state of the effective local Hamiltonian.
- **i0** (`int`) – Site index at which the local update has taken place.
- **move_right** (`bool`) – Whether the next *i0* of the sweep will be right or left of the current one.
- **next_B** (`Array`) – The subspace expansion requires to change the tensor on the next site as well. If *move_right*, it should correspond to `engine.psi.get_B(i0+1, form='B')`. If not *move_right*, it should correspond to `engine.psi.get_B(i0-1, form='A')`.

Returns

- *theta* – Local MPS tensor at site *i0* after subspace expansion.
- *next_B* – MPS tensor at site *i0*+1 or *i0*-1 (depending on sweep direction) after subspace expansion.

update_amplitude (*sweeps*)

Update the amplitude, possibly disable the mixer.

Parameters **sweeps** (`int`) – The number of performed sweeps, to check if we need to disable the mixer.

Returns **mixer** – Returns *self* if we should continue mixing, or `None`, if the mixer should be disabled.

Return type `Mixer` | `None`

Functions

<code>chi_list(chi_max[, dchi, nsweeps])</code>	Compute a ‘ramping-up’ <code>chi_list</code> .
<code>full_diag_effH(effH, theta_guess[, keep_sector])</code>	Perform an exact diagonalization of <code>effH</code> .
<code>run(psi, model, options)</code>	Run the DMRG algorithm to find the ground state of the given model.

`chi_list`

- full name: `tenpy.algorithms.dmr.chi_list`
- parent module: `tenpy.algorithms.dmr`
- type: function

`tenpy.algorithms.dmr.chi_list(chi_max, dchi=20, nsweeps=20)`
 Compute a ‘ramping-up’ `chi_list`.

The resulting `chi_list` allows to increase `chi` by `dchi` every `nsweeps` sweeps up to a given maximal `chi_max`.

Parameters

- **`chi_max`** (`int`) – Final value for the bond dimension.
- **`dchi`** (`int`) – Step size how to increase `chi`
- **`nsweeps`** (`int`) – Step size for sweeps

Returns `chi_list` – To be used as `chi_list` parameter for DMRG, see `run()`. Keys increase by `nsweeps`, values by `dchi`, until a maximum of `chi_max` is reached.

Return type `dict`

`full_diag_effH`

- full name: `tenpy.algorithms.dmr.full_diag_effH`
- parent module: `tenpy.algorithms.dmr`
- type: function

`tenpy.algorithms.dmr.full_diag_effH(effH, theta_guess, keep_sector=True)`
 Perform an exact diagonalization of `effH`.

This function offers an alternative to `lanczos()`.

Parameters

- **`effH`** (`EffectiveH`) – The effective Hamiltonian.
- **`theta_guess`** (`Array`) – Current guess to select the charge sector. Labels as specified by `effH.acts_on`.

Module description

Density Matrix Renormalization Group (DMRG).

Although it was originally not formulated with tensor networks, the DMRG algorithm (invented by Steven White in 1992 [[White1992](#)]) opened the whole field with its enormous success in finding ground states in 1D.

We implement DMRG in the modern formulation of matrix product states [[Schollwoeck2011](#)], both for finite systems ('finite' or 'segment' boundary conditions) and in the thermodynamic limit ('infinite' b.c.).

The function `run()` - well - runs one DMRG simulation. Internally, it generates an instance of an `Sweep`. This class implements the common functionality like defining a *sweep*, but leaves the details of the contractions to be performed to the derived classes.

Currently, there are two derived classes implementing the contractions: `SingleSiteDMRGEngine` and `TwoSiteDMRGEngine`. They differ (as their name implies) in the number of sites which are optimized simultaneously. They should both give the same results (up to rounding errors). However, if started from a product state, `SingleSiteDMRGEngine` depends critically on the use of a `Mixer`, while `TwoSiteDMRGEngine` is in principle more computationally expensive to run and has occasionally displayed some convergence issues.. Which one is preferred in the end is not obvious a priori and might depend on the used model. Just try both of them.

A `Mixer` should be used initially to avoid that the algorithm gets stuck in local energy minima, and then slowly turned off in the end. For `SingleSiteDMRGEngine`, using a mixer is crucial, as the one-site algorithm cannot increase the MPS bond dimension by itself.

Todo: Write UserGuide!!!

7.7.5 tdvp

- full name: `tenpy.algorithms.tdvp`
- parent module: `tenpy.algorithms`
- type: module

Classes

Engine

H0_mixed

H1_mixed

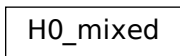
H2_mixed

<code>Engine(psi, model, options[, environment])</code>	Time dependent variational principle 'Engine'.
<code>H0_mixed(Lp, Rp)</code>	Class defining the zero site Hamiltonian for Lanczos.
<code>H1_mixed(Lp, Rp, W)</code>	Class defining the one site Hamiltonian for Lanczos.
<code>H2_mixed(Lp, Rp, W0, W1)</code>	Class defining the two sites Hamiltonian for Lanczos.

H0_mixed

- full name: `tenpy.algorithms.tdvp.H0_mixed`
- parent module: `tenpy.algorithms.tdvp`
- type: class

Inheritance Diagram



Methods

<code>H0_mixed.__init__(Lp, Rp)</code>	Initialize self.
<code>H0_mixed.matvec(x)</code>	

class `tenpy.algorithms.tdvp.H0_mixed` (*Lp*, *Rp*)

Bases: `object`

Class defining the zero site Hamiltonian for Lanczos.

Parameters

- **Lp** (`tenpy.linalg.np_conserved.Array`) – left part of the environment
- **Rp** (`tenpy.linalg.np_conserved.Array`) – right part of the environment

Lp

left part of the environment

Type `tenpy.linalg.np_conserved.Array`

Rp

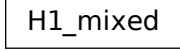
right part of the environment

Type `tenpy.linalg.np_conserved.Array`

H1_mixed

- full name: `tenpy.algorithms.tdvp.H1_mixed`
- parent module: `tenpy.algorithms.tdvp`
- type: class

Inheritance Diagram



Methods

<code>H1_mixed.__init__(Lp, Rp, W)</code>	Initialize self.
<code>H1_mixed.matvec(theta)</code>	

class `tenpy.algorithms.tdvp.H1_mixed(Lp, Rp, W)`

Bases: `object`

Class defining the one site Hamiltonian for Lanczos.

Parameters

- **Lp** (`tenpy.linalg.np_conserved.Array`) – left part of the environment
- **Rp** (`tenpy.linalg.np_conserved.Array`) – right part of the environment
- **M** (`tenpy.linalg.np_conserved.Array`) – MPO which is applied to the ‘p’ leg of theta

Lp

left part of the environment

Type `tenpy.linalg.np_conserved.Array`

Rp

right part of the environment

Type `tenpy.linalg.np_conserved.Array`

W

MPO which is applied to the ‘p0’ leg of theta

Type `tenpy.linalg.np_conserved.Array`

H2_mixed

- full name: `tenpy.algorithms.tdvp.H2_mixed`
- parent module: `tenpy.algorithms.tdvp`
- type: class

Inheritance Diagram

H2_mixed

Methods

H2_mixed.__init__(Lp, Rp, W0, W1)	Initialize self.
H2_mixed.matvec(theta)	

class tenpy.algorithms.tdvp.**H2_mixed**(*Lp*, *Rp*, *W0*, *W1*)

Bases: `object`

Class defining the two sites Hamiltonian for Lanczos.

Parameters

- **Lp** (*tenpy.linalg.np_conserved.Array*) – left part of the environment
- **Rp** (*tenpy.linalg.np_conserved.Array*) – right part of the environment
- **W** (*tenpy.linalg.np_conserved.Array*) – MPO which is applied to the ‘p0’ leg of theta

Lp

left part of the environment

Type *tenpy.linalg.np_conserved.Array*

Rp

right part of the environment

Type *tenpy.linalg.np_conserved.Array*

W0

MPO which is applied to the ‘p0’ leg of theta

Type *tenpy.linalg.np_conserved.Array*

W1

MPO which is applied to the ‘p1’ leg of theta

Type *tenpy.linalg.np_conserved.Array*

Module description

Time Dependant Variational Principle (TDVP) with MPS (finite version only).

The TDVP MPS algorithm was first proposed by [Haegeman2011]. However the stability of the algorithm was later improved in [Haegeman2016], that we are following in this implementation. The general idea of the algorithm is to project the quantum time evolution in the manifold of MPS with a given bond dimension. Compared to e.g. TEBD, the algorithm has several advantages: e.g. it conserves the unitarity of the time evolution and the energy (for the single-site version), and it is suitable for time evolution of Hamiltonian with arbitrary long range in the form of MPOs. We have implemented the one-site formulation which **does not** allow for growth of the bond dimension, and the two-site algorithm which does allow the bond dimension to grow - but requires truncation as in the TEBD case.

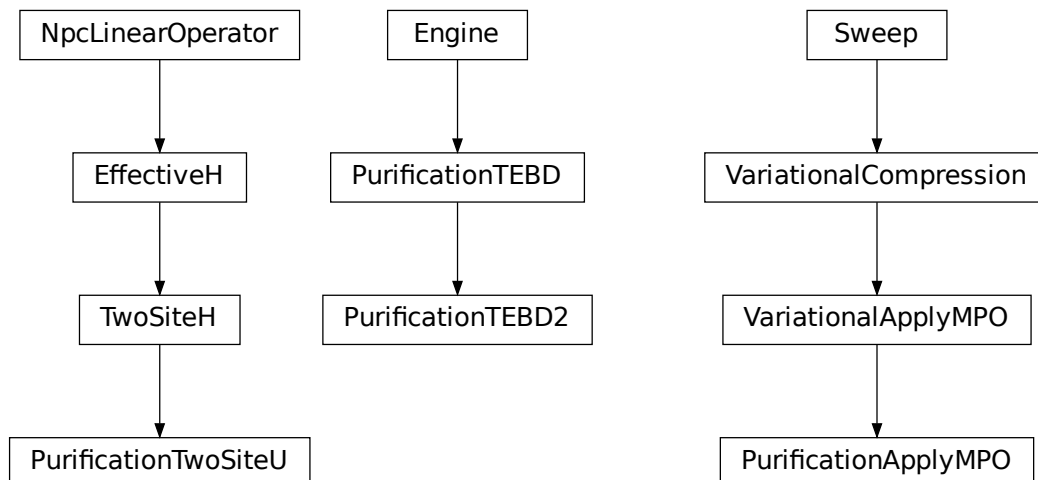
Todo: This is still a beta version, use with care. The interface might still change.

Todo: long-term: Much of the code is similar as in DMRG. To avoid too much duplicated code, we should have a general way to sweep through an MPS and updated one or two sites, used in both cases.

7.7.6 purification

- full name: `tenpy.algorithms.purification`
- parent module: `tenpy.algorithms`
- type: module

Classes

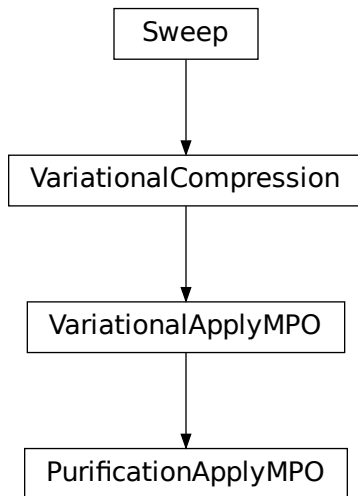


<code>PurificationApplyMPO(psi, U_MPO, options)</code>	Variant of <i>VariationalApplyMPO</i> suitable for purification.
<code>PurificationTEBD(psi, model, options)</code>	Time evolving block decimation (TEBD) for purification MPS.
<code>PurificationTEBD2(psi, model, options)</code>	Similar as <i>PurificationTEBD</i> , but perform sweeps instead of brickwall.
<code>PurificationTwoSiteU(env, i0[, combine, ...])</code>	Variant of <i>TwoSiteH</i> suitable for purification.

PurificationApplyMPO

- full name: `tenpy.algorithms.purification.PurificationApplyMPO`
- parent module: `tenpy.algorithms.purification`
- type: class

Inheritance Diagram



Methods

<code>PurificationApplyMPO.__init__(psi, U_MPO, ...)</code>	Initialize self.
<code>PurificationApplyMPO.environment_sweeps(N_sweeps)</code>	Perform <i>N_sweeps</i> sweeps without optimization to update the environment.
<code>PurificationApplyMPO.get_sweep_schedule()</code>	Define the schedule of the sweep.

continues on next page

Table 30 – continued from previous page

<code>PurificationApplyMPO.init_env(U_MPO)</code>	Initialize the environment.
<code>PurificationApplyMPO.make_eff_H()</code>	Create new instance of <i>self.EffectiveH</i> at <i>self.i0</i> and set it to <i>self.eff_H</i> .
<code>PurificationApplyMPO.post_update_local(...)</code>	Algorithm-specific actions to be taken after local update.
<code>PurificationApplyMPO.prepare_update()</code>	Prepare everything algorithm-specific to perform a local update.
<code>PurificationApplyMPO.reset_stats()</code>	Reset the statistics.
<code>PurificationApplyMPO.run()</code>	Run the compression.
<code>PurificationApplyMPO.sweep([optimize])</code>	One ‘sweep’ of a sweeper algorithm.
<code>PurificationApplyMPO.update_LP(_)</code>	
<code>PurificationApplyMPO.update_RP(_)</code>	
<code>PurificationApplyMPO.update_local(_, optimize)</code>	Perform local update.
<code>PurificationApplyMPO.update_new_psi(theta)</code>	

Class Attributes and Properties

<code>PurificationApplyMPO.engine_params</code>

class `tenpy.algorithms.purification.PurificationApplyMPO` (*psi*, *U_MPO*, *options*)

Bases: `tenpy.algorithms.mps_common.VariationalApplyMPO`

Variant of *VariationalApplyMPO* suitable for purification.

EffectiveH

alias of *PurificationTwoSiteU*

update_local (*_*, *optimize=True*)

Perform local update.

This simply contracts the environments and *theta* from the *ket* to get an updated *theta* for the bra *self.psi* (to be changed in place).

environment_sweeps (*N_sweeps*)

Perform *N_sweeps* sweeps without optimization to update the environment.

Parameters *N_sweeps* (*int*) – Number of sweeps to run without optimization

get_sweep_schedule ()

Define the schedule of the sweep.

One ‘sweep’ is a full sequence from the leftmost site to the right and back. Only those *LP* and *RP* that can be used later should be updated.

Returns *schedule* – Schedule for the sweep. Each entry is (*i0*, *move_right*, (*update_LP*, *update_RP*)), where *i0* is the leftmost of the *self.EffectiveH*. *length* sites to be updated in *update_local()*, *move_right* indicates whether the next *i0* in the schedule is right (*True*) of the current one, and *update_LP*, *update_RP* indicate whether it is necessary to update the *LP* and *RP*. The latter are chosen such that the environment is growing for infinite systems, but we only keep the minimal number of environment tensors in memory.

Return type iterable of (*int*, *bool*, (*bool*, *bool*))

init_env (*U_MPO*)

Initialize the environment.

Parameters *U_MPO* (MPO) – The MPO to be applied to the state.

make_eff_H ()

Create new instance of *self.EffectiveH* at *self.i0* and set it to *self.eff_H*.

post_update_local (*update_data*)

Algorithm-specific actions to be taken after local update.

An example would be to collect statistics.

prepare_update ()

Prepare everything algorithm-specific to perform a local update.

reset_stats ()

Reset the statistics. Useful if you want to start a new Sweep run.

This method is expected to be overwritten by subclass, and should then define *self.update_stats* and *self.sweep_stats* dicts consistent with the statistics generated by the algorithm particular to that subclass.

option *Sweep.sweep_0*: **int**

Number of sweeps that have already been performed.

run ()

Run the compression.

The state *psi* is compressed in place.

Returns *max_trunc_err* – The maximal truncation error of a two-site wave function.

Return type *TruncationError*

sweep (*optimize=True*)

One ‘sweep’ of a sweeper algorithm.

Iterate over the bond which is optimized, to the right and then back to the left to the starting point. If *optimize=False*, don’t actually diagonalize the effective hamiltonian, but only update the environment.

Parameters *optimize* (*bool*, *optional*) – Whether we actually optimize to find the ground state of the effective Hamiltonian. (If False, just update the environments).

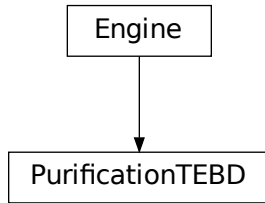
Returns *max_trunc_err* – Maximal truncation error introduced.

Return type *float*

PurificationTEBD

- full name: *tenpy.algorithms.purification.PurificationTEBD*
- parent module: *tenpy.algorithms.purification*
- type: class

Inheritance Diagram



Methods

<code>PurificationTEBD.__init__(psi, model, options)</code>	Initialize self.
<code>PurificationTEBD.calc_U(order, delta_t[, ...])</code>	see <code>calc_U()</code>
<code>PurificationTEBD.disentangle(theta)</code>	Disentangle <i>theta</i> before splitting with svd.
<code>PurificationTEBD.disentangle_global([pair])</code>	Try global disentangling by determining the maximally entangled pairs of sites.
<code>PurificationTEBD.disentangle_global_nsite([n])</code>	Perform a sweep through the system and disentangle with <code>disentangle_nsite()</code> .
<code>PurificationTEBD.disentangle_nsite(i, n, theta)</code>	Generalization of <code>disentangle()</code> to <i>n</i> sites.
<code>PurificationTEBD.run()</code>	(Real-)time evolution with TEBD (time evolving block decimation).
<code>PurificationTEBD.run_GS()</code>	TEBD algorithm in imaginary time to find the ground state.
<code>PurificationTEBD.run_imaginary(beta)</code>	Run imaginary time evolution to cool down to the given <i>beta</i> .
<code>PurificationTEBD.suzuki_trotter_decomposition(...)</code>	Returns list of necessary steps for the suzuki trotter decomposition.
<code>PurificationTEBD.suzuki_trotter_time_steps(order)</code>	Return time steps of U for the Suzuki Trotter decomposition of desired order.
<code>PurificationTEBD.update(N_steps)</code>	Evolve by <code>N_steps * U_param['dt']</code> .
<code>PurificationTEBD.update_bond(i, U_bond)</code>	Updates the B matrices on a given bond.
<code>PurificationTEBD.update_bond_imag(i, U_bond)</code>	Update a bond with a (possibly non-unitary) <i>U_bond</i> .
<code>PurificationTEBD.update_imag(N_steps)</code>	Perform an update suitable for imaginary time evolution.
<code>PurificationTEBD.update_step(U_idx_dt, odd)</code>	Updates either even <i>or</i> odd bonds in unit cell.

Class Attributes and Properties

<code>PurificationTEBD.TEBD_params</code>	
<code>PurificationTEBD.disent_iterations</code>	For each bond the total number of iterations performed in any <code>Disentangler</code> .
<code>PurificationTEBD.trunc_err_bonds</code>	truncation error introduced on each non-trivial bond.

class `tenpy.algorithms.purification.PurificationTEBD` (*psi*, *model*, *options*)

Bases: `tenpy.algorithms.tebd.Engine`

Time evolving block decimation (TEBD) for purification MPS.

Deprecated since version 0.6.0: Renamed parameter/attribute *TEBD_params* to *options*.

Parameters

- **psi** (`PurificationMPS`) – Initial state to be time evolved. Modified in place.
- **model** (`NearestNeighborModel`) – The model representing the Hamiltonian for which we want to find the ground state.
- **options** (*dict*) – Further optional parameters as described in the following table. Use `verbose=1` to print the used parameters during runtime. See `run()` and `run_GS()` for more details.

`used_disentangler`

The disentangler to be used on the auxiliar indices. Chosen by `get_disentangler()`, called with the TEBD parameter 'disentangle'. Defaults to the trivial disentangler for `options['disentangle']=None`.

Type `Disentangler`

`_disent_iterations`

Number of iterations performed on all bonds, including trivial bonds; lenght *L*.

Type 1D ndarray

`_guess_U_disent`

Same index structure as *self.U*: for each two-site *U* of the physical time evolution the disentangler from the last application. Initialized to identities.

Type list of list of `npc.Array`

`run_imaginary` (*beta*)

Run imaginary time evolution to cool down to the given *beta*.

Note that we don't change the *norm* attribute of the MPS, i.e. normalization is preserved.

Parameters **beta** (*float*) – The inverse temperature $\beta = 1/T$, by which we should cool down. We evolve to the closest multiple of `options['dt']`, see also `evolved_time`.

property `disent_iterations`

For each bond the total number of iterations performed in any `Disentangler`.

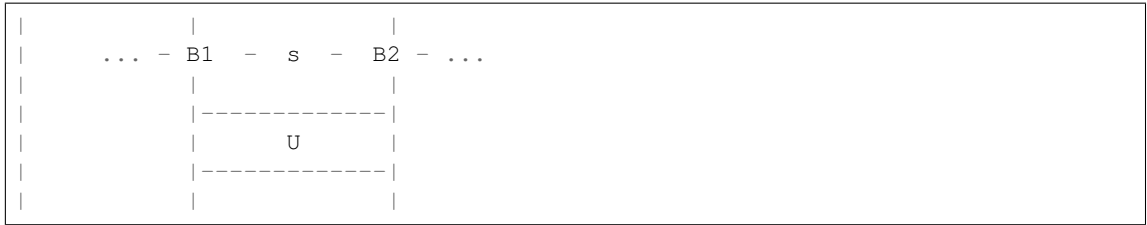
`calc_U` (*order*, *delta_t*, *type_evo*='real', *E_offset*=None)

see `calc_U()`

`update_bond` (*i*, *U_bond*)

Updates the B matrices on a given bond.

Function that updates the B matrices, the bond matrix *s* between and the bond dimension *chi* for bond *i*. This would look something like:

**Parameters**

- **i** (*int*) – Bond index; we update the matrices at sites $i-1$, i .
- **U_bond** (*Array*) – The bond operator which we apply to the wave function. We expect labels 'p0', 'p1', 'p0*', 'p1*' for *U_bond*.

Returns **trunc_err** – The error of the represented state which is introduced by the truncation during this update step.

Return type *TruncationError*

update_bond_imag (*i*, *U_bond*)

Update a bond with a (possibly non-unitary) *U_bond*.

Similar as *update_bond()*; but after the SVD just keep the *A*, *S*, *B* canonical form. In that way, one can sweep left or right without using old singular values, thus preserving the canonical form during imaginary time evolution.

Parameters

- **i** (*int*) – Bond index; we update the matrices at sites $i-1$, i .
- **U_bond** (*Array*) – The bond operator which we apply to the wave function. We expect labels 'p0', 'p1', 'p0*', 'p1*'.

Returns **trunc_err** – The error of the represented state which is introduced by the truncation during this update step.

Return type *TruncationError*

disentangle (*theta*)

Disentangle *theta* before splitting with svd.

For the purification we write $\rho_P = \text{Tr}_Q |\psi_{P,Q}\rangle\langle\psi_{P,Q}|$. Thus, we can actually apply any unitary to the auxiliar *Q* space of $|\psi\rangle$ without changing the result.

Note: We have to apply the *same* unitary to the ‘bra’ and ‘ket’ used for expectation values / correlation functions!

The behaviour of this function is set by *used_disentangler*, which in turn is obtained from *get_disentangler(options['disentangle'])*, see *get_disentangler()* for details on the syntax.

Parameters **theta** (*Array*) – Wave function to disentangle, with legs 'vL', 'vR', 'p0', 'p1', 'q0', 'q1'.

Returns

- **theta_disentangled** (*Array*) – Disentangled *theta*; `npc.tensordot(U, theta, axes=[['q0*', 'q1*'], ['q0', 'q1']])`.

- **U (Array)** – The unitary used to disentangle *theta*, with labels 'q0', 'q1', 'q0*', 'q1*'. If no unitary was found/applied, it might also be None.

disentangle_global (*pair=None*)

Try global disentangling by determining the maximally entangled pairs of sites.

Calculate the mutual information (in the auxiliary space) between two sites and determine where it is maximal. Disentangle these two sites with `disentangle()`

disentangle_global_nsite (*n=2*)

Perform a sweep through the system and disentangle with `disentangle_n_site()`.

Parameters *n* (*int*) – maximal number of sites to disentangle at once.

disentangle_n_site (*i, n, theta*)

Generalization of `disentangle()` to *n* sites.

Simply group left and right *n*/2 physical legs, adjust labels, and apply `disentangle()` to disentangle the central bond. Recursively proceed to disentangle left and right parts afterwards. Scales (for even *n*) as $O(\chi^3 d^n d^{n/2})$.

run()

(Real-)time evolution with TEBD (time evolving block decimation).

option `TEBD.dt: float`

Time step.

option `TEBD.N_steps: int`

Number of time steps *dt* to evolve. The Trotter decompositions of order > 1 are slightly more efficient if more than one step is performed at once.

option `TEBD.order: int`

Order of the algorithm. The total error scales as $O(t * dt^{\text{order}})$.

run_GS()

TEBD algorithm in imaginary time to find the ground state.

Note: It is almost always more efficient (and hence advisable) to use DMRG. This algorithms can nonetheless be used quite well as a benchmark and for comparison.

option `TEBD.delta_tau_list: list`

A list of floats: the timesteps to be used. Choosing a large timestep *delta_tau* introduces large (Trotter) errors, but a too small time step requires a lot of steps to reach $\exp(-\tau H) \rightarrow |\psi_0\rangle\langle\psi_0|$. Therefore, we start with fairly large time steps for a quick time evolution until convergence, and then gradually decrease the time step.

option `TEBD.order: int`

Order of the Suzuki-Trotter decomposition.

option `TEBD.N_steps: int`

Number of steps before measurement can be performed

static `suzuki_trotter_decomposition` (*order, N_steps*)

Returns list of necessary steps for the suzuki trotter decomposition.

We split the Hamiltonian as $H = H_{\text{even}} + H_{\text{odd}} = H[0] + H[1]$. The Suzuki-Trotter decomposition is an approximation $\exp(tH) \approx \prod_{(j,k) \in ST} \exp(d[j]tH[k]) + O(t^{\text{order}+1})$.

Parameters *order* (1, 2, 4, '4_opt') – The desired order of the Suzuki-Trotter decomposition. Order 1 approximation is simply $e^A e^B$. Order 2 is the “leapfrog” $e^{A/2} e^B e^{A/2}$. Order 4 is the fourth-order from [Suzuki1991] (also referenced

in [Schollwoeck2011]), and '4_opt' gives the optimized version of Equ. (30a) in [Barthel2020].

Returns ST_decomposition – Indices j, k of the time-steps $d = \text{suzuki_trotter_time_step}(\text{order})$ and the decomposition of H . They are chosen such that a subsequent application of $\exp(d[j] \pm H[k])$ to a given state $|\psi\rangle$ yields $(\exp(N_steps \pm H[k]) + O(N_steps \pm^{\{\text{order}+1\}})) |\psi\rangle$.

Return type list of (int, int)

static suzuki_trotter_time_steps (order)

Return time steps of U for the Suzuki Trotter decomposition of desired order.

See `suzuki_trotter_decomposition()` for details.

Parameters order (int) – The desired order of the Suzuki-Trotter decomposition.

Returns time_steps – We need $U = \exp(-i H_{\{\text{even/odd}\}} \delta t \pm dt)$ for the dt returned in this list.

Return type list of float

property trunc_err_bonds

truncation error introduced on each non-trivial bond.

update (N_steps)

Evolve by $N_steps * U_{\text{param}}['dt']$.

Parameters N_steps (int) – The number of steps for which the whole lattice should be updated.

Returns trunc_err – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type `TruncationError`

update_imag (N_steps)

Perform an update suitable for imaginary time evolution.

Instead of the even/odd brick structure used for ordinary TEBD, we ‘sweep’ from left to right and right to left, similar as DMRG. Thanks to that, we are actually able to preserve the canonical form.

Parameters N_steps (int) – The number of steps for which the whole lattice should be updated.

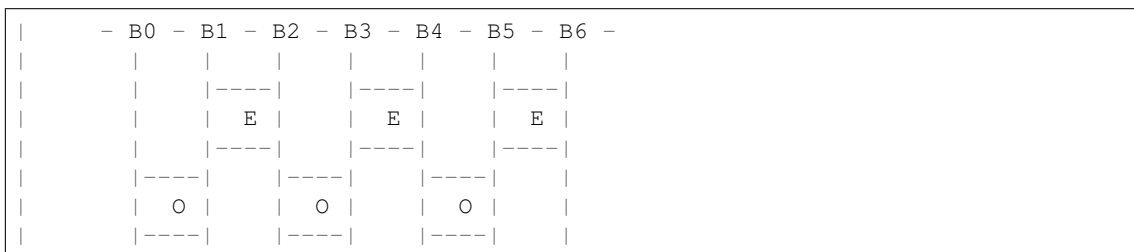
Returns trunc_err – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type `TruncationError`

update_step (U_idx_dt, odd)

Updates either even *or* odd bonds in unit cell.

Depending on the choice of p , this function updates all even (E, odd=False,0) **or** odd (O) (odd=True,1) bonds:



Note that finite boundary conditions are taken care of by having `Us[0] = None`.

Parameters

- **U_idx_dt** (*int*) – Time step index in `self._U`, evolve with `Us[i] = self.U[U_idx_dt][i]` at bond `(i-1, i)`.
- **odd** (*bool/int*) – Indication of whether to update even (`odd=False, 0`) or even (`odd=True, 1`) sites

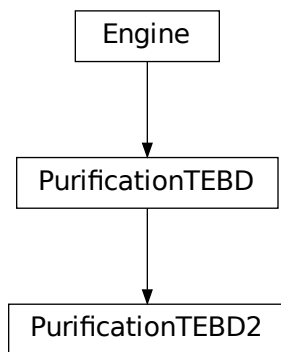
Returns `trunc_err` – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type `TruncationError`

PurificationTEBD2

- full name: `tenpy.algorithms.purification.PurificationTEBD2`
- parent module: `tenpy.algorithms.purification`
- type: class

Inheritance Diagram



Methods

<code>PurificationTEBD2.__init__(psi, model, options)</code>	Initialize self.
<code>PurificationTEBD2.calc_U(order, delta_t[, ...])</code>	see <code>calc_U()</code>
<code>PurificationTEBD2.disentangle(theta)</code>	Disentangle <i>theta</i> before splitting with svd.
<code>PurificationTEBD2.disentangle_global(pair)</code>	Try global disentangling by determining the maximally entangled pairs of sites.

continues on next page

Table 34 – continued from previous page

<code>PurificationTEBD2.disentangle_global_nsite([n])</code>	Perform a sweep through the system and disentangle with <code>disentangle_n_site()</code> .
<code>PurificationTEBD2.disentangle_n_site(i, n, theta)</code>	Generalization of <code>disentangle()</code> to n sites.
<code>PurificationTEBD2.run()</code>	(Real-)time evolution with TEBD (time evolving block decimation).
<code>PurificationTEBD2.run_GS()</code>	TEBD algorithm in imaginary time to find the ground state.
<code>PurificationTEBD2.run_imaginary(beta)</code>	Run imaginary time evolution to cool down to the given <i>beta</i> .
<code>PurificationTEBD2.suzuki_trotter_decomposition(...)</code>	Returns list of necessary steps for the Suzuki Trotter decomposition.
<code>PurificationTEBD2.suzuki_trotter_time_steps(order)</code>	Return time steps of U for the Suzuki Trotter decomposition of desired order.
<code>PurificationTEBD2.update(N_steps)</code>	Evolve by $N_steps * U_param['dt']$.
<code>PurificationTEBD2.update_bond(i, U_bond)</code>	Updates the B matrices on a given bond.
<code>PurificationTEBD2.update_bond_imag(i, U_bond)</code>	Update a bond with a (possibly non-unitary) U_bond .
<code>PurificationTEBD2.update_imag(N_steps)</code>	Perform an update suitable for imaginary time evolution.
<code>PurificationTEBD2.update_step(U_idx_dt, odd)</code>	Updates bonds in unit cell.

Class Attributes and Properties

<code>PurificationTEBD2.TEBD_params</code>	
<code>PurificationTEBD2.disent_iterations</code>	For each bond the total number of iterations performed in any Disentangler.
<code>PurificationTEBD2.trunc_err_bonds</code>	truncation error introduced on each non-trivial bond.

class `tenpy.algorithms.purification.PurificationTEBD2` (*psi, model, options*)

Bases: `tenpy.algorithms.purification.PurificationTEBD`

Similar as `PurificationTEBD`, but perform sweeps instead of brickwall.

Instead of the A-B pattern of even/odd bonds used in TEBD, perform sweeps similar as in DMRG for real-time evolution (similar as `update_imag()` does for imaginary time evolution).

update (N_steps)

Evolve by $N_steps * U_param['dt']$.

Parameters N_steps (*int*) – The number of steps for which the whole lattice should be updated.

Returns `trunc_err` – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type `TruncationError`

update_step (U_idx_dt, odd)

Updates bonds in unit cell.

Depending on the choice of *odd*, perform a sweep to the left or right, updating once per site with a time step given by U_idx_dt .

Parameters

- **U_idx_dt** (*int*) – Time step index in `self._U`, evolve with `Us[i] = self.U[U_idx_dt][i]` at bond `(i-1, i)`.
- **odd** (*bool/int*) – Indication of whether to update even (`odd=False, 0`) or even (`odd=True, 1`) sites

Returns **trunc_err** – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type *TruncationError*

calc_U (*order, delta_t, type_evo='real', E_offset=None*)
see `calc_U()`

property disent_iterations

For each bond the total number of iterations performed in any `Disentangler`.

disentangle (*theta*)

Disentangle *theta* before splitting with `svd`.

For the purification we write $\rho_P = \text{Tr}_Q |\psi_{P,Q}\rangle\langle\psi_{P,Q}|$. Thus, we can actually apply any unitary to the auxiliary *Q* space of $|\psi\rangle$ without changing the result.

Note: We have to apply the *same* unitary to the ‘bra’ and ‘ket’ used for expectation values / correlation functions!

The behaviour of this function is set by `used_disentangler`, which in turn is obtained from `get_disentangler(options['disentangle'])`, see `get_disentangler()` for details on the syntax.

Parameters **theta** (*Array*) – Wave function to disentangle, with legs 'vL', 'vR', 'p0', 'p1', 'q0', 'q1'.

Returns

- **theta_disentangled** (*Array*) – Disentangled *theta*; `npc.tensordot(U, theta, axes=[['q0*', 'q1*'], ['q0', 'q1']])`.
- **U** (*Array*) – The unitary used to disentangle *theta*, with labels 'q0', 'q1', 'q0*', 'q1*'. If no unitary was found/applied, it might also be `None`.

disentangle_global (*pair=None*)

Try global disentangling by determining the maximally entangled pairs of sites.

Calculate the mutual information (in the auxiliary space) between two sites and determine where it is maximal. Disentangle these two sites with `disentangle()`

disentangle_global_nsite (*n=2*)

Perform a sweep through the system and disentangle with `disentangle_n_site()`.

Parameters **n** (*int*) – maximal number of sites to disentangle at once.

disentangle_n_site (*i, n, theta*)

Generalization of `disentangle()` to *n* sites.

Simply group left and right *n/2* physical legs, adjust labels, and apply `disentangle()` to disentangle the central bond. Recursively proceed to disentangle left and right parts afterwards. Scales (for even *n*) as $O(\chi^3 d^n d^{n/2})$.

```
run()
    (Real-)time evolution with TEBD (time evolving block decimation).

    option TEBD.dt: float
        Time step.

    option TEBD.N_steps: int
        Number of time steps  $dt$  to evolve. The Trotter decompositions of order  $> 1$  are slightly more efficient
        if more than one step is performed at once.

    option TEBD.order: int
        Order of the algorithm. The total error scales as  $O(t * dt^{\text{order}})$ .

run_GS()
    TEBD algorithm in imaginary time to find the ground state.
```

Note: It is almost always more efficient (and hence advisable) to use DMRG. This algorithms can nonetheless be used quite well as a benchmark and for comparison.

```
option TEBD.delta_tau_list: list
    A list of floats: the timesteps to be used. Choosing a large timestep  $\delta\tau$  introduces large
    (Trotter) errors, but a too small time step requires a lot of steps to reach  $\exp(-\tau H) \rightarrow |\psi_0\rangle\langle\psi_0|$ .
    Therefore, we start with fairly large time steps for a quick time evolution until
    convergence, and the gradually decrease the time step.

option TEBD.order: int
    Order of the Suzuki-Trotter decomposition.

option TEBD.N_steps: int
    Number of steps before measurement can be performed

run_imaginary(beta)
    Run imaginary time evolution to cool down to the given  $\beta$ .

    Note that we don't change the norm attribute of the MPS, i.e. normalization is preserved.
```

Parameters β (*float*) – The inverse temperature $\beta = 1/T$, by which we should cool down. We evolve to the closest multiple of `options['dt']`, see also `evolved_time`.

```
static suzuki_trotter_decomposition(order, N_steps)
    Returns list of necessary steps for the suzuki trotter decomposition.
```

We split the Hamiltonian as $H = H_{\text{even}} + H_{\text{odd}} = H[0] + H[1]$. The Suzuki-Trotter decomposition is an approximation $\exp(tH) \approx \prod_{(j,k) \in ST} \exp(d[j]tH[k]) + O(t^{\text{order}+1})$.

Parameters order (*1, 2, 4, '4_opt'*) – The desired order of the Suzuki-Trotter decomposition. Order 1 approximation is simply $e^A e^B$. Order 2 is the “leapfrog” $e^{A/2} e^B e^{A/2}$. Order 4 is the fourth-order from [Suzuki1991] (also referenced in [Schollwoeck2011]), and ‘4_opt’ gives the optimized version of Equ. (30a) in [Barthel2020].

Returns ST_decomposition – Indices j, k of the time-steps $d = \text{suzuki_trotter_time_step}(\text{order})$ and the decomposition of H . They are chosen such that a subsequent application of $\exp(d[j]tH[k])$ to a given state $|\psi\rangle$ yields $(\exp(N_steps tH[k]) + O(N_steps t^{\{\text{order}+1\}})) |\psi\rangle$.

Return type list of (*int, int*)

```
static suzuki_trotter_time_steps(order)
    Return time steps of  $U$  for the Suzuki Trotter decomposition of desired order.
```

See `suzuki_trotter_decomposition()` for details.

Parameters `order` (*int*) – The desired order of the Suzuki-Trotter decomposition.

Returns `time_steps` – We need $U = \exp(-i H_{\{\text{even/odd}\}} \text{delta_t} * dt)$ for the dt returned in this list.

Return type list of float

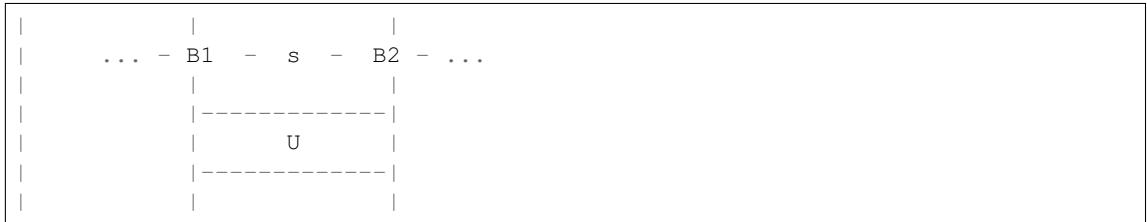
property `trunc_err_bonds`

truncation error introduced on each non-trivial bond.

update_bond (*i*, *U_bond*)

Updates the B matrices on a given bond.

Function that updates the B matrices, the bond matrix *s* between and the bond dimension *chi* for bond *i*. This would look something like:



Parameters

- `i` (*int*) – Bond index; we update the matrices at sites *i*-1, *i*.
- `U_bond` (*Array*) – The bond operator which we apply to the wave function. We expect labels 'p0', 'p1', 'p0*', 'p1*' for *U_bond*.

Returns `trunc_err` – The error of the represented state which is introduced by the truncation during this update step.

Return type *TruncationError*

update_bond_imag (*i*, *U_bond*)

Update a bond with a (possibly non-unitary) *U_bond*.

Similar as `update_bond()`; but after the SVD just keep the *A*, *S*, *B* canonical form. In that way, one can sweep left or right without using old singular values, thus preserving the canonical form during imaginary time evolution.

Parameters

- `i` (*int*) – Bond index; we update the matrices at sites *i*-1, *i*.
- `U_bond` (*Array*) – The bond operator which we apply to the wave function. We expect labels 'p0', 'p1', 'p0*', 'p1*'.

Returns `trunc_err` – The error of the represented state which is introduced by the truncation during this update step.

Return type *TruncationError*

update_imag (*N_steps*)

Perform an update suitable for imaginary time evolution.

Instead of the even/odd brick structure used for ordinary TEBD, we ‘sweep’ from left to right and right to left, similar as DMRG. Thanks to that, we are actually able to preserve the canonical form.

Parameters `N_steps` (*int*) – The number of steps for which the whole lattice should be updated.

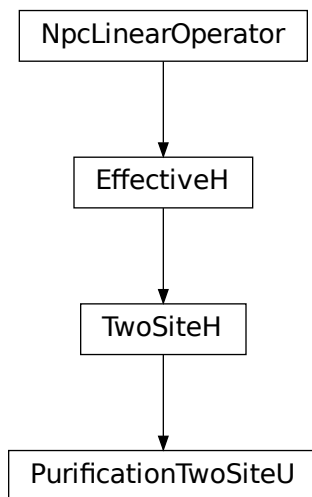
Returns `trunc_err` – The error of the represented state which is introduced due to the truncation during this sequence of update steps.

Return type *TruncationError*

PurificationTwoSiteU

- full name: `tenpy.algorithms.purification.PurificationTwoSiteU`
- parent module: `tenpy.algorithms.purification`
- type: class

Inheritance Diagram



Methods

<code>PurificationTwoSiteU.__init__(env, i0[, ...])</code>	Initialize self.
<code>PurificationTwoSiteU.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>PurificationTwoSiteU.combine_Heff()</code>	Combine LP and RP with W to form LHeff and RHeff.
<code>PurificationTwoSiteU.combine_theta(theta)</code>	Combine the legs of <i>theta</i> , such that it fits to how we combined the legs of <i>self</i> .
<code>PurificationTwoSiteU.matvec(theta)</code>	Apply the effective Hamiltonian to <i>theta</i> .
<code>PurificationTwoSiteU.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

PurificationTwoSiteU.acts_on
PurificationTwoSiteU.length

class `tenpy.algorithms.purification.PurificationTwoSiteU` (*env*, *i0*, *combine=False*,
move_right=True)

Bases: `tenpy.algorithms.mps_common.TwoSiteH`

Variant of *TwoSiteH* suitable for purification.

The MPO gets only applied to the physical legs *p0*, *p1*, the ancilla legs *q0*, *q1* of *theta* are ignored.

combine_Heff ()

Combine LP and RP with W to form LHeff and RHeff.

Combine LP with W0 and RP with W1 to get the effective parts of the Hamiltonian with piped legs.

adjoint ()

Return the hermitian conjugate of *self*.

combine_theta (*theta*)

Combine the legs of *theta*, such that it fits to how we combined the legs of *self*.

Parameters *theta* (*Array*) – Wave function with labels 'vL', 'p0', 'p1', 'vR'

Returns *theta* – Wave function with labels 'vL', 'p0', 'p1', 'vR'

Return type *Array*

matvec (*theta*)

Apply the effective Hamiltonian to *theta*.

Parameters *theta* (*Array*) – Labels: vL, p0, p1, vR if *combine=False*, (vL.p0),
(p1.vR) if *True*

Returns Product of *theta* and the effective Hamiltonian.

Return type *theta Array*

to_matrix ()

Contract *self* to a matrix.

Module description

Algorithms for using Purification.

An example is shown in [Example code purification.py](#).

7.7.7 mpo_evolution

- full name: `tenpy.algorithms.mpo_evolution`
- parent module: `tenpy.algorithms`
- type: module

Classes

ExpMPOEvolution

`ExpMPOEvolution(psi, model, options)`Time evolution of an MPS using the W_I or W_II approximation for $\exp(H \cdot dt)$.

Module description

Time evolution using the WI or WII approximation of the time evolution operator.

7.7.8 network_contractor

- full name: `tenpy.algorithms.network_contractor`
- parent module: `tenpy.algorithms`
- type: module

Functions

`contract(tensor_list[, tensor_names, ...])`

Contract a network of tensors.

`ncon(tensor_list, leg_links, sequence)`Implementation of `ncon.m` for TeNPy Arrays.

contract

- full name: `tenpy.algorithms.network_contractor.contract`
- parent module: `tenpy.algorithms.network_contractor`
- type: function

```
tenpy.algorithms.network_contractor.contract(tensor_list, tensor_names=None,
                                              leg_contractions=None, open_legs=None,
                                              sequence=None)
```

Contract a network of tensors.

Based on the MatLab function `ncon.m` as described in [arXiv:1402.0939](https://arxiv.org/abs/1402.0939).

Parameters

- **tensor_list** (list of `Array`) – The tensors to be contracted.
- **leg_contractions** (list of `[n1, l1, n2, l2]`) – A list of contraction instructions. An entry of `leg_contractions` has the form `[n1, l1, n2, l2]`, where `n1`, `n2` are entries of `tensor_names` and each identify an `Array` in `tensor_list`. `l1`, `l2` are leg labels of

the corresponding *Array*. The instruction implies to contract leg `l1` of tensor `n1` with leg `l2` of tensor `n2`.

- **open_legs** (list of [n1, l1, l]) – A list of instructions for “open” (uncontracted) legs. [n1, l1, l] implies that leg `l1` of tensor `n1` is not contracted and is labelled `l` in the result.
- **tensor_names** (list of str) – A list of names for each tensor, to be used in *leg_contractions* and *open_legs*. The default value is `list(range(len(tensor_list)))`, so that the tensor “names” are `0, 1, 2, ...`
- **sequence** (list of int) – The order in which the *leg_contractions* are to be performed. An entry of `network_contractor.outer_product` indicates performing an outer product. This corresponds to the zero-in-sequence convention of [arXiv:1304.6112](#)

Returns **result** – The number or tensor resulting from the contraction.

Return type `Array | complex`

ncon

- full name: `tenpy.algorithms.network_contractor.ncon`
- parent module: `tenpy.algorithms.network_contractor`
- type: function

`tenpy.algorithms.network_contractor.ncon(tensor_list, leg_links, sequence)`

Implementation of `ncon.m` for TeNPy Arrays.

This function is a python implementation of `ncon.m` ([arXiv:1304.6112](#)) for `tenpy Array`. `contract()` is a wrapper that translates from a more python/tenpy input style

Parameters

- **tensor_list** (list of :class:'Array') – Tensors to be contracted.
- **leg_links** (list of list of int) – Each entry of *leg_links* describes the connectivity of the corresponding tensor in *tensor_list*. Each entry is a list that has an entry for each leg of the corresponding tensor. Values `0, 1, 2, ...` are labels of contracted legs and should appear exactly twice in *leg_links*. Values `-1, -2, -3, ...` are labels of uncontracted legs and indicate the final ordering (`-1` is first axis).
- **sequence** (list of int) – The order in which the contractions are to be performed. An entry of `network_contractor.outer_product` indicates performing an outer product. This corresponds to the zero-in-sequence convention of [arXiv:1304.6112](#)

Returns **result** – The number or tensor resulting from the contraction.

Return type `Array | complex`

Module description

Network Contractor.

A tool to contract a network of multiple tensors.

This is an implementation of ‘NCON: A tensor network contractor for MATLAB’ by Robert N. C. Pfeifer, Glen Evenbly, Sukhwinder Singh, Guifre Vidal, see [arXiv:1402.0939](https://arxiv.org/abs/1402.0939)

`tenpy.algorithms.network_contractor.outer_product = -66666666`
a constant that represents an outer product in the sequence of ncon

Todo:

- **implement or wrap `netcon.m`, a function to find optimal contraction sequences** ([arXiv:1304.6112](https://arxiv.org/abs/1304.6112))
 - improve helpfulness of Warnings
 - `_do_trace`: trace over all pairs of legs at once. need the corresponding `npc` function first.
-

7.7.9 exact_diag

- full name: `tenpy.algorithms.exact_diag`
- parent module: `tenpy.algorithms`
- type: module

Classes

ExactDiag

<code>ExactDiag(model[, charge_sector, sparse, ...])</code>	(Full) exact diagonalization of the Hamiltonian.
---	--

ExactDiag

- full name: `tenpy.algorithms.exact_diag.ExactDiag`
- parent module: `tenpy.algorithms.exact_diag`
- type: class

Inheritance Diagram

ExactDiag

Methods

<code>ExactDiag.__init__(model[, charge_sector, ...])</code>	Initialize self.
<code>ExactDiag.build_full_H_from_bonds()</code>	Calculate <code>self.full_H</code> from <code>self.mpo</code> .
<code>ExactDiag.build_full_H_from_mpo()</code>	Calculate <code>self.full_H</code> from <code>self.mpo</code> .
<code>ExactDiag.exp_H(dt)</code>	Return $U(dt) := \exp(-i H dt)$.
<code>ExactDiag.from_H_mpo(H_MPO, *args, **kwargs)</code>	Wrapper taking directly an MPO instead of a Model.
<code>ExactDiag.full_diagonalization(*args, **kwargs)</code>	Full diagonalization to obtain all eigenvalues and eigenvectors.
<code>ExactDiag.full_to_mps(psi[, canonical_form])</code>	Convert a full state (with a single leg) to an MPS.
<code>ExactDiag.groundstate([charge_sector])</code>	Pick the ground state energy and ground state from <code>self.V</code> .
<code>ExactDiag.matvec(psi)</code>	Allow to use <i>self</i> as <code>LinearOperator</code> for lanczos.
<code>ExactDiag.mps_to_full(mps)</code>	Contract an MPS along the virtual bonds and combine its legs.
<code>ExactDiag.sparse_diag(k, *args, **kwargs)</code>	Call <code>speigs()</code> .

class `tenpy.algorithms.exact_diag.ExactDiag` (*model*, *charge_sector*=None, *sparse*=False, *max_size*=2000000.0)

Bases: `object`

(Full) exact diagonalization of the Hamiltonian.

Parameters

- **model** (`MPOmodel` | `CouplingModel`) – The model which is to be diagonalized.
- **charge_sector** (None | charges) – If not None, project onto the given charge sector.
- **sparse** (*bool*) – If True, don't sort/bunch the LegPipe used to combine the physical legs. This results in array *blocks* with just one entry, requires much more charge data, and is not what *np_conserved* was designed for, so it's not recommended.
- **max_size** (*int*) – The *build_H_** functions will do nothing (but emit a warning) if the total size of the Hamiltonian would be larger than this.

model

The model which is to be diagonalized.

Type `MPOmodel` | `CouplingModel`

chinfo

The nature of the charge (which is the same for all sites).

Type *ChargeInfo*

charge_sector

If not None, we project onto the given charge sector.

Type None | charges

max_size

The `build_H_*` functions will do nothing (but emit a warning) if the total size of the Hamiltonian would be larger than this.

Type int

full_H

The full Hamiltonian to be diagonalized with legs '`p0.p1....`', '`(p0*,p1*....)`' (in that order). None if the `build_H_*` functions haven't been called yet, or if `max_size` would have been exceeded.

Type *Array* | None

E

1D array of eigenvalues.

Type ndarray | None

V

Eigenvectors. First leg 'ps' are physical legs, the second leg 'ps*' corresponds to the eigenvalues.

Type *Array* | None

_sites

The sites in the given order.

Type list of *Site*

_labels_p

The labels use for the physical legs; just ['p0', 'p1', ..., 'p{L-1}'].

Type list or str

_labels_pconj

Just each of `_labels_p` with an *.

Type list or str

_pipe

The pipe from the single physical legs to the full combined leg.

Type *LegPipe*

_pipe_conj

Just `_pipe.conj()`.

Type *LegPipe*

_mask

Bool mask, which of the indices of the pipe are in the desired *charge_sector*.

Type 1D bool ndarray | None

classmethod from_H_mpo (*H_MPO*, *args, **kwargs)

Wrapper taking directly an MPO instead of a Model.

Parameters

- **H_MPO** (MPO) – The MPO representing the Hamiltonian.

- ***args** – Further keyword arguments as for the `__init__` of the class.
- ****kwargs** – Further keyword arguments as for the `__init__` of the class.

build_full_H_from_mpo ()

Calculate `self.full_H` from `self.mpo`.

build_full_H_from_bonds ()

Calculate `self.full_H` from `self.mpo`.

full_diagonalization (*args, **kwargs)

Full diagonalization to obtain all eigenvalues and eigenvectors.

Arguments are given to `eigh`.

groundstate (charge_sector=None)

Pick the ground state energy and ground state from `self.V`.

Parameters `charge_sector` (None | 1D ndarray) – By default (None), consider all charge sectors. Alternatively, give the *qtotal* which the returned state should have.

Returns

- **E0** (float) – Ground state energy (possibly in the given sector).
- **psi0** (Array) – Ground state (possibly in the given sector).

exp_H (dt)

Return $U(dt) := \exp(-i H dt)$.

mps_to_full (mps)

Contract an MPS along the virtual bonds and combine its legs.

Parameters `mps` (MPS) – The MPS to be contracted.

Returns `psi` – The MPO contracted along the virtual bonds.

Return type Array

full_to_mps (psi, canonical_form='B')

Convert a full state (with a single leg) to an MPS.

Parameters

- **psi** (Array) – The state (with a single leg) which should be splitted into an MPS.
- **canonical_from** (Array) – The form in which the MPS will be afterwards.

Returns `mps` – An normalized MPS representation in canonical form.

Return type MPS

matvec (psi)

Allow to use `self` as LinearOperator for lanczos.

Just applies `full_H` to (the first axis of) the given `psi`.

sparse_diag (k, *args, **kwargs)

Call `speigs`.

Module description

Full diagonalization (ED) of the Hamiltonian.

The full diagonalization of a small system is a simple approach to test other algorithms. In case you need the full spectrum, a full diagonalization is often the only way. This module provides functionality to quickly diagonalize the Hamiltonian of a given model. This might be used to obtain the spectrum, the ground state or highly excited states.

Note: Good use of symmetries is crucial to increase the treatable system size. While we can simply use the defined *LegCharge* of a model, we don't make use of any other symmetries like translation symmetry, SU(2) symmetry or inversion symmetries. In other words, this code does not aim to provide state-of-the-art exact diagonalization, but just the ability to diagonalize the defined models for small system sizes without additional extra work.

7.8 linalg

- full name: `tenpy.linalg`
- parent module: `tenpy`
- type: module

Module description

Linear-algebra tools for tensor networks.

Most notably is the module `np_conserved`, which contains everything needed to make use of charge conservation in the context of tensor networks.

Relevant contents of `charges` are imported to `np_conserved`, so you probably won't need to import `charges` directly.

Submodules

<code>np_conserved</code>	A module to handle charge conservation in tensor networks.
<code>charges</code>	Basic definitions of a charge.
<code>svd_robust</code>	(More) robust version of singular value decomposition.
<code>random_matrix</code>	Provide some random matrix ensembles for numpy.
<code>sparse</code>	Providing support for sparse algorithms (using matrix-vector products only).
<code>lanczos</code>	Lanczos algorithm for <code>np_conserved</code> arrays.

7.8.1 np_conserved

- full name: `tenpy.linalg.np_conserved`
- parent module: `tenpy.linalg`
- type: module

Classes

Array

<code>Array</code> (legcharges[, dtype, qtotal, labels])	A multidimensional array (=tensor) for using charge conservation.
--	---

Array

- full name: `tenpy.linalg.np_conserved.Array`
- parent module: `tenpy.linalg.np_conserved`
- type: class

Inheritance Diagram

Array

Methods

<code>Array.__init__(legcharges[, dtype, qtotal, ...])</code>	see <code>help(self)</code>
<code>Array.add_charge</code> (add_legs[, chinfo, qtotal])	Add charges.
<code>Array.add_leg</code> (leg, i[, axis, label])	Add a leg to <i>self</i> , setting the current array as slice for a given index.
<code>Array.add_trivial_leg</code> ([axis, label, qconj])	Add a trivial leg (with just one entry) to <i>self</i> .

continues on next page

Table 44 – continued from previous page

<code>Array.as_completely_blocked()</code>	Gives a version of self which is completely blocked by charges.
<code>Array.astype(dtype[, copy])</code>	Return copy with new dtype, upcasting all blocks in <code>_data</code> .
<code>Array.binary_blockwise(func, other, *args, ...)</code>	Roughly return <code>func(self, other)</code> , block-wise.
<code>Array.change_charge(charge, new_qmod[, ...])</code>	Change the <i>qmod</i> of one charge in <i>chinfo</i> .
<code>Array.combine_legs(combine_legs[, new_axes, ...])</code>	Reshape: combine multiple legs into multiple pipes.
<code>Array.complex_conj()</code>	Return copy which is complex conjugated <i>without</i> conjugating the charge data.
<code>Array.conj([complex_conj, inplace])</code>	Conjugate: complex conjugate data, conjugate charge data.
<code>Array.copy([deep])</code>	Return a (deep or shallow) copy of self.
<code>Array.drop_charge([charge, chinfo])</code>	Drop (one of) the charges.
<code>Array.extend(axis, extra)</code>	Increase the dimension of a given axis, filling the values with zeros.
<code>Array.from_func(func, legcharges[, dtype, ...])</code>	Create an Array from a numpy func.
<code>Array.from_func_square(func, leg[, dtype, ...])</code>	Create an Array from a (numpy) function.
<code>Array.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Array.from_ndarray(data_flat, legcharges[, ...])</code>	convert a flat (numpy) ndarray to an Array.
<code>Array.from_ndarray_trivial(data_flat[, ...])</code>	convert a flat numpy ndarray to an Array with trivial charge conservation.
<code>Array.gauge_total_charge(axis[, newqtotal, ...])</code>	Changes the total charge by adjusting the charge on a certain leg.
<code>Array.get_block(qindices[, insert])</code>	Return the ndarray in <code>_data</code> representing the block corresponding to <i>qindices</i> .
<code>Array.get_leg(label)</code>	Return <code>self.legs[self.get_leg_index(label)]</code> .
<code>Array.get_leg_index(label)</code>	translate a leg-index or leg-label to a leg-index.
<code>Array.get_leg_indices(labels)</code>	Translate a list of leg-indices or leg-labels to leg indices.
<code>Array.get_leg_labels()</code>	Return list of the leg labels, with <i>None</i> for anonymous legs.
<code>Array.has_label(label)</code>	Check whether a given label exists.
<code>Array.iadd_prefactor_other(prefactor, other)</code>	<code>self += prefactor * other</code> for scalar <i>prefactor</i> and <i>Array other</i> .
<code>Array.ibinary_blockwise(func, other, *args, ...)</code>	Roughly <code>self = func(self, other)</code> , block-wise; in place.
<code>Array.iconj([complex_conj])</code>	Wrapper around <code>self.conj()</code> with <code>inplace=True</code> .
<code>Array.idrop_labels([old_labels])</code>	Remove leg labels from self; in place.
<code>Array.iproject(mask, axes)</code>	Applying masks to one or multiple axes; in place.
<code>Array.ipurge_zeros([cutoff, norm_order])</code>	Removes <code>self._data</code> blocks with <i>norm</i> less than cutoff; in place.
<code>Array.replace_label(old_label, new_label)</code>	Replace the leg label <i>old_label</i> with <i>new_label</i> ; in place.
<code>Array.replace_labels(old_labels, new_labels)</code>	Replace leg label <code>old_labels[i]</code> with <code>new_labels[i]</code> ; in place.
<code>Array.is_completely_blocked()</code>	Return bool whether all legs are blocked by charge.
<code>Array.iscale_axis(s[, axis])</code>	Scale with varying values along an axis; in place.
<code>Array.iscale_prefactor(prefactor)</code>	<code>self *= prefactor</code> for scalar <i>prefactor</i> .

continues on next page

Table 44 – continued from previous page

<code>Array.isset_leg_labels(labels)</code>	Set labels for the different axes/legs; in place.
<code>Array.isort_qdata()</code>	(Lexicographically) sort <code>self._qdata</code> ; in place.
<code>Array.iswapaxes(axis1, axis2)</code>	Similar as <code>np.swapaxes</code> ; in place.
<code>Array.itranspose([axes])</code>	Transpose axes like <code>np.transpose</code> ; in place.
<code>Array.iunary_blockwise(func, *args, **kwargs)</code>	Roughly <code>self = f(self)</code> , block-wise; in place.
<code>Array.make_pipe(axes, **kwargs)</code>	Generates a <i>LegPipe</i> for specified axes.
<code>Array.matvec(other)</code>	This function is used by the Lanczos algorithm needed for DMRG.
<code>Array.norm([ord, convert_to_float])</code>	Norm of flattened data.
<code>Array.permute(perm, axis)</code>	Apply a permutation in the indices of an axis.
<code>Array.replace_label(old_label, new_label)</code>	Return a shallow copy with the leg label <i>old_label</i> replaced by <i>new_label</i> .
<code>Array.replace_labels(old_labels, new_labels)</code>	Return a shallow copy with <code>old_labels[i]</code> replaced by <code>new_labels[i]</code> .
<code>Array.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Array.scale_axis(s[, axis])</code>	Same as <code>iscale_axis()</code> , but return a (deep) copy.
<code>Array.sort_legcharge([sort, bunch])</code>	Return a copy with one or all legs sorted by charges.
<code>Array.sparse_stats()</code>	Returns a string detailing the sparse statistics.
<code>Array.split_legs([axes, cutoff])</code>	Reshape: opposite of <code>combine_legs</code> : split (some) legs which are <i>LegPipes</i> .
<code>Array.squeeze([axes])</code>	Like <code>np.squeeze</code> .
<code>Array.take_slice(indices, axes)</code>	Return a copy of <i>self</i> fixing <i>indices</i> along one or multiple <i>axes</i> .
<code>Array.test_sanity()</code>	Sanity check.
<code>Array.to_ndarray()</code>	Convert <i>self</i> to a dense numpy ndarray.
<code>Array.transpose([axes])</code>	Like <code>itranspose()</code> , but on a deep copy.
<code>Array.unary_blockwise(func, *args, **kwargs)</code>	Roughly return <code>func(self)</code> , block-wise.
<code>Array.zeros_like()</code>	Return a copy of <i>self</i> with only zeros as entries, containing no <i>_data</i> .

Class Attributes and Properties

<code>Array.labels</code>	
<code>Array.ndim</code>	Alias for <code>rank</code> or <code>len(self.shape)</code> .
<code>Array.size</code>	The number of dtype-objects stored.
<code>Array.stored_blocks</code>	The number of (non-zero) blocks stored in <i>_data</i> .

class `tenpy.linalg.np_conserved.Array` (*legcharges*, *dtype*=<class 'numpy.float64'>, *qtotal*=None, *labels*=None)

Bases: `object`

A multidimensional array (=tensor) for using charge conservation.

An *Array* represents a multi-dimensional tensor, together with the charge structure of its legs (for abelian charges). Further information can be found in *Charge conservation with np_conserved*.

The default `__init__()` (i.e. `Array(...)`) does not insert any data, and thus yields an *Array* ‘full’ of zeros, equivalent to `zeros()`. Further, new arrays can be created with one of `from_ndarray_trivial()`, `from_ndarray()`, or `from_func()`, and of course by copying/tensordot/svd etc.

In-place methods are indicated by a name starting with *i*. (But *is_completely_blocked* is not inplace...)

Parameters

- **legcharges** (list of *LegCharge*) – The leg charges for each of the legs. The *ChargeInfo* is read out from it.
- **dtype** (*type or string*) – The data type of the array entries. Defaults to `np.float64`.
- **qtotal** (*1D array of QTYPE*) – The total charge of the array. Defaults to 0.
- **labels** (*list of {str | None}*) – Labels associated to each leg, `None` for non-named labels.

rank

The rank or “number of dimensions”, equivalent to `len(shape)`.

Type `int`

shape

The number of indices for each of the legs.

Type `tuple(int)`

dtype

The data type of the entries.

Type `np.dtype`

chinfo

The nature of the charge.

Type *ChargeInfo*

qtotal

The total charge of the tensor.

Type `1D array`

legs

The leg charges for each of the legs.

Type list of *LegCharge*

_labels

Labels for the different legs, `None` for non-labeled legs.

Type list of { `str` | `None` }

_data

The actual entries of the tensor.

Type list of arrays

_qdata

For each of the `_data` entries the qindices of the different legs.

Type `2D array (len(_data), rank), dtype np.intp`

_qdata_sorted

Whether `self._qdata` is lexsorted. Defaults to *True*, but *must* be set to *False* by algorithms changing `_qdata`.

Type `Bool`

test_sanity()

Sanity check.

Raises `ValueErrors`, if something is wrong.

copy (*deep=True*)

Return a (deep or shallow) copy of self.

Both deep and shallow copies will share `chinfo` and the *LegCharges* in `legs`.

In contrast to a deep copy, the shallow copy will also share the tensor entries, namely the *same* instances of `_qdata` and `_data` and `labels` (and other ‘immutable’ properties like the shape or dtype).

Note: Shallow copies are *not* recommended unless you know the consequences! See the following examples illustrating some of the pitfalls.

Examples

Be (very!) careful when making non-deep copies: In the following example, the original *a* is changed if and only if the corresponding block existed in *a* before. `>>> b = a.copy(deep=False) # shallow copy >>> b[1, 2] = 4.`

Other *inplace* operations might have no effect at all (although we don’t guarantee that):

```
>>> a *= 2 # has no effect on `b`
>>> b.iconj() # nor does this change `a`
```

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

Specifically, it saves `chinfo`, `legs`, `dtype` under these names, `qtotal` as "total_charge", `_data` as "blocks", `_qdata` as ":block_inds", the labels in the list-form (as returned by `get_leg_labels()`). Moreover, it saves `rank`, `shape` and `_qdata_sorted` (under the name "block_inds_sorted") as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

classmethod from_ndarray_trivial (*data_flat, dtype=None, labels=None*)

convert a flat numpy ndarray to an Array with trivial charge conservation.

Parameters

- **data_flat** (*array_like*) – The data to be converted to a Array.
- **dtype** (`np.dtype`) – The data type of the array entries. Defaults to dtype of *data_flat*.
- **labels** (*list of {str | None}*) – Labels associated to each leg, None for non-named labels.

Returns *res* – An Array with data of *data_flat*.

Return type *Array*

classmethod from_ndarray (*data_flat*, *legcharges*, *dtype=None*, *qtotal=None*, *cutoff=None*, *labels=None*)
convert a flat (numpy) ndarray to an Array.

Parameters

- **data_flat** (*array_like*) – The flat ndarray which should be converted to a *npc Array*. The shape has to be compatible with *legcharges*.
- **legcharges** (*list of LegCharge*) – The leg charges for each of the legs. The *ChargeInfo* is read out from it.
- **dtype** (`np.dtype`) – The data type of the array entries. Defaults to dtype of *data_flat*.
- **qtotal** (*None | charges*) – The total charge of the new array.
- **cutoff** (*float*) – Blocks with `np.max(np.abs(block)) > cutoff` are considered as zero. Defaults to *QCUTOFF*.
- **labels** (*list of {str | None}*) – Labels associated to each leg, None for non-named labels.

Returns *res* – An Array with data of *data_flat*.

Return type *Array*

See also:

detect_qtotal() used to detect *qtotal* if not given.

classmethod from_func (*func*, *legcharges*, *dtype=None*, *qtotal=None*, *func_args=()*, *func_kwargs={}*, *shape_kw=None*, *labels=None*)
Create an Array from a numpy func.

This function creates an array and fills the blocks *compatible* with the charges using *func*, where *func* is a function returning a *array_like* when given a shape, e.g. one of `np.ones` or `np.random.standard_normal`.

Parameters

- **func** (*callable*) – A function-like object which is called to generate the data blocks. We expect that *func* returns a flat array of the given *shape* convertible to *dtype*. If no *shape_kw* is given, it is called as `func(shape, *func_args, **func_kwargs)`, otherwise as `func(*func_args, `shape_kw`=shape, **func_kwargs)`. *shape* is a tuple of int.
- **legcharges** (*list of LegCharge*) – The leg charges for each of the legs. The *ChargeInfo* is read out from it.
- **dtype** (*None | type | string*) – The data type of the output entries. Defaults to `np.float64`. Defaults to *None*: obtain it from the return value of the function. Note that this argument is not given to *func*, but rather a type conversion is performed afterwards. You might want to set a *dtype* in *func_kwargs* as well.

- **qtotal** (*None* | *charges*) – The total charge of the new array. Defaults to charge 0.
- **func_args** (*iterable*) – Additional arguments given to *func*.
- **func_kwargs** (*dict*) – Additional keyword arguments given to *func*.
- **shape_kw** (*None* | *str*) – If given, the keyword with which shape is given to *func*.
- **labels** (*list of {str | None}*) – Labels associated to each leg, *None* for non-named labels.

Returns *res* – An Array with blocks filled using *func*.

Return type *Array*

classmethod from_func_square (*func*, *leg*, *dtype=None*, *func_args=()*, *func_kwargs={}*,
shape_kw=None, *labels=None*)

Create an Array from a (numpy) function.

This function creates an array and fills the blocks *compatible* with the charges using *func*, where *func* is a function returning a *array_like* when given a shape, e.g. one of `np.ones` or `np.random.standard_normal` or the functions defined in *random_matrix*.

Parameters

- **func** (*callable*) – A function-like object which is called to generate the data blocks. We expect that *func* returns a flat array of the given *shape* convertible to *dtype*. If no *shape_kw* is given, it is called like `func(shape, *fargs, **fkwards)`, otherwise as `func(*fargs, `shape_kw`=shape, **fkwards)`. *shape* is a tuple of int.
- **leg** (*LegCharge*) – The leg charges for the first leg; the second leg is set to `leg.conj()`. The *ChargeInfo* is read out from it.
- **dtype** (*None* | *type* | *string*) – The data type of the output entries. Defaults to *None*: obtain it from the return value of the function. Note that this argument is not given to *func*, but rather a type conversion is performed afterwards. You might want to set a *dtype* in *func_kwargs* as well.
- **func_args** (*iterable*) – Additional arguments given to *func*.
- **func_kwargs** (*dict*) – Additional keyword arguments given to *func*.
- **shape_kw** (*None* | *str*) – If given, the keyword with which shape is given to *func*.
- **labels** (*list of {str | None}*) – Labels associated to each leg, *None* for non-named labels.

Returns *res* – An Array with blocks filled using *func*.

Return type *Array*

zeros_like ()

Return a copy of self with only zeros as entries, containing no *_data*.

property size

The number of dtype-objects stored.

property stored_blocks

The number of (non-zero) blocks stored in *_data*.

property ndim

Alias for *rank* or `len(self.shape)`.

get_leg_index (*label*)

translate a leg-index or leg-label to a leg-index.

Parameters `label` (*int* | *string*) – The leg-index directly or a label (string) set before.

Returns `leg_index` – The index of the label.

Return type `int`

See also:

`get_leg_indices()` calls `get_leg_index` for a list of labels.

`iset_leg_labels()` set the labels of different legs.

get_leg_indices (*labels*)

Translate a list of leg-indices or leg-labels to leg indices.

Parameters `labels` (*iterable of string/int*) – The leg-labels (or directly indices) to be translated in leg-indices.

Returns `leg_indices` – The translated labels.

Return type list of int

See also:

`get_leg_index()` used to translate each of the single entries.

`iset_leg_labels()` set the labels of different legs.

iset_leg_labels (*labels*)

Set labels for the different axes/legs; in place.

Introduction to leg labeling can be found in *Charge conservation with `np_conserved`*.

Parameters `labels` (*iterable (strings | None)*, *len=self.rank*) – One label for each of the legs. An entry can be None for an anonymous leg.

See also:

`get_leg()` translate the labels to indices.

get_leg_labels ()

Return list of the leg labels, with *None* for anonymous legs.

has_label (*label*)

Check whether a given label exists.

get_leg (*label*)

Return `self.legs[self.get_leg_index(label)]`.

Convenient function returning the leg corresponding to a leg label/index.

ireplace_label (*old_label*, *new_label*)

Replace the leg label *old_label* with *new_label*; in place.

replace_label (*old_label*, *new_label*)

Return a shallow copy with the leg label *old_label* replaced by *new_label*.

ireplace_labels (*old_labels*, *new_labels*)

Replace leg label `old_labels[i]` with `new_labels[i]`; in place.

replace_labels (*old_labels*, *new_labels*)

Return a shallow copy with `old_labels[i]` replaced by `new_labels[i]`.

idrop_labels (*old_labels=None*)

Remove leg labels from self; in place.

Parameters *old_labels* (*list of str/int*) – The leg labels/indices for which the label should be removed. By default (None), remove all labels.

sparse_stats ()

Returns a string detailing the sparse statistics.

to_ndarray ()

Convert self to a dense numpy ndarray.

get_block (*qindices, insert=False*)

Return the ndarray in *_data* representing the block corresponding to *qindices*.

Parameters

- **qindices** (*1D array of np.intp*) – The qindices, for which we need to look in *_qdata*.
- **insert** (*bool*) – If True, insert a new (zero) block, if *qindices* is not existent in *self._data*. Otherwise just return None.

Returns *block* – The block in *_data* corresponding to *qindices*. If *insert=False* and there is not block with *qindices*, return *None*.

Return type ndarray | None

Raises **IndexError** – If *qindices* are incompatible with charge and *raise_incomp_q*.

take_slice (*indices, axes*)

Return a copy of self fixing *indices* along one or multiple *axes*.

For a rank-4 Array *A*, *take_slice* (*[i, j], [1, 2]*) is equivalent to *A[:, i, j, :]*.

Parameters

- **indices** (*(iterable of) int*) – The (flat) index for each of the legs specified by *axes*.
- **axes** (*(iterable of) str/int*) – Leg labels or indices to specify the legs for which the indices are given.

Returns *sliced_self* – A copy of self, equivalent to taking slices with indices inserted in axes.

Return type Array

See also:

[*add_leg\(\)*](#) opposite action of inserting a new leg.

add_trivial_leg (*axis=0, label=None, qconj=1*)

Add a trivial leg (with just one entry) to *self*.

Parameters

- **axis** (*int*) – The new leg is inserted before index *axis*.
- **label** (*str | None*) – If not None, use it as label for the new leg.
- **qconj** (*+1 | -1*) – The direction of the new leg.

Returns *extended* – A (possibly) *shallow* copy of self with an additional leg of *ind_len* 1 and charge 0.

Return type Array

add_leg (*leg*, *i*, *axis*=0, *label*=None)

Add a leg to *self*, setting the current array as slice for a given index.

Parameters

- **leg** (LegCharge) – The charge data of the leg to be added.
- **i** (*int*) – Index within the leg for which the data of *self* should be set.
- **axis** (*axis*) – The new leg is inserted before this current axis.
- **label** (*str* | None) – If not None, use it as label for the new leg.

Returns **extended** – A copy of *self* with the new *leg* at axis *axis*, such that `extended.take_slice(i, axis)` returns a copy of *self*.

Return type *Array*

See also:

`take_slice()` opposite action reducing the number of legs.

extend (*axis*, *extra*)

Increase the dimension of a given axis, filling the values with zeros.

Parameters

- **axis** (*int* | *str*) – The axis (or axis-label) to be extended.
- **extra** (LegCharge | *int*) – By what to extend, i.e. the charges to be appended to the leg of *axis*. An *int* stands for extending the length of the array by a single new block of that size with zero charges.

Returns **extended** – A copy of *self* with the specified axis increased.

Return type *Array*

gauge_total_charge (*axis*, *newqtotal*=None, *new_qconj*=None)

Changes the total charge by adjusting the charge on a certain leg.

The total charge is given by finding a nonzero entry [*i*₁, *i*₂, ...] and calculating:

```
qtotal = self.chinfo.make_valid(  
    np.sum([l.get_charge(l.get_qindex(qi)[0])  
           for i, l in zip([i1,i2,...], self.legs)], axis=0))
```

Thus, the total charge can be changed by redefining (= shifting) the LegCharge of a single given leg. This is exactly what this function does.

Parameters

- **axis** (*int* or *string*) – The new leg (index or label), for which the charge is changed.
- **newqtotal** (*charge values*, defaults to 0) – The new total charge.
- **new_qconj** ({+1, -1, None}) – Whether the new LegCharge points inward (+1) or outward (-1) afterwards. By default (None) use the previous `self.legs[leg].qconj`.

Returns **copy** – A shallow copy of *self* with `copy.qtotal == newqtotal` and new `copy.legs[leg]`. The new leg will be a `:class`LegCharge``, even if the old leg was a `LegPipe`.

Return type *Array*

add_charge (*add_legs*, *chinfo=None*, *qtotal=None*)

Add charges.

Parameters

- **add_legs** (iterable of `LegCharge`) – One *LegCharge* for each axis of *self*, to be added to the one in *legs*.
- **chargeinfo** (`ChargeInfo`) – The `ChargeInfo` for all charges; create new if `None`.
- **qtotal** (`None` | *charges*) – The total charge with respect to *add_legs*. If `None`, derive it from non-zero entries of *self*.

Returns **charges_added** – A copy of *self*, where the `LegCharges` *add_legs* where added to *self.legs*. Note that the `LegCharges` are neither bunched or sorted; you might want to use `sort_legcharge()`.

Return type `Array`

drop_charge (*charge=None*, *chinfo=None*)

Drop (one of) the charges.

Parameters

- **charge** (*int* | *str*) – Number or *name* of the charge (within *chinfo*) which is to be dropped. `None` means dropping all charges.
- **chinfo** (`ChargeInfo`) – The `ChargeInfo` with *charge* dropped; create a new one if `None`.

Returns **dropped** – A copy of *self*, where the specified *charge* has been removed. Note that the `LegCharges` are neither bunched or sorted; you might want to use `sort_legcharge()`.

Return type `Array`

change_charge (*charge*, *new_qmod*, *new_name=""*, *chinfo=None*)

Change the *qmod* of one charge in *chinfo*.

Parameters

- **charge** (*int* | *str*) – Number or *name* of the charge (within *chinfo*) which is to be changed. `None` means dropping all charges.
- **new_qmod** (*int*) – The new *qmod* to be set.
- **new_name** (*str*) – The new name of the charge.
- **chinfo** (`ChargeInfo`) – The `ChargeInfo` with *qmod* of *charge* changed; create a new one if `None`.

Returns **changed** – A copy of *self*, where the *qmod* of the specified *charge* has been changed. Note that the `LegCharges` are neither bunched or sorted; you might want to use `sort_legcharge()`.

Return type `Array`

is_completely_blocked ()

Return bool whether all legs are blocked by charge.

sort_legcharge (*sort=True*, *bunch=True*)

Return a copy with one or all legs sorted by charges.

Sort/bunch one or multiple of the `LegCharges`. Legs which are sorted *and* bunched are guaranteed to be blocked by charge.

Parameters

- **sort** (*True | False | list of {True, False, perm}*) – A single bool holds for all legs, default=True. Else, *sort* should contain one entry for each leg, with a bool for sort/don't sort, or a 1D array *perm* for a given permutation to apply to a leg.
- **bunch** (*True | False | list of {True, False}*) – A single bool holds for all legs, default=True. Whether or not to bunch at each leg, i.e. combine contiguous blocks with equal charges.

Returns

- **perm** (*tuple of 1D arrays*) – The permutation applied to each of the legs, such that `cp.to_ndarray() = self.to_ndarray()[np.ix_(*perm)]`.
- **result** (*Array*) – A shallow copy of self, with legs sorted/bunched.

isort_qdata()

(Lexiographically) sort `self._qdata`; in place.

Lexsort `self._qdata` and `self._data` and set `self._qdata_sorted = True`.

make_pipe (*axes, **kwargs*)

Generates a [*LegPipe*](#) for specified axes.

Parameters

- **axes** (*iterable of str|int*) – The leg labels for the axes which should be combined. Order matters!
- ****kwargs** – Additional keyword arguments given to [*LegPipe*](#).

Returns **pipe** – A pipe of the legs specified by axes.

Return type [*LegPipe*](#)

combine_legs (*combine_legs, new_axes=None, pipes=None, qconj=None*)

Reshape: combine multiple legs into multiple pipes. If necessary, transpose before.

Parameters

- **combine_legs** (*(iterable of) iterable of {str|int}*) – Bundles of leg indices or labels, which should be combined into a new output pipes. If multiple pipes should be created, use a list for each new pipe.
- **new_axes** (*None | (iterable of) int*) – The leg-indices, at which the combined legs should appear in the resulting array. Default: for each pipe the position of its first pipe in the original array, (taking into account that some axes are 'removed' by combining). Thus no transposition is performed if *combine_legs* contains only contiguous ranges.
- **pipes** (*None | (iterable of) {LegPipes | None}*) – Optional: provide one or multiple of the resulting [*LegPipes*](#) to avoid overhead of computing new leg pipes for the same legs multiple times. The [*LegPipes*](#) are conjugated, if that is necessary for compatibility with the legs.
- **qconj** (*(iterable of) {+1, -1}*) – Specify whether new created pipes point inward or outward. Defaults to +1. Ignored for given *pipes*, which are not newly calculated.

Returns **reshaped** – A copy of self, with some legs combined into pipes as specified by the arguments.

Return type [*Array*](#)

See also:

`split_legs()` inverse reshaping splitting LegPipes.

Notes

Labels are inherited from `self`. New pipe labels are generated as `'(' + '.'.join(*leglabels) + ')'`. For these new labels, previously unlabeled legs are replaced by `'?#'`, where `#` is the leg-index in the original tensor `self`.

Examples

```
>>> oldarray.iset_leg_labels(['a', 'b', 'c', 'd', 'e'])
>>> c1 = oldarray.combine_legs([1, 2], qconj=-1) # only single output pipe
>>> c1.get_leg_labels()
['a', '(b.c)', 'd', 'e']
```

Indices of `combine_legs` refer to the original array. If transposing is necessary, it is performed automatically:

```
>>> c2 = oldarray.combine_legs([[0, 3], [4, 1]], qconj=[+1, -1]) # two output_
↳ pipes
>>> c2.get_leg_labels()
['(a.d)', 'c', '(e.b)']
>>> c3 = oldarray.combine_legs([['a', 'd'], ['e', 'b']], new_axes=[2, 1],
>>>                               pipes=[c2.legs[0], c2.legs[2]])
>>> c3.get_leg_labels()
['c', '(e.b)', '(a.d)']
```

split_legs (*axes=None, cutoff=0.0*)

Reshape: opposite of `combine_legs`: split (some) legs which are LegPipes.

Reverts `combine_legs()` (except a possibly performed *transpose*). The splitted legs are replacing the LegPipes at their position, see the examples below. Labels are split reverting what was done in `combine_legs()`. `'?#'` labels are replaced with `None`.

Parameters

- **axes** (*iterable of int/str*) – Leg labels or indices determining the axes to split. The corresponding entries in `self.legs` must be LegPipe instances. Defaults to all legs, which are LegPipe instances.
- **cutoff** (*float*) – Splitted data blocks with `np.max(np.abs(block)) > cutoff` are considered as zero. Defaults to 0.

Returns **reshaped** – A copy of `self` where the specified legs are splitted.

Return type *Array*

See also:

`combine_legs()` this is reversed by `split_legs`.

Examples

Given a rank-5 Array `old_array`, you can combine it and split it again:

```

>>> old_array.isset_leg_labels(['a', 'b', 'c', 'd', 'e'])
>>> comb_array = old_array.combine_legs([[0, 3], [2, 4]] )
>>> comb_array.get_leg_labels()
['(a.d)', 'b', '(c.e)']
>>> split_array = comb_array.split_legs([0, 2])
>>> split_array.get_leg_labels()
['a', 'd', 'b', 'c', 'e']

```

as_completely_blocked()

Gives a version of self which is completely blocked by charges.

Functions like `svd()` or `eigh()` require a complete blocking by charges. This can be achieved by encapsulating each leg which is not completely blocked into a `LegPipe` (containing only that single leg). The `LegPipe` will then contain all necessary information to revert the blocking.

Returns

- **encapsulated_axes** (*list of int*) – The leg indices which have been encapsulated into Pipes.
- **blocked_self** (*Array*) – Self (if `len(encapsulated_axes) == 0`) or a copy of self, which is completely blocked.

squeeze (*axes=None*)

Like `np.squeeze`.

If a squeezed leg has non-zero charge, this charge is added to `qtotal`.

Parameters **axes** (*None | (iterable of) {int|str}*) – Labels or indices of the legs which should be ‘squeezed’, i.e. the legs removed. The corresponding legs must be trivial, i.e., have `ind_len 1`.

Returns **squeezed** – A scalar of `self.dtype`, if all axes were squeezed. Else a copy of self with reduced rank as specified by *axes*.

Return type :class:Array | scalar

astype (*dtype, copy=True*)

Return copy with new dtype, upcasting all blocks in `_data`.

Parameters

- **dtype** (*convertible to a np.dtype*) – The new data type. If `None`, deduce the new dtype as common type of `self._data`.
- **copy** (*bool*) – Whether to make a copy of the blocks even if the type didn’t change.

Returns **copy** – Deep copy of self with new dtype.

Return type *Array*

ipurge_zeros (*cutoff=2.220446049250313e-15, norm_order=None*)

Removes `self._data` blocks with *norm* less than *cutoff*; in place.

Parameters

- **cutoff** (*float*) – Blocks with `norm <= cutoff` are removed. defaults to `QCUTOFF`.
- **norm_order** – A valid *ord* argument for `np.linalg.norm`. Default `None` gives the Frobenius norm/2-norm for matrices/everything else. Note that this differs from other methods, e.g. `from_ndarray()`, which use the maximum norm.

iproject (*mask, axes*)

Applying masks to one or multiple axes; in place.

This function is similar as `np.compress` with boolean arrays. For each specified axis, a boolean 1D array `mask` can be given, which chooses the indices to keep.

Warning: Although it is possible to use an 1D int array as a mask, the order is ignored! If you need to permute an axis, use `permute()` or `sort_legcharge()`.

Parameters

- **mask** ((list of) 1D array (bool|int)) – For each axis specified by `axes` a mask, which indices of the axes should be kept. If `mask` is a bool array, keep the indices where `mask` is True. If `mask` is an int array, keep the indices listed in the mask, ignoring the order or multiplicity.
- **axes** ((list of) int | string) – The *i*th entry in this list specifies the axis for the *i*th entry of `mask`, either as an int, or with a leg label. If `axes` is just a single int/string, specify just a single mask.

Returns

- **map_qind** (list of 1D arrays) – The mapping of qindices for each of the specified axes.
- **block_masks** (list of lists of 1D bool arrays) – `block_masks[a][qind]` is a boolean mask which indices to keep in block qindex of `axes[a]`.

permute (*perm*, *axis*)

Apply a permutation in the indices of an axis.

Similar as `np.take` with a 1D array. Roughly equivalent to `res[:, ...] = self[perm, ...]` for the corresponding *axis*. Note: This function is quite slow, and usually not needed!

Parameters

- **perm** (array_like 1D int) – The permutation which should be applied to the leg given by *axis*.
- **axis** (str | int) – A leg label or index specifying on which leg to take the permutation.

Returns `res` – A copy of `self` with leg *axis* permuted, such that `res[i, ...] = self[perm[i], ...]` for *i* along *axis*.

Return type `Array`

See also:

`sort_legcharge()` can also be used to perform a general permutation. Preferable, since it is faster for permutations which don't mix charge blocks.

itranspose (*axes=None*)

Transpose axes like `np.transpose`; in place.

Parameters **axes** (iterable (int|str), len rank | None) – The new order of the axes. By default (None), reverse axes.

transpose (*axes=None*)

Like `itranspose()`, but on a deep copy.

iswapaxes (*axis1*, *axis2*)

Similar as `np.swapaxes`; in place.

iscale_axis (*s*, *axis=-1*)

Scale with varying values along an axis; in place.

Rescale to `new_self[i1, ..., i_axis, ...] = s[i_axis] * self[i1, ..., i_axis, ...]`.

Parameters

- **s** (*1D array*, *len=self.shape[axis]*) – The vector with which the axis should be scaled.
- **axis** (*str/int*) – The leg label or index for the axis which should be scaled.

See also:

[`iproject\(\)`](#) can be used to discard indices for which *s* is zero.

scale_axis (*s*, *axis=-1*)

Same as [`iscale_axis\(\)`](#), but return a (deep) copy.

iunary_blockwise (*func*, **args*, ***kwargs*)

Roughly `self = f(self)`, block-wise; in place.

Applies an unary function *func* to the non-zero blocks in `self._data`.

Note: Assumes implicitly that `func(np.zeros(...), *args, **kwargs)` gives 0, since we don't let *func* act on zero blocks!

Parameters

- **func** (*function*) – A function acting on flat arrays, returning flat arrays. It is called like `new_block = func(block, *args, **kwargs)`.
- ***args** – Additional arguments given to function *after* the block.
- ****kwargs** – Keyword arguments given to the function.

Examples

```
>>> a.iunary_blockwise(np.real) # get real part
>>> a.iunary_blockwise(np.conj) # same data as a.iconj(), but doesn't_
↪ charge conjugate.
```

unary_blockwise (*func*, **args*, ***kwargs*)

Roughly return `func(self)`, block-wise. Copies.

Same as [`iunary_blockwise\(\)`](#), but makes a **shallow** copy first.

iconj (*complex_conj=True*)

Wrapper around `self.conj()` with `inplace=True`.

conj (*complex_conj=True*, *inplace=False*)

Conjugate: complex conjugate data, conjugate charge data.

Conjugate all legs, set negative qtotal.

Labeling: takes 'a' -> 'a*', 'a*' -> 'a' and '(a,(b*,c))' -> '(a*, (b, c*))'

Parameters

- **complex_conj** (*bool*) – Whether the data should be complex conjugated.
- **inplace** (*bool*) – Whether to apply changes to *self*, or to return a *deep* copy.

complex_conj ()

Return copy which is complex conjugated *without* conjugating the charge data.

norm (*ord=None, convert_to_float=True*)

Norm of flattened data.

See `norm()` for details.

ibinary_blockwise (*func, other, *args, **kwargs*)

Roughly `self = func(self, other)`, block-wise; in place.

Applies a binary function ‘block-wise’ to the non-zero blocks of `self._data` and `other._data`, storing result in place. Assumes that *other* is an `Array` as well, with the same shape and compatible legs. If leg labels of *other* and *self* are same up to permutations, *other* gets transposed accordingly before the action.

Note: Assumes implicitly that `func(np.zeros(...), np.zeros(...), *args, **kwargs)` gives 0, since we don’t let *func* act on zero blocks!

Parameters

- **func** (*function*) – Binary function, called as `new_block = func(block_self, block_other, *args, **kwargs)` for blocks (=Numpy arrays) of equal shape.
- **other** (*Array*) – Other Array from which to take blocks. Should have the same leg structure as *self*.
- ***args** – Extra arguments given to *func*.
- ****kwargs** – Extra keyword arguments given to *func*.

Examples

```
>>> a.ibinary_blockwise(np.add, b)  # equivalent to ``a += b``, if ``b`` is
↳an `Array`.
>>> a.ibinary_blockwise(np.max, b)  # overwrites ``a`` to ``a = max(a, b)``
```

binary_blockwise (*func, other, *args, **kwargs*)

Roughly return `func(self, other)`, block-wise. Copies.

Same as `ibinary_blockwise()`, but makes a **shallow** copy first.

matvec (*other*)

This function is used by the Lanczos algorithm needed for DMRG.

It is supposed to calculate the matrix - vector - product for a rank-2 matrix *self* and a rank-1 vector *other*.

iadd_prefactor_other (*prefactor, other*)

`self += prefactor * other` for scalar *prefactor* and `Array` *other*.

Note that we allow the type of *self* to change if necessary. Moreover, if *self* and *other* have the same labels in different order, *other* gets **transposed** before the action.

iscale_prefactor (*prefactor*)

self *= *prefactor* for scalar *prefactor*.

Note that we allow the type of *self* to change if necessary.

Functions

<code>concatenate(arrays[, axis, copy])</code>	Stack arrays along a given axis, similar as <code>np.concatenate</code> .
<code>detect_grid_outer_legcharge(grid, grid_legs)</code>	Derive a <code>LegCharge</code> for a grid used for <code>grid_outer()</code> .
<code>detect_legcharge(flat_array, chargeinfo, ...)</code>	Calculate a missing <i>LegCharge</i> by looking for nonzero entries of a flat array.
<code>detect_qtotal(flat_array, legcharges[, cutoff])</code>	Returns the total charge (w.r.t <i>legs</i>) of first non-zero sector found in <i>flat_array</i> .
<code>diag(s, leg[, dtype, labels])</code>	Returns a square, diagonal matrix of entries <i>s</i> .
<code>eig(a[, sort])</code>	Calculate eigenvalues and eigenvectors for a non-hermitian matrix.
<code>eigh(a[, UPLO, sort])</code>	Calculate eigenvalues and eigenvectors for a hermitian matrix.
<code>eigvals(a[, sort])</code>	Calculate eigenvalues for a hermitian matrix.
<code>eigvalsh(a[, UPLO, sort])</code>	Calculate eigenvalues for a hermitian matrix.
<code>expm(a)</code>	Use <code>scipy.linalg.expm</code> to calculate the matrix exponential of a square matrix.
<code>eye_like(a[, axis, labels])</code>	Return an identity matrix contractible with the leg <i>axis</i> of the <i>Array</i> <i>a</i> .
<code>grid_concat(grid, axes[, copy])</code>	Given an <code>np.array</code> of <code>npc.Arrays</code> , performs a multi-dimensional concatenation along 'axes'.
<code>grid_outer(grid, grid_legs[, qtotal, ...])</code>	Given an <code>np.array</code> of <code>npc.Arrays</code> , return the corresponding higher-dimensional <i>Array</i> .
<code>inner(a, b[, axes, do_conj])</code>	Contract all legs in <i>a</i> and <i>b</i> , return scalar.
<code>norm(a[, ord, convert_to_float])</code>	Norm of flattened data.
<code>ones(legcharges[, dtype, qtotal, labels])</code>	Short-hand for <code>Array.from_func()</code> with function <code>numpy.ones()</code> .
<code>outer(a, b)</code>	Forms the outer tensor product, equivalent to <code>tensordot(a, b, axes=0)</code> .
<code>pinv(a[, cutoff])</code>	Compute the (Moore-Penrose) pseudo-inverse of a matrix.
<code>qr(a[, mode, inner_labels, cutoff])</code>	Q-R decomposition of a matrix.
<code>speigs(a, charge_sector, k, *args, **kwargs)</code>	Sparse eigenvalue decomposition w, v of square <i>a</i> in a given charge sector.
<code>svd(a[, full_matrices, compute_uv, cutoff, ...])</code>	Singular value decomposition of an <i>Array</i> <i>a</i> .
<code>tensordot(a, b[, axes])</code>	Similar as <code>np.tensordot</code> but for <i>Array</i> .
<code>to_iterable_arrays(array_list)</code>	Similar as <code>to_iterable()</code> , but also enclose <code>npc Arrays</code> in a list.
<code>trace(a[, leg1, leg2])</code>	Trace of <i>a</i> , summing over <i>leg1</i> and <i>leg2</i> .
<code>zeros(legcharges[, dtype, qtotal, labels])</code>	Create a <code>npc array</code> full of zeros (with no <code>_data</code>).

concatenate

- full name: `tenpy.linalg.np_conserved.concatenate`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.concatenate` (*arrays*, *axis=0*, *copy=True*)

Stack arrays along a given axis, similar as `np.concatenate`.

Stacks the kind of the array, without sorting/blocking. Labels are inherited from the first array only.

Parameters

- **arrays** (iterable of `Array`) – The arrays to be stacked. They must have the same shape and charge data except on the specified axis.
- **axis** (*int* | *str*) – Leg index or label of the first array. Defines the axis along which the arrays are stacked.
- **copy** (*bool*) – Whether to copy the data blocks.

Returns `stacked` – Concatenation of the given *arrays* along the specified axis.

Return type `Array`

See also:

`Array.sort_legcharge()` can be used to block by charges along the axis.

detect_grid_outer_legcharge

- full name: `tenpy.linalg.np_conserved.detect_grid_outer_legcharge`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.detect_grid_outer_legcharge` (*grid*, *grid_legs*, *qtotal=None*,
qconj=1, *bunch=False*)

Derive a LegCharge for a grid used for `grid_outer()`.

Note: The resulting LegCharge is *not* bunched.

Parameters

- **grid** (array_like of {`Array` | `None`}) – The grid as it will be given to `grid_outer()`.
- **grid_legs** (list of {`LegCharge` | `None`}) – One LegCharge for each dimension of the grid, except for one entry which is `None`. This missing entry is to be calculated.
- **qtotal** (*charge*) – The desired total charge of the array. Defaults to 0.

Returns `new_grid_legs` – A copy of the given *grid_legs* with the `None` replaced by a compatible LegCharge. The new LegCharge is neither bunched nor sorted!

Return type list of LegCharge

See also:

`detect_legcharge()` similar functionality for a flat numpy array instead of a grid.

detect_legcharge

- full name: `tenpy.linalg.np_conserved.detect_legcharge`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.detect_legcharge` (*flat_array*, *chargeinfo*, *legcharges*, *qtotal=None*, *qconj=1*, *cutoff=None*)

Calculate a missing *LegCharge* by looking for nonzero entries of a flat array.

Parameters

- **flat_array** (*ndarray*) – A flat array, in which we look for non-zero entries.
- **chargeinfo** (*ChargeInfo*) – The nature of the charge.
- **legcharges** (list of *LegCharge*) – One *LegCharge* for each dimension of *flat_array*, except for one entry which is *None*. This missing entry is to be calculated.
- **qconj** (*{+1, -1}*) – *qconj* for the new calculated *LegCharge*.
- **qtotal** (*charges*) – Desired total charge of the array. Defaults to zeros.
- **cutoff** (*float*) – Blocks with `np.max(np.abs(block)) > cutoff` are considered as zero. Defaults to `QCUTOFF`.

Returns *new_legcharges* – A copy of the given *legcharges* with the *None* replaced by a compatible *LegCharge*. The new *legcharge* is ‘bunched’, but not sorted!

Return type list of *LegCharge*

See also:

`detect_grid_outer_legcharge()` similar functionality if the flat array is given by a ‘grid’.

`detect_qtotal()` detects the total charge, if all legs are known.

detect_qtotal

- full name: `tenpy.linalg.np_conserved.detect_qtotal`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.detect_qtotal` (*flat_array*, *legcharges*, *cutoff=None*)

Returns the total charge (w.r.t *legs*) of first non-zero sector found in *flat_array*.

Parameters

- **flat_array** (*array*) – The flat numpy array from which you want to detect the charges.
- **legcharges** (list of *LegCharge*) – For each leg the *LegCharge*.
- **cutoff** (*float*) – Blocks with `np.max(np.abs(block)) > cutoff` are considered as zero. Defaults to `QCUTOFF`.

Returns *qtotal* – The total charge for the first non-zero (i.e. > cutoff) charge block.

Return type charge

See also:

`detect_legcharge()` detects the charges of one missing LegCharge if *qtotal* is known.

`detect_grid_outer_legcharge()` similar functionality if the flat array is given by a 'grid'.

diag

- full name: `tenpy.linalg.np_conserved.diag`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.diag(s, leg, dtype=None, labels=None)`

Returns a square, diagonal matrix of entries *s*.

The resulting matrix has legs (`leg, leg.conj()`) and charge 0.

Parameters

- **s** (*scalar* | *1D array*) – The entries to put on the diagonal. If scalar, all diagonal entries are the same.
- **leg** (*LegCharge*) – The first leg of the resulting matrix.
- **dtype** (*None* | *type*) – The data type to be used for the result. By default, use dtype of *s*.
- **labels** (*list of {str | None}*) – Labels associated to each leg, None for non-named labels.

Returns diagonal – A square matrix with diagonal entries *s*.

Return type *Array*

See also:

`Array.scale_axis()` similar as `tensordot(diag(s), ...)`, but faster.

eig

- full name: `tenpy.linalg.np_conserved.eig`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.eig(a, sort=None)`

Calculate eigenvalues and eigenvectors for a non-hermitian matrix.

$W, V = \text{eig}(a)$ yields $aV = V \text{diag}(w)$.

Parameters

- **a** (*Array*) – The hermitian square matrix to be diagonalized.
- **sort** (*{'m>', 'm<', '>', '<', None}*) – How the eigenvalues should be sorted *within* each charge block. Defaults to *None*, which is same as '<'. See `argsort()` for details.

Returns

- **W** (*1D ndarray*) – The eigenvalues, sorted within the same charge blocks according to *sort*.
- **V** (*Array*) – Unitary matrix; $V[:, i]$ is normalized eigenvector with eigenvalue $W[i]$. The first label is inherited from *A*, the second label is 'eig'.

Notes

Requires the legs to be contractible. If a is not blocked by charge, a blocked copy is made via a permutation P , $a = P a P = V' W' (V')^\dagger$. The eigenvectors V are then obtained by the reverse permutation, $V = P^{-1} V'$ such that $A = V W V^\dagger$.

eigh

- full name: `tenpy.linalg.np_conserved.eigh`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.eigh(a, UPLO='L', sort=None)`

Calculate eigenvalues and eigenvectors for a hermitian matrix.

$W, V = \text{eigh}(a)$ yields $a = V \text{diag}(w) V^\dagger$. **Assumes** that a is hermitian, `a.conj().transpose() == a`.

Parameters

- **a** (`Array`) – The hermitian square matrix to be diagonalized.
- **UPLO** (`{'L', 'U'}`) – Whether to take the lower ('L', default) or upper ('U') triangular part of a .
- **sort** (`{'m>', 'm<', '>', '<', None}`) – How the eigenvalues should be sorted *within* each charge block. Defaults to `None`, which is same as '`<`'. See `argsort()` for details.

Returns

- **W** (`1D ndarray`) – The eigenvalues, sorted within the same charge blocks according to *sort*.
- **V** (`Array`) – Unitary matrix; `V[:, i]` is normalized eigenvector with eigenvalue `W[i]`. The first label is inherited from A , the second label is 'eig'.

Notes

Requires the legs to be contractible. If a is not blocked by charge, a blocked copy is made via a permutation P , $a = P a P = V' W' (V')^\dagger$. The eigenvectors V are then obtained by the reverse permutation, $V = P^{-1} V'$ such that $A = V W V^\dagger$.

eigvals

- full name: `tenpy.linalg.np_conserved.eigvals`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.eigvals(a, sort=None)`

Calculate eigenvalues for a hermitian matrix.

Parameters

- **a** (`Array`) – The hermitian square matrix to be diagonalized.
- **sort** (`{'m>', 'm<', '>', '<', None}`) – How the eigenvalues should be sorted *within* each charge block. Defaults to `None`, which is same as '`<`'. See `argsort()` for details.

Returns **W** – The eigenvalues, sorted within the same charge blocks according to *sort*.

Return type 1D ndarray

Notes

The eigenvalues are sorted within blocks of the completely blocked legs.

eigvalsh

- full name: `tenpy.linalg.np_conserved.eigvalsh`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.eigvalsh(a, UPLO='L', sort=None)`
Calculate eigenvalues for a hermitian matrix.

Assumes that *a* is hermitian, `a.conj().transpose() == a`.

Parameters

- **a** (*Array*) – The hermitian square matrix to be diagonalized.
- **UPLO** (`{ 'L', 'U' }`) – Whether to take the lower ('L', default) or upper ('U') triangular part of *a*.
- **sort** (`{ 'm>', 'm<', '>', '<', None }`) – How the eigenvalues should be sorted *within* each charge block. Defaults to `None`, which is same as '`<`'. See `argsort()` for details.

Returns **W** – The eigenvalues, sorted within the same charge blocks according to *sort*.

Return type 1D ndarray

Notes

The eigenvalues are sorted within blocks of the completely blocked legs.

expm

- full name: `tenpy.linalg.np_conserved.expm`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.expm(a)`
Use `scipy.linalg.expm` to calculate the matrix exponential of a square matrix.

Parameters **a** (*Array*) – A square matrix to be exponentiated.

Returns **exp_a** – The matrix exponential `expm(a)`, calculated using `scipy.linalg.expm`. Same legs/labels as *a*.

Return type *Array*

eye_like

- full name: `tenpy.linalg.np_conserved.eye_like`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.eye_like(a, axis=0, labels=None)`
Return an identity matrix contractible with the leg *axis* of the *Array* *a*.

grid_concat

- full name: `tenpy.linalg.np_conserved.grid_concat`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.grid_concat(grid, axes, copy=True)`
Given an np.array of npc.Arrays, performs a multi-dimensional concatenation along ‘axes’.

Similar to `numpy.block()`, but only for uniform blocking.

Stacks the qind of the array, *without* sorting/blocking.

Parameters

- **grid** (array_like of *Array*) – The grid of arrays.
- **axes** (*list of int*) – The axes along which to concatenate the arrays, same len as the dimension of the grid. Concatenate arrays of the *i*th axis of the grid along the axis ‘axes[i]’
- **copy** (*bool*) – Whether the `_data` blocks are copied.

Examples

Assume we have rank 2 Arrays A, B, C, D of shapes (1, 2), (1, 4), (3, 2), (3, 4) sharing the legs of equal sizes. Then the following grid will result in a (1+3, 2+4) shaped array:

```
>>> g = grid_concat([[A, B], [C, D]], axes=[0, 1])
>>> g.shape
(4, 6)
```

If A, B, C, D were rank 4 arrays, with the first and last leg as before, and sharing *common* legs 1 and 2 of dimensions 1, 2, then you would get a rank-4 array:

```
>>> g = grid_concat([[A, B], [C, D]], axes=[0, 3])
>>> g.shape
(4, 1, 2, 6)
```

See also:

Array.sort_legcharge() can be used to block by charges.

grid_outer

- full name: `tenpy.linalg.np_conserved.grid_outer`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.grid_outer` (*grid*, *grid_legs*, *qtotal=None*, *grid_labels=None*)

Given an np.array of npc.Arrays, return the corresponding higher-dimensional Array.

Parameters

- **grid** (array_like of {Array | None}) – The grid gives the first part of the axes of the resulting array. Entries have to have all the same shape and charge-data, giving the remaining axes. None entries in the grid are interpreted as zeros.
- **grid_legs** (list of LegCharge) – One LegCharge for each dimension of the grid along the grid.
- **qtotal** (*charge*) – The total charge of the Array. By default (None), derive it out from a non-trivial entry of the grid.
- **grid_labels** (list of {str | None}) – One label associated to each of the grid axes. None for non-named labels.

Returns **res** – An Array with shape `grid.shape + nontrivial_grid_entry.shape`. Constructed such that `res[idx] == grid[idx]` for any index `idx` of the *grid* the *grid* entry is not trivial (None).

Return type `Array`

See also:

`detect_grid_outer_legcharge()` can calculate one missing LegCharge of the grid.

Examples

A typical use-case for this function is the generation of an MPO. Say you have npc.Arrays `Splus`, `Sminus`, `Sz`, `Id`, each with legs `[phys.conj(), phys]`. Further, you have to define appropriate LegCharges `l_left` and `l_right`. Then one ‘matrix’ of the MPO for a nearest neighbour Heisenberg Hamiltonian could look like:

```
>>> W_mpo = grid_outer([[Id, Splus, Sminus, Sz, None],
...                     [None, None, None, None, J*0.5*Sminus],
...                     [None, None, None, None, J*0.5*Splus],
...                     [None, None, None, None, J*Sz],
...                     [None, None, None, None, Id]],
...                     leg_charges=[l_left, l_right])
>>> W_mpo.shape
(5, 5, 2, 2)
```

inner

- full name: `tenpy.linalg.np_conserved.inner`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.inner(a, b, axes=None, do_conj=False)`

Contract all legs in *a* and *b*, return scalar.

Parameters

- **b** (*a*,) – The arrays for which to calculate the product. Must have same rank, and compatible LegCharges.
- **axes** ((*axes_a*, *axes_b*) | 'range', 'labels') – *axes_a* and *axes_b* specify the legs of *a* and *b*, respectively, which should be contracted. Legs can be specified with leg labels or indices. We contract leg *axes_a*[*i*] of *a* with leg *axes_b*[*i*] of *b*. The default *axes*='range' is equivalent to `(range(rank), range(rank))`. *axes*='labels' is equivalent to either `(a.get_leg_labels(), a.get_leg_labels())` for *do_conj*=True, or to `(a.get_leg_labels(), conj_labels(a.get_leg_labels()))` for *do_conj*=False. In other words, *axes*='labels' requires *a* and *b* to have the same/conjugated labels up to a possible transposition, which is then reverted.
- **do_conj** (*bool*) – If False (Default), ignore it. if True, conjugate *a* before, i.e., return `inner(a.conj(), b, axes)`

Returns inner_product – A scalar (of common dtype of *a* and *b*) giving the full contraction of *a* and *b*.

Return type dtype

norm

- full name: `tenpy.linalg.np_conserved.norm`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.norm(a, ord=None, convert_to_float=True)`

Norm of flattened data.

Equivalent to `np.linalg.norm(a.to_ndarray().flatten(), ord)`.

In contrast to numpy, we don't distinguish between matrices and vectors, but simply calculate the norm for the **flat** (block) data. The usual *ord*-norm is defined as $(\sum_i |a_i|^{ord})^{1/ord}$.

ord	norm
None/'fro'	Frobenius norm (same as 2-norm)
np.inf	<code>max(abs(x))</code>
-np.inf	<code>min(abs(x))</code>
0	<code>sum(a != 0) == np.count_nonzero(x)</code>
other	usual <i>ord</i> -norm

Parameters

- **a** (*Array* | *np.ndarray*) – The array of which the norm should be calculated.

- **ord** – The order of the norm. See table above.
- **convert_to_float** – Convert integer to float before calculating the norm, avoiding int overflow.

Returns **norm** – The norm over the *flat* data of the array.

Return type `float`

ones

- full name: `tenpy.linalg.np_conserved.ones`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.ones` (*legcharges*, *dtype*=<class 'numpy.float64'>, *qtotal*=None, *labels*=None)

Short-hand for `Array.from_func()` with function `numpy.ones()`.

Warning: For non-trivial charges, only blocks with compatible charges are filled with ones!

outer

- full name: `tenpy.linalg.np_conserved.outer`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.outer` (*a*, *b*)

Forms the outer tensor product, equivalent to `tensordot(a, b, axes=0)`.

Labels are inherited from *a* and *b*. In case of a collision (same label in both *a* and *b*), they are both dropped.

Parameters **b** (*a*,) – The arrays for which to form the product.

Returns

c –

Array of rank `a.rank + b.rank` such that (for `Ra = a.rank`; `Rb = b.rank`):

```
c[i_1, ..., i_Ra, j_1, ... j_R] = a[i_1, ..., i_Ra] * b[j_1, ..., j_
↪rank_b]
```

Return type `Array`

pinv

- full name: `tenpy.linalg.np_conserved.pinv`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.pinv(a, cutoff=1e-15)`

Compute the (Moore-Penrose) pseudo-inverse of a matrix.

Equivalent to the following procedure: Perform a SVD, $U, S, V^H = \text{svd}(a, \text{cutoff}=\text{cutoff})$ with a *cutoff* > 0, calculate $P = U * \text{diag}(1/S) * V^H$ (with $*$ denoting `tensor.dot`) and return `P.conj().transpose()`.

Parameters

- **a** ((M, N) *Array*) – Matrix to be pseudo-inverted.
- **cutoff** (*float*) – Cutoff for small singular values, as given to `svd()`. (Note: different convention than numpy.)

Returns **B** – The pseudo-inverse of *a*.

Return type (N, M) *Array*

qr

- full name: `tenpy.linalg.np_conserved.qr`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.qr(a, mode='reduced', inner_labels=[None, None], cutoff=None)`

Q-R decomposition of a matrix.

Decomposition such that $A == \text{npc.tensor.dot}(q, r, \text{axes}=1)$ up to numerical rounding errors.

Parameters

- **a** (*Array*) – A square matrix to be exponentiated, shape (M, N).
- **mode** ('reduced', 'complete') – 'reduced': return *q* and *r* with shapes (M,K) and (K,N), where $K=\min(M,N)$ 'complete': return *q* with shape (M,M).
- **inner_labels** ([{*str*|None}, {*str*|None}]) – The first label is used for *Q*. `legs[1]`, the second for *R*. `legs[0]`.
- **cutoff** (None or float) – If not None, discard linearly dependent vectors to given precision, which might reduce *K* of the 'reduced' mode even further.

Returns

- **q** (*Array*) – If *mode* is 'complete', a unitary matrix. For *mode* 'reduced' such that Otherwise such that $q_{j,i}^* q_{j,k} = \delta_{i,k}$
- **r** (*Array*) – Upper triangular matrix if both legs of *A* are sorted by charges; Otherwise a simple transposition (performed when sorting by charges) brings it to upper triangular form.

speigs

- full name: `tenpy.linalg.np_conserved.speigs`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.speigs(a, charge_sector, k, *args, **kwargs)`

Sparse eigenvalue decomposition w, v of square a in a given charge sector.

Finds k right eigenvectors (chosen by `kwargs['which']`) in a given charge sector, `tensor_dot(A, V[i], axes=1) = W[i] * V[i]`.

Parameters

- **a** (`Array`) – A square array with contractible legs and vanishing total charge.
- **charge_sector** (`charges`) – $ndim$ charges to select the block.
- **k** (`int`) – How many eigenvalues/vectors should be calculated. If the block of `charge_sector` is smaller than k , k may be reduced accordingly.
- ***args** – Additional arguments given to `scipy.sparse.linalg.eigs`.
- ****kwargs** – Additional keyword arguments given to `scipy.sparse.linalg.eigs`.

Returns

- **W** (`ndarray`) – k (or less) eigenvalues
- **V** (list of `Array`) – k (or less) right eigenvectors of A with total charge `charge_sector`. Note that when interpreted as a matrix, this is the transpose of what `np.eigs` normally gives.

svd

- full name: `tenpy.linalg.np_conserved.svd`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.svd(a, full_matrices=False, compute_uv=True, cutoff=None, qtotal_LR=[None, None], inner_labels=[None, None], inner_qconj=1)`

Singular value decomposition of an Array a .

Factorizes $U, S, VH = \text{svd}(a)$, such that $a = U * \text{diag}(S) * VH$ (where $*$ stands for a `tensor_dot()` and `diag` creates an correctly shaped Array with S on the diagonal). For a non-zero `cutoff` this holds only approximately.

There is a gauge freedom regarding the charges, see also `Array.gauge_total_charge()`. We ensure contractibility by setting `U.legs[1] = VH.legs[0].conj()`. Further, we gauge the `LegCharge` such that U and V have the desired `qtotal_LR`.

Parameters

- **a** (`Array`, shape (M, N)) – The matrix to be decomposed.
- **full_matrices** (`bool`) – If `False` (default), U and V have shapes (M, K) and (K, N) , where $K = \text{len}(S)$. If `True`, U and V are full square unitary matrices with shapes (M, M) and (N, N) . Note that the arrays are not directly contractible in that case; `diag(S)` would need to be a rectangular (M, N) matrix.

- **compute_uv** (*bool*) – Whether to compute and return U and V .
- **cutoff** (*None* | *float*) – Keep only singular values which are (strictly) greater than *cutoff*. (Then the factorization holds only approximately). If *None* (default), ignored.
- **qtotal_LR** (*[{charges|None}, {charges|None}]*) – The desired *qtotal* for U and VH , respectively. [*None*, *None*] (Default) is equivalent to [*None*, *a.qtotal*]. A single *None* entry is replaced the unique charge satisfying the requirement $U.qtotal + VH.qtotal = a.qtotal \pmod{qmod}$.
- **inner_labels_LR** (*[{str|None}, {str|None}]*) – The first label corresponds to $U.legs[1]$, the second to $VH.legs[0]$.
- **inner_qconj** (*{+1, -1}*) – Direction of the charges for the new leg. Default +1. The new *LegCharge* is constructed such that $VH.legs[0].qconj = qconj$.

Returns

- **U** (*Array*) – Matrix with left singular vectors as columns. Shape (M , M) or (M , K) depending on *full_matrices*.
- **S** (*1D ndarray*) – The singular values of the array. If no *cutoff* is given, it has length $\min(M, N)$.
- **VH** (*Array*) – Matrix with right singular vectors as rows. Shape (N , N) or (K , N) depending on *full_matrices*.

tensor_dot

- full name: `tenpy.linalg.np_conserved.tensor_dot`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.tensor_dot(a, b, axes=2)`

Similar as `np.tensor_dot` but for *Array*.

Builds the tensor product of a and b and sums over the specified axes. Does not require complete blocking of the charges.

Labels are inherited from a and b . In case of a collision (= the same label would be inherited from a and b after the contraction), both labels are dropped.

Detailed implementation notes are available in the doc-string of `_tensor_dot_worker()`.

Parameters

- **b** (a ,) – The first and second *np* Array for which axes are to be contracted.
- **axes** (*((axes_a, axes_b) | int)*) – A single integer is equivalent to `(range(-axes, 0), range(axes))`. Alternatively, *axes_a* and *axes_b* specify the legs of a and b , respectively, which should be contracted. Legs can be specified with leg labels or indices. Contract leg `axes_a[i]` of a with leg `axes_b[i]` of b .

Returns **a_dot_b** – The tensorproduct of a and b , summed over the specified axes. Returns a scalar in case of a full contraction.

Return type *Array*

to_iterable_arrays

- full name: `tenpy.linalg.np_conserved.to_iterable_arrays`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.to_iterable_arrays(array_list)`
 Similar as `to_iterable()`, but also enclose npc Arrays in a list.

trace

- full name: `tenpy.linalg.np_conserved.trace`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.trace(a, leg1=0, leg2=1)`
 Trace of a , summing over $leg1$ and $leg2$.

Requires that the contracted legs are contractible (i.e. have opposite charges). Labels are inherited from a .

Parameters `leg2 (leg1,)` – The leg label or index for the two legs which should be contracted (i.e. summed over).

Returns `traced` – A scalar if $a.rank == 2$, else an `Array` of rank $a.rank - 2$. Equivalent to `sum([a.take_slice([i, i], [leg1, leg2]) for i in range(a.shape[leg1])])`.

Return type `Array` | $a.dtype$

zeros

- full name: `tenpy.linalg.np_conserved.zeros`
- parent module: `tenpy.linalg.np_conserved`
- type: function

`tenpy.linalg.np_conserved.zeros(legcharges, dtype=<class 'numpy.float64'>, qtotal=None, labels=None)`
 Create a npc array full of zeros (with no `_data`).

This is just a wrapper around `Array(...)`, detailed documentation can be found in the class doc-string of `Array`.

Module description

A module to handle charge conservation in tensor networks.

A detailed introduction to this module (including notations) can be found in *Charge conservation with `np_conserved`*.

This module `np_conserved` implements a class `Array` designed to make use of charge conservation in tensor networks. The idea is that the `Array` class is used in a fashion very similar to the `numpy.ndarray`, e.g you can call the functions `tensordot()` or `svd()` (of this module) on them. The structure of the algorithms (as DMRG) is thus the same as with basic numpy ndarrays.

Internally, an *Array* saves charge meta data to keep track of blocks which are nonzero. All possible operations (e.g. `tensordot`, `svd`, ...) on such arrays preserve the total charge structure. In addition, these operations make use of the charges to figure out which of the blocks it has to use/combine - this is the basis for the speed-up.

```
tenpy.linalg.np_conserved.QCUTOFF = 2.220446049250313e-15
```

A cutoff to ignore machine precision rounding errors when determining charges

```
tenpy.linalg.np_conserved.QTYPE = <class 'numpy.int64'>
```

the type used for charges

Overview

Classes

<i>Array</i> (legcharges[, dtype, qtotal, labels])	A multidimensional array (=tensor) for using charge conservation.
<i>ChargeInfo</i> ([mod, names])	Meta-data about the charge of a tensor.
<i>LegCharge</i> (chargeinfo, slices, charges[, qconj])	Save the charge data associated to a leg of a tensor.
<i>LegPipe</i> (legs[, qconj, sort, bunch])	A <i>LegPipe</i> combines multiple legs of a tensor to one.

Array creation

<i>Array.from_ndarray_trivial</i> (data_flat[, ...])	convert a flat numpy ndarray to an Array with trivial charge conservation.
<i>Array.from_ndarray</i> (data_flat, legcharges[, ...])	convert a flat (numpy) ndarray to an Array.
<i>Array.from_func</i> (func, legcharges[, dtype, ...])	Create an Array from a numpy func.
<i>Array.from_func_square</i> (func, leg[, dtype, ...])	Create an Array from a (numpy) function.
<i>zeros</i> (legcharges[, dtype, qtotal, labels])	Create a npc array full of zeros (with no <code>_data</code>).
<i>eye_like</i> (a[, axis, labels])	Return an identity matrix contractible with the leg <i>axis</i> of the <i>Array</i> <i>a</i> .
<i>diag</i> (s, leg[, dtype, labels])	Returns a square, diagonal matrix of entries <i>s</i> .

Concatenation

<i>concatenate</i> (arrays[, axis, copy])	Stack arrays along a given axis, similar as <code>np.concatenate</code> .
<i>grid_concat</i> (grid, axes[, copy])	Given an np.array of npc.Arrays, performs a multi-dimensional concatenation along 'axes'.
<i>grid_outer</i> (grid, grid_legs[, qtotal, ...])	Given an np.array of npc.Arrays, return the corresponding higher-dimensional Array.

Detecting charges of flat arrays

<code>detect_qtotal(flat_array, legcharges[, cutoff])</code>	Returns the total charge (w.r.t <i>legs</i>) of first non-zero sector found in <i>flat_array</i> .
<code>detect_legcharge(flat_array, chargeinfo, ...)</code>	Calculate a missing <i>LegCharge</i> by looking for nonzero entries of a flat array.
<code>detect_grid_outer_legcharge(grid, grid_legs)</code>	Derive a <i>LegCharge</i> for a grid used for <i>grid_outer()</i> .

Contraction of some legs

<code>tensordot(a, b[, axes])</code>	Similar as <code>np.tensordot</code> but for <i>Array</i> .
<code>outer(a, b)</code>	Forms the outer tensor product, equivalent to <code>tensordot(a, b, axes=0)</code> .
<code>inner(a, b[, axes, do_conj])</code>	Contract all legs in <i>a</i> and <i>b</i> , return scalar.
<code>trace(a[, leg1, leg2])</code>	Trace of <i>a</i> , summing over <i>leg1</i> and <i>leg2</i> .

Linear algebra

<code>svd(a[, full_matrices, compute_uv, cutoff, ...])</code>	Singular value decomposition of an <i>Array a</i> .
<code>pinv(a[, cutoff])</code>	Compute the (Moore-Penrose) pseudo-inverse of a matrix.
<code>norm(a[, ord, convert_to_float])</code>	Norm of flattened data.
<code>qr(a[, mode, inner_labels, cutoff])</code>	Q-R decomposition of a matrix.
<code>expm(a)</code>	Use <code>scipy.linalg.expm</code> to calculate the matrix exponential of a square matrix.

Eigen systems

<code>eigh(a[, UPLO, sort])</code>	Calculate eigenvalues and eigenvectors for a hermitian matrix.
<code>eig(a[, sort])</code>	Calculate eigenvalues and eigenvectors for a non-hermitian matrix.
<code>eigvalsh(a[, UPLO, sort])</code>	Calculate eigenvalues for a hermitian matrix.
<code>eigvals(a[, sort])</code>	Calculate eigenvalues for a hermitian matrix.
<code>speigs(a, charge_sector, k, *args, **kwargs)</code>	Sparse eigenvalue decomposition w, v of square <i>a</i> in a given charge sector.

7.8.2 charges

- full name: `tenpy.linalg.charges`
- parent module: `tenpy.linalg`
- type: module

Classes



<i>ChargeInfo</i> ([mod, names])	Meta-data about the charge of a tensor.
<i>LegCharge</i> (chargeinfo, slices, charges[, qconj])	Save the charge data associated to a leg of a tensor.
<i>LegPipe</i> (legs[, qconj, sort, bunch])	A <i>LegPipe</i> combines multiple legs of a tensor to one.

ChargeInfo

- full name: `tenpy.linalg.charges.ChargeInfo`
- parent module: `tenpy.linalg.charges`
- type: class

Inheritance Diagram



Methods

<code>ChargeInfo.__init__((mod, names))</code>	Initialize self.
<code>ChargeInfo.add(chinfos)</code>	Create a <i>ChargeInfo</i> combining multiple charges.
<code>ChargeInfo.change(chinfo, charge, new_qmod)</code>	Change the <i>qmod</i> of a given charge.
<code>ChargeInfo.check_valid(charges)</code>	Check, if <i>charges</i> has all entries as expected from self.mod.
<code>ChargeInfo.drop(chinfo[, charge])</code>	Remove a charge from a <i>ChargeInfo</i> .
<code>ChargeInfo.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>ChargeInfo.make_valid([charges])</code>	Take charges modulo self.mod.
<code>ChargeInfo.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>ChargeInfo.test_sanity()</code>	Sanity check, raises ValueErrors, if something is wrong.

Class Attributes and Properties

<code>ChargeInfo.mod</code>	Modulo how much each of the charges is taken.
<code>ChargeInfo.qnumber</code>	The number of charges.

class `tenpy.linalg.charges.ChargeInfo` (*mod*=[], *names*=None)

Bases: `object`

Meta-data about the charge of a tensor.

Saves info about the nature of the charge of a tensor. Provides *make_valid()* for taking modulo *m*.

(This class is implemented in *tenpy.linalg.charges* but also imported in *tenpy.linalg.np_conserved* for convenience.)

Parameters

- **mod** (*iterable of QTYPE*) – The len gives the number of charges, *qnumber*. For each charge one entry *m*: the charge is conserved modulo *m*. Defaults to trivial, i.e., no charge.
- **names** (*list of str*) – Descriptive names for the charges. Defaults to `[]*qnumber`.

names

A descriptive name for each of the charges. May have “” entries.

Type list of strings

_mask

mask (*mod* == 1), to speed up *make_valid* in pure python.

Type 1D array bool

_mod_masked

Equivalent to `self.mod[self._mask_mod1]`

Type 1D array QTYPE

_qnumber, _mod

Storage of *qnumber* and *mod*.

Notes

Instances of this class can (should) be shared between different *LegCharge* and *Array*'s.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

It stores the *names* under the path "names", and *mod* as dataset "U1_ZN".

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (:class`Group`) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

The "U1_ZN" dataset is mandatory, 'names' are optional.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

classmethod add (*chinfos*)

Create a *ChargeInfo* combining multiple charges.

Parameters *chinfos* (iterable of *ChargeInfo*) – *ChargeInfo* instances to be combined into a single one (in the given order).

Returns *chinfo* – *ChargeInfo* combining all the given charges.

Return type *ChargeInfo*

classmethod drop (*chinfo*, *charge=None*)

Remove a charge from a *ChargeInfo*.

Parameters

- **chinfo** (*ChargeInfo*) – The *ChargeInfo* from where to drop/remove a charge.
- **charge** (*int* | *str*) – Number or *name* of the charge (within *chinfo*) which is to be dropped. None means dropping all charges.

Returns *chinfo* – *ChargeInfo* where the specified charge is dropped.

Return type *ChargeInfo*

classmethod change (*chinfo*, *charge*, *new_qmod*, *new_name=""*)

Change the *qmod* of a given charge.

Parameters

- **chinfo** (*ChargeInfo*) – The *ChargeInfo* for which *qmod* of *charge* should be changed.

- **new_qmod** (*int*) – The new *qmod* to be set.
- **new_name** (*str*) – The new name of the charge.

Returns **chinfo** – ChargeInfo where *qmod* of the specified charge was changed.

Return type *ChargeInfo*

test_sanity ()

Sanity check, raises ValueErrors, if something is wrong.

property qnumber

The number of charges.

property mod

Modulo how much each of the charges is taken.

1 for a $U(1)$ charge, N for a Z_N symmetry.

make_valid (*charges=None*)

Take charges modulo self.mod.

Parameters **charges** (*array_like or None*) – 1D or 2D array of charges, last dimension *self.qnumber* None defaults to trivial charges `np.zeros(qnumber, dtype=QTYPE)`.

Returns A copy of *charges* taken modulo *mod*, but with $x \% 1 := x$

Return type *charges*

check_valid (*charges*)

Check, if *charges* has all entries as expected from self.mod.

Parameters **charges** (*2D ndarray QTYPE_t*) – Charge values to be checked.

Returns **res** – True, if all $0 \leq \text{charges} \leq \text{self.mod}$ (wherever $\text{self.mod} \neq 1$)

Return type *bool*

LegCharge

- full name: `tenpy.linalg.charges.LegCharge`
- parent module: `tenpy.linalg.charges`
- type: class

Inheritance Diagram

LegCharge

Methods

<code>LegCharge.__init__(chargeinfo, slices, charges)</code>	Initialize self.
<code>LegCharge.bunch()</code>	Return a copy with bunched self.charges: form blocks for contiguous equal charges.
<code>LegCharge.charge_sectors()</code>	Return unique rows of self.charges.
<code>LegCharge.conj()</code>	Return a (shallow) copy with opposite <code>self.qconj</code> .
<code>LegCharge.copy()</code>	Return a (shallow) copy of self.
<code>LegCharge.extend(extra)</code>	Return a new <i>LegCharge</i> , which extends self with further charges.
<code>LegCharge.flip_charges_qconj()</code>	Return a copy with both negative <i>qconj</i> and <i>charges</i> .
<code>LegCharge.from_add_charge(legs[, chargeinfo])</code>	Add the (independent) charges of two or more legs to get larger <i>qnumber</i> .
<code>LegCharge.from_change_charge(leg, charge, ...)</code>	Remove a charge from a LegCharge.
<code>LegCharge.from_drop_charge(leg[, charge, ...])</code>	Remove a charge from a LegCharge.
<code>LegCharge.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>LegCharge.from_qdict(chargeinfo, qdict[, qconj])</code>	Create a LegCharge from qdict form.
<code>LegCharge.from_qflat(chargeinfo, qflat[, qconj])</code>	Create a LegCharge from qflat form.
<code>LegCharge.from_qind(chargeinfo, slices, charges)</code>	Just a wrapper around <code>self.__init__()</code> , see class docstring for parameters.
<code>LegCharge.from_trivial(ind_len[, ...])</code>	Create trivial (<i>qnumber</i> =0) LegCharge for given len of indices <i>ind_len</i> .
<code>LegCharge.get_block_sizes()</code>	Return the sizes of the individual blocks.
<code>LegCharge.get_charge(qindex)</code>	Return charge <code>self.charges[qindex] * self.qconj</code> for a given <i>qindex</i> .
<code>LegCharge.get_qindex(flat_index)</code>	Find <i>qindex</i> containing a flat index.
<code>LegCharge.get_qindex_of_charges(charges)</code>	Return the slice selecting the block for given charge values.
<code>LegCharge.get_slice(qindex)</code>	Return slice selecting the block for a given <i>qindex</i> .
<code>LegCharge.is_blocked()</code>	Returns whether self is blocked, i.e.
<code>LegCharge.is_bunched()</code>	Checks whether <code>bunch()</code> would change something.
<code>LegCharge.is_sorted()</code>	Returns whether <i>self.charges</i> is sorted lexicographically.
<code>LegCharge.perm_flat_from_perm_qind(perm_qind)</code>	Convert a permutation of <i>qind</i> (acting on self) into a flat permutation.
<code>LegCharge.perm_qind_from_perm_flat(perm_flat)</code>	Convert flat permutation into <i>qind</i> permutation.
<code>LegCharge.project(mask)</code>	Return copy keeping only the indices specified by <i>mask</i> .
<code>LegCharge.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>LegCharge.sort([bunch])</code>	Return a copy of <i>self</i> sorted by charges (but maybe not bunched).
<code>LegCharge.test_contractible(other)</code>	Raises a <code>ValueError</code> if charges are incompatible for contraction with <i>other</i> .
<code>LegCharge.test_equal(other)</code>	Test if charges are <i>equal</i> including <i>qconj</i> .
<code>LegCharge.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>LegCharge.to_qdict()</code>	Return charges in <i>qdict</i> form.
<code>LegCharge.to_qflat()</code>	Return charges in <i>qflat</i> form.

class `tenpy.linalg.charges.LegCharge` (*chargeinfo, slices, charges, qconj=1*)

Bases: `object`

Save the charge data associated to a leg of a tensor.

This class is more or less a wrapper around a 2D numpy array *charges* and a 1D array *slices*. See *Charge conservation with np_conserved* for more details.

(This class is implemented in `tenpy.linalg.charges` but also imported in `tenpy.linalg.np_conserved` for convenience.)

Parameters

- **chargeinfo** (*ChargeInfo*) – The nature of the charge.
- **slices** (*1D array_like, len(block_number+1)*) – A block with ‘qindex’ *qi* correspondes to the leg indices in `slice(slices[qi], slices[qi+1])`.
- **charges** (*2D array_like, shape(block_number, chargeinfo.qnumber)*) – `charges[qi]` gives the charges for a block with ‘qindex’ *qi*.
- **qconj** (*{+1, -1}*) – A flag telling whether the charge points inwards (+1, default) or outwards (-1).

ind_len

The number of indices for this leg.

Type `int`

block_number

The number of blocks, i.e., a ‘qindex’ for this leg is in `range(block_number)`.

chinfo

The nature of the charge. Can be shared between LegCharges.

Type *ChargeInfo* instance

slices

A block with ‘qindex’ *qi* correspondes to the leg indices in `slice(self.slices[qi], self.slices[qi+1])`. See `get_slice()`.

Type `ndarray[np.intp_t, ndim=1]` (`block_number+1`)

charges

`charges[qi]` gives the charges for a block with ‘qindex’ *qi*. Note: the sign might be changed by *qconj*. See also `get_charge()`.

Type `ndarray[QTYPE_t, ndim=1]` (`block_number, chinfo.qnumber`)

qconj

A flag telling whether the charge points inwards (+1) or outwards (-1). Whenever charges are added, they should be multiplied with their *qconj* value.

Type `{-1, 1}`

sorted

Whether the charges are guaranteed to be sorted.

Type `bool`

bunched

Whether the charges are guaranteed to be bunched.

Type `bool`

Notes

Instances of this class can be shared between different *npc.Array*. Thus, functions changing *self.slices* or *self.charges* *must* always make copies. Further they *must* set *sorted* and *bunched* to *False* (if they might not preserve them).

copy()

Return a (shallow) copy of *self*.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Checks *format* for an output format key "LegCharge". Possible choices are:

"blocks" (default) Store *slices* and *charges* directly as datasets, and *block_number*, *sorted*, *bunched* as further attributes.

"compact" A single array `np.hstack([self.slices[:-1], self.slices[1:], self.charges])` as dataset "blockcharges", and *block_number*, *sorted*, *bunched* as further attributes.

"flat" Insufficient (!) to recover the exact blocks; saves only the array returned by *to_flat()* as dataset 'charges'.

The *ind_len*, *qconj*, and the *format* parameter are saved as group attributes under the same names. *chinfo* is always saved as subgroup.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

classmethod from_trivial (*ind_len*, *chargeinfo=None*, *qconj=1*)

Create trivial (qnumber=0) LegCharge for given len of indices *ind_len*.

classmethod from_qflat (*chargeinfo*, *qflat*, *qconj=1*)

Create a LegCharge from qflat form.

Does *neither* bunch *nor* sort. We recommend to sort (and bunch) afterwards, if you expect that tensors using the LegCharge have entries at all positions compatible with the charges.

Parameters

- **chargeinfo** (*ChargeInfo*) – The nature of the charge.

- **qflat** (array_like (ind_len, *qnumber*)) – *qnumber* charges for each index of the leg on entry.
- **qconj** (*{-1, 1}*) – A flag telling whether the charge points inwards (+1) or outwards (-1).

See also:

sort() sorts by charges

bunch() bunches contiguous blocks of the same charge.

classmethod from_qind (*chargeinfo, slices, charges, qconj=1*)

Just a wrapper around self.__init__(), see class doc-string for parameters.

See also:

sort() sorts by charges

bunch() bunches contiguous blocks of the same charge.

classmethod from_qdict (*chargeinfo, qdict, qconj=1*)

Create a LegCharge from qdict form.

Parameters

- **chargeinfo** (*ChargeInfo*) – The nature of the charge.
- **qdict** (*dict*) – A dictionary mapping a tuple of charges to slices.

classmethod from_add_charge (*legs, chargeinfo=None*)

Add the (independent) charges of two or more legs to get larger *qnumber*.

Parameters

- **legs** (iterable of *LegCharge*) – The legs for which the charges are to be combined/added.
- **chargeinfo** (*ChargeInfo*) – The ChargeInfo for all charges; create new if None.

Returns combined – A LegCharge with the charges of both legs. Is neither sorted nor bunched!

Return type *LegCharge*

classmethod from_drop_charge (*leg, charge=None, chargeinfo=None*)

Remove a charge from a LegCharge.

Parameters

- **leg** (*LegCharge*) – The leg from which to drop/remove a charge.
- **charge** (*int | str*) – Number or *name* of the charge (within *chinfo*) which is to be dropped. None means dropping all charges.
- **chargeinfo** (*ChargeInfo*) – The ChargeInfo with *charge* dropped; create new if None.

Returns dropped – A LegCharge with the specified charge dropped. Is neither sorted nor bunched!

Return type *LegCharge*

classmethod from_change_charge (*leg, charge, new_qmod, new_name="", chargeinfo=None*)

Remove a charge from a LegCharge.

Parameters

- **leg** (*LegCharge*) – The leg from which to drop/remove a charge.
- **charge** (*int* | *str*) – Number or *name* of the charge (within *chinfo*) for which *mod* is to be changed.
- **new_qmod** (*int*) – The new *mod* to be set for *charge* in the *ChargeInfo*.
- **new_name** (*str*) – The new name for *charge*.
- **chargeinfo** (*ChargeInfo*) – The *ChargeInfo* with *charge* changed; create new if *None*.

Returns **leg** – A *LegCharge* with the specified charge changed. Is neither sorted nor bunched!

Return type *LegCharge*

test_sanity ()

Sanity check, raises *ValueErrors*, if something is wrong.

conj ()

Return a (shallow) copy with opposite *self.qconj*.

Returns **conjugated** – Shallow copy of *self* with flipped *qconj*. *test_contractible()* of *self* with *conjugated* will not raise an error.

Return type *LegCharge*

flip_charges_qconj ()

Return a copy with both negative *qconj* and *charges*.

Returns **conj_charges** – (Shallow) copy of *self* with negative *qconj* and *charges*, thus representing the very same charges. *test_equal()* of *self* with *conj_charges* will not raise an error.

Return type *LegCharge*

to_qflat ()

Return charges in *qflat* form.

to_qdict ()

Return charges in *qdict* form.

Raises *ValueError*, if not blocked.

is_blocked ()

Returns whether *self* is blocked, i.e. *qindex* map 1:1 to charge values.

is_sorted ()

Returns whether *self.charges* is sorted lexicographically.

is_bunched ()

Checks whether *bunch()* would change something.

test_contractible (*other*)

Raises a *ValueError* if charges are incompatible for contraction with *other*.

Parameters **other** (*LegCharge*) – The *LegCharge* of the other leg considered for contraction.

Raises **ValueError** – If the charges are incompatible for direct contraction.

Notes

This function checks that two legs are *ready* for contraction. This is the case, if all of the following conditions are met:

- the `ChargeInfo` is equal
- the *slices* are equal
- the *charges* are the same up to *opposite* signs `qconj`:

```
self.charges * self.qconj = - other.charges * other.qconj
```

In general, there could also be a change of the total charge, see *Charge conservation with `np_conserved`*. This special case is not considered here - instead use `gauge_total_charge()`, if a change of the charge is desired.

If you are sure that the legs should be contractable, check whether the charges are actually valid or whether `self` and `other` are blocked or should be sorted.

See also:

`test_equal()` `self.test_contractible(other)` just performs `self.test_equal(other.conj())`.

`test_equal(other)`

Test if charges are *equal* including *qconj*.

Check that all of the following conditions are met:

- the `ChargeInfo` is equal
- the *slices* are equal
- the *charges* are the same up to the signs `qconj`:

```
self.charges * self.qconj = other.charges * other.qconj
```

See also:

`test_contractible()` `self.test_equal(other)` is equivalent to `self.test_contractible(other.conj())`.

`get_block_sizes()`

Return the sizes of the individual blocks.

Returns sizes – The sizes of the individual blocks; `sizes[i] = slices[i+1] - slices[i]`.

Return type ndarray, shape (block_number,)

`get_slice(qindex)`

Return slice selecting the block for a given *qindex*.

`get_qindex(flat_index)`

Find *qindex* containing a flat index.

Given a flat index, to find the corresponding entry in an Array, we need to determine the block it is saved in. For example, if `slices = [[0, 3], [3, 7], [7, 12]]`, the flat index 5 corresponds to the second entry, `qindex = 1` (since 5 is in [3:7]), and the index within the block would be `2 = 5 - 3`.

Parameters flat_index (*int*) – A flat index of the leg. Negative index counts from behind.

Returns

- **qindex** (*int*) – The qindex, i.e. the index of the block containing *flat_index*.
- **index_within_block** (*int*) – The index of *flat_index* within the block given by *qindex*.

get_qindex_of_charges (*charges*)

Return the slice selecting the block for given charge values.

Inverse function of *get_charge()*.

Parameters **charges** (*1D array_like*) – Charge values for which the slice of the block is to be determined.

Returns **slice(i, j)** – Slice of the charge values for

Return type *slice*

:raises *ValueError* : if the answer is not unique (because *self* is not blocked).:

get_charge (*qindex*)

Return charge *self.charges[qindex] * self.qconj* for a given *qindex*.

sort (*bunch=True*)

Return a copy of *self* sorted by charges (but maybe not bunched).

If *bunch=True*, the returned copy is completely blocked by charge.

Parameters **bunch** (*bool*) – Whether *self.bunch* is called after sorting. If *True*, the leg is guaranteed to be fully blocked by charge.

Returns

- **perm_qind** (*array (self.block_len,)*) – The permutation of the qindices (before bunching) used for the sorting. To obtain the flat permutation such that *sorted_array[... , :] = unsorted_array[... , perm_flat]*, use *perm_flat = unsorted_leg.perm_flat_from_perm_qind(perm_qind)*
- **sorted_copy** (*LegCharge*) – A shallow copy of *self*, with new qind sorted (and thus blocked if *bunch*) by charges.

See also:

bunch() enlarge blocks for contiguous qind of the same charges.

numpy.take() can apply *perm_flat* to a given axis

tenpy.tools.misc.inverse_permutation() returns inverse of a permutation

bunch ()

Return a copy with bunched *self.charges*: form blocks for contiguous equal charges.

Returns

- **idx** (*1D array*) – *idx[:-1]* are the indices of the old qind which are kept, *idx[-1] = old_block_number*.
- **cp** (*LegCharge*) – A new *LegCharge* with the same charges at given indices of the leg, but (possibly) shorter *self.charges* and *self.slices*.

See also:

sort() sorts by charges, thus enforcing complete blocking in combination with *bunch*.

project (*mask*)

Return copy keeping only the indices specified by *mask*.

Parameters **mask** (*1D array (bool)*) – Whether to keep of the indices.

Returns

- **map_qind** (*1D array*) – Map of qindices, such that `qind_new = map_qind[qind_old]`, and `map_qind[qind_old] = -1` for qindices projected out.
- **block_masks** (*1D array*) – The bool mask for each of the *remaining* blocks.
- **projected_copy** (*LegCharge*) – Copy of self with the qind projected by *mask*.

extend (*extra*)

Return a new *LegCharge*, which extends self with further charges.

This is needed to formally increase the dimension of an Array.

Parameters **extra** (*LegCharge | int*) – By what to extend, i.e. the charges to be appended to *self*. An int stands for extending the length of the array by a single new block of that size and zero charges.

Returns **extended_leg** – Copy of *self* extended by the charge blocks of the *extra* leg.

Return type *LegCharge*

charge_sectors ()

Return unique rows of self.charges.

Returns **charges** – Rows are the rows of self.charges lexsorted and without duplicates.

Return type `array[QTYPE, ndim=2]`

perm_flat_from_perm_qind (*perm_qind*)

Convert a permutation of qind (acting on self) into a flat permutation.

perm_qind_from_perm_flat (*perm_flat*)

Convert flat permutation into qind permutation.

Parameters **perm_flat** (*1D array*) – A permutation acting on self, which doesn't mix the blocks of qind.

Returns **perm_qind** – The permutation of self.qind described by perm_flat.

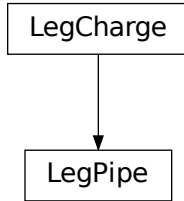
Return type *1D array*

Raises **ValueError** – If perm_flat mixes blocks of different qindex.

LegPipe

- full name: `tenpy.linalg.charges.LegPipe`
- parent module: `tenpy.linalg.charges`
- type: class

Inheritance Diagram



Methods

<code>LegPipe.__init__(legs[, qconj, sort, bunch])</code>	Initialize self.
<code>LegPipe.bunch(*args, **kwargs)</code>	Convert to <code>LegCharge</code> and call <code>LegCharge.bunch()</code> .
<code>LegPipe.charge_sectors()</code>	Return unique rows of <code>self.charges</code> .
<code>LegPipe.conj()</code>	Return a shallow copy with opposite <code>self.qconj</code> .
<code>LegPipe.copy()</code>	Return a (shallow) copy of self.
<code>LegPipe.extend(extra)</code>	Return a new <code>LegCharge</code> , which extends self with further charges.
<code>LegPipe.flip_charges_qconj()</code>	Return a copy with both negative <code>qconj</code> and <code>charges</code> .
<code>LegPipe.from_add_charge(legs[, chargeinfo])</code>	Add the (independent) charges of two or more legs to get larger <code>qnumber</code> .
<code>LegPipe.from_change_charge(leg, charge, new_qmod)</code>	Remove a charge from a <code>LegCharge</code> .
<code>LegPipe.from_drop_charge(leg[, charge, ...])</code>	Remove a charge from a <code>LegCharge</code> .
<code>LegPipe.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>LegPipe.from_qdict(chargeinfo, qdict[, qconj])</code>	Create a <code>LegCharge</code> from <code>qdict</code> form.
<code>LegPipe.from_qflat(chargeinfo, qflat[, qconj])</code>	Create a <code>LegCharge</code> from <code>qflat</code> form.
<code>LegPipe.from_qind(chargeinfo, slices, charges)</code>	Just a wrapper around <code>self.__init__()</code> , see class docstring for parameters.
<code>LegPipe.from_trivial(ind_len[, chargeinfo, ...])</code>	Create trivial (<code>qnumber=0</code>) <code>LegCharge</code> for given len of indices <code>ind_len</code> .
<code>LegPipe.get_block_sizes()</code>	Return the sizes of the individual blocks.
<code>LegPipe.get_charge(qindex)</code>	Return <code>charge self.charges[qindex] * self.qconj</code> for a given <code>qindex</code> .
<code>LegPipe.get_qindex(flat_index)</code>	Find <code>qindex</code> containing a flat index.
<code>LegPipe.get_qindex_of_charges(charges)</code>	Return the slice selecting the block for given charge values.
<code>LegPipe.get_slice(qindex)</code>	Return slice selecting the block for a given <code>qindex</code> .
<code>LegPipe.is_blocked()</code>	Returns whether self is blocked, i.e.
<code>LegPipe.is_bunched()</code>	Checks whether <code>bunch()</code> would change something.
<code>LegPipe.is_sorted()</code>	Returns whether <code>self.charges</code> is sorted lexicographically.

continues on next page

Table 58 – continued from previous page

<code>LegPipe.map_incoming_flat(incoming_indices)</code>	Map (flat) incoming indices to an index in the outgoing pipe.
<code>LegPipe.outer_conj()</code>	Like <code>conj()</code> , but don't change <code>qconj</code> for incoming legs.
<code>LegPipe.perm_flat_from_perm_qind(perm_qind)</code>	Convert a permutation of <code>qind</code> (acting on self) into a flat permutation.
<code>LegPipe.perm_qind_from_perm_flat(perm_flat)</code>	Convert flat permutation into <code>qind</code> permutation.
<code>LegPipe.project(*args, **kwargs)</code>	Convert self to <code>LegCharge</code> and call <code>LegCharge.project()</code> .
<code>LegPipe.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>LegPipe.sort(*args, **kwargs)</code>	Convert to <code>LegCharge</code> and call <code>LegCharge.sort()</code> .
<code>LegPipe.test_contractible(other)</code>	Raises a <code>ValueError</code> if charges are incompatible for contraction with <code>other</code> .
<code>LegPipe.test_equal(other)</code>	Test if charges are <i>equal</i> including <code>qconj</code> .
<code>LegPipe.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>LegPipe.to_LegCharge()</code>	Convert self to a <code>LegCharge</code> , discarding the information how to split the legs.
<code>LegPipe.to_qdict()</code>	Return charges in <i>qdict</i> form.
<code>LegPipe.to_qflat()</code>	Return charges in <i>qflat</i> form.

class `tenpy.linalg.charges.LegPipe` (*legs*, *qconj*=1, *sort*=True, *bunch*=True)

Bases: `tenpy.linalg.charges.LegCharge`

A *LegPipe* combines multiple legs of a tensor to one.

Often, it is necessary to “combine” multiple legs into one: for example to perform a SVD, the tensor needs to be viewed as a matrix.

This class does exactly this job: it combines multiple `LegCharges` (‘incoming legs’) into one ‘pipe’ (the ‘outgoing leg’). The pipe itself is a *LegCharge*, with indices running from 0 to the product of the individual legs’ *ind_len*, corresponding to all possible combinations of input leg indices.

(This class is implemented in `tenpy.linalg.charges` but also imported in `tenpy.linalg.np_conserved` for convenience.)

Parameters

- **legs** (list of *LegCharge*) – The legs which are to be combined.
- **qconj** (*{+1, -1}*) – A flag telling whether the charge of the *resulting* pipe points inwards (+1, default) or outwards (-1).
- **sort** (*bool*) – Whether the outgoing pipe should be sorted. Default `True`; recommended. Note: calling `sort()` after initialization converts to a `LegCharge`.
- **bunch** (*bool*) – Whether the outgoing pipe should be bunched. Default `True`; recommended. Note: calling `bunch()` after initialization converts to a `LegCharge`.

nlegs

The number of legs.

Type `int`

legs

The original legs, which were combined in the pipe.

Type tuple of *LegCharge*

subshape

ind_len for each of the incoming legs.

Type tuple of int

subqshape

block_number for each of the incoming legs.

Type tuple of int

q_map

Shape (*block_number*, 3 + *nlegs*). Rows: [*b_j*, *b_{j+1}*, *I_s*, *i_1*, ..., *i_{nlegs}*], See Notes below for details.

Type array[np.intp, ndim=2]

q_map_slices

Defined such that the row indices of in range (*q_map_slices*[*I_s*], *q_map_slices*[*I_s*+1]) have *q_map*[:, 2] == *I_s*.

Type array[np.intp, ndim=1]

_perm

A permutation such that *q_map*[_perm, 3:] is sorted by *i_l*.

Type 1D array

_strides

Strides for mapping incoming qindices *i_l* to the index of *q_map*[_perm, :].

Type 1D array

Notes

For np.reshape, taking, for example, $i, j, \dots \rightarrow k$ amounted to $k = s_1 * i + s_2 * j + \dots$ for appropriate strides s_1, s_2 .

In the charged case, however, we want to block k by charge, so we must implicitly permute as well. This reordering is encoded in *q_map*.

Each qindex combination of the *nlegs* input legs (i_1, \dots, i_{nlegs}), will end up getting placed in some slice $a_j : a_{j+1}$ of the outgoing pipe. Within this slice, the data is simply reshaped in usual row-major fashion ('C'-order), i.e., with strides $s_1 > s_2 > \dots$

It will be a subslice of a new total block labeled by qindex I_s . Because many charge combinations fuse to the same total charge, in general there will be many tuples (i_1, \dots, i_{nlegs}) belonging to the same I_s . The rows of *q_map* are precisely the collections of [*b_j*, *b_{j+1}*, *I_s*, *i_1*, ..., *i_{nlegs}*]. Here, $b_j : b_{j+1}$ denotes the slice of this qindex combination *within* the total block I_s , i.e., $b_j = a_j - \text{self.slices}[I_s]$.

The rows of *q_map* are lex-sorted first by I_s , then the *i*. Each I_s will have multiple rows, and the order in which they are stored in *q_map* is the order the data is stored in the actual tensor, i.e., it might look like

```
[ ...,
 [ b_j,      b_{j+1},  I_s,      i_1,      ..., i_{nlegs} ],
 [ b_{j+1}, b_{j+2},  I_s,      i'_1,     ..., i'_{nlegs} ],
 [ 0,       b_{j+3},  I_s + 1, i''_1,    ..., i''_{nlegs} ],
 [ b_{j+3}, b_{j+4},  I_s + 1, i'''_1,   ..., i'''_{nlegs} ],
 ...]
```

The charge fusion rule is:


```
self.charges[Qi]*self.qconj == sum([l.charges[qi_l]*l.qconj for l in self.legs])
↪mod qmod
```

Here the qindex Q_i of the pipe corresponds to qindices $q_{i,l}$ on the individual legs.

copy()

Return a (shallow) copy of self.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

In addition to the data saved for the *LegCharge*, it just saves the *legs* as subgroup.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type

cls

test_sanity()

Sanity check, raises ValueErrors, if something is wrong.

to_LegCharge()

Convert self to a LegCharge, discarding the information how to split the legs.

Usually not needed, but called by functions, which are not implemented for a LegPipe.

conj()

Return a shallow copy with opposite *self.qconj*.

Returns *conjugated* – Shallow copy of *self* with flipped *qconj*. Whenever we contract two legs, they need to be conjugated to each other. The incoming legs of the pipe are also conjugated.

Return type *LegCharge*

outer_conj()

Like *conj()*, but don't change *qconj* for incoming legs.

sort (**args, **kwargs*)

Convert to LegCharge and call *LegCharge.sort()*.

bunch (**args, **kwargs*)

Convert to LegCharge and call *LegCharge.bunch()*.

project (*args, **kwargs)

Convert self to LegCharge and call `LegCharge.project()`.

In general, this could be implemented for a LegPipe, but would make `split_legs()` more complicated, thus we keep it simple. If you really want to project and split afterwards, use the following work-around, which is for example used in `exact_diagonalization`:

- 1) Create the full pipe and save it separately.
- 2) Convert the Pipe to a Leg & project the array with it.
- 3) [... do calculations ...]
- 4) To split the ‘projected pipe’ of *A*, create an empty array *B* with the legs of *A*, but replace the projected leg by the full pipe. Set *A* as a slice of *B*. Finally split the pipe.

map_incoming_flat (incoming_indices)

Map (flat) incoming indices to an index in the outgoing pipe.

Parameters **incoming_indices** (*iterable of int*) – One (flat) index on each of the incoming legs.

Returns **outgoing_index** – The index in the outgoing leg.

Return type `int`

charge_sectors ()

Return unique rows of self.charges.

Returns **charges** – Rows are the rows of self.charges lexsorted and without duplicates.

Return type `array[QTYPE, ndim=2]`

extend (extra)

Return a new `LegCharge`, which extends self with further charges.

This is needed to formally increase the dimension of an Array.

Parameters **extra** (`LegCharge` | `int`) – By what to extend, i.e. the charges to be appended to *self*. An `int` stands for extending the length of the array by a single new block of that size and zero charges.

Returns **extended_leg** – Copy of *self* extended by the charge blocks of the *extra* leg.

Return type `LegCharge`

flip_charges_qconj ()

Return a copy with both negative *qconj* and *charges*.

Returns **conj_charges** – (Shallow) copy of self with negative *qconj* and *charges*, thus representing the very same charges. `test_equal()` of *self* with *conj_charges* will not raise an error.

Return type `LegCharge`

classmethod from_add_charge (legs, chargeinfo=None)

Add the (independent) charges of two or more legs to get larger *qnumber*.

Parameters

- **legs** (*iterable of LegCharge*) – The legs for which the charges are to be combined/added.
- **chargeinfo** (`ChargeInfo`) – The `ChargeInfo` for all charges; create new if `None`.

Returns **combined** – A `LegCharge` with the charges of both legs. Is neither sorted nor bunched!

Return type *LegCharge*

classmethod from_change_charge (*leg, charge, new_qmod, new_name="", chargeinfo=None*)
Remove a charge from a LegCharge.

Parameters

- **leg** (*LegCharge*) – The leg from which to drop/remove a charge.
- **charge** (*int | str*) – Number or *name* of the charge (within *chinfo*) for which *mod* is to be changed.
- **new_qmod** (*int*) – The new *mod* to be set for *charge* in the *ChargeInfo*.
- **new_name** (*str*) – The new name for *charge*.
- **chargeinfo** (*ChargeInfo*) – The ChargeInfo with *charge* changed; create new if None.

Returns leg – A LegCharge with the specified charge changed. Is neither sorted nor bunched!

Return type *LegCharge*

classmethod from_drop_charge (*leg, charge=None, chargeinfo=None*)
Remove a charge from a LegCharge.

Parameters

- **leg** (*LegCharge*) – The leg from which to drop/remove a charge.
- **charge** (*int | str*) – Number or *name* of the charge (within *chinfo*) which is to be dropped. None means dropping all charges.
- **chargeinfo** (*ChargeInfo*) – The ChargeInfo with *charge* dropped; create new if None.

Returns dropped – A LegCharge with the specified charge dropped. Is neither sorted nor bunched!

Return type *LegCharge*

classmethod from_qdict (*chargeinfo, qdict, qconj=1*)
Create a LegCharge from qdict form.

Parameters

- **chargeinfo** (*ChargeInfo*) – The nature of the charge.
- **qdict** (*dict*) – A dictionary mapping a tuple of charges to slices.

classmethod from_qflat (*chargeinfo, qflat, qconj=1*)
Create a LegCharge from qflat form.

Does *neither* bunch *nor* sort. We recommend to sort (and bunch) afterwards, if you expect that tensors using the LegCharge have entries at all positions compatible with the charges.

Parameters

- **chargeinfo** (*ChargeInfo*) – The nature of the charge.
- **qflat** (*array_like (ind_len, qnumber)*) – *qnumber* charges for each index of the leg on entry.
- **qconj** (*{-1, 1}*) – A flag telling whether the charge points inwards (+1) or outwards (-1).

See also:

sort() sorts by charges

bunch() bunches contiguous blocks of the same charge.

classmethod from_qind(*chargeinfo*, *slices*, *charges*, *qconj=1*)

Just a wrapper around `self.__init__()`, see class doc-string for parameters.

See also:

sort() sorts by charges

bunch() bunches contiguous blocks of the same charge.

classmethod from_trivial(*ind_len*, *chargeinfo=None*, *qconj=1*)

Create trivial (*qnumber=0*) LegCharge for given len of indices *ind_len*.

get_block_sizes()

Return the sizes of the individual blocks.

Returns sizes – The sizes of the individual blocks; `sizes[i] = slices[i+1] - slices[i]`.

Return type ndarray, shape (block_number,)

get_charge(*qindex*)

Return charge `self.charges[qindex] * self.qconj` for a given *qindex*.

get_qindex(*flat_index*)

Find *qindex* containing a flat index.

Given a flat index, to find the corresponding entry in an Array, we need to determine the block it is saved in. For example, if `slices = [[0, 3], [3, 7], [7, 12]]`, the flat index 5 corresponds to the second entry, *qindex* = 1 (since 5 is in [3:7]), and the index within the block would be $2 = 5 - 3$.

Parameters flat_index (*int*) – A flat index of the leg. Negative index counts from behind.

Returns

- **qindex** (*int*) – The *qindex*, i.e. the index of the block containing *flat_index*.
- **index_within_block** (*int*) – The index of *flat_index* within the block given by *qindex*.

get_qindex_of_charges(*charges*)

Return the slice selecting the block for given charge values.

Inverse function of `get_charge()`.

Parameters charges (*1D array_like*) – Charge values for which the slice of the block is to be determined.

Returns slice(*i*, *j*) – Slice of the charge values for

Return type slice

:raises ValueError : if the answer is not unique (because *self* is not blocked):

get_slice(*qindex*)

Return slice selecting the block for a given *qindex*.

is_blocked()

Returns whether *self* is blocked, i.e. *qindex* map 1:1 to charge values.

is_bunched()

Checks whether `bunch()` would change something.

is_sorted()

Returns whether *self.charges* is sorted lexicographically.

perm_flat_from_perm_qind(*perm_qind*)

Convert a permutation of qind (acting on self) into a flat permutation.

perm_qind_from_perm_flat(*perm_flat*)

Convert flat permutation into qind permutation.

Parameters **perm_flat** (*1D array*) – A permutation acting on self, which doesn't mix the blocks of qind.

Returns **perm_qind** – The permutation of self.qind described by perm_flat.

Return type 1D array

Raises **ValueError** – If perm_flat mixes blocks of different qindex.

test_contractible(*other*)

Raises a ValueError if charges are incompatible for contraction with other.

Parameters **other** (*LegCharge*) – The LegCharge of the other leg considered for contraction.

Raises **ValueError** – If the charges are incompatible for direct contraction.

Notes

This function checks that two legs are *ready* for contraction. This is the case, if all of the following conditions are met:

- the ChargeInfo is equal
- the *slices* are equal
- the *charges* are the same up to *opposite* signs *qconj*:

```
self.charges * self.qconj = - other.charges * other.qconj
```

In general, there could also be a change of the total charge, see [Charge conservation with np_conserved](#). This special case is not considered here - instead use `gauge_total_charge()`, if a change of the charge is desired.

If you are sure that the legs should be contractable, check whether the charges are actually valid or whether *self* and *other* are blocked or should be sorted.

See also:

test_equal() `self.test_contractible(other)` just performs `self.test_equal(other.conj())`.

test_equal(*other*)

Test if charges are *equal* including *qconj*.

Check that all of the following conditions are met:

- the ChargeInfo is equal
- the *slices* are equal
- the *charges* are the same up to the signs *qconj*:

```
self.charges * self.qconj = other.charges * other.qconj
```

See also:

`test_contractible()` `self.test_equal(other)` is equivalent to `self.test_contractible(other.conj())`.

`to_qdict()`

Return charges in *qdict* form.

Raises `ValueError`, if not blocked.

`to_qflat()`

Return charges in *qflat* form.

Module description

Basic definitions of a charge.

This module contains implementations for handling the quantum numbers (“charges”) of the *Array*.

In particular, the classes *ChargeInfo*, *LegCharge* and *LegPipe* are implemented here.

Note: The contents of this module are imported in *np_conserved*, so you usually don’t need to import this module in your application.

A detailed introduction to *np_conserved* can be found in *Charge conservation with np_conserved*.

In this module, some functions have the python decorator `@use_cython`. Functions with this decorator are replaced by the ones written in Cython, implemented in the file `tenpy/linalg/_npc_helper.pyx`. For further details, see the definition of `use_cython()`.

```
tenpy.linalg.charges.QTYPE = <class 'numpy.int64'>
```

Numpy data type for the charges.

7.8.3 svd_robust

- full name: `tenpy.linalg.svd_robust`
- parent module: `tenpy.linalg`
- type: module

Functions

<code>svd(a[, full_matrices, compute_uv, ...])</code>	Wrapper around <code>scipy.linalg.svd()</code> with <i>gesvd</i> backup plan.
<code>svd_gesvd(a[, full_matrices, compute_uv, ...])</code>	<i>svd</i> with LAPACK’s ‘#gesvd’ (with # = d/z for float/complex).

svd

- full name: `tenpy.linalg.svd_robust.svd`
- parent module: `tenpy.linalg.svd_robust`
- type: function

`tenpy.linalg.svd_robust.svd(a, full_matrices=True, compute_uv=True, overwrite_a=False, check_finite=True, lapack_driver='gesdd', warn=True)`
 Wrapper around `scipy.linalg.svd()` with `gesvd` backup plan.

Tries to avoid raising an `LinAlgError` by using using the `lapack_driver gesvd`, if `gesdd` failed.

Parameters not described below are as in `scipy.linalg.svd()`

Parameters

- **overwrite_a** (*bool*) – Ignored (i.e. set to `False`) if `lapack_driver='gesdd'`. Otherwise described in `scipy.linalg.svd()`.
- **lapack_driver** (`{'gesdd', 'gesvd'}`, *optional*) – Whether to use the more efficient divide-and-conquer approach (`'gesdd'`) or general rectangular approach (`'gesvd'`) to compute the SVD. MATLAB and Octave use the `'gesvd'` approach. Default is `'gesdd'`. If `'gesdd'` fails, `'gesvd'` is used as backup.
- **warn** (*bool*) – Whether to create a warning when the SVD failed.

Returns `U, S, Vh` – As described in doc-string of `scipy.linalg.svd()`.

Return type `ndarray`

svd_gesvd

- full name: `tenpy.linalg.svd_robust.svd_gesvd`
- parent module: `tenpy.linalg.svd_robust`
- type: function

`tenpy.linalg.svd_robust.svd_gesvd(a, full_matrices=True, compute_uv=True, check_finite=True)`
 svd with LAPACK's `'#gesvd'` (with `# = d/z` for float/complex).

Similar as `numpy.linalg.svd()`, but use LAPACK `'gesvd'` driver. Works only with 2D arrays. Outer part is based on the code of `numpy.linalg.svd`.

Parameters

- **full_matrices, compute_uv** (*a,*) – See `numpy.linalg.svd()` for details.
- **check_finite** – check whether input arrays contain `'NaN'` or `'inf'`.

Returns `U, S, Vh` – See `numpy.linalg.svd()` for details.

Return type `ndarray`

Module description

(More) robust version of singular value decomposition.

We often need to perform an SVD. In general, an SVD is a matrix factorization that is always well defined and should also work for ill-conditioned matrices. But sadly, both `numpy.linalg.svd()` and `scipy.linalg.svd()` fail from time to time, raising `LinalgError("SVD did not converge")`. The reason is that both of them call the LAPACK function `#gesdd` (where `#` depends on the data type), which takes an iterative approach that can fail. However, it is usually much faster than the alternative (and robust) `#gesvd`.

Our workaround is as follows: we provide a function `svd()` with call signature as `scipy.svd`. This function is basically just a wrapper around `scipy.svd`, i.e., we keep calling the faster `dgesdd`. But if that fails, we can still use `dgesvd` as a backup.

Sadly, `dgesvd` and `zgesvd` were not included into `scipy` until version '0.18.0' (nor in `numpy`), which is as the time of this writing the latest stable `scipy` version. For `scipy` version newer than '0.18.0', we make use of the new keyword 'lapack_driver' for `svd`, otherwise we (try to) load `dgesvd` and `zgesvd` from shared LAPACK libraries.

The tribute for the `dgesvd` wrapper code goes to 'jgarcke', originally posted at <http://projects.scipy.org/numpy/ticket/990>, which is now hosted at <https://github.com/numpy/numpy/issues/1588> He explains a bit more in detail what fails.

The include of `dgesvd` to `scipy` was done in <https://github.com/scipy/scipy/pull/5994>.

Examples

The idea is that you just import the `svd` from this module and use it as replacement for `np.linalg.svd` or `scipy.linalg.svd`:

```
>>> from svd_robust import svd
>>> U, S, VT = svd([[1., 1.], [0., [1.]])
```

7.8.4 random_matrix

- full name: `tenpy.linalg.random_matrix`
- parent module: `tenpy.linalg`
- type: module

Functions

<code>COE(size)</code>	Circular orthogonal ensemble (COE).
<code>CRE(size)</code>	Circular real ensemble (CRE).
<code>CUE(size)</code>	Circular unitary ensemble (CUE).
<code>GOE(size)</code>	Gaussian orthogonal ensemble (GOE).
<code>GUE(size)</code>	Gaussian unitary ensemble (GUE).
<code>O_close_1(size[, a])</code>	return an random orthogonal matrix 'close' to the Identity.
<code>U_close_1(size[, a])</code>	return an random orthogonal matrix 'close' to the identity.
<code>box(size[, W])</code>	return random number uniform in $(-W, W]$.
<code>standard_normal_complex(size)</code>	return $(R + 1.j*I)$ for independent R and I from <code>np.random.standard_normal</code> .

COE

- full name: `tenpy.linalg.random_matrix.COE`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.COE` (*size*)
Circular orthogonal ensemble (COE).

Parameters *size* (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.

Returns *U* – Unitary, symmetric (complex) matrix drawn from the COE (=Haar measure on this space).

Return type ndarray

CRE

- full name: `tenpy.linalg.random_matrix.CRE`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.CRE` (*size*)
Circular real ensemble (CRE).

Parameters *size* (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.

Returns *U* – Orthogonal matrix drawn from the CRE (=Haar measure on $O(n)$).

Return type ndarray

CUE

- full name: `tenpy.linalg.random_matrix.CUE`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.CUE` (*size*)
Circular unitary ensemble (CUE).

Parameters *size* (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.

Returns *U* – Unitary matrix drawn from the CUE (=Haar measure on $U(n)$).

Return type ndarray

GOE

- full name: `tenpy.linalg.random_matrix.GOE`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.GOE` (*size*)
Gaussian orthogonal ensemble (GOE).

Parameters *size* (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.

Returns **H** – Real, symmetric numpy matrix drawn from the GOE, i.e. $p(H) = 1/Z \exp(-n/4 \text{tr}(H^2))$

Return type ndarray

GUE

- full name: `tenpy.linalg.random_matrix.GUE`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.GUE` (*size*)
Gaussian unitary ensemble (GUE).

Parameters *size* (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.

Returns **H** – Hermitian (complex) numpy matrix drawn from the GUE, i.e. $p(H) = 1/Z \exp(-n/4 \text{tr}(H^2))$.

Return type ndarray

O_close_1

- full name: `tenpy.linalg.random_matrix.O_close_1`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.O_close_1` (*size*, *a=0.01*)
return an random orthogonal matrix ‘close’ to the Identity.

Parameters

- **size** (*tuple*) – (*n*, *n*), where *n* is the dimension of the output matrix.
- **a** (*float*) – Parameter determining how close the result is on *O*; $\lim_{a \rightarrow 0} \langle |O - E| \rangle_a = 0$ (where *E* is the identity).

Returns **O** – Orthogonal matrix close to the identity (for small *a*).

Return type ndarray

U_close_1

- full name: `tenpy.linalg.random_matrix.U_close_1`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.U_close_1(size, a=0.01)`
 return an random orthogonal matrix ‘close’ to the identity.

Parameters

- **size** (*tuple*) – (n, n) , where n is the dimension of the output matrix.
- **a** (*float*) – Parameter determining how close the result is to the identity. $\lim_{a \rightarrow 0} < |O - E| >_a = 0$ (where E is the identity).

Returns **U** – Unitary matrix close to the identity (for small a). Eigenvalues are chosen i.i.d. as $\exp(1.j*a*x)$ with x uniform in $[-1, 1]$.

Return type ndarray

box

- full name: `tenpy.linalg.random_matrix.box`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.box(size, W=1.0)`
 return random number uniform in $(-W, W]$.

standard_normal_complex

- full name: `tenpy.linalg.random_matrix.standard_normal_complex`
- parent module: `tenpy.linalg.random_matrix`
- type: function

`tenpy.linalg.random_matrix.standard_normal_complex(size)`
 return $(R + 1.j*I)$ for independent R and I from `np.random.standard_normal`.

Module description

Provide some random matrix ensembles for numpy.

The implemented ensembles are:

ensemble	matrix class drawn from	measure	invariant under	beta
GOE	real, symmetric	$\sim \exp(-n/4 \operatorname{tr}(H^2))$	orthogonal O	1
GUE	hermitian	$\sim \exp(-n/2 \operatorname{tr}(H^2))$	unitary U	2
CRE	$O(n)$	Haar	orthogonal O	/
COE	U in $U(n)$ with $U = U^T$	Haar	orthogonal O	1
CUE	$U(n)$	Haar	unitary U	2
O_close_1	$O(n)$?	/	/
U_close_1	$U(n)$?	/	/

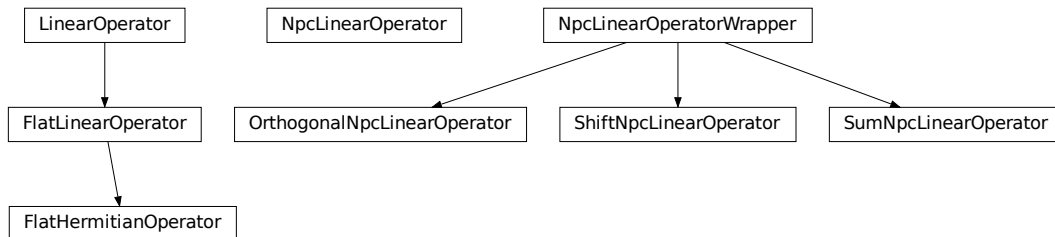
All functions in this module take a tuple (n, n) as first argument, such that we can use the function `from_func()` to generate a block diagonal `Array` with the block from the corresponding ensemble, for example:

```
npc.Array.from_func_square(GOE, [leg, leg.conj()])
```

7.8.5 sparse

- full name: `tenpy.linalg.sparse`
- parent module: `tenpy.linalg`
- type: module

Classes

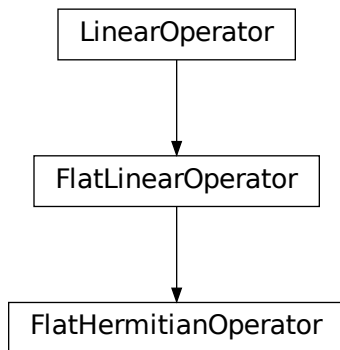


<code>FlatHermitianOperator(npc_matvec, leg, dtype)</code>	Hermitian variant of <code>FlatLinearOperator</code> .
<code>FlatLinearOperator(npc_matvec, leg, dtype[, ...])</code>	Square Linear operator acting on numpy arrays based on a <i>matvec</i> acting on npc Arrays.
<code>NpcLinearOperator</code>	Prototype for a Linear Operator acting on <code>Array</code> .
<code>NpcLinearOperatorWrapper(orig_operator)</code>	Base class for wrapping around another <code>NpcLinearOperator</code> .
<code>OrthogonalNpcLinearOperator(orig_operator, ...)</code>	Replace $H \rightarrow P H P$ with the projector $P = 1 - \sum_o o\rangle \langle o $.
<code>ShiftNpcLinearOperator(orig_operator, shift)</code>	Represents $\text{original_operator} + \text{shift} * \text{identity}$.
<code>SumNpcLinearOperator(orig_operator, ...)</code>	Sum of two linear operators.

FlatHermitianOperator

- full name: `tenpy.linalg.sparse.FlatHermitianOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram



Methods

<code>FlatHermitianOperator.__init__(npc_matvec, ...)</code>	Initialize this <code>LinearOperator</code> .
<code>FlatHermitianOperator.adjoint()</code>	Hermitian adjoint.
<code>FlatHermitianOperator.dot(x)</code>	Matrix-matrix or matrix-vector multiplication.
<code>FlatHermitianOperator.flat_to_npc(vec)</code>	Convert flat vector of selected charge sector into npc Array.
<code>FlatHermitianOperator.flat_to_npc_None_sector(vec)</code>	Convert flat vector of undetermined charge sectors into npc Array.
<code>FlatHermitianOperator.flat_to_npc_all_sectors(vec)</code>	Convert flat vector of <i>all</i> charge sectors into npc Array with extra “charge” leg.
<code>FlatHermitianOperator.from_NpcArray(mat[, ...])</code>	Create a <code>FlatLinearOperator</code> from a square <code>Array</code> .
<code>FlatHermitianOperator.from_guess_with_pipe(...)</code>	Create a <code>FlatLinearOperator</code> from a <code>matvec</code> function acting on multiple legs.
<code>FlatHermitianOperator.matmat(X)</code>	Matrix-matrix multiplication.
<code>FlatHermitianOperator.matvec(x)</code>	Matrix-vector multiplication.
<code>FlatHermitianOperator npc_to_flat(npc_vec)</code>	Convert npc Array with <code>qtotal = self.charge_sector</code> into ndarray.
<code>FlatHermitianOperator npc_to_flat_all_sectors(npc_vec)</code>	Convert npc Array with <code>qtotal = self.charge_sector</code> into ndarray.

continues on next page

Table 62 – continued from previous page

<code>FlatHermitianOperator.rmatmat(X)</code>	Adjoint matrix-matrix multiplication.
<code>FlatHermitianOperator.rmatvec(x)</code>	Adjoint matrix-vector multiplication.
<code>FlatHermitianOperator.transpose()</code>	Transpose this linear operator.

Class Attributes and Properties

<code>FlatHermitianOperator.H</code>	Hermitian adjoint.
<code>FlatHermitianOperator.T</code>	Transpose this linear operator.
<code>FlatHermitianOperator.charge_sector</code>	Charge sector of the vector which is acted on.
<code>FlatHermitianOperator.ndim</code>	

class `tenpy.linalg.sparse.FlatHermitianOperator` (*npc_matvec*, *leg*, *dtype*,
charge_sector=0, *vec_label=None*)

Bases: `tenpy.linalg.sparse.FlatLinearOperator`

Hermitian variant of `FlatLinearOperator`.

Note that we don't check `matvec()` to return a hermitian result, we only define an adjoint to be *self*.

property **H**

Hermitian adjoint.

Returns the Hermitian adjoint of self, aka the Hermitian conjugate or Hermitian transpose. For a complex matrix, the Hermitian adjoint is equal to the conjugate transpose.

Can be abbreviated `self.H` instead of `self.adjoint()`.

Returns **A_H** – Hermitian adjoint of self.

Return type `LinearOperator`

property **T**

Transpose this linear operator.

Returns a `LinearOperator` that represents the transpose of this one. Can be abbreviated `self.T` instead of `self.transpose()`.

adjoint ()

Hermitian adjoint.

Returns the Hermitian adjoint of self, aka the Hermitian conjugate or Hermitian transpose. For a complex matrix, the Hermitian adjoint is equal to the conjugate transpose.

Can be abbreviated `self.H` instead of `self.adjoint()`.

Returns **A_H** – Hermitian adjoint of self.

Return type `LinearOperator`

property **charge_sector**

Charge sector of the vector which is acted on.

dot (x)

Matrix-matrix or matrix-vector multiplication.

Parameters **x** (*array_like*) – 1-d or 2-d array, representing a vector or matrix.

Returns **Ax** – 1-d or 2-d array (depending on the shape of x) that represents the result of applying this linear operator on x.

Return type `array`

flat_to_npc (*vec*)

Convert flat vector of selected charge sector into npc Array.

Parameters **vec** (*1D ndarray*) – Numpy vector to be converted. Should have the entries according to `self.charge_sector`.

Returns **npc_vec** – Same as *vec*, but converted into a npc array.

Return type `Array`

flat_to_npc_None_sector (*vec*)

Convert flat vector of undetermined charge sectors into npc Array.

The charge sector to be used is chosen as the block with the maximal norm, not by *self.charge_sector* (which might be *None*).

Parameters **vec** (*1D ndarray*) – Numpy vector to be converted.

Returns **npc_vec** – Same as *vec*, but converted into a npc array.

Return type `Array`

flat_to_npc_all_sectors (*vec*)

Convert flat vector of *all* charge sectors into npc Array with extra “charge” leg.

Parameters **vec** (*1D ndarray*) – Numpy vector to be converted.

Returns **npc_vec** – Same as *vec*, but converted into a npc array.

Return type `Array`

classmethod from_NpcArray (*mat*, *charge_sector=0*)

Create a *FlatLinearOperator* from a square `Array`.

Parameters

- **mat** (`Array`) – A square matrix, with contractable legs.
- **charge_sector** (*None* | *charges* | *0*) – Selects the charge sector of the vector onto which the Linear operator acts. *None* stands for *all* sectors, *0* stands for the zero-charge sector. Defaults to *0*, i.e., *assumes* the dominant eigenvector is in charge sector *0*.

classmethod from_guess_with_pipe (*npc_matvec*, *v0_guess*, *labels_split=None*, *dtype=None*)

Create a *FlatLinearOperator* from a *matvec* function acting on multiple legs.

This function creates a wrapper *matvec* function to allow acting on a “vector” with multiple legs. The wrapper combines the legs into a *LegPipe* before calling the actual *matvec* function, and splits them again in the end.

Parameters

- **npc_matvec** (*function*) – Function to calculate the action of the linear operator on an npc vector with the given split labels *labels_split*. Has to return an npc vector with the same legs.
- **v0_guess** (`Array`) – Initial guess/starting vector which can be applied to *npc_matvec*.
- **labels_split** (*None* | *list of str*) – Labels of *v0_guess* in the order in which they are to be combined into a *LegPipe*. *None* defaults to *v0_guess.get_leg_labels()*.
- **dtype** (*np.dtype* | *None*) – The data type of the arrays. *None* defaults to dtype of *v0_guess* (!).

Returns

- **lin_op** (*cls*) – Instance of the class to be used as linear operator
- **guess_flat** (*np.ndarray*) – Numpy vector representing the guess *v0_guess*.

matmat (*X*)

Matrix-matrix multiplication.

Performs the operation $y=A*X$ where A is an $M \times N$ linear operator and X dense $N \times K$ matrix or ndarray.

Parameters **X** (*{matrix, ndarray}*) – An array with shape (N,K) .

Returns **Y** – A matrix or ndarray with shape (M,K) depending on the type of the X argument.

Return type {matrix, ndarray}

Notes

This matmat wraps any user-specified matmat routine or overridden `_matmat` method to ensure that y has the correct type.

matvec (*x*)

Matrix-vector multiplication.

Performs the operation $y=A*x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array.

Parameters **x** (*{matrix, ndarray}*) – An array with shape $(N,)$ or $(N,1)$.

Returns **y** – A matrix or ndarray with shape $(M,)$ or $(M,1)$ depending on the type and shape of the x argument.

Return type {matrix, ndarray}

Notes

This matvec wraps the user-specified matvec routine or overridden `_matvec` method to ensure that y has the correct shape and type.

npc_to_flat (*npc_vec*)

Convert npc Array with `qtotal = self.charge_sector` into ndarray.

Parameters **npc_vec** (*Array*) – Npc Array to be converted. Should only have entries in *self.charge_sector*.

Returns **vec** – Same as *npc_vec*, but converted into a flat Numpy array.

Return type 1D ndarray

npc_to_flat_all_sectors (*npc_vec*)

Convert npc Array with `qtotal = self.charge_sector` into ndarray.

Parameters **npc_vec** (*Array*) – Npc Array to be converted. Should only have entries in *self.charge_sector*.

Returns **vec** – Same as *npc_vec*, but converted into a flat Numpy array.

Return type 1D ndarray

rmatmat (*X*)

Adjoint matrix-matrix multiplication.

Performs the operation $y = A^H * x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array, or 2-d array. The default implementation defers to the adjoint.

Parameters \mathbf{x} (*{matrix, ndarray}*) – A matrix or 2D array.

Returns \mathbf{Y} – A matrix or 2D array depending on the type of the input.

Return type {matrix, ndarray}

Notes

This `rmatmat` wraps the user-specified `rmatmat` routine.

`rmatvec(x)`

Adjoint matrix-vector multiplication.

Performs the operation $y = A^H * x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array.

Parameters \mathbf{x} (*{matrix, ndarray}*) – An array with shape $(M,)$ or $(M,1)$.

Returns \mathbf{y} – A matrix or ndarray with shape $(N,)$ or $(N,1)$ depending on the type and shape of the x argument.

Return type {matrix, ndarray}

Notes

This `rmatvec` wraps the user-specified `rmatvec` routine or overridden `_rmatvec` method to ensure that y has the correct shape and type.

`transpose()`

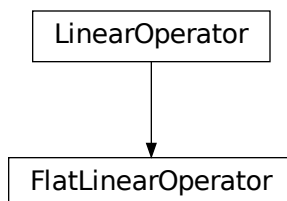
Transpose this linear operator.

Returns a `LinearOperator` that represents the transpose of this one. Can be abbreviated `self.T` instead of `self.transpose()`.

FlatLinearOperator

- full name: `tenpy.linalg.sparse.FlatLinearOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram



Methods

<code>FlatLinearOperator.__init__(npc_matvec, leg, ...)</code>	Initialize this LinearOperator.
<code>FlatLinearOperator.adjoint()</code>	Hermitian adjoint.
<code>FlatLinearOperator.dot(x)</code>	Matrix-matrix or matrix-vector multiplication.
<code>FlatLinearOperator.flat_to_npc(vec)</code>	Convert flat vector of selected charge sector into npc Array.
<code>FlatLinearOperator.flat_to_npc_None_sector(vec)</code>	Convert flat vector of undetermined charge sectors into npc Array.
<code>FlatLinearOperator.flat_to_npc_all_sectors(vec)</code>	Convert flat vector of <i>all</i> charge sectors into npc Array with extra “charge” leg.
<code>FlatLinearOperator.from_NpcArray(mat[, ...])</code>	Create a <i>FlatLinearOperator</i> from a square <i>Array</i> .
<code>FlatLinearOperator.from_guess_with_pipe(...)</code>	Create a <i>FlatLinearOperator</i> from a <i>matvec</i> function acting on multiple legs.
<code>FlatLinearOperator.matmat(X)</code>	Matrix-matrix multiplication.
<code>FlatLinearOperator.matvec(x)</code>	Matrix-vector multiplication.
<code>FlatLinearOperator npc_to_flat(npc_vec)</code>	Convert npc Array with <code>qtotal = self.charge_sector</code> into ndarray.
<code>FlatLinearOperator npc_to_flat_all_sectors(npc_vec)</code>	Convert npc Array with <code>qtotal = self.charge_sector</code> into ndarray.
<code>FlatLinearOperator.rmatmat(X)</code>	Adjoint matrix-matrix multiplication.
<code>FlatLinearOperator.rmatvec(x)</code>	Adjoint matrix-vector multiplication.
<code>FlatLinearOperator.transpose()</code>	Transpose this linear operator.

Class Attributes and Properties

<code>FlatLinearOperator.H</code>	Hermitian adjoint.
<code>FlatLinearOperator.T</code>	Transpose this linear operator.
<code>FlatLinearOperator.charge_sector</code>	Charge sector of the vector which is acted on.
<code>FlatLinearOperator.ndim</code>	

class `tenpy.linalg.sparse.FlatLinearOperator` (*npc_matvec*, *leg*, *dtype*, *charge_sector*=0, *vec_label*=None)

Bases: `scipy.sparse.linalg.interface.LinearOperator`

Square Linear operator acting on numpy arrays based on a *matvec* acting on npc Arrays.

Note that this class represents a square linear operator. In terms of charges, this means it has legs `[self.leg.conj(), self.leg]` and trivial (zero) `qtotal`.

Parameters

- **npc_matvec** (*function*) – Function to calculate the action of the linear operator on an npc vector (with the specified *leg*). Has to return an npc vector with the same leg.
- **leg** (*LegCharge*) – Leg of the vector on which *npc_matvec* can act on.
- **dtype** (*np.dtype*) – The data type of the arrays.
- **charge_sector** (None | charges | 0) – Selects the charge sector of the vector onto which the Linear operator acts. None stands for *all* sectors, 0 stands for the zero-charge sector. Defaults to 0, i.e., *assumes* the dominant eigenvector is in charge sector 0.

- **vec_label** (*None* | *str*) – Label to be set to the npc vector before acting on it with *npc_matvec*. Ignored if *None*.

possible_charge_sectors

Each row corresponds to one possible choice for *charge_sector*.

Type ndarray[QTYPE, ndim=2]

shape

The dimensions for the selected charge sector.

Type (int, int)

dtype

The data type of the arrays.

Type np.dtype

leg

Leg of the vector on which *npc_matvec* can act on.

Type *LegCharge*

vec_label

Label to be set to the npc vector before acting on it with *npc_matvec*. Ignored if *None*.

Type None | str

npc_matvec

Function to calculate the action of the linear operator on an npc vector (with one *leg*).

Type function

matvec_count

The number of times *npc_matvec* was called.

Type int

_mask

The indices of *leg* corresponding to the *charge_sector* to be diagonalized.

Type ndarray[ndim=1, bool]

_npc_matvec_multileg

Only set if initialized with *from_guess_with_pipe()*. The *npc_matvec* function to be wrapped around. Takes the npc Array in multidimensional form and returns it that way.

Type function | None

_labels_split

Only set if initialized with *from_guess_with_pipe()*. Labels of the guess before combining them into a pipe (stored as *leg*).

Type list of str

classmethod from_NpcArray (*mat*, *charge_sector*=0)

Create a *FlatLinearOperator* from a square *Array*.

Parameters

- **mat** (*Array*) – A square matrix, with contractable legs.
- **charge_sector** (None | charges | 0) – Selects the charge sector of the vector onto which the Linear operator acts. None stands for *all* sectors, 0 stands for the zero-charge sector. Defaults to 0, i.e., *assumes* the dominant eigenvector is in charge sector 0.

classmethod `from_guess_with_pipe` (*npc_matvec*, *v0_guess*, *labels_split=None*, *dtype=None*)

Create a `FlatLinearOperator` from a `matvec` function acting on multiple legs.

This function creates a wrapper `matvec` function to allow acting on a “vector” with multiple legs. The wrapper combines the legs into a `LegPipe` before calling the actual `matvec` function, and splits them again in the end.

Parameters

- **npc_matvec** (*function*) – Function to calculate the action of the linear operator on an npc vector with the given split labels *labels_split*. Has to return an npc vector with the same legs.
- **v0_guess** (*Array*) – Initial guess/starting vector which can be applied to *npc_matvec*.
- **labels_split** (*None* | *list of str*) – Labels of *v0_guess* in the order in which they are to be combined into a `LegPipe`. *None* defaults to *v0_guess.get_leg_labels()*.
- **dtype** (*np.dtype* | *None*) – The data type of the arrays. *None* defaults to dtype of *v0_guess* (!).

Returns

- **lin_op** (*cls*) – Instance of the class to be used as linear operator
- **guess_flat** (*np.ndarray*) – Numpy vector representing the guess *v0_guess*.

property `charge_sector`

Charge sector of the vector which is acted on.

flat_to_npc (*vec*)

Convert flat vector of selected charge sector into npc Array.

Parameters *vec* (*1D ndarray*) – Numpy vector to be converted. Should have the entries according to *self.charge_sector*.

Returns *npc_vec* – Same as *vec*, but converted into a npc array.

Return type *Array*

npc_to_flat (*npc_vec*)

Convert npc Array with *qtotal = self.charge_sector* into ndarray.

Parameters *npc_vec* (*Array*) – Npc Array to be converted. Should only have entries in *self.charge_sector*.

Returns *vec* – Same as *npc_vec*, but converted into a flat Numpy array.

Return type *1D ndarray*

flat_to_npc_all_sectors (*vec*)

Convert flat vector of *all* charge sectors into npc Array with extra “charge” leg.

Parameters *vec* (*1D ndarray*) – Numpy vector to be converted.

Returns *npc_vec* – Same as *vec*, but converted into a npc array.

Return type *Array*

flat_to_npc_None_sector (*vec*)

Convert flat vector of undetermined charge sectors into npc Array.

The charge sector to be used is chosen as the block with the maximal norm, not by *self.charge_sector* (which might be *None*).

Parameters `vec` (1D *ndarray*) – Numpy vector to be converted.

Returns `npc_vec` – Same as `vec`, but converted into a npc array.

Return type *Array*

`npc_to_flat_all_sectors` (*npc_vec*)

Convert npc Array with `qtotal = self.charge_sector` into ndarray.

Parameters `npc_vec` (*Array*) – Npc Array to be converted. Should only have entries in `self.charge_sector`.

Returns `vec` – Same as `npc_vec`, but converted into a flat Numpy array.

Return type 1D ndarray

property `H`

Hermitian adjoint.

Returns the Hermitian adjoint of self, aka the Hermitian conjugate or Hermitian transpose. For a complex matrix, the Hermitian adjoint is equal to the conjugate transpose.

Can be abbreviated `self.H` instead of `self.adjoint()`.

Returns `A_H` – Hermitian adjoint of self.

Return type *LinearOperator*

property `T`

Transpose this linear operator.

Returns a *LinearOperator* that represents the transpose of this one. Can be abbreviated `self.T` instead of `self.transpose()`.

`adjoint` ()

Hermitian adjoint.

Returns the Hermitian adjoint of self, aka the Hermitian conjugate or Hermitian transpose. For a complex matrix, the Hermitian adjoint is equal to the conjugate transpose.

Can be abbreviated `self.H` instead of `self.adjoint()`.

Returns `A_H` – Hermitian adjoint of self.

Return type *LinearOperator*

`dot` (*x*)

Matrix-matrix or matrix-vector multiplication.

Parameters `x` (*array_like*) – 1-d or 2-d array, representing a vector or matrix.

Returns `Ax` – 1-d or 2-d array (depending on the shape of `x`) that represents the result of applying this linear operator on `x`.

Return type *array*

`matmat` (*X*)

Matrix-matrix multiplication.

Performs the operation $y=A*X$ where `A` is an $M \times N$ linear operator and `X` dense $N \times K$ matrix or ndarray.

Parameters `X` (*{matrix, ndarray}*) – An array with shape (N,K).

Returns `Y` – A matrix or ndarray with shape (M,K) depending on the type of the `X` argument.

Return type *{matrix, ndarray}*

Notes

This `matmat` wraps any user-specified `matmat` routine or overridden `_matmat` method to ensure that `y` has the correct type.

matvec (*x*)

Matrix-vector multiplication.

Performs the operation $y=A*x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array.

Parameters **x** (*{matrix, ndarray}*) – An array with shape (N,) or (N,1).

Returns **y** – A matrix or ndarray with shape (M,) or (M,1) depending on the type and shape of the `x` argument.

Return type {matrix, ndarray}

Notes

This `matvec` wraps the user-specified `matvec` routine or overridden `_matvec` method to ensure that `y` has the correct shape and type.

rmatmat (*X*)

Adjoint matrix-matrix multiplication.

Performs the operation $y = A^H * x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array, or 2-d array. The default implementation defers to the adjoint.

Parameters **x** (*{matrix, ndarray}*) – A matrix or 2D array.

Returns **Y** – A matrix or 2D array depending on the type of the input.

Return type {matrix, ndarray}

Notes

This `rmatmat` wraps the user-specified `rmatmat` routine.

rmatvec (*x*)

Adjoint matrix-vector multiplication.

Performs the operation $y = A^H * x$ where A is an $M \times N$ linear operator and x is a column vector or 1-d array.

Parameters **x** (*{matrix, ndarray}*) – An array with shape (M,) or (M,1).

Returns **y** – A matrix or ndarray with shape (N,) or (N,1) depending on the type and shape of the `x` argument.

Return type {matrix, ndarray}

Notes

This `rmatvec` wraps the user-specified `rmatvec` routine or overridden `_rmatvec` method to ensure that `y` has the correct shape and type.

`transpose()`

Transpose this linear operator.

Returns a `LinearOperator` that represents the transpose of this one. Can be abbreviated `self.T` instead of `self.transpose()`.

NpcLinearOperator

- full name: `tenpy.linalg.sparse.NpcLinearOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram

```

class NpcLinearOperator

```

Methods

<code>NpcLinearOperator.__init__</code>	Initialize self.
<code>NpcLinearOperator.adjoint()</code>	Return the hermitian conjugate of <i>self</i>
<code>NpcLinearOperator.matvec(vec)</code>	Calculate the action of the operator on a vector <i>vec</i> .
<code>NpcLinearOperator.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

<code>NpcLinearOperator.acts_on</code>
--

`class tenpy.linalg.sparse.NpcLinearOperator`

Bases: `object`

Prototype for a Linear Operator acting on `Array`.

Note that an `Array` implements a `matvec` function. Thus you can use any (square) `npc` `Array` as an `NpcLinearOperator`.

`dtype`

The data type of its action.

Type `np.type`

acts_on

Labels of the state on which the operator can act. NB: Class attribute.

Type list of str

matvec (*vec*)

Calculate the action of the operator on a vector *vec*.

Note that we don't require *vec* to be one-dimensional. However, for square operators we require that the result of *matvec* has the same legs (in the same order) as *vec* such that they can be added. Note that this excludes a non-trivial *qtotal* for square operators.

to_matrix ()

Contract *self* to a matrix.

If *self* represents an operator with very small shape, e.g. because the MPS bond dimension is very small, an algorithm might choose to contract *self* to a single tensor.

Returns **matrix** – Contraction of the represented operator.

Return type `Array`

adjoint ()

Return the hermitian conjugate of *self*

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

NpcLinearOperatorWrapper

- full name: `tenpy.linalg.sparse.NpcLinearOperatorWrapper`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram

NpcLinearOperatorWrapper

Methods

<code>NpcLinearOperatorWrapper.__init__(orig_operator)</code>	Initialize self.
<code>NpcLinearOperatorWrapper.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>NpcLinearOperatorWrapper.to_matrix()</code>	Contract <i>self</i> to a matrix.
<code>NpcLinearOperatorWrapper.unwrapped()</code>	Return to the original NpcLinearOperator.

class `tenpy.linalg.sparse.NpcLinearOperatorWrapper` (*orig_operator*)

Bases: `object`

Base class for wrapping around another `NpcLinearOperator`.

Attributes not explicitly set with *self.attribute = value* (or by defining methods) default to the attributes of the wrapped *orig_operator*.

Warning: If there are multiple levels of wrapping operators, the order might be critical to get correct results; e.g. `OrthogonalNpcLinearOperator` needs to be the outer-most wrapper to produce correct results and/or be efficient.

Parameters `orig_operator` (`NpcLinearOperator`) – The original operator implementing the *matvec*.

orig_operator

The original operator implementing the *matvec*.

Type `NpcLinearOperator`

unwrapped()

Return to the original `NpcLinearOperator`.

If multiple levels of wrapping were used, this returns the most unwrapped one.

to_matrix()

Contract *self* to a matrix.

adjoint()

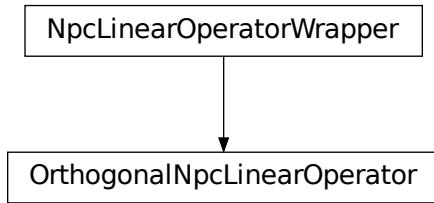
Return the hermitian conjugate of *self*.

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

OrthogonalNpcLinearOperator

- full name: `tenpy.linalg.sparse.OrthogonalNpcLinearOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram



Methods

<code>OrthogonalNpcLinearOperator.__init__(...)</code>	Initialize <i>self</i> .
<code>OrthogonalNpcLinearOperator.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>OrthogonalNpcLinearOperator.matvec(vec)</code>	
<code>OrthogonalNpcLinearOperator.to_matrix()</code>	Contract <i>self</i> to a matrix.
<code>OrthogonalNpcLinearOperator.unwrapped()</code>	Return to the original <code>NpcLinearOperator</code> .

class `tenpy.linalg.sparse.OrthogonalNpcLinearOperator` (*orig_operator*, *ortho_vecs*)

Bases: `tenpy.linalg.sparse.NpcLinearOperatorWrapper`

Replace $H \rightarrow P H P$ with the projector $P = 1 - \sum_o |o\rangle \langle o|$.

Here, $|o\rangle$ are the vectors from `ortho_vecs`.

Parameters

- **orig_operator** (`EffectiveH`) – The original *EffectiveH* instance to wrap around.
- **ortho_vecs** (list of `Array`) – The vectors to orthogonalize against.

to_matrix()

Contract *self* to a matrix.

adjoint()

Return the hermitian conjugate of *self*.

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

unwrapped()

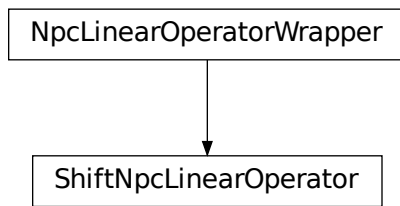
Return to the original `NpcLinearOperator`.

If multiple levels of wrapping were used, this returns the most unwrapped one.

ShiftNpcLinearOperator

- full name: `tenpy.linalg.sparse.ShiftNpcLinearOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram



Methods

<code>ShiftNpcLinearOperator.__init__(...)</code>	Initialize self.
<code>ShiftNpcLinearOperator.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>ShiftNpcLinearOperator.matvec(vec)</code>	
<code>ShiftNpcLinearOperator.to_matrix()</code>	Contract <i>self</i> to a matrix.
<code>ShiftNpcLinearOperator.unwrapped()</code>	Return to the original NpcLinearOperator.

class `tenpy.linalg.sparse.ShiftNpcLinearOperator` (*orig_operator*, *shift*)

Bases: `tenpy.linalg.sparse.NpcLinearOperatorWrapper`

Represents `original_operator + shift * identity`.

This can be useful e.g. for better Lanczos convergence.

to_matrix()

Contract *self* to a matrix.

adjoint()

Return the hermitian conjugate of *self*.

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

unwrapped()

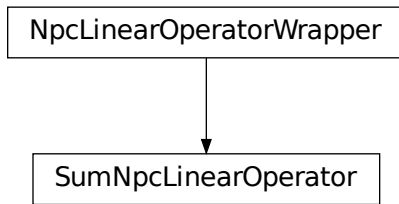
Return to the original NpcLinearOperator.

If multiple levels of wrapping were used, this returns the most unwrapped one.

SumNpcLinearOperator

- full name: `tenpy.linalg.sparse.SumNpcLinearOperator`
- parent module: `tenpy.linalg.sparse`
- type: class

Inheritance Diagram



Methods

<code>SumNpcLinearOperator.__init__(orig_operator, ...)</code>	Initialize self.
<code>SumNpcLinearOperator.adjoint()</code>	Return the hermitian conjugate of <i>self</i> .
<code>SumNpcLinearOperator.matvec(vec)</code>	
<code>SumNpcLinearOperator.to_matrix()</code>	Contract <i>self</i> to a matrix.
<code>SumNpcLinearOperator.unwrapped()</code>	Return to the original NpcLinearOperator.

class `tenpy.linalg.sparse.SumNpcLinearOperator` (*orig_operator*, *other_operator*)

Bases: `tenpy.linalg.sparse.NpcLinearOperatorWrapper`

Sum of two linear operators.

to_matrix ()

Contract *self* to a matrix.

adjoint ()

Return the hermitian conjugate of *self*.

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

unwrapped ()

Return to the original NpcLinearOperator.

If multiple levels of wrapping were used, this returns the most unwrapped one.

Module description

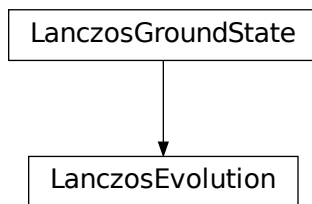
Providing support for sparse algorithms (using matrix-vector products only).

Some linear algebra algorithms, e.g. Lanczos, do not require the full representations of a linear operator, but only the action on a vector, i.e., a matrix-vector product *matvec*. Here we define the structure of such a general operator, *NpcLinearOperator*, as it is used in our own implementations of these algorithms (e.g., *lanczos*). Moreover, the *FlatLinearOperator* allows to use all the *scipy* sparse methods by providing functionality to convert flat *numpy* arrays to and from *np_conserved* arrays.

7.8.6 lanczos

- full name: `tenpy.linalg.lanczos`
- parent module: `tenpy.linalg`
- type: module

Classes



<code>LanczosEvolution(H, psi0, options)</code>	Calculate $\exp(\delta H) \psi_0\rangle$ using Lanczos.
<code>LanczosGroundState(H, psi0, options[, ...])</code>	Lanczos algorithm working on <i>npc</i> arrays.

Functions

<code>gram_schmidt(vecs[, rcond, verbose])</code>	In place Gram-Schmidt Orthogonalization and normalization for <i>npc</i> Arrays.
<code>lanczos(H, psi[, options, orthogonal_to])</code>	Simple wrapper calling <code>LanczosGroundState(H, psi, options, orthogonal_to).run()</code>
<code>lanczos_arnpack(H, psi[, options, orthogonal_to])</code>	Use <code>scipy.sparse.linalg.eigsh()</code> to find the ground state of <i>H</i> .
<code>plot_stats(ax, Es)</code>	Plot the convergence of the energies.

gram_schmidt

- full name: `tenpy.linalg.lanczos.gram_schmidt`
- parent module: `tenpy.linalg.lanczos`
- type: function

`tenpy.linalg.lanczos.gram_schmidt` (*vecs*, *rcond*=*1e-14*, *verbose*=0)

In place Gram-Schmidt Orthogonalization and normalization for npc Arrays.

Parameters

- **vecs** (list of *Array*) – The vectors which should be orthogonalized. All with the same *order* of the legs. Entries are modified *in place*. if a norm < *rcond*, the entry is set to *None*.
- **rcond** (*float*) – Vectors of norm < *rcond* (after projecting out previous vectors) are discarded.
- **verbose** (*int*) – Print additional output if *verbose* >= 1.

Returns

- **vecs** (list of *Array*) – The ortho-normalized vectors (without any *None*).
- **ov** (2D *Array*) – For *j* >= *i*, `ov[j, i] = npc.inner(vecs[j], vecs[i], 'range', do_conj=True)` (where `vecs[j]` was orthogonalized to all `vecs[k]`, *k* < *i*).

lanczos

- full name: `tenpy.linalg.lanczos.lanczos`
- parent module: `tenpy.linalg.lanczos`
- type: function

`tenpy.linalg.lanczos.lanczos` (*H*, *psi*, *options*={}, *orthogonal_to*=[])

Simple wrapper calling `LanczosGroundState(H, psi, options, orthogonal_to).run()`

Deprecated since version 0.6.0: Going to remove the *orthogonal_to* argument. Instead, replace *H* with *OrthogonalNpcLinearOperator(H, orthogonal_to)* using the *OrthogonalNpcLinearOperator*.

Parameters *psi*, *options*, *orthogonal_to* (*H*,) – See `LanczosGroundState`.

Returns See `LanczosGroundState.run()`.

Return type *E0*, *psi0*, *N*

lanczos_arnoldi

- full name: `tenpy.linalg.lanczos.lanczos_arnoldi`
- parent module: `tenpy.linalg.lanczos`
- type: function

`tenpy.linalg.lanczos.lanczos_arnoldi` (*H*, *psi*, *options*={}, *orthogonal_to*=[])

Use `scipy.sparse.linalg.eigsh()` to find the ground state of *H*.

This function has the same call/return structure as `lanczos()`, but uses the ARPACK package through the functions `speigsh()` instead of the custom lanczos implementation in `LanczosGroundState`. This function is mostly intended for debugging, since it requires to convert the vector from `np_conserved Array` into a flat numpy array and back during *each matvec*-operation!

Deprecated since version 0.6.0: Going to remove the `orthogonal_to` argument. Instead, replace `H` with `OrthogonalNpcLinearOperator(H, orthogonal_to)` using the `OrthogonalNpcLinearOperator`.

Parameters `psi`, `options`, `orthogonal_to` (`H`,) – See `LanczosGroundState`. `H` and `psi` should have/use labels.

Returns

- `E0` (*float*) – Ground state energy.
- `psi0` (*Array*) – Ground state vector.

plot_stats

- full name: `tenpy.linalg.lanczos.plot_stats`
- parent module: `tenpy.linalg.lanczos`
- type: function

`tenpy.linalg.lanczos.plot_stats(ax, Es)`

Plot the convergence of the energies.

Parameters

- `ax` (`matplotlib.axes.Axes`) – The axes on which we should plot.
- `Es` (*list of ndarray.*) – The energies `Lanczos.Es`.

Module description

Lanczos algorithm for `np_conserved` arrays.

7.9 models

- full name: `tenpy.models`
- parent module: `tenpy`
- type: module

Module description

Definition of the various models.

For an introduction to models see [Models](#).

The module `tenpy.models.model` contains base classes for models. The module `tenpy.models.lattice` contains base classes and implementations of lattices. All other modules in this folder contain model classes derived from these base classes.

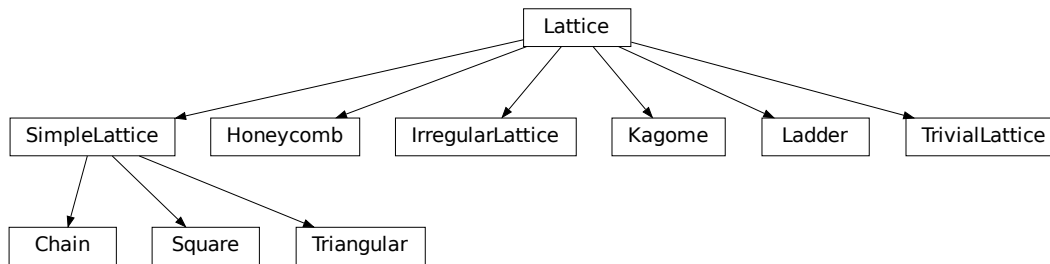
Submodules

<code>lattice</code>	Classes to define the lattice structure of a model.
<code>model</code>	This module contains some base classes for models.

7.9.1 lattice

- full name: `tenpy.models.lattice`
- parent module: `tenpy.models`
- type: module

Classes

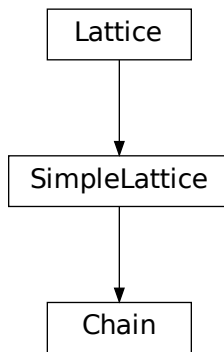


<code>Chain(L, site, **kwargs)</code>	A chain of L equal sites.
<code>Honeycomb(Lx, Ly, sites, **kwargs)</code>	A honeycomb lattice.
<code>IrregularLattice(regular_lattice[, remove, ...])</code>	A variant of a regular lattice, where we might have extra sites or sites missing.
<code>Kagome(Lx, Ly, sites, **kwargs)</code>	A Kagome lattice.
<code>Ladder(L, sites, **kwargs)</code>	A ladder coupling two chains.
<code>Lattice(Ls, unit_cell[, order, bc, bc_MPS, ...])</code>	A general, regular lattice.
<code>SimpleLattice(Ls, site, **kwargs)</code>	A lattice with a unit cell consisting of just a single site.
<code>Square(Lx, Ly, site, **kwargs)</code>	A square lattice.
<code>Triangular(Lx, Ly, site, **kwargs)</code>	A triangular lattice.
<code>TrivialLattice(mps_sites, **kwargs)</code>	Trivial lattice consisting of a single (possibly large) unit cell in 1D.

Chain

- full name: `tenpy.models.lattice.Chain`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>Chain.__init__(L, site, **kwargs)</code>	Initialize self.
<code>Chain.count_neighbors([u, key])</code>	Count e.g.
<code>Chain.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Chain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Chain.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Chain.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Chain.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Chain.mps2lat_values(A[, axes, u])</code>	same as <code>Lattice.mps2lat_values()</code> , but ignore u , setting it to 0.
<code>Chain.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Chain.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>Chain.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Chain.mps_sites()</code>	Return a list of sites for all MPS indices.

continues on next page

Table 76 – continued from previous page

<code>Chain.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Chain.number_nearest_neighbors([u])</code>	Deprecated.
<code>Chain.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Chain.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Chain.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Chain.plot_bc_identified(ax[, direction, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>Chain.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Chain.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Chain.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Chain.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Chain.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Chain.possible_multi_couplings(ops)</code>	Generalization of possible_couplings() to couplings with more than 2 sites.
<code>Chain.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Chain.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index i
<code>Chain.test_sanity()</code>	Sanity check.

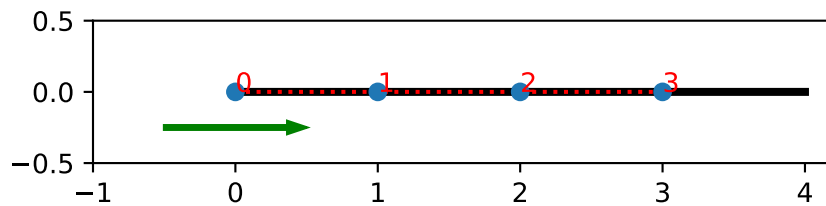
Class Attributes and Properties

<code>Chain.boundary_conditions</code>	Human-readable list of boundary conditions from bc and bc_shift.
<code>Chain.dim</code>	
<code>Chain.nearest_neighbors</code>	
<code>Chain.next_nearest_neighbors</code>	
<code>Chain.next_next_nearest_neighbors</code>	
<code>Chain.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Chain` (L , *site*, ***kwargs*)

Bases: `tenpy.models.lattice.SimpleLattice`

A chain of L equal sites.



Parameters

- **L** (*int*) – The length of the chain.
- **site** (*Site*) – The local lattice site. The *unit_cell* of the *Lattice* is just [*site*].

- ****kwargs** – Additional keyword arguments given to the `Lattice`. `pairs` are initialize with `[next_]next_]nearest_neighbors`. `positions` can be specified as a single vector.

ordering (*order*)

Provide possible orderings of the N lattice sites.

The following orders are defined in this method compared to `Lattice.ordering()`:

<i>order</i>	Resulting order
'default'	0, 1, 2, 3, 4, ... , L-1
'folded'	0, L-1, 1, L-2, ... , L//2. This order might be usefull if you want to consider a ring with periodic boundary conditions with a finite MPS: It avoids the ultra-long range of the coupling from site 0 to L present in the default order.

property boundary_conditions

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of `pairs` to select what to count.

Returns `number` – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type `int`

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in

the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

classmethod `from_hdf5` (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type `cls`

lat2mps_idx (*lat_idx*)

Translate lattice indices $(x_0, \dots, x_{\{D-1\}}, u)$ to MPS index i .

Parameters **lat_idx** (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices $(x_0, \dots, x_{\{D-1\}}, u)$. All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an x_0 outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type `array_like`

mps2lat_idx (*i*)

Translate MPS index i to lattice indices $(x_0, \dots, x_{\{dim-1\}}, u)$.

Parameters **i** (*int | array_like of int*) – MPS index/indices.

Returns **lat_idx** – First dimensions like i , last dimension has len $dim+1$ and contains the lattice indices ```(x_0, ..., x_{dim-1}, u)``` corresponding to i . For i accross the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.

Return type `array`

mps2lat_values (*A*, *axes=0*, *u=None*)

same as `Lattice.mps2lat_values()`, but ignore u , setting it to 0.

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array A to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of A .

Parameters

- **A** (*ndarray*) – Some values.
- **axes** (*(iterable of) int*) – Chooses the axis of A which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** (*(list of) 1D ndarray*) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of A . Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.

- **include_u** (*(list of) bool*) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by *self.unit_cell[u]*.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns *mps_idx* – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type `array`

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

mps_sites ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (*2D array*, shape (*N_ops*, *dim*)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

plot_basis (*ax, origin=0.0, 0.0, shade=None, **kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax, direction=-1, origin=None, cylinder_axis=False, **kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If `None`, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None | np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot()`.

plot_coupling (*ax, coupling=None, wrap=False, **kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (`None`), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If `True`, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax, order=None, textkwargs={}, **kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None | 2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (`None`) use `order`.

- **textkwargs** (None | dict) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return 'space' position of one or multiple sites.

Parameters *lat_idx* (`ndarray`, (... , dim+1)) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray`, (... , dim)

possible_couplings (*u1*, *u2*, *dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `LS[a]` and runs through `range(LS[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < LS[a]` and `0 <= x_a+dx[a] < lat.LS[a]`.

Parameters

- **u2** (*u1*,) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length dim. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (list of (opname, dx, u)) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices *i,j,k,l,...* for each of the operators positions. The positions are defined by *dx* (*j,k,l,...* relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a ' / ' in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

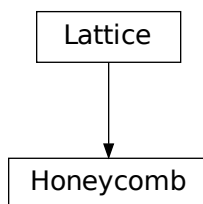
Sanity check.

Raises *ValueErrors*, if something is wrong.

Honeycomb

- full name: `tenpy.models.lattice.Honeycomb`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>Honeycomb.__init__(Lx, Ly, sites, **kwargs)</code>	Initialize self.
<code>Honeycomb.count_neighbors([u, key])</code>	Count e.g.
<code>Honeycomb.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Honeycomb.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Honeycomb.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Honeycomb.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Honeycomb.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Honeycomb.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>Honeycomb.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Honeycomb.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>Honeycomb.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Honeycomb.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Honeycomb.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Honeycomb.number_nearest_neighbors([u])</code>	Deprecated.
<code>Honeycomb.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Honeycomb.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Honeycomb.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Honeycomb.plot_bc_identified(ax[, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>Honeycomb.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Honeycomb.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Honeycomb.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Honeycomb.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Honeycomb.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Honeycomb.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Honeycomb.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Honeycomb.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index i
<code>Honeycomb.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>Honeycomb.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Honeycomb.dim</code>	
<code>Honeycomb.fifth_nearest_neighbors</code>	
<code>Honeycomb.fourth_nearest_neighbors</code>	
<code>Honeycomb.nearest_neighbors</code>	
<code>Honeycomb.next_nearest_neighbors</code>	
<code>Honeycomb.next_next_nearest_neighbors</code>	
<code>Honeycomb.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Honeycomb` (*Lx*, *Ly*, *sites*, ****kwargs**)

Bases: `tenpy.models.lattice.Lattice`

A honeycomb lattice.

Parameters

- **Ly** (*Lx*,) – The length in each direction.
- **sites** ((list of) *Site*) – The two local lattice sites making the *unit_cell* of the *Lattice*. If only a single *Site* is given, it is used for both sites.
- ****kwargs** – Additional keyword arguments given to the *Lattice*. *basis*, *pos* and *pairs* are set accordingly. For the Honeycomb lattice 'fourth_nearest_neighbors', 'fifth_nearest_neighbors' are set in *pairs*.

ordering (*order*)

Provide possible orderings of the *N* lattice sites.

The following orders are defined in this method compared to `Lattice.ordering()`:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'default'	(0, 2, 1)	(False, False, False)
'snake'	(0, 2, 1)	(False, True, False)

property `boundary_conditions`

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

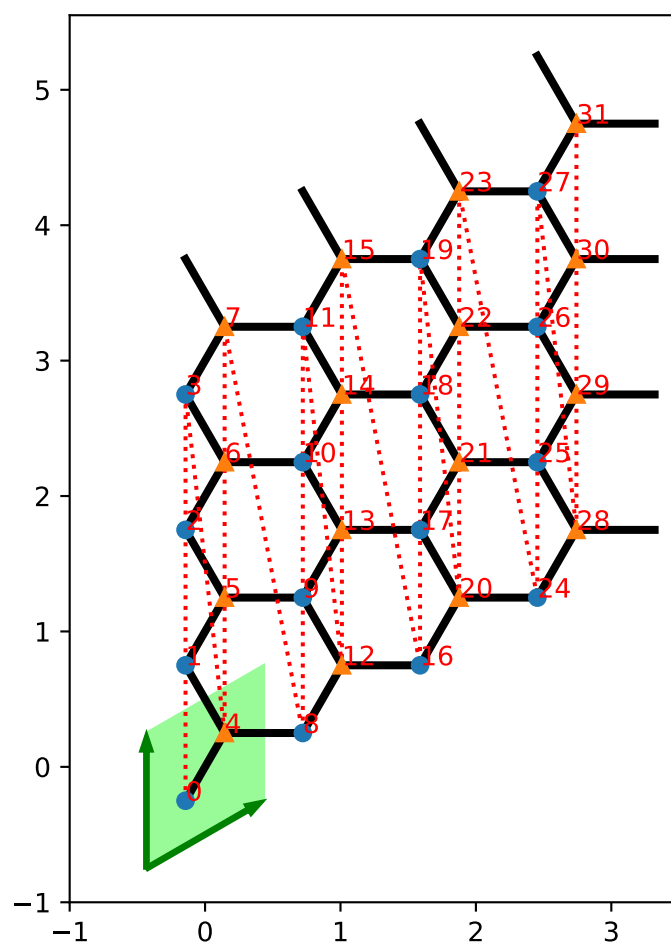
Return type list of str

`count_neighbors` (*u=0*, *key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of *pairs* to select what to count.



Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type `int`

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod **from_hdf5** (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type `cls`

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters **lat_idx** (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an *x_0* outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type `array_like`

mps2lat_idx (*i*)

Translate MPS index *i* to lattice indices (*x_0*, ..., *x_{dim-1}*, *u*).

Parameters **i** (*int | array_like of int*) – MPS index/indices.

Returns `lat_idx` – First dimensions like i , last dimension has $\text{len } \text{dim} + 1$ and contains the lattice indices `((x_0, ..., x_{dim-1}, u))` corresponding to i . For i across the MPS unit cell and “infinite” `bc_MPS`, we shift x_0 accordingly.

Return type array

mps2lat_values (A , $\text{axes}=0$, $u=\text{None}$)

Reshape/reorder A to replace an MPS index by lattice indices.

Parameters

- **A** (`ndarray`) – Some values. Must have $A.\text{shape}[\text{axes}] = \text{self.N_sites}$ if u is `None`, or $A.\text{shape}[\text{axes}] = \text{self.N_cells}$ if u is an `int`.
- **axes** (`(iterable of) int`) – chooses the axis which should be replaced.
- **u** (`None | int`) – Optionally choose a subset of MPS indices present in the axes of A , namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of u .

Returns `res_A` – Reshaped and reordered versions of A . Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type `ndarray`

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array A , where $A[i]$ is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument u of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** ((*iterable of int*) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** ((*list of 1D ndarray*) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** ((*list of bool*) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters *u* (*None | int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns *mps_idx* – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type `array`

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None | int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

mps_sites ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (2D array, shape (N_ops, dim)) – *dx*[*i*, :] is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

plot_basis (*ax*, *origin=0.0, 0.0*, *shade=None*, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction=-1*, *origin=None*, *cylinder_axis=False*, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If *None*, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None* | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling=None*, *wrap=False*, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (`None`), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If `True`, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax, order=None, textkwargs={}, **kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None | 2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (`None`) use `order`.
- **textkwargs** (*None | dict*) – If not `None`, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax, markers=['o', '^', 's', 'p', 'h', 'D'], **kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters *lat_idx* (`ndarray, (... , dim+1)`) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray, (... , dim)`

possible_couplings (*u1, u2, dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `LS[a]` and runs through `range(LS[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < LS[a]` and `0 <= x_a+dx[a] < lat.LS[a]`.

Parameters

- **u2** (*u1,)* – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.

- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of *possible_couplings()* to couplings with more than 2 sites.

Parameters **ops** (list of (opname, dx, u)) – Same as the argument *ops* of *add_multi_coupling()*.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices i, j, k, l, \dots for each of the operators positions. The positions are defined by *dx* (j,k,l,... relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, pairs under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

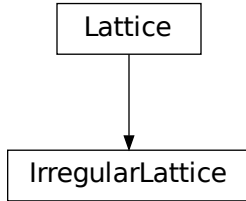
Sanity check.

Raises *ValueErrors*, if something is wrong.

IrregularLattice

- full name: *tenpy.models.lattice.IrregularLattice*
- parent module: *tenpy.models.lattice*
- type: class

Inheritance Diagram



Methods

<code>IrregularLattice.__init__(regular_lattice[, ...])</code>	Initialize self.
<code>IrregularLattice.count_neighbors([u, key])</code>	Count e.g.
<code>IrregularLattice.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>IrregularLattice.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>IrregularLattice.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>IrregularLattice.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>IrregularLattice.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>IrregularLattice.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>IrregularLattice.mps2lat_values_masked(A[, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>IrregularLattice.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>IrregularLattice.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>IrregularLattice.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>IrregularLattice.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>IrregularLattice.number_nearest_neighbors([u])</code>	Deprecated.
<code>IrregularLattice.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>IrregularLattice.ordering(order)</code>	Provide possible orderings of the lattice sites.
<code>IrregularLattice.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>IrregularLattice.plot_bc_identified(ax[, ...])</code>	Mark two sites indified by periodic boundary conditions.

continues on next page

Table 80 – continued from previous page

<code>IrregularLattice.plot_coupling(ax[, ...])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>IrregularLattice.plot_order(ax[, order, ...])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>IrregularLattice.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>IrregularLattice.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>IrregularLattice.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>IrregularLattice.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>IrregularLattice.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>IrregularLattice.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index <i>i</i>
<code>IrregularLattice.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>IrregularLattice.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>IrregularLattice.dim</code>	The dimension of the lattice.
<code>IrregularLattice.nearest_neighbors</code>	
<code>IrregularLattice.next_nearest_neighbors</code>	
<code>IrregularLattice.next_next_nearest_neighbors</code>	
<code>IrregularLattice.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.IrregularLattice` (*regular_lattice*, *remove=None*, *add=None*, *add_unit_cell=[]*, *add_positions=None*)

Bases: `tenpy.models.lattice.Lattice`

A variant of a regular lattice, where we might have extra sites or sites missing.

Note: The lattice defines only the geometry of the sites, not the couplings; you can have position-dependent couplings/onsite terms despite having a regular lattice.

By adjusting the `order` and a few private attributes and methods, we can make functions like `possible_couplings()` work with a more “irregular” lattice structure, where some of the sites are missing and other sites added instead.

Parameters

- **regular_lattice** (*Lattice*) – The lattice this is based on.
- **remove** (*2D array* | *None*) – Each row is a lattice index (`x_0`, ..., `x_{dim-1}`, `u`) of a site to be removed. If *None*, don’t remove something.
- **add** (*Tuple[2D array, list]* | *None*) – Each row of the 2D array is a lattice index (`x_0`, ..., `x_{dim-1}`, `u`) specifying where a site is to be added; *u* is the index of the site within the final `unit_cell` of the irregular lattice. For each row of the 2D array, there is one entry in the list specifying where the site is inserted in the MPS; the values are compared to the MPS indices of the *regular* lattice and sorted into it, so “2.5”

goes between what was site 2 and 3 in the regular lattice. An entry *None* indicates that the site should be inserted after the lattice site $(x_0, \dots, x_{\{\text{dim}-1\}}, -1)$ of the *regular_lattice*.

- **add_unit_cell** (list of *Site*) – Extra sites to be added to the unit cell.
- **add_positions** (*iterable of 1D arrays*) – For each extra site in *add_unit_cell* the position within the unit cell. Defaults to `np.zeros((len(add_unit_cell), dim))`.

regular_lattice

The lattice this is based on.

Type *Lattice*

remove, add

See above. Used in *ordering()* only.

Type 2D array | None

Examples

Let's imagine that we have two different sites; for concreteness we can think of a fermion site, which we represent with 'F', and a spin site 'S'.

You could now imagine that to have fermion chain with spins on the “bonds”. In the periodic/infinite case, you would simply define

```
>>> lat = Lattice([2], unit_cell=['F', 'S'], bc='periodic', bc_MPS='infinite')
>>> lat.mps_sites()
['F', 'S', 'F', 'S']
```

For a finite system, you don't want to terminate with a spin on the right, so you need to remove the very last site by specifying the lattice index `[L-1, 1]` of that site:

```
>>> L = 4
>>> reg_lat = Lattice([L], unit_cell=['F', 'S'], bc='open', bc_MPS='finite')
>>> irr_lat = IrregularLattice(reg_lat, remove=[[L-1, 1]])
>>> irr_lat.mps_sites()
['F', 'S', 'F', 'S', 'F', 'S', 'F']
```

Another simple example would be to add a spin in the center of a fermion chain. In that case, we add another site to the unit cell and specify the lattice index as `[(L-1)//2, 1]` (where the 1 is the index of 'S' in the unit cell `['F', 'S']` of the irregular lattice). The *None* for the MPS index is equivalent to $(L-1)/2$ in this case.

```
>>> reg_lat = Lattice([L], unit_cell=['F'])
>>> irr_lat = IrregularLattice(reg_lat, add=[[ (L-1)//2, 1]], [None]),
...                                     add_unit_cell=['S'])
['F', 'F', 'S', 'F', 'F']
```

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves `unit_cell`, `Ls`, `unit_cell_positions`, `basis`, *boundary_conditions*, *pairs* under their name, `bc_MPS` as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and `N_sites` as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

ordering (*order*)

Provide possible orderings of the lattice sites.

Parameters *order* – Argument for the *Lattice.ordering()* of the *regular_lattice*, or 2D ndarray providing the order of the *regular lattice*.

Returns *order* – The order to be used for *order*, i.e. *order* with added/removed sites as specified by *remove* and *add*.

Return type *array*, shape (N, D+1)

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through through the lattice.

You can visualize the order with *plot_order()*.

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by *self.unit_cell[u]*.

Parameters *u* (*None* / *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns *mps_idx* – MPS indices for which *self.site(i)* is *self.unit_cell[u]*. Ordered ascending.

Return type *array*

property boundary_conditions

Human-readable list of boundary conditions from *bc* and *bc_shift*.

Returns *boundary_conditions* – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of pairs to select what to count.

Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

property dim

The dimension of the lattice.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters **lat_idx** (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an *x_0* outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type *array_like*

mps2lat_idx (*i*)

Translate MPS index *i* to lattice indices (*x_0*, ..., *x_{dim-1}*, *u*).

Parameters **i** (*int | array_like of int*) – MPS index/indices.

Returns **lat_idx** – First dimensions like *i*, last dimension has len *dim`+1* and contains the lattice indices ``(x_0, ..., x_{dim-1}, u)`` corresponding to *i*. For *i* accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.

Return type array

mps2lat_values (*A*, *axes=0*, *u=None*)

Reshape/reorder *A* to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have `A.shape[axes] = self.N_sites` if *u* is `None`, or `A.shape[axes] = self.N_cells` if *u* is an int.
- **axes** (*iterable of int*) – chooses the axis which should be replaced.
- **u** (`None` | *int*) – Optionally choose a subset of MPS indices present in the axes of *A*, namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of *u*.

Returns **res_A** – Reshaped and reordered versions of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type ndarray

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you a 1D array *A*, where *A[i]* is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument *u* of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** (*(iterable of) int*) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** (*(list of) 1D ndarray*) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices across the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** (*(list of) bool*) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

mps_sites ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (*2D array*, shape (*N_ops*, *dim*)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

plot_basis (*ax, origin=0.0, 0.0, shade=None, **kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax, direction=-1, origin=None, cylinder_axis=False, **kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If *None*, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None* | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax, coupling=None, wrap=False, **kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (*None*), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If *True*, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax, order=None, textkwargs={}, **kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None* | *2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (*None*) use `order`.
- **textkwargs** (*None* | *dict*) – If not *None*, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.

- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return 'space' position of one or multiple sites.

Parameters *lat_idx* (`ndarray, (... , dim+1)`) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray, (... , dim)`

possible_couplings (*u1*, *u2*, *dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `LS[a]` and runs through `range(LS[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < LS[a]` and `0 <= x_a+dx[a] < lat.LS[a]`.

Parameters

- **u2** (*u1*,) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (list of (*opname*, *dx*, *u*)) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices *i,j,k,l,...* for each of the operators positions. The positions are defined by *dx* (*j,k,l,...* relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

```

site (i)
    return Site instance corresponding to an MPS index i

test_sanity ()
    Sanity check.

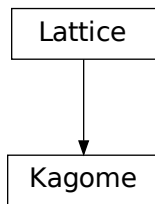
    Raises ValueErrors, if something is wrong.

```

Kagome

- full name: `tenpy.models.lattice.Kagome`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>Kagome.__init__(Lx, Ly, sites, **kwargs)</code>	Initialize self.
<code>Kagome.count_neighbors([u, key])</code>	Count e.g.
<code>Kagome.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Kagome.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Kagome.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Kagome.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index <i>i</i> .
<code>Kagome.mps2lat_idx(i)</code>	Translate MPS index <i>i</i> to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Kagome.mps2lat_values(A[, axes, u])</code>	Reshape/reorder <i>A</i> to replace an MPS index by lattice indices.
<code>Kagome.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array <i>A</i> to replace an MPS index by lattice indices.
<code>Kagome.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is <i>u</i> .

continues on next page

Table 82 – continued from previous page

<code>Kagome.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Kagome.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Kagome.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Kagome.number_nearest_neighbors([u])</code>	Deprecated.
<code>Kagome.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Kagome.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Kagome.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Kagome.plot_bc_identified(ax[, direction, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>Kagome.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Kagome.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Kagome.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Kagome.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Kagome.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Kagome.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Kagome.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Kagome.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index i
<code>Kagome.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>Kagome.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Kagome.dim</code>	
<code>Kagome.nearest_neighbors</code>	
<code>Kagome.next_nearest_neighbors</code>	
<code>Kagome.next_next_nearest_neighbors</code>	
<code>Kagome.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Kagome` ($Lx, Ly, sites, **kwargs$)

Bases: `tenpy.models.lattice.Lattice`

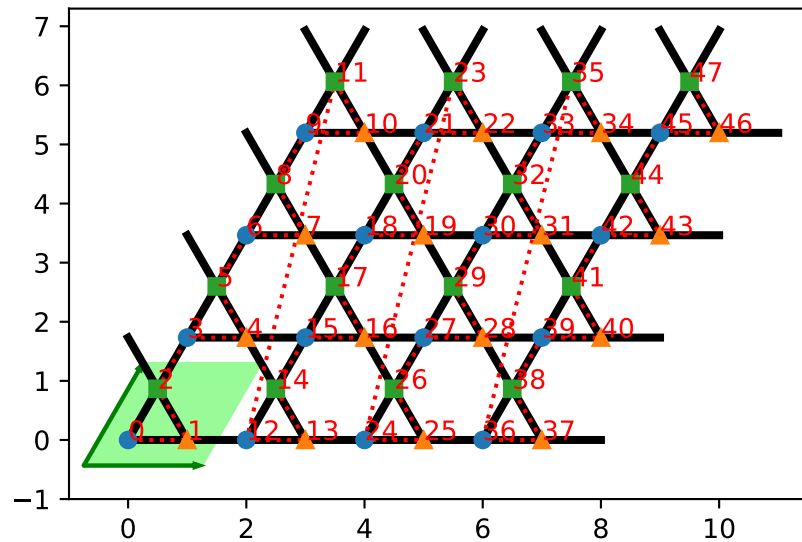
A Kagome lattice.

Parameters

- **Ly** ($Lx,$) – The length in each direction.
- **sites** ((list of) *Site*) – The two local lattice sites making the *unit_cell* of the *Lattice*. If only a single *Site* is given, it is used for both sites.
- ****kwargs** – Additional keyword arguments given to the *Lattice*. *basis*, *pos* and *pairs* are set accordingly.

property `boundary_conditions`

Human-readable list of boundary conditions from `bc` and `bc_shift`.



Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors ($u=0$, $key='nearest_neighbors'$)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of `pairs` to select what to count.

Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

coupling_shape (dx)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type *cls*

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters **lat_idx** (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and smaller than the corresponding entry in *self.shape*. Exception: for “infinite” *bc_MPS*, an *x_0* outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type *array_like*

mps2lat_idx (*i*)

Translate MPS index *i* to lattice indices (*x_0*, ..., *x_{dim-1}*, *u*).

Parameters **i** (*int | array_like of int*) – MPS index/indices.

Returns **lat_idx** – First dimensions like *i*, last dimension has len *dim*+1 and contains the lattice indices ``(x_0, ..., x_{dim-1}, u)`` corresponding to *i*. For *i* accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.

Return type *array*

mps2lat_values (*A, axes=0, u=None*)

Reshape/reorder *A* to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have *A.shape[axes] = self.N_sites* if *u* is None, or *A.shape[axes] = self.N_cells* if *u* is an int.
- **axes** (*(iterable of int)*) – chooses the axis which should be replaced.
- **u** (*None | int*) – Optionally choose a subset of MPS indices present in the axes of *A*, namely the indices corresponding to *self.unit_cell[u]*, as returned by

`mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of u .

Returns `res_A` – Reshaped and reordered versions of A . Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site $(x0, x1, x2)$, then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type ndarray

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array A , where $A[i]$ is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument u of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

`mps2lat_values_masked` (A , *axes*=-1, *mps_inds*=None, *include_u*=None)

Reshape/reorder an array A to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of A .

Parameters

- **A** (ndarray) – Some values.
- ***axes*** ((iterable of) int) – Chooses the axis of A which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.

- **mps_inds** ((list of) 1D ndarray) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices across the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** ((list of) bool) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns *mps_idx* – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type `array`

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

mps_sites ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (2D array, shape (N_ops, dim)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors ($u=0$)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors ($u=0$)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

ordering (order)

Provide possible orderings of the N lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters *order* (str | ('standard', snake_winding, priority) | ('grouped', groups)) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns *order* – the order to be used for *order*.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin=0.0, 0.0, shade=None, **kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=-1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None* | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order*=None, *textkwargs*={}, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None* | *2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (None) use `order`.
- **textkwargs** (*None* | *dict*) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters `lat_idx` (ndarray, (... , dim+1)) – Lattice indices.

Returns `pos` – The position of the lattice sites specified by `lat_idx` in real-space.

Return type ndarray, (... , dim)

possible_couplings (`u1`, `u2`, `dx`)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index `x_a` is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, `x_a` is limited to $0 \leq x_a < Ls[a]$ and $0 \leq x_a + dx[a] < lat.Ls[a]$.

Parameters

- `u2` (`u1`,) – Indices within the unit cell; the `u1` and `u2` of `add_coupling()`
- `dx` (array) – Length dim. The translation in terms of basis vectors for the coupling.

Returns

- `mps1`, `mps2` (array) – For each possible two-site coupling the MPS indices for the `u1` and `u2`.
- `lat_indices` (2D int array) – Rows of `lat_indices` correspond to rows of `mps_ijkl` and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- `coupling_shape` (tuple of int) – Len dim. The correct shape for an array specifying the coupling strength. `lat_indices` has only rows within this shape.

possible_multi_couplings (`ops`)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters `ops` (list of (opname, dx, u)) – Same as the argument `ops` of `add_multi_coupling()`.

Returns

- `mps_ijkl` (2D int array) – Each row contains MPS indices `i,j,k,l,...` for each of the operators positions. The positions are defined by `dx` (`j,k,l,...` relative to `i`) and boundary conditions of `self` (how much the `box` for given `dx` can be shifted around without hitting a boundary - these are the different rows).
- `lat_indices` (2D int array) – Rows of `lat_indices` correspond to rows of `mps_ijkl` and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- `coupling_shape` (tuple of int) – Len dim. The correct shape for an array specifying the coupling strength. `lat_indices` has only rows within this shape.

save_hdf5 (`hdf5_saver`, `h5gr`, `subpath`)

Export `self` into a HDF5 file.

This method saves all the data it needs to reconstruct `self` with `from_hdf5()`.

Specifically, it saves `unit_cell`, `Ls`, `unit_cell_positions`, `basis`, `boundary_conditions`, pairs under their name, `bc_MPS` as “boundary_conditions_MPS”, and `order` as “order_for_MPS”. Moreover, it saves `dim` and `N_sites` as HDF5 attributes.

Parameters

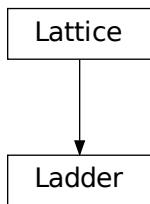
- `hdf5_saver` (`Hdf5Saver`) – Instance of the saving engine.
- `h5gr` (:class`Group`) – HDF5 group which is supposed to represent `self`.
- `subpath` (str) – The name of `h5gr` with a ‘/’ in the end.

```
site (i)  
    return Site instance corresponding to an MPS index i  
  
test_sanity ()  
    Sanity check.  
  
    Raises ValueErrors, if something is wrong.
```

Ladder

- full name: `tenpy.models.lattice.Ladder`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>Ladder.__init__(L, sites, **kwargs)</code>	Initialize self.
<code>Ladder.count_neighbors([u, key])</code>	Count e.g.
<code>Ladder.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Ladder.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Ladder.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Ladder.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Ladder.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Ladder.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>Ladder.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Ladder.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .

continues on next page

Table 84 – continued from previous page

<code>Ladder.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Ladder.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Ladder.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Ladder.number_nearest_neighbors([u])</code>	Deprecated.
<code>Ladder.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Ladder.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Ladder.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Ladder.plot_bc_identified(ax[, direction, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>Ladder.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Ladder.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Ladder.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Ladder.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Ladder.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Ladder.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Ladder.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Ladder.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index i
<code>Ladder.test_sanity()</code>	Sanity check.

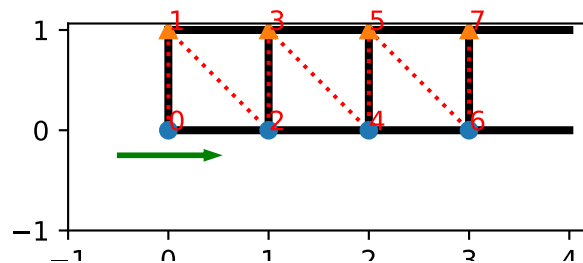
Class Attributes and Properties

<code>Ladder.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Ladder.dim</code>	
<code>Ladder.nearest_neighbors</code>	
<code>Ladder.next_nearest_neighbors</code>	
<code>Ladder.next_next_nearest_neighbors</code>	
<code>Ladder.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Ladder` (L , *sites*, ***kwargs*)

Bases: `tenpy.models.lattice.Lattice`

A ladder coupling two chains.



Parameters

- L (*int*) – The length of each chain, we have $2*L$ sites in total.

- **sites** ((list of) *Site*) – The two local lattice sites making the *unit_cell* of the *Lattice*. If only a single *Site* is given, it is used for both chains.
- ****kwargs** – Additional keyword arguments given to the *Lattice*. *basis*, *pos* and *pairs* are set accordingly.

property boundary_conditions

Human-readable list of boundary conditions from *bc* and *bc_shift*.

Returns *boundary_conditions* – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0*, *key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of *pairs* to select what to count.

Returns *number* – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

lat2mps_idx (*lat_idx*)

Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .

Parameters **lat_idx** (*array_like* [\dots , $dim+1$]) – The last dimension corresponds to lattice indices (x_0, \dots, x_{D-1}, u) . All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” `bc_MPS`, an x_0 outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type `array_like`

mps2lat_idx (*i*)

Translate MPS index i to lattice indices $(x_0, \dots, x_{dim-1}, u)$.

Parameters **i** (*int* | *array_like of int*) – MPS index/indices.

Returns **lat_idx** – First dimensions like i , last dimension has `len dim`+1` and contains the lattice indices `“(x_0, ..., x_{dim-1}, u)”` corresponding to i . For i accross the MPS unit cell and “infinite” `bc_MPS`, we shift x_0 accordingly.

Return type `array`

mps2lat_values (*A*, *axes=0*, *u=None*)

Reshape/reorder *A* to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have `A.shape[axes] = self.N_sites` if *u* is `None`, or `A.shape[axes] = self.N_cells` if *u* is an `int`.
- **axes** (*(iterable of int)*) – chooses the axis which should be replaced.
- **u** (`None` | `int`) – Optionally choose a subset of MPS indices present in the axes of *A*, namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of *u*.

Returns **res_A** – Reshaped and reordered versions of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type `ndarray`

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array *A*, where *A[i]* is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument `u` of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** ((*iterable of int*)) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** ((*list of 1D ndarray*)) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** ((*list of bool*)) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns **res_A** – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters **u** (*None* / *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns `mps_idx` – MPS indices for which `self.site(i)` is `self.unit_cell[u]`.
Ordered ascending.

Return type array

`mps_lat_idx_fix_u` (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **`mps_idx`** (array) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **`lat_idx`** (2D array) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

`mps_sites` ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

`multi_coupling_shape` (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (2D array, shape (N_ops, dim)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **`coupling_shape`** (tuple of int) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **`shift_lat_indices`** (array) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

`number_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

`number_next_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

ordering (*order*)

Provide possible orderings of the *N* lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters *order* (str | ('standard', snake_winding, priority) | ('grouped', groups)) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns *order* – the order to be used for *order*.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin*=0.0, 0.0, *shade*=None, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=-1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (None | `np.ndarray`) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.

- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax, order=None, textkwargs={}, **kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None | 2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (None) use `order`.
- **textkwargs** (*None | dict*) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax, markers=['o', '^', 's', 'p', 'h', 'D'], **kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword `marker` of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters *lat_idx* (`ndarray, (... , dim+1)`) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray, (... , dim)`

possible_couplings (*u1, u2, dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < Ls[a]` and `0 <= x_a+dx[a] < lat.Ls[a]`.

Parameters

- **u2** (*u1, ...*) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.

- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of *possible_couplings()* to couplings with more than 2 sites.

Parameters **ops** (list of (opname, dx, u)) – Same as the argument *ops* of *add_multi_coupling()*.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices i, j, k, l, \dots for each of the operators positions. The positions are defined by *dx* (j,k,l,... relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

Sanity check.

Raises *ValueErrors*, if something is wrong.

Lattice

- full name: *tenpy.models.lattice.Lattice*
- parent module: *tenpy.models.lattice*
- type: class

Inheritance Diagram

Lattice

Methods

<code>Lattice.__init__(Ls, unit_cell[, order, bc, ...])</code>	Initialize self.
<code>Lattice.count_neighbors([u, key])</code>	Count e.g.
<code>Lattice.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Lattice.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Lattice.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Lattice.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Lattice.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Lattice.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>Lattice.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Lattice.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>Lattice.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Lattice.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Lattice.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Lattice.number_nearest_neighbors([u])</code>	Deprecated.
<code>Lattice.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Lattice.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Lattice.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Lattice.plot_bc_identified(ax[, direction, ...])</code>	Mark two sites identified by periodic boundary conditions.
<code>Lattice.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Lattice.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Lattice.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Lattice.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Lattice.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Lattice.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Lattice.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Lattice.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index i

continues on next page

Table 86 – continued from previous page

<code>Lattice.test_sanity()</code>	Sanity check.
------------------------------------	---------------

Class Attributes and Properties

<code>Lattice.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Lattice.dim</code>	The dimension of the lattice.
<code>Lattice.nearest_neighbors</code>	
<code>Lattice.next_nearest_neighbors</code>	
<code>Lattice.next_next_nearest_neighbors</code>	
<code>Lattice.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

```
class tenpy.models.lattice.Lattice(Ls,      unit_cell,      order='default',      bc='open',
                                   bc_MPS='finite', basis=None, positions=None, nearest_neighbors=None,
                                   next_nearest_neighbors=None, next_next_nearest_neighbors=None, pairs=None)
```

Bases: `object`

A general, regular lattice.

The lattice consists of a **unit cell** which is repeated in `dim` different directions. A site of the lattice is thus identified by **lattice indices** $(x_0, \dots, x_{\text{dim}-1}, u)$, where $0 \leq x_l < L_s[l]$ pick the position of the unit cell in the lattice and $0 \leq u < \text{len}(\text{unit_cell})$ picks the site within the unit cell. The site is located in 'space' at $\text{sum}_l x_l * \text{basis}[l] + \text{unit_cell_positions}[u]$ (see `position()`). (Note that the position in space is only used for plotting, not for defining the couplings.)

In addition to the pure geometry, this class also defines an *order* of all sites. This order maps the lattice to a finite 1D chain and defines the geometry of MPSs and MPOs. The **MPS index** i corresponds thus to the lattice sites given by $(x_0, \dots, x_{\text{dim}-1}, u) = \text{tuple}(\text{self.order}[i])$. Infinite boundary conditions of the MPS repeat in the first spatial direction of the lattice, i.e., if the site at $(x_0, x_1, \dots, x_{\text{dim}-1}, u)$ has MPS index i , the site at $(x_0 + L_s[0], x_1, \dots, x_{\text{dim}-1}, u)$ corresponds to MPS index $i + N_{\text{sites}}$. Use `mps2lat_idx()` and `lat2mps_idx()` for conversion of indices. The function `mps2lat_values()` performs the necessary reshaping and re-ordering from arrays indexed in MPS form to arrays indexed in lattice form.

Deprecated since version 0.5.0: The parameters and attributes `nearest_neighbors`, `next_nearest_neighbors` and `next_next_nearest_neighbors` are deprecated. Instead, we use a dictionary `pairs` with those names as keys and the corresponding values as specified before.

Parameters

- **Ls** (*list of int*) – the length in each direction
- **unit_cell** (*list of Site*) – The sites making up a unit cell of the lattice. If you want to specify it only after initialization, use `None` entries in the list.
- **order** (*str* | *('standard', snake_winding, priority)* | *('grouped', groups)*) – A string or tuple specifying the order, given to `ordering()`.
- **bc** (*(iterable of) {'open' | 'periodic' | int}*) – Boundary conditions in each direction of the lattice. A single string holds for all directions. An integer *shift* means that we have periodic boundary conditions along this direction, but shift/tilt by $-\text{shift} * \text{lattice.basis}[0]$ (~cylinder axis for `bc_MPS='infinite'`) when going around the boundary along this direction.

- **bc_MPS** (*'finite' | 'segment' | 'infinite'*) – Boundary conditions for an MPS/MPO living on the ordered lattice. If the system is *'infinite'*, the infinite direction is always along the first basis vector (justifying the definition of *N_rings* and *N_sites_per_ring*).
- **basis** (*iterable of 1D arrays*) – For each direction one translation vectors shifting the unit cell. Defaults to the standard ONB `np.eye(dim)`.
- **positions** (*iterable of 1D arrays*) – For each site of the unit cell the position within the unit cell. Defaults to `np.zeros((len(unit_cell), dim))`.
- **nearest_neighbors** (*None | list of (u1, u2, dx)*) – Deprecated. Specify as `pairs['nearest_neighbors']` instead.
- **next_nearest_neighbors** (*None | list of (u1, u2, dx)*) – Deprecated. Specify as `pairs['next_nearest_neighbors']` instead.
- **next_next_nearest_neighbors** (*None | list of (u1, u2, dx)*) – Deprecated. Specify as `pairs['next_next_nearest_neighbors']` instead.
- **pairs** (*dict*) – Of the form `{'nearest_neighbors': [(u1, u2, dx), ...], ...}`. Typical keys are *'nearest_neighbors'*, *'next_nearest_neighbors'*. For each of them, it specifies a list of tuples *(u1, u2, dx)* which can be used as parameters for `add_coupling()` to generate couplings over each pair of, e.g., *'nearest_neighbors'*. Note that this adds couplings for each pair *only in one direction*!

Ls

the length in each direction.

Type tuple of int

shape

the ‘shape’ of the lattice, same as `Ls + (len(unit_cell),)`

Type tuple of int

N_cells

the number of unit cells in the lattice, `np.prod(self.Ls)`.

Type int

N_sites

the number of sites in the lattice, `np.prod(self.shape)`.

Type int

N_sites_per_ring

Defined as `N_sites / Ls[0]`, for an infinite system the number of sites per “ring”.

Type int

N_rings

Alias for `Ls[0]`, for an infinite system the number of “rings” in the unit cell.

Type int

unit_cell

the sites making up a unit cell of the lattice.

Type list of *Site*

bc
Boundary conditions of the couplings in each direction of the lattice, translated into a bool array with the global `bc_choices`.
Type bool ndarray

bc_shift
The shift in x-direction when going around periodic boundaries in other directions.
Type None | ndarray(int)

bc_MPS
Boundary conditions for an MPS/MPO living on the ordered lattice. If the system is 'infinite', the infinite direction is always along the first basis vector (justifying the definition of `N_rings` and `N_sites_per_ring`).
Type 'finite' | 'segment' | 'infinite'

basis
translation vectors shifting the unit cell. The row *i* gives the vector shifting in direction *i*.
Type ndarray (dim, Dim)

unit_cell_positions
for each site in the unit cell a vector giving its position within the unit cell.
Type ndarray, shape (len(unit_cell), Dim)

pairs
See above.
Type dict

_order
The place where `order` is stored.
Type ndarray (N_sites, dim+1)

_strides
necessary for `lat2mps_idx()`.
Type ndarray (dim,)

_perm
permutation needed to make `order` lexsorted, `_perm = np.lexsort(_order.T)`.
Type ndarray (N,)

_mps2lat_vals_idx
index array for reshape/reordering in `mps2lat_vals()`
Type ndarray *shape*

_mps_fix_u
for each site of the unit cell an index array selecting the mps indices of that site.
Type tuple of ndarray (N_cells,) np.intp

_mps2lat_vals_idx_fix_u
similar as `_mps2lat_vals_idx`, but for a fixed *u* picking a site from the unit cell.
Type tuple of ndarray of shape *Ls*

test_sanity()
Sanity check.

Raises ValueErrors, if something is wrong.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

property dim

The dimension of the lattice.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through through the lattice.

You can visualize the order with *plot_order()*.

ordering (*order*)

Provide possible orderings of the *N* lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters *order* (*str* | ('standard', *snake_winding*, *priority*) | ('grouped', *groups*)) – Specifies the desired ordering using one of the strings

of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns `order` – the order to be used for `order`.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the `order` from equivalent `priority` and `snake_winding`.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting `order`.

property `boundary_conditions`

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

enlarge_mps_unit_cell (`factor=2`)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters `factor` (`int`) – The new number of sites in the MPS unit cell will be increased from `N_sites` to `factor*N_sites_per_ring`. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (`Lx`, `Ly`, ..., `Lu`) to (`Lx*factor`, `Ly`, ..., `Lu`).

position (`lat_idx`)

return 'space' position of one or multiple sites.

Parameters `lat_idx` (ndarray, (... , dim+1)) – Lattice indices.

Returns `pos` – The position of the lattice sites specified by `lat_idx` in real-space.

Return type ndarray, (... , dim)

site (`i`)

return `Site` instance corresponding to an MPS index `i`

mps_sites ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

mps2lat_idx (`i`)

Translate MPS index `i` to lattice indices (`x_0`, ..., `x_{dim-1}`, `u`).

Parameters `i` (`int` | *array_like of int*) – MPS index/indices.

Returns `lat_idx` – First dimensions like `i`, last dimension has len `dim`+1` and contains the lattice indices ``(`x_0`, ..., `x_{dim-1}`, `u`)` corresponding to `i`. For `i` across the MPS unit cell and "infinite" `bc_MPS`, we shift `x_0` accordingly.

Return type array

lat2mps_idx (*lat_idx*)

Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .

Parameters **lat_idx** (*array_like* [$\dots, dim+1$]) – The last dimension corresponds to lattice indices (x_0, \dots, x_{D-1}, u). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an x_0 outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type *array_like*

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is u .

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters **u** (*None | int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns **mps_idx** – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type *array*

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters **u** (*None | int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices i for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row j contains the lattice index (without u) corresponding to `mps_idx[j]`.

mps2lat_values (*A, axes=0, u=None*)

Reshape/reorder A to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have `A.shape[axes] = self.N_sites` if u is *None*, or `A.shape[axes] = self.N_cells` if u is an *int*.
- **axes** (*(iterable of) int*) – chooses the axis which should be replaced.
- **u** (*None | int*) – Optionally choose a subset of MPS indices present in the axes of A , namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of u .

Returns **res_A** – Reshaped and reordered versions of A . Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[... , x0, x1, x2, ...] = A[... , j, ...]`.

Return type *ndarray*

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array A , where $A[i]$ is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function $C[i, j]$, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument u of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked(A , $axes=-1$, $mps_inds=None$, $include_u=None$)

Reshape/reorder an array A to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of A .

Parameters

- **A** (*ndarray*) – Some values.
- **$axes$** ((*iterable of int*)) – Chooses the axis of A which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** ((*list of 1D ndarray*)) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of A . Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.
- **$include_u$** ((*list of bool*)) – Specifies for each *axis* in *axes*, whether the u index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns `res_A` – Reshaped and reordered copy of `A`. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site $(x0, x1, x2)$, then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

count_neighbors ($u=0$, $key='nearest_neighbors'$)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of *pairs* to select what to count.

Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the u -th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

number_nearest_neighbors ($u=0$)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors ($u=0$)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

coupling_shape (dx)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

possible_couplings ($u1, u2, dx$)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index x_a is taken modulo $Ls[a]$ and runs through `range(Ls[a])`. For open boundary conditions, x_a is limited to $0 \leq x_a < Ls[a]$ and $0 \leq x_a + dx[a] < lat.Ls[a]$.

Parameters

- **u2** ($u1,$) – Indices within the unit cell; the $u1$ and $u2$ of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the $u1$ and $u2$.

- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

multi_coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (2D array, shape (N_ops, *dim*)) – *dx[i, :]* is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (list of (opname, *dx*, *u*)) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices *i,j,k,l,...* for each of the operators positions. The positions are defined by *dx* (*j,k,l,...* relative to *i*) and boundary condition of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order*=None, *textkwargs*={}, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (None | 2D array (*self.N_sites*, *self.dim+1*)) – The order as returned by `ordering()`; by default (None) use `order`.
- **textkwargs** (None | dict) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.

- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_coupling (*ax*, *coupling=None*, *wrap=False*, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (`None`), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If `True`, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_basis (*ax*, *origin=0.0, 0.0*, *shade=None*, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction=-1*, *origin=None*, *cylinder_axis=False*, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

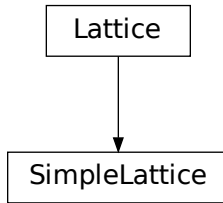
Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If `None`, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None | np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

SimpleLattice

- full name: `tenpy.models.lattice.SimpleLattice`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>SimpleLattice.__init__(Ls, site, **kwargs)</code>	Initialize self.
<code>SimpleLattice.count_neighbors([u, key])</code>	Count e.g.
<code>SimpleLattice.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>SimpleLattice.enlarge_mps_unit_cell([factor, repeat])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>SimpleLattice.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>SimpleLattice.lat2mps_idx(lat_idx)</code>	Translate lattice indices $(x_0, \dots, x_{\{D-1\}}, u)$ to MPS index i .
<code>SimpleLattice.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\{dim-1\}}, u)$.
<code>SimpleLattice.mps2lat_values(A[, axes, u])</code>	same as <code>Lattice.mps2lat_values()</code> , but ignore u , setting it to 0.
<code>SimpleLattice.mps2lat_values_masked(A[, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>SimpleLattice.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>SimpleLattice.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>SimpleLattice.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>SimpleLattice.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>SimpleLattice.number_nearest_neighbors(D)</code>	Deprecated.
<code>SimpleLattice.number_next_nearest_neighbors(D)</code>	Deprecated.
<code>SimpleLattice.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>SimpleLattice.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>SimpleLattice.plot_bc_identified(ax[, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>SimpleLattice.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>SimpleLattice.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.

continues on next page

Table 88 – continued from previous page

<code>SimpleLattice.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>SimpleLattice.position(lat_idx)</code>	return 'space' position of one or multiple sites.
<code>SimpleLattice.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>SimpleLattice.possible_multi_couplings()</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>SimpleLattice.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>SimpleLattice.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index <i>i</i>
<code>SimpleLattice.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>SimpleLattice.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>SimpleLattice.dim</code>	The dimension of the lattice.
<code>SimpleLattice.nearest_neighbors</code>	
<code>SimpleLattice.next_nearest_neighbors</code>	
<code>SimpleLattice.next_next_nearest_neighbors</code>	
<code>SimpleLattice.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.SimpleLattice` (*Ls*, *site*, ****kwargs**)

Bases: `tenpy.models.lattice.Lattice`

A lattice with a unit cell consisting of just a single site.

In many cases, the unit cell consists just of a single site, such that the the last entry of *u* of an 'lattice index' can only be 0. From the point of internal algorithms, we handle this class like a `Lattice` – in that way we don't need to distinguish special cases in the algorithms.

Yet, from the point of a tenpy user, for example if you measure an expectation value on each site in a `SimpleLattice`, you expect to get an ndarray of dimensions `self.Ls`, not `self.shape`. To avoid that problem, `SimpleLattice` overwrites just the meaning of `u=None` in `mps2lat_values()` to be the same as `u=0`.

Parameters

- **Ls** (*list of int*) – the length in each direction
- **site** (*Site*) – the lattice site. The *unit_cell* of the `Lattice` is just `[site]`.
- ****kwargs** – Additional keyword arguments given to the `Lattice`. If *order* is specified in the form `('standard', snake_windingi, priority)`, the *snake_winding* and *priority* should only be specified for the spatial directions. Similarly, *positions* can be specified as a single vector.

mps2lat_values (*A*, *axes=0*, *u=None*)

same as `Lattice.mps2lat_values()`, but ignore *u*, setting it to 0.

property boundary_conditions

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns boundary_conditions – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of pairs to select what to count.

Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

property dim

The dimension of the lattice.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type *cls*

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters **lat_idx** (*array_like [..., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and

smaller than the corresponding entry in `self.shape`. Exception: for “infinite” `bc_MPS`, an `x_0` outside indicates shifts accross the boundary.

Returns `i` – MPS index/indices corresponding to `lat_idx`. Has the same shape as `lat_idx` without the last dimension.

Return type `array_like`

`mps2lat_idx(i)`

Translate MPS index `i` to lattice indices `(x_0, ..., x_{dim-1}, u)`.

Parameters `i` (`int` | `array_like of int`) – MPS index/indices.

Returns `lat_idx` – First dimensions like `i`, last dimension has `len dim + 1` and contains the lattice indices `((x_0, ..., x_{dim-1}, u))` corresponding to `i`. For `i` accross the MPS unit cell and “infinite” `bc_MPS`, we shift `x_0` accordingly.

Return type `array`

`mps2lat_values_masked(A, axes=-1, mps_inds=None, include_u=None)`

Reshape/reorder an array `A` to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of `A`.

Parameters

- `A` (`ndarray`) – Some values.
- `axes` (`(iterable of) int`) – Chooses the axis of `A` which should be replaced. If multiple axes are given, you also need to give multiple index arrays as `mps_inds`.
- `mps_inds` (`(list of) 1D ndarray`) – Specifies for each `axis` in `axes`, for which MPS indices we have values in the corresponding `axis` of `A`. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” `bc_MPS`, we shift `x_0` accordingly.
- `include_u` (`(list of) bool`) – Specifies for each `axis` in `axes`, whether the `u` index of the lattice should be included into the output array `res_A`. Defaults to `len(self.unit_cell) > 1`.

Returns `res_A` – Reshaped and reordered copy of `A`. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index `j` maps to lattice site `(x0, x1, x2)`, then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

`mps_idx_fix_u(u=None)`

return an index array of MPS indices for which the site within the unit cell is `u`.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters `u` (`None` | `int`) – Selects a site of the unit cell. `None` (default) means all sites.

Returns `mps_idx` – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type `array`

`mps_lat_idx_fix_u(u=None)`

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters `u` (`None` | `int`) – Selects a site of the unit cell. `None` (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices i for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row j contains the lattice index (without u) corresponding to `mps_idx[j]`.

mps_sites()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape(dx)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters **dx** (2D array, shape (N_ops, *dim*)) – `dx[i, :]` is the translation vector in the lattice for the i -th operator. Corresponds to the dx of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by dx . (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

ordering(order)

Provide possible orderings of the N lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters `order` (str | (('standard', snake_winding, priority) | ('grouped', groups)) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns `order` – the order to be used for `order`.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin*=0.0, 0.0, *shade*=None, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=- 1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (None | `np.ndarray`) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order=None*, *textkwargs={}*, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (`None` | `2D array (self.N_sites, self.dim+1)`) – The order as returned by `ordering()`; by default (`None`) use `order`.
- **textkwargs** (`None` | `dict`) – If not `None`, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers=['o', '^', 's', 'p', 'h', 'D']*, ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (`list`) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters *lat_idx* (`ndarray, (... , dim+1)`) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray, (... , dim)`

possible_couplings (*u1, u2, dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < Ls[a]` and `0 <= x_a+dx[a] < lat.Ls[a]`.

Parameters

- **u2** (*u1*,) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (`array`) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (`array`) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.
- **lat_indices** (`2D int array`) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (`tuple of int`) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (`list of (opname, dx, u)`) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices i, j, k, l, \dots for each of the operators positions. The positions are defined by dx (j, k, l, \dots relative to i) and boundary conditions of *self* (how much the *box* for given dx can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

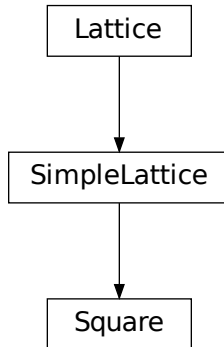
Sanity check.

Raises *ValueErrors*, if something is wrong.

Square

- full name: *tenpy.models.lattice.Square*
- parent module: *tenpy.models.lattice*
- type: class

Inheritance Diagram



Methods

<code>Square.__init__(Lx, Ly, site, **kwargs)</code>	Initialize self.
<code>Square.count_neighbors([u, key])</code>	Count e.g.
<code>Square.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Square.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Square.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Square.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Square.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Square.mps2lat_values(A[, axes, u])</code>	same as <code>Lattice.mps2lat_values()</code> , but ignore u , setting it to 0.
<code>Square.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Square.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>Square.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Square.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Square.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Square.number_nearest_neighbors([u])</code>	Deprecated.
<code>Square.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Square.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Square.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Square.plot_bc_identified(ax[, direction, ...])</code>	Mark two sites identified by periodic boundary conditions.
<code>Square.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.

continues on next page

Table 90 – continued from previous page

<code>Square.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Square.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Square.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Square.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Square.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Square.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Square.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index <i>i</i>
<code>Square.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>Square.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Square.dim</code>	
<code>Square.nearest_neighbors</code>	
<code>Square.next_nearest_neighbors</code>	
<code>Square.next_next_nearest_neighbors</code>	
<code>Square.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Square` (*Lx, Ly, site, **kwargs*)

Bases: `tenpy.models.lattice.SimpleLattice`

A square lattice.

Parameters

- **Ly** (*Lx*,) – The length in each direction.
- **site** (*Site*) – The local lattice site. The *unit_cell* of the *Lattice* is just [*site*].
- ****kwargs** – Additional keyword arguments given to the *Lattice*. *pairs* are set accordingly. If *order* is specified in the form ('standard', *snake_winding*, *priority*), the *snake_winding* and *priority* should only be specified for the spatial directions. Similarly, *positions* can be specified as a single vector.

property `boundary_conditions`

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

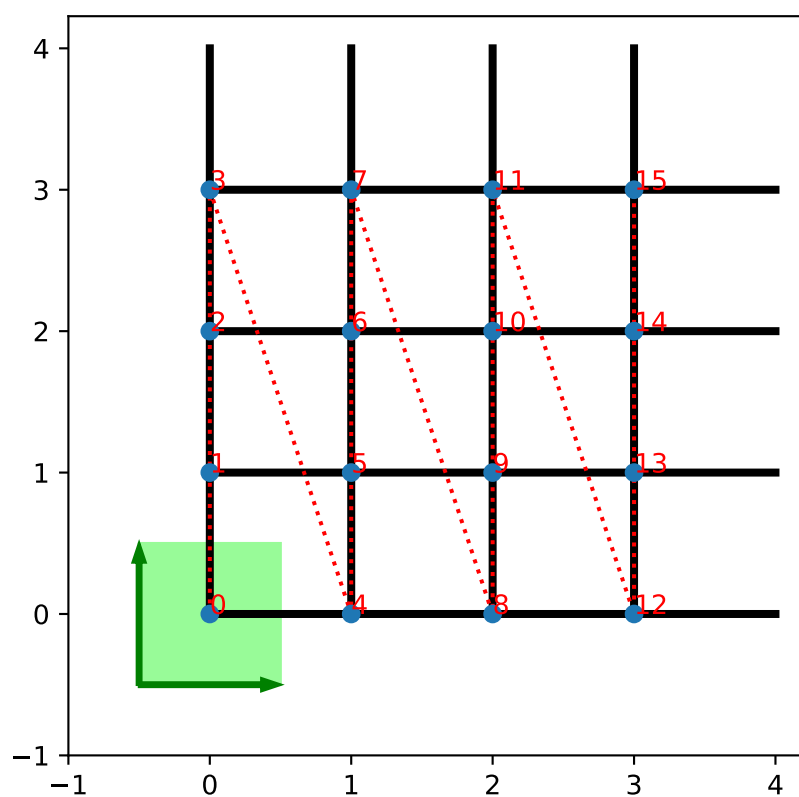
Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of *pairs* to select what to count.



Returns **number** – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type `int`

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters **dx** (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type `cls`

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters **lat_idx** (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an *x_0* outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type `array_like`

mps2lat_idx (*i*)

Translate MPS index *i* to lattice indices (*x_0*, ..., *x_{dim-1}*, *u*).

Parameters **i** (*int | array_like of int*) – MPS index/indices.

Returns `lat_idx` – First dimensions like i , last dimension has `len dim + 1` and contains the lattice indices `((x_0, ..., x_{dim-1}, u))` corresponding to i . For i across the MPS unit cell and “infinite” `bc_MPS`, we shift `x_0` accordingly.

Return type array

`mps2lat_values` (A , `axes=0`, `u=None`)

same as `Lattice.mps2lat_values()`, but ignore `u`, setting it to 0.

`mps2lat_values_masked` (A , `axes=-1`, `mps_inds=None`, `include_u=None`)

Reshape/reorder an array A to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of A .

Parameters

- **`A`** (`ndarray`) – Some values.
- **`axes`** ((`iterable of int`)) – Chooses the axis of A which should be replaced. If multiple axes are given, you also need to give multiple index arrays as `mps_inds`.
- **`mps_inds`** ((`list of 1D ndarray`)) – Specifies for each `axis` in `axes`, for which MPS indices we have values in the corresponding `axis` of A . Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices across the MPS unit cell and “infinite” `bc_MPS`, we shift `x_0` accordingly.
- **`include_u`** ((`list of bool`)) – Specifies for each `axis` in `axes`, whether the `u` index of the lattice should be included into the output array `res_A`. Defaults to `len(self.unit_cell) > 1`.

Returns `res_A` – Reshaped and reordered copy of A . Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

`mps_idx_fix_u` (`u=None`)

return an index array of MPS indices for which the site within the unit cell is `u`.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters `u` (`None` / `int`) – Selects a site of the unit cell. `None` (default) means all sites.

Returns `mps_idx` – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type array

`mps_lat_idx_fix_u` (`u=None`)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters `u` (`None` / `int`) – Selects a site of the unit cell. `None` (default) means all sites.

Returns

- **`mps_idx`** (array) – MPS indices i for which `self.site(i)` is `self.unit_cell[u]`.
- **`lat_idx`** (2D array) – The row j contains the lattice index (without `u`) corresponding to `mps_idx[j]`.

mps_sites()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape(dx)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters **dx** (2D array, shape (N_ops, dim)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

ordering(order)

Provide possible orderings of the *N* lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters **order** (str | (('standard', snake_winding, priority) | ('grouped', groups))) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns **order** – the order to be used for `order`.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin*=0.0, 0.0, *shade*=None, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=- 1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites indified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None* | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order*=None, *textkwargs*={}, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None* | *2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (None) use `order`.

- **textkwargs** (None | dict) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return 'space' position of one or multiple sites.

Parameters *lat_idx* (`ndarray`, (... , dim+1)) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray`, (... , dim)

possible_couplings (*u1*, *u2*, *dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `LS[a]` and runs through `range(LS[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < LS[a]` and `0 <= x_a+dx[a] < lat.LS[a]`.

Parameters

- **u2** (*u1*,) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length dim. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (list of (opname, dx, u)) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices *i,j,k,l,...* for each of the operators positions. The positions are defined by *dx* (*j,k,l,...* relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

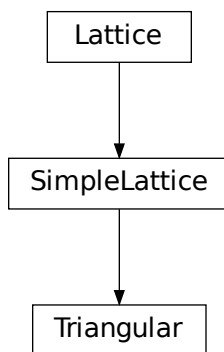
Sanity check.

Raises *ValueErrors*, if something is wrong.

Triangular

- full name: `tenpy.models.lattice.Triangular`
- parent module: `tenpy.models.lattice`
- type: class

Inheritance Diagram



Methods

<code>Triangular.__init__(Lx, Ly, site, **kwargs)</code>	Initialize self.
<code>Triangular.count_neighbors([u, key])</code>	Count e.g.
<code>Triangular.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>Triangular.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Triangular.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>Triangular.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .
<code>Triangular.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1}, u)$.
<code>Triangular.mps2lat_values(A[, axes, u])</code>	same as <code>Lattice.mps2lat_values()</code> , but ignore u , setting it to 0.
<code>Triangular.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>Triangular.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>Triangular.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>Triangular.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>Triangular.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>Triangular.number_nearest_neighbors([u])</code>	Deprecated.
<code>Triangular.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>Triangular.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>Triangular.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>Triangular.plot_bc_identified(ax[, ...])</code>	Mark two sites indified by periodic boundary conditions.
<code>Triangular.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>Triangular.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>Triangular.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>Triangular.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>Triangular.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>Triangular.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>Triangular.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>Triangular.site(i)</code>	return <code>Site</code> instance corresponding to an MPS index i
<code>Triangular.test_sanity()</code>	Sanity check.

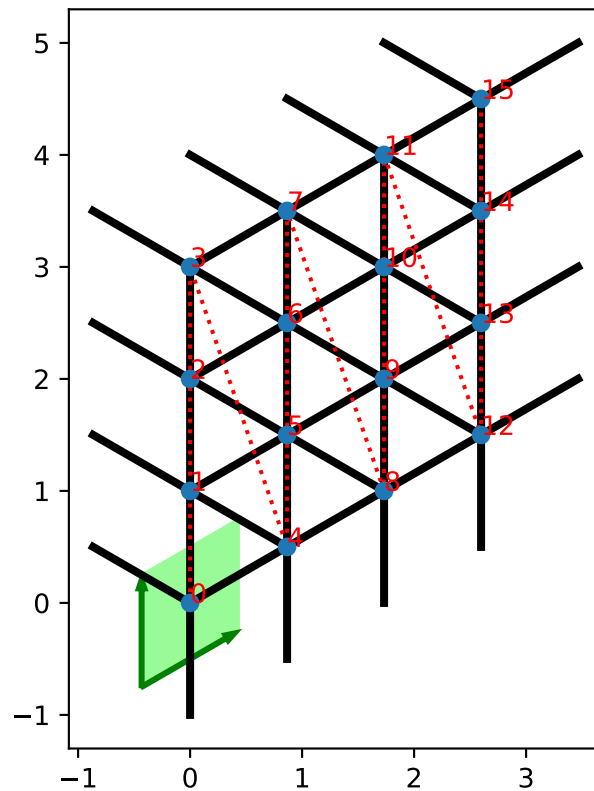
Class Attributes and Properties

<code>Triangular.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>Triangular.dim</code>	
<code>Triangular.nearest_neighbors</code>	
<code>Triangular.next_nearest_neighbors</code>	
<code>Triangular.next_next_nearest_neighbors</code>	
<code>Triangular.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.Triangular` (*Lx*, *Ly*, *site*, ****kwargs**)

Bases: `tenpy.models.lattice.SimpleLattice`

A triangular lattice.



Parameters

- **Ly** (*Lx*,) – The length in each direction.
- **site** (*Site*) – The local lattice site. The *unit_cell* of the *Lattice* is just [*site*].
- ****kwargs** – Additional keyword arguments given to the *Lattice*. *pairs* are set ac-

cordingly. If *order* is specified in the form ('standard', snake_windingi, priority), the *snake_winding* and *priority* should only be specified for the spatial directions. Similarly, *positions* can be specified as a single vector.

property boundary_conditions

Human-readable list of boundary conditions from *bc* and *bc_shift*.

Returns boundary_conditions – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of *pairs* to select what to count.

Returns number – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type *int*

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters dx (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters factor (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns obj – Newly generated class instance containing the required data.

Return type cls

lat2mps_idx(*lat_idx*)

Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .

Parameters *lat_idx* (*array_like* [$\dots, dim+1$]) – The last dimension corresponds to lattice indices (x_0, \dots, x_{D-1}, u). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an x_0 outside indicates shifts across the boundary.

Returns *i* – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type array_like

mps2lat_idx(*i*)

Translate MPS index i to lattice indices (x_0, \dots, x_{dim-1}, u).

Parameters *i* (*int* | *array_like of int*) – MPS index/indices.

Returns *lat_idx* – First dimensions like i , last dimension has `len dim + 1` and contains the lattice indices `((x_0, ..., x_{dim-1}), u)` corresponding to i . For i across the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.

Return type array

mps2lat_values(*A*, *axes=0*, *u=None*)

same as `Lattice.mps2lat_values()`, but ignore u , setting it to 0.

mps2lat_values_masked(*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** (*iterable of int*) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** (*list of 1D ndarray*) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices across the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.
- **include_u** (*list of bool*) – Specifies for each *axis* in *axes*, whether the u index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type np.ma.MaskedArray

mps_idx_fix_u(*u=None*)

return an index array of MPS indices for which the site within the unit cell is u .

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters `u` (*None* / *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns `mps_idx` – MPS indices for which `self.site(i)` is `self.unit_cell[u]`.
Ordered ascending.

Return type array

`mps_lat_idx_fix_u` (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters `u` (*None* / *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- `mps_idx` (array) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- `lat_idx` (2D array) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

`mps_sites` ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

`multi_coupling_shape` (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters `dx` (2D array, shape (N_ops, dim)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- `coupling_shape` (tuple of int) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- `shift_lat_indices` (array) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

`number_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

`number_next_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through through the lattice.

You can visualize the order with `plot_order()`.

ordering (*order*)

Provide possible orderings of the *N* lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters *order* (str | ('standard', snake_winding, priority) | ('grouped', groups)) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns *order* – the order to be used for *order*.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin*=0.0, 0.0, *shade*=None, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=-1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (None | `np.ndarray`) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.

- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax, order=None, textkwargs={}, **kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None | 2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (None) use `order`.
- **textkwargs** (*None | dict*) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax, markers=['o', '^', 's', 'p', 'h', 'D'], **kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword `marker` of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters *lat_idx* (`ndarray, (... , dim+1)`) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray, (... , dim)`

possible_couplings (*u1, u2, dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < Ls[a]` and `0 <= x_a+dx[a] < lat.Ls[a]`.

Parameters

- **u2** (*u1, ...*) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.

- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of *possible_couplings()* to couplings with more than 2 sites.

Parameters **ops** (list of (opname, dx, u)) – Same as the argument *ops* of *add_multi_coupling()*.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices i, j, k, l, \dots for each of the operators positions. The positions are defined by *dx* (j,k,l,... relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len dim. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

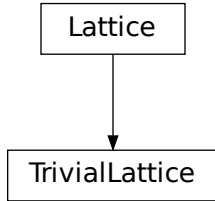
Sanity check.

Raises *ValueErrors*, if something is wrong.

TrivialLattice

- full name: *tenpy.models.lattice.TrivialLattice*
- parent module: *tenpy.models.lattice*
- type: class

Inheritance Diagram



Methods

<code>TrivialLattice.__init__(mps_sites, **kwargs)</code>	Initialize self.
<code>TrivialLattice.count_neighbors([u, key])</code>	Count e.g.
<code>TrivialLattice.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>TrivialLattice.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>TrivialLattice.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>TrivialLattice.lat2mps_idx(lat_idx)</code>	Translate lattice indices $(x_0, \dots, x_{\{D-1\}}, u)$ to MPS index i .
<code>TrivialLattice.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\{dim-1\}}, u)$.
<code>TrivialLattice.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>TrivialLattice.mps2lat_values_masked(A[, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>TrivialLattice.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>TrivialLattice.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>TrivialLattice.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>TrivialLattice.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>TrivialLattice.number_nearest_neighbors()</code>	Deprecated.
<code>TrivialLattice.number_next_nearest_neighbors()</code>	Deprecated.
<code>TrivialLattice.ordering(order)</code>	Provide possible orderings of the N lattice sites.
<code>TrivialLattice.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>TrivialLattice.plot_bc_identified(ax[, ...])</code>	Mark two sites identified by periodic boundary conditions.
<code>TrivialLattice.plot_coupling(ax[, coupling, ...])</code>	Plot lines connecting nearest neighbors of the lattice.

continues on next page

Table 94 – continued from previous page

<code>TrivialLattice.plot_order(ax[, order, ...])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>TrivialLattice.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>TrivialLattice.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>TrivialLattice.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>TrivialLattice.possible_multi_couplings</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>TrivialLattice.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>TrivialLattice.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index <i>i</i>
<code>TrivialLattice.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>TrivialLattice.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>TrivialLattice.dim</code>	The dimension of the lattice.
<code>TrivialLattice.nearest_neighbors</code>	
<code>TrivialLattice.next_nearest_neighbors</code>	
<code>TrivialLattice.next_next_nearest_neighbors</code>	
<code>TrivialLattice.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.lattice.TrivialLattice` (*mps_sites*, ***kwargs*)

Bases: `tenpy.models.lattice.Lattice`

Trivial lattice consisting of a single (possibly large) unit cell in 1D.

This is usefull if you need a valid *Lattice* with given *mps_sites()* and don’t care about the actual geometry, e.g. because you don’t intend to use the *CouplingModel*.

Parameters

- **mps_sites** (list of *Site*) – The sites making up a unit cell of the lattice.
- ****kwargs** – Further keyword arguments given to *Lattice*.

property `boundary_conditions`

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns `boundary_conditions` – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

`count_neighbors` (*u=0*, *key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of `pairs` to select what to count.

Returns `number` – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type `int`

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters `dx` (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

property `dim`

The dimension of the lattice.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters `factor` (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor*N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx*factor*, *Ly*, ..., *Lu*).

classmethod **from_hdf5** (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

lat2mps_idx (*lat_idx*)

Translate lattice indices (*x_0*, ..., *x_{D-1}*, *u*) to MPS index *i*.

Parameters `lat_idx` (*array_like [.., dim+1]*) – The last dimension corresponds to lattice indices (*x_0*, ..., *x_{D-1}*, *u*). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an *x_0* outside indicates shifts accross the boundary.

Returns `i` – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type `array_like`

mps2lat_idx (*i*)

Translate MPS index *i* to lattice indices (*x_0*, ..., *x_{dim-1}*, *u*).

Parameters *i* (*int* | *array_like of int*) – MPS index/indices.

Returns *lat_idx* – First dimensions like *i*, last dimension has `len dim + 1` and contains the lattice indices `((x_0, ..., x_{dim-1}, u))` corresponding to *i*. For *i* across the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.

Return type *array*

mps2lat_values (*A*, *axes=0*, *u=None*)

Reshape/reorder *A* to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have `A.shape[axes] = self.N_sites` if *u* is *None*, or `A.shape[axes] = self.N_cells` if *u* is an *int*.
- **axes** (*iterable of int*) – chooses the axis which should be replaced.
- **u** (*None* | *int*) – Optionally choose a subset of MPS indices present in the axes of *A*, namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of *u*.

Returns *res_A* – Reshaped and reordered versions of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type *ndarray*

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array *A*, where *A[i]* is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:

```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument *u* of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
```

(continues on next page)

(continued from previous page)

```
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** (*iterable of int*) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** (*list of 1D ndarray*) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** (*list of bool*) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns *mps_idx* – MPS indices for which `self.site(i)` is `self.unit_cell[u]`. Ordered ascending.

Return type `array`

mps_lat_idx_fix_u (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **mps_idx** (*array*) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **lat_idx** (*2D array*) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

mps_sites()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

multi_coupling_shape(dx)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters **dx** (2D array, shape (N_ops, *dim*)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (tuple of int) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (array) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

number_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

number_next_nearest_neighbors(u=0)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through through the lattice.

You can visualize the order with `plot_order()`.

ordering(order)

Provide possible orderings of the *N* lattice sites.

This function can be overwritten by derived lattices to define additional orderings. The following orders are defined in this method:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'Cstyle'	(0, 1, ..., dim-1, dim)	(False, ..., False, False)
'default'		
'snake'	(0, 1, ..., dim-1, dim)	(True, ..., True, True)
'snakeCstyle'		
'Fstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)
'snakeFstyle'	(dim-1, ..., 1, 0, dim)	(False, ..., False, False)

Parameters **order** (str | (('standard', snake_winding, priority) | ('grouped', groups)) – Specifies the desired ordering using one of the strings of the above tables. Alternatively, an ordering is specified by a tuple with first entry specifying a function, 'standard' for `get_order()` and 'grouped' for `get_order_grouped()`, and other arguments in the tuple as specified in the documentation of these functions.

Returns **order** – the order to be used for `order`.

Return type array, shape (N, D+1), dtype np.intp

See also:

`get_order()` generates the *order* from equivalent *priority* and *snake_winding*.

`get_order_grouped()` variant of `get_order`.

`plot_order()` visualizes the resulting *order*.

plot_basis (*ax*, *origin*=0.0, 0.0, *shade*=None, ***kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- ****kwargs** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=-1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (None | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order*=None, *textkwargs*={}, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (None | 2D array (*self.N_sites, self.dim+1*)) – The order as returned by `ordering()`; by default (None) use `order`.

- **textkwargs** (None | dict) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return 'space' position of one or multiple sites.

Parameters *lat_idx* (`ndarray`, (... , dim+1)) – Lattice indices.

Returns *pos* – The position of the lattice sites specified by *lat_idx* in real-space.

Return type `ndarray`, (... , dim)

possible_couplings (*u1*, *u2*, *dx*)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index *x_a* is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, *x_a* is limited to `0 <= x_a < Ls[a]` and `0 <= x_a+dx[a] < lat.Ls[a]`.

Parameters

- **u2** (*u1*,) – Indices within the unit cell; the *u1* and *u2* of `add_coupling()`
- **dx** (*array*) – Length *dim*. The translation in terms of basis vectors for the coupling.

Returns

- **mps1, mps2** (*array*) – For each possible two-site coupling the MPS indices for the *u1* and *u2*.
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

possible_multi_couplings (*ops*)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters *ops* (list of (opname, dx, u)) – Same as the argument *ops* of `add_multi_coupling()`.

Returns

- **mps_ijkl** (*2D int array*) – Each row contains MPS indices *i,j,k,l,...* for each of the operators positions. The positions are defined by *dx* (*j,k,l,...* relative to *i*) and boundary conditions of *self* (how much the *box* for given *dx* can be shifted around without hitting a boundary - these are the different rows).
- **lat_indices** (*2D int array*) – Rows of *lat_indices* correspond to rows of *mps_ijkl* and contain the lattice indices of the “lower left corner” of the box containing the coupling.

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

Specifically, it saves *unit_cell*, *Ls*, *unit_cell_positions*, *basis*, *boundary_conditions*, *pairs* under their name, *bc_MPS* as "boundary_conditions_MPS", and *order* as "order_for_MPS". Moreover, it saves *dim* and *N_sites* as HDF5 attributes.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

site (*i*)

return *Site* instance corresponding to an MPS index *i*

test_sanity ()

Sanity check.

Raises *ValueErrors*, if something is wrong.

Functions

<i>get_lattice</i> (<i>lattice_name</i>)	Given the name of a <i>Lattice</i> class, get the lattice class itself.
<i>get_order</i> (<i>shape</i> , <i>snake_winding</i> [, <i>priority</i>])	Built the <i>Lattice.order</i> in (Snake-) C-Style for a given lattice shape.
<i>get_order_grouped</i> (<i>shape</i> , <i>groups</i>)	Variant of <i>get_order()</i> , grouping some sites of the unit cell.

get_lattice

- full name: `tenpy.models.lattice.get_lattice`
- parent module: `tenpy.models.lattice`
- type: function

`tenpy.models.lattice.get_lattice(lattice_name)`

Given the name of a *Lattice* class, get the lattice class itself.

Parameters *lattice_name* (*str*) – Name of a *Lattice* class defined in the module *lattice*, for example "Chain", "Square", "Honeycomb",

Returns *LatticeClass* – The lattice class (type, not instance) specified by *lattice_name*.

Return type *Lattice*

get_order

- full name: `tenpy.models.lattice.get_order`
- parent module: `tenpy.models.lattice`
- type: function

`tenpy.models.lattice.get_order(shape, snake_winding, priority=None)`

Build the `Lattice.order` in (Snake-) C-Style for a given lattice shape.

In this function, the word ‘direction’ referst to a physical direction of the lattice or the index u of the unit cell as an “artificial direction”.

Parameters

- **shape** (*tuple of int*) – The shape of the lattice, i.e., the length in each direction.
- **snake_winding** (*tuple of bool*) – For each direction one bool, whether we should wind as a “snake” (True) in that direction (i.e., going forth and back) or simply repeat ascending (False)
- **priority** (`None` | *tuple of float*) – If `None` (default), use C-Style ordering. Otherwise, this defines the priority along which direction to wind first; the direction with the highest priority increases fastest. For example, “C-Style” order is enforced by `priority=(0, 1, 2, ...)`, and Fortrans F-style order is enforced by `priority=(dim, dim-1, ..., 1, 0)`
- **group** (`None` | *tuple of tuple*) – If `None` (default), ignore it. Otherwise, it specifies that we group the fastest changing dimension

Returns `order` – An order of the sites for `Lattice.order` in the specified *ordering*.

Return type `ndarray (np.prod(shape), len(shape))`

See also:

`Lattice.ordering()` method in `Lattice` to obtain the order from parameters.

`Lattice.plot_order()` visualizes the resulting order in a `Lattice`.

`get_order_grouped()` a variant grouping sites of the unit cell.

get_order_grouped

- full name: `tenpy.models.lattice.get_order_grouped`
- parent module: `tenpy.models.lattice`
- type: function

`tenpy.models.lattice.get_order_grouped(shape, groups)`

Variant of `get_order()`, grouping some sites of the unit cell.

In this function, the word ‘direction’ referst to a physical direction of the lattice or the index u of the unit cell as an “artificial direction”. This function is usefull for lattices with a unit cell of more than 2 sites (e.g. Kagome). The argument *group* is a To explain the order, assume we have a 3-site unit cell in a 2D lattice with shape (Lx, Ly, Lu). Calling this function with `groups=((1,), (2, 0))` returns an order of the following form:

```
# columns: [x, y, u]
[0, 0, 1] # first for u = 1 along y
[0, 1, 1]
:
[0, Ly-1, 1]
[0, 0, 2] # then for u = 2 and 0
[0, 0, 0]
[0, 1, 2]
[0, 1, 0]
:
[0, Ly-1, 2]
[0, Ly-1, 0]
# and then repeat the above for increasing `x`.
```

Parameters

- **shape** (*tuple of int*) – The shape of the lattice, i.e., the length in each direction.
- **groups** (*tuple of tuple of int*) – A partition and reordering of `range(shape[-1])` into smaller groups. The ordering goes first within a group, then along the last spatial dimensions, then changing between different groups and finally in Cstyle order along the remaining spatial dimensions.

Returns **order** – An order of the sites for `Lattice.order` in the specified *ordering*.

Return type ndarray (np.prod(shape), len(shape))

See also:

`Lattice.ordering()` method in `Lattice` to obtain the order from parameters.

`Lattice.plot_order()` visualizes the resulting order in a `Lattice`.

Module description

Classes to define the lattice structure of a model.

The base class `Lattice` defines the general structure of a lattice, you can subclass this to define you own lattice. The `SimpleLattice` is a slight simplification for lattices with a single-site unit cell. Further, we have some predefined lattices, namely `Chain`, `Ladder` in 1D and `Square`, `Triangular`, `Honeycomb`, and `Kagome` in 2D.

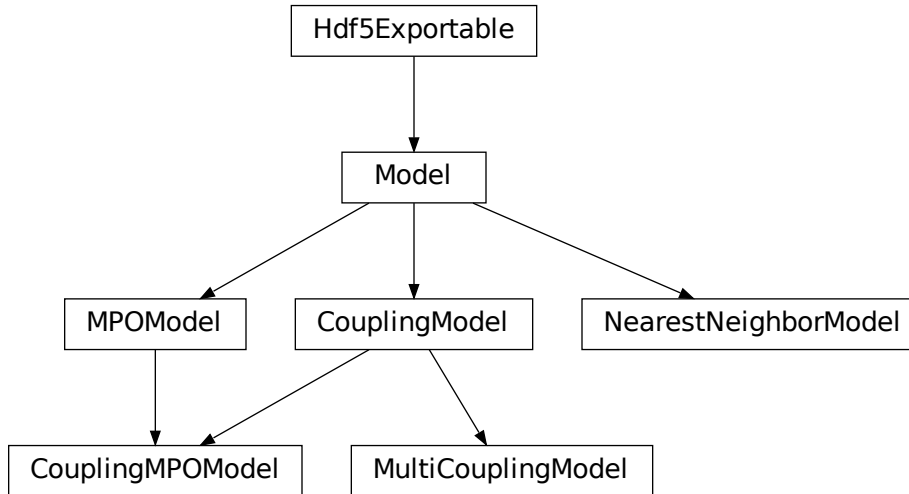
The `IrregularLattice` provides a way to remove or add sites to an existing, regular lattice.

See also the `Models`.

7.9.2 model

- full name: `tenpy.models.model`
- parent module: `tenpy.models`
- type: module

Classes

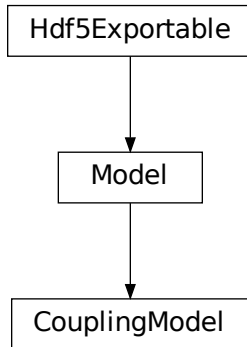


<code>CouplingMPOModel(model_params)</code>	Combination of the <i>CouplingModel</i> and <i>MPOModel</i> .
<i>CouplingModel</i> (lattice[, bc_coupling, ...])	Base class for a general model of a Hamiltonian consisting of two-site couplings.
<i>MPOModel</i> (lattice, H_MPO)	Base class for a model with an MPO representation of the Hamiltonian.
<i>Model</i> (lattice)	Base class for all models.
<i>MultiCouplingModel</i> (lattice[, bc_coupling, ...])	Generalizes <i>CouplingModel</i> to allow couplings involving more than two sites.
<i>NearestNeighborModel</i> (lattice, H_bond)	Base class for a model of nearest neighbor interactions w.r.t.

CouplingModel

- full name: `tenpy.models.model.CouplingModel`
- parent module: `tenpy.models.model`
- type: class

Inheritance Diagram



Methods

<code>CouplingModel.__init__(lattice[,...])</code>	Initialize self.
<code>CouplingModel.add_coupling(strength, ul, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>CouplingModel.add_coupling_term(strength, i, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>CouplingModel.add_local_term(strength, term)</code>	Add a single term to <i>self</i> .
<code>CouplingModel.add_onsite(strength, u, opname)</code>	Add onsite terms to <code>onsite_terms</code> .
<code>CouplingModel.add_onsite_term(strength, i, op)</code>	Add an onsite term on a given MPS site.
<code>CouplingModel.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>CouplingModel.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>CouplingModel.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>CouplingModel.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>CouplingModel.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <i>self.onsite_terms</i> .
<code>CouplingModel.coupling_strength_add_extflux([factor])</code>	Add an external flux to the coupling strength.
<code>CouplingModel.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>CouplingModel.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>CouplingModel.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>CouplingModel.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>CouplingModel.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.

```
class tenpy.models.model.CouplingModel (lattice, bc_coupling=None, ex-
                                         plicit_plus_hc=False)
```

Bases: `tenpy.models.model.Model`

Base class for a general model of a Hamiltonian consisting of two-site couplings.

In this class, the terms of the Hamiltonian are specified explicitly as `OnsiteTerms` or `CouplingTerms`.

Deprecated since version 0.4.0: `bc_coupling` will be removed in 1.0.0. To specify the full geometry in the lattice, use the `bc` parameter of the `Lattice`.

Parameters

- **lattice** (`Lattice`) – The lattice defining the geometry and the local Hilbert space(s).
- **bc_coupling** ((iterable of) {'open' | 'periodic' | int}) – Boundary conditions of the couplings in each direction of the lattice. Defines how the couplings are added in `add_coupling()`. A single string holds for all directions. An integer *shift* means that we have periodic boundary conditions along this direction, but shift/tilt by $-\text{shift} \times \text{lattice.basis}[0]$ (~cylinder axis for `bc_MPS='infinite'`) when going around the boundary along this direction.
- **explicit_plus_hc** (*bool*) – If True, the Hermitian conjugate of the MPO is computed at runtime, rather than saved in the MPO.

onsite_terms

The `OnsiteTerms` ordered by category.

Type {'category': `OnsiteTerms`}

coupling_terms

The `CouplingTerms` ordered by category. In a `MultiCouplingModel`, values may also be `MultiCouplingTerms`.

Type {'category': `CouplingTerms`}

explicit_plus_hc

If *True*, *self* represents the terms in `onsite_terms` and `coupling_terms` and their hermitian conjugate added. The flag will be carried on the MPO, which will have a reduced bond dimension if `self.add_coupling(..., plus_hc=True)` was used. Note that `add_onsite()` and `add_coupling()` respect this flag, ensuring that the *represented* Hamiltonian is independent of the `explicit_plus_hc` flag.

Type *bool*

test_sanity()

Sanity check, raises `ValueErrors`, if something is wrong.

add_local_term (strength, term, category=None, plus_hc=False)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see `Lattice`.

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice

index *lat_idx*. Here, *lat_idx* is for example $[x, y, u]$ for a 2D lattice, with *u* being the index within the unit cell.

- **category** – Descriptive name used as key for *onsite_terms* or *coupling_terms*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength, u, opname, category=None, plus_hc=False*)

Add onsite terms to *onsite_terms*.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index $(x_0, \dots, x_{\{\text{dim}-1\}}, u)$,

The necessary terms are just added to *onsite_terms*; doesn't rebuild the MPO.

Parameters

- **strength** (*scalar | array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a Site $\text{lat.unit_cell}[u]$ out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in $\text{lat.unit_cell}[u]$.
- **category** (*str*) – Descriptive name used as key for *onsite_terms*. Defaults to *opname*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

add_coupling() Add a terms acting on two sites.

add_onsite_term() Add a single term without summing over *vecx*.

add_onsite_term (*strength, i, op, category=None, plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for *onsite_terms*. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_onsite_terms ()

Sum of all *onsite_terms*.

add_coupling (*strength, u1, op1, u2, op2, dx, op_string=None, str_on_first=True, raise_op2_left=False, category=None, plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\text{dim}-1}} \text{strength}[\text{shift}(\vec{x})] * OP0 * OP1$, where $OP0 := \text{lat.unit_cell}[u0].\text{get_op}(op0)$ acts on the site $(x_0, \dots, x_{\{\text{dim}-1\}}, u1)$, and $OP1 := \text{lat.unit_cell}[u1].\text{get_op}(op1)$ acts on the site $(x_0+dx[0], \dots,$

$x_{\{\text{dim}-1\}+dx[\text{dim}-1]}$, $u1$). Possible combinations $x_0, \dots, x_{\{\text{dim}-1\}}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on dx , and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments `str_on_first` and `raise_op2_left` will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* / *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* / *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```


The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap *u1* <-> *u2*), and use the opposite direction *-dx*, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **`strength`** (*float*) – The strength of the coupling term.
- **`j`** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **`op2`** (*op1*,) – Names of the involved operators.

- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for *coupling_terms*. Defaults to a string of the form "{op1}_i {op2}_j".
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms ()
Sum of all *coupling_terms*.

calc_H_onsite (*tol_zero=1e-15*)
Calculate *H_onsite* from *self.onsite_terms*.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take *explicit_plus_hc* into account.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- **H_onsite** (*list of np.ndarray*)
- onsite terms of the Hamiltonian. If *explicit_plus_hc* is *True*, – Hermitian conjugates of the onsite terms will be included.

calc_H_bond (*tol_zero=1e-15*)
calculate *H_bond* from *coupling_terms* and *onsite_terms*.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of *NearestNeighborModel*.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises *ValueError* : if the Hamiltonian contains longer-range terms.:

calc_H_MPO (*tol_zero=1e-15*)
Calculate MPO representation of the Hamiltonian.

Uses *onsite_terms* and *coupling_terms* to build an MPO graph (and then an MPO).

Parameters *tol_zero* (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type *MPO*

coupling_strength_add_ext_flux (*strength, dx, phase*)
Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase *phi* when hopping around the cylinder.

Returns **strength** – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the *x*-direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase *phi* given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to `factor*N_sites_per_ring`. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (`Lx*factor`, *Ly*, ..., *Lu*).

classmethod **from_hdf5** (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which represents the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type `cls`

group_sites ($n=2$, *grouped_sites*=None)

Modify *self* in place to group sites.

Group each n sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (None | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

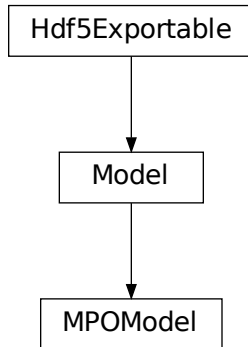
Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

MPOModel

- full name: `tenpy.models.model.MPOModel`
- parent module: `tenpy.models.model`
- type: class

Inheritance Diagram



Methods

<code>MPOModel.__init__(lattice, H_MPO)</code>	Initialize self.
<code>MPOModel.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>MPOModel.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>MPOModel.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>MPOModel.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>MPOModel.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>MPOModel.test_sanity()</code>	

class `tenpy.models.model.MPOModel` (*lattice*, *H_MPO*)

Bases: `tenpy.models.model.Model`

Base class for a model with an MPO representation of the Hamiltonian.

In this class, the Hamiltonian gets represented by an MPO. Thus, instances of this class are suitable for MPO-based algorithms like DMRG *dmrg* and MPO time evolution.

Todo: implement MPO for time evolution...

Parameters **H_MPO** (MPO) – The Hamiltonian rewritten as an MPO.

H_MPO

MPO representation of the Hamiltonian. If the *explicit_plus_hc* flag of the MPO is *True*, the represented Hamiltonian is $H_MPO + \text{hermitian_cojugate}(H_MPO)$.

Type `tenpy.networks.mpo.MPO`

enlarge_mps_unit_cell (*factor*=2)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor***N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx***factor*, *Ly*, ..., *Lu*).

group_sites (*n*=2, *grouped_sites*=None)

Modify *self* in place to group sites.

Group each *n* sites together using the [GroupedSite](#). This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (None | list of [GroupedSite](#)) – The sites grouped together.

Returns **grouped_sites** – The sites grouped together.

Return type list of [GroupedSite](#)

calc_H_bond_from_MPO (*tol_zero*=1e-15)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm < *tol_zero* are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of [NearestNeighborModel](#).
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of [Array](#)

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

classmethod **from_hdf5** (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with [save_hdf5\(\)](#).

Parameters

- **hdf5_loader** ([Hdf5Loader](#)) – Instance of the loading engine.
- **h5gr** ([Group](#)) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type cls

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with [from_hdf5\(\)](#).

This implementation saves the content of `__dict__` with [save_dict_content\(\)](#), storing the format under the attribute 'format'.

Parameters

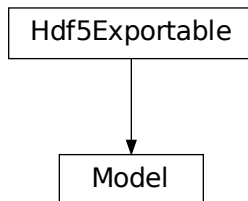
- **hdf5_saver** ([Hdf5Saver](#)) – Instance of the saving engine.

- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Model

- full name: `tenpy.models.model.Model`
- parent module: `tenpy.models.model`
- type: class

Inheritance Diagram



Methods

<code>Model.__init__(lattice)</code>	Initialize <i>self</i> .
<code>Model.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>Model.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Model.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>Model.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.

class `tenpy.models.model.Model` (*lattice*)

Bases: `tenpy.tools.hdf5_io.Hdf5Exportable`

Base class for all models.

The common base to all models is the underlying Hilbert space and geometry, specified by a `Lattice`.

Parameters **lattice** (`Lattice`) – The lattice defining the geometry and the local Hilbert space(s).

lat

The lattice defining the geometry and the local Hilbert space(s).

Type `Lattice`

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

group_sites ($n=2$, *grouped_sites=None*)
Modify *self* in place to group sites.

Group each n sites together using the [GroupedSite](#). This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of [GroupedSite](#)) – The sites grouped together.

Returns **grouped_sites** – The sites grouped together.

Return type list of [GroupedSite](#)

classmethod **from_hdf5** (*hdf5_loader, h5gr, subpath*)
Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with [save_hdf5\(\)](#).

Parameters

- **hdf5_loader** ([Hdf5Loader](#)) – Instance of the loading engine.
- **h5gr** ([Group](#)) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `' / '` in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type *cls*

save_hdf5 (*hdf5_saver, h5gr, subpath*)
Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with [from_hdf5\(\)](#).

This implementation saves the content of `__dict__` with [save_dict_content\(\)](#), storing the format under the attribute `'format'`.

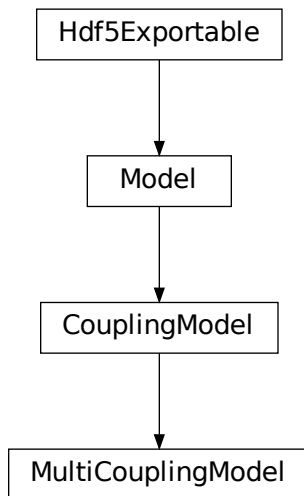
Parameters

- **hdf5_saver** ([Hdf5Saver](#)) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a `' / '` in the end.

MultiCouplingModel

- full name: `tenpy.models.model.MultiCouplingModel`
- parent module: `tenpy.models.model`
- type: class

Inheritance Diagram



Methods

<code>MultiCouplingModel.__init__(lattice[, ...])</code>	Initialize self.
<code>MultiCouplingModel.add_coupling(strength, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>MultiCouplingModel.add_coupling_term(...[, ...])</code>	Add a two-site coupling term on given MPS sites.
<code>MultiCouplingModel.add_local_term(strength, term)</code>	Add a single term to <i>self</i> .
<code>MultiCouplingModel.add_multi_coupling(...[, ...])</code>	Add multi-site coupling terms to the Hamiltonian, summing over lattice sites.
<code>MultiCouplingModel.add_multi_coupling_term(...)</code>	Add a general M-site coupling term on given MPS sites.
<code>MultiCouplingModel.add_onsite(strength, u, ...)</code>	Add onsite terms to <code>onsite_terms</code> .
<code>MultiCouplingModel.add_onsite_term(strength, ...)</code>	Add an onsite term on a given MPS site.

continues on next page

Table 101 – continued from previous page

<code>MultiCouplingModel.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>MultiCouplingModel.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>MultiCouplingModel.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>MultiCouplingModel.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>MultiCouplingModel.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>MultiCouplingModel.coupling_strength_add_ext_flux(...)</code>	Add an external flux to the coupling strength.
<code>MultiCouplingModel.enlarge_mps_unit_cell([...])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>MultiCouplingModel.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>MultiCouplingModel.group_sites([n, ...])</code>	Modify <code>self</code> in place to group sites.
<code>MultiCouplingModel.save_hdf5(hdf5_saver, ...)</code>	Export <code>self</code> into a HDF5 file.
<code>MultiCouplingModel.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.

class `tenpy.models.model.MultiCouplingModel` (*lattice*, *bc_coupling=None*, *explicit_plus_hc=False*)

Bases: `tenpy.models.model.CouplingModel`

Generalizes `CouplingModel` to allow couplings involving more than two sites.

The corresponding couplings can be added with `add_multi_coupling()` and `add_multi_coupling_term()` and are saved in `coupling_terms`, which can now contain instances of `MultiCouplingTerms`.

add_multi_coupling (*strength*, *ops*, *_deprecate_1='DEPRECATED'*, *_deprecate_2='DEPRECATED'*, *op_string=None*, *category=None*, *plus_hc=False*)

Add multi-site coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{\vec{x}} \text{strength}[\text{shift}(\vec{x})] * OP_0 * OP_1 * \dots * OP_{M-1}$, involving M operators. Here, OP_m stands for the operator defined by the m -th tuple (*opname*, *dx*, *u*) given in the argument *ops*, which determines the position $\vec{x} + \vec{dx}$ and unit-cell index u of the site it acts on; the actual operator is given by `self.lat.unit_cell[u].get_op(opname)`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_multi_couplings()` and depends on the boundary conditions. The `shift(...)` depends on the *dx* entries of *ops* and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.6.0: We switched from the three arguments *u0*, *op0* and *other_op* with `other_ops=[(u1, op1, dx1), (op2, u2, dx2), ...]` to a single, equivalent argument *ops* which should now read `ops=[(op0, dx0, u0), (op1, dx1, u1), (op2, dx2, u2), ...]`, where `dx0 = [0]*self.lat.dim`. Note the changed order inside the tuples!

Parameters

- **strength** (*scalar* / *array*) – Prefactor of the coupling. May vary spatially, and is tiled to the required shape.

- **ops** (list of (opname, dx, u)) – Each tuple determines one operator of the coupling, see the description above. *opname* (str) is the name of the operator, *dx* (list of length *lat.dim*) is a translation vector, and *u* (int) is the index of *lat.unit_cell* on which the operator acts. The first entry of *ops* corresponds to OP_0 and acts last in the physical sense.
- **op_string** (str | None) – If a string is given, we use this as the name of an operator to be used inbetween the operators, *excluding* the sites on which any operators act. This operator should be defined on all sites in the unit cell.
If None, auto-determine whether a Jordan-Wigner string is needed (using *op_needs_JW()*) for each of the segments inbetween the operators and also on the sites of the left operators.
- **category** (str) – Descriptive name used as key for *coupling_terms*. Defaults to a string of the form "{op0}_i {other_ops[0]}_j {other_ops[1]}_k ...".
- **plus_hc** (bool) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

A call to *add_coupling()* with arguments *add_coupling(strength, u1, 'A', u2, 'B', dx)* is equivalent to the following:

```
>>> dx_0 = [0] * self.lat.dim # = [0] for a 1D lattice, [0, 0] in 2D
>>> self.add_coupling(strength, [('A', dx_0, u1), ('B', dx, u2)])
```

To explicitly add the hermitian conjugate, you need to take the complex conjugate of the *strength*, reverse the order of the operators and take the hermitian conjugates of the individual operator names:

```
>>> self.add_coupling(np.conj(strength), [(hc('B'), dx, u2), (hc('A'), dx_0,
↪u1)]) # h.c.
```

See also:

add_onsite() Add terms acting on one site only.

add_coupling() Add terms acting on two sites.

add_multi_coupling_term() Add a single term, not summing over the possible \vec{x} .

add_multi_coupling_term (*strength, ijl, ops_ijkl, op_string, category=None, plus_hc=False*)
Add a general M-site coupling term on given MPS sites.

Wrapper for *self.coupling_terms[category].add_multi_coupling_term(...)*.

Warning: This function does not handle Jordan-Wigner strings! You might want to use *add_local_term()* instead.

Parameters

- **strength** (float) – The strength of the coupling term.
- **ijkl** (list of int) – The MPS indices of the sites on which the operators acts. With *i, j, k, ... = ijl*, we require that they are ordered ascending, $i < j < k < \dots$ and that $0 \leq i < N_{\text{sites}}$. Indices $\geq N_{\text{sites}}$ indicate couplings between different unit cells of an infinite MPS.

- **ops_ijkl** (*list of str*) – Names of the involved operators on sites i, j, k, \dots
- **op_string** (*list of str*) – Names of the operator to be inserted between the operators, e.g., `op_string[0]` is inserted between i and j .
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op0}_{i} {op1}_{j} {op2}_{k} ..."`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_coupling (*strength, u1, op1, u2, op2, dx, op_string=None, str_on_first=True, raise_op2_left=False, category=None, plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{dim-1}} strength[shift(\vec{x})] * OP0 * OP1$, where `OP0 := lat.unit_cell[u0].get_op(op0)` acts on the site $(x_0, \dots, x_{dim-1}, u1)$, and `OP1 := lat.unit_cell[u1].get_op(op1)` acts on the site $(x_0+dx[0], \dots, x_{dim-1}+dx[dim-1], u1)$. Possible combinations x_0, \dots, x_{dim-1} are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar | array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str | None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.

- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form "{op1}_i {op2}_j".
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪ Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

add_onsite() Add terms acting on one site only.

MultiCouplingModel.add_multi_coupling_term() for terms on more than two sites.

add_coupling_term() Add a single term without summing over *vecx*.

add_coupling_term (*strength*, *i*, *j*, *op_i*, *op_j*, *op_string*='Id', *category*=None, *plus_hc*=False)

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category*=None, *plus_hc*=False)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category*=None, *plus_hc*=False)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x_0*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to `onsite_terms`; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar | array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.

- **u** (*int*) – Picks a `Site lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

`add_coupling()` Add a terms acting on two sites.

`add_onsite_term()` Add a single term without summing over *vecx*.

`add_onsite_term(strength, i, op, category=None, plus_hc=False)`

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

`all_coupling_terms()`

Sum of all `coupling_terms`.

`all_onsite_terms()`

Sum of all `onsite_terms`.

`calc_H_MPO(tol_zero=1e-15)`

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

`calc_H_bond(tol_zero=1e-15)`

calculate *H_bond* from `coupling_terms` and `onsite_terms`.

Parameters **tol_zero** (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of *NearestNeighborModel*.

Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_onsite (*tol_zero=1e-15*)

Calculate *H_onsite* from *self.onsite_terms*.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- **H_onsite** (*list of npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase *phi* when hopping around the cylinder.

Returns **strength** – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let’s say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the *FermionSite*. The cylinder axis is the *x*-direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase *phi* given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
```

(continues on next page)

(continued from previous page)

```

...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)

```

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n=2, grouped_sites=None*)

Modify *self* in place to group sites.

Group each n sites together using the `GroupedSite`. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of `GroupedSite`) – The sites grouped together.

Returns **grouped_sites** – The sites grouped together.

Return type list of `GroupedSite`

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute `'format'`.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

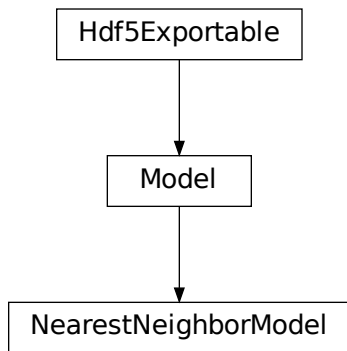
test_sanity()

Sanity check, raises ValueErrors, if something is wrong.

NearestNeighborModel

- full name: `tenpy.models.model.NearestNeighborModel`
- parent module: `tenpy.models.model`
- type: class

Inheritance Diagram



Methods

<code>NearestNeighborModel.__init__(lattice, H_bond)</code>	Initialize self.
<code>NearestNeighborModel.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>NearestNeighborModel.calc_H_MPO_from_bond(...)</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>NearestNeighborModel.enlarge_mps_unit_cell(...)</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>NearestNeighborModel.from_MPOModel(mpo_model)</code>	Initialize a NearestNeighborModel from a model class defining an MPO.
<code>NearestNeighborModel.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>NearestNeighborModel.group_sites([n, ...])</code>	Modify <i>self</i> in place to group sites.
<code>NearestNeighborModel.save_hdf5(hdf5_saver, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>NearestNeighborModel.test_sanity()</code>	

continues on next page

Table 102 – continued from previous page

<code>NearestNeighborModel.</code> <code>trivial_like_NNModel()</code>	Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.
---	---

class `tenpy.models.model.NearestNeighborModel` (*lattice*, *H_bond*)

Bases: `tenpy.models.model.Model`

Base class for a model of nearest neighbor interactions w.r.t. the MPS index.

In this class, the Hamiltonian $H = \sum_i H_{i,i+1}$ is represented by “bond terms” $H_{i,i+1}$ acting only on two neighboring sites i and $i+1$, where i is an integer. Instances of this class are suitable for *tebd*.

Note that the “nearest-neighbor” in the name refers to the MPS index, not the lattice. In short, this works only for 1-dimensional (1D) nearest-neighbor models: A 2D lattice is internally mapped to a 1D MPS “snake”, and even a nearest-neighbor coupling in 2D becomes long-range in the MPS chain.

Parameters

- **lattice** (`tenpy.model.lattice.Lattice`) – The lattice defining the geometry and the local Hilbert space(s).
- **H_bond** (list of {`Array` | `None`}) – The Hamiltonian rewritten as $\sum_i H_bond[i]$ for MPS indices i . $H_bond[i]$ acts on sites $(i-1, i)$; we require $\text{len}(H_bond) == \text{lat.N_sites}$. Legs of each $H_bond[i]$ are `['p0', 'p0*', 'p1', 'p1*']`.

H_bond

The Hamiltonian rewritten as $\sum_i H_bond[i]$ for MPS indices i . $H_bond[i]$ acts on sites $(i-1, i)$, `None` represents 0. Legs of each $H_bond[i]$ are `['p0', 'p0*', 'p1', 'p1*']`. *H_bond* is not affected by the *explicit_plus_hc* flag of a *CouplingModel*.

Type list of {`Array` | `None`}

classmethod from_MPOModel (*mpo_model*)

Initialize a NearestNeighborModel from a model class defining an MPO.

This is especially usefull in combination with *MPOModel.group_sites()*.

Parameters *mpo_model* (*MPOModel*) – A model instance implementing the MPO. Does not need to be a *NearestNeighborModel*, but should only have nearest-neighbor couplings.

Examples

The *SpinChainNNN2* has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn’t define *H_bond*. However, we can initialize a NearestNeighborModel from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

trivial_like_NNModel()

Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.

bond_energies(*psi*)

Calculate bond energies $\langle \psi | H_{\text{bond}} | \psi \rangle$.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, $E_{\text{Bond}}[i]$ is the energy of bond i , $i+1$. (i.e. we omit bond 0 between sites $L-1$ and 0); for infinite bc $E_{\text{bond}}[i]$ is the energy of bond $i-1$, i .

Return type 1D ndarray

enlarge_mps_unit_cell(*factor*=2)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} * N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x * \text{factor}, L_y, \dots, L_u)$.

group_sites(*n*=2, *grouped_sites*=None)

Modify *self* in place to group sites.

Group each n sites together using the [GroupedSite](#). This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (None | list of [GroupedSite](#)) – The sites grouped together.

Returns **grouped_sites** – The sites grouped together.

Return type list of [GroupedSite](#)

calc_H_MPO_from_bond(*tol_zero*=1e-15)

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm $< \text{tol_zero}$ are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

classmethod from_hdf5(*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with [save_hdf5\(\)](#).

Parameters

- **hdf5_loader** ([Hdf5Loader](#)) – Instance of the loading engine.
- **h5gr** ([Group](#)) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `' / '` in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Module description

This module contains some base classes for models.

A ‘model’ is supposed to represent a Hamiltonian in a generalized way. The *Lattice* specifies the geometry and underlying Hilbert space, and is thus common to all models. It is needed to initialize the common base class *Model* of all models.

Different algorithms require different representations of the Hamiltonian. For example for DMRG, the Hamiltonian needs to be given as an MPO, while TEBD needs the Hamiltonian to be represented by ‘nearest neighbor’ bond terms. This module contains the base classes defining these possible representations, namely the *MPOModel* and *NearestNeighborModel*.

A particular model like the *XXZChain* should then yet another class derived from these classes. In its `__init__`, it needs to explicitly call the *MPOModel.__init__(self, lattice, H_MPO)*, providing an MPO representation of *H*, and also the *NearestNeighborModel.__init__(self, lattice, H_bond)*, providing a representation of *H* by bond terms *H_bond*.

The *CouplingModel* is the attempt to generalize the representation of *H* by explicitly specifying the couplings in a general way, and providing functionality for converting them into *H_MPO* and *H_bond*. This allows to quickly generate new model classes for a very broad class of Hamiltonians.

For simplicity, the *CouplingModel* is limited to interactions involving only two sites. Yet, we also provide the *MultiCouplingModel* to generate Models for Hamiltonians involving couplings between multiple sites.

The *CouplingMPOModel* aims at structuring the initialization for most models and is used as base class in (most of) the predefined models in TeNPy.

See also the introduction in *Models*.

Specific models

<i>tf_ising</i>	Prototypical example of a quantum model: the transverse field Ising model.
<i>xxz_chain</i>	Prototypical example of a 1D quantum model: the spin-1/2 XXZ chain.
<i>spins</i>	Nearest-neighbour spin-S models.
<i>spins_nnn</i>	Next-Nearest-neighbour spin-S models.

continues on next page

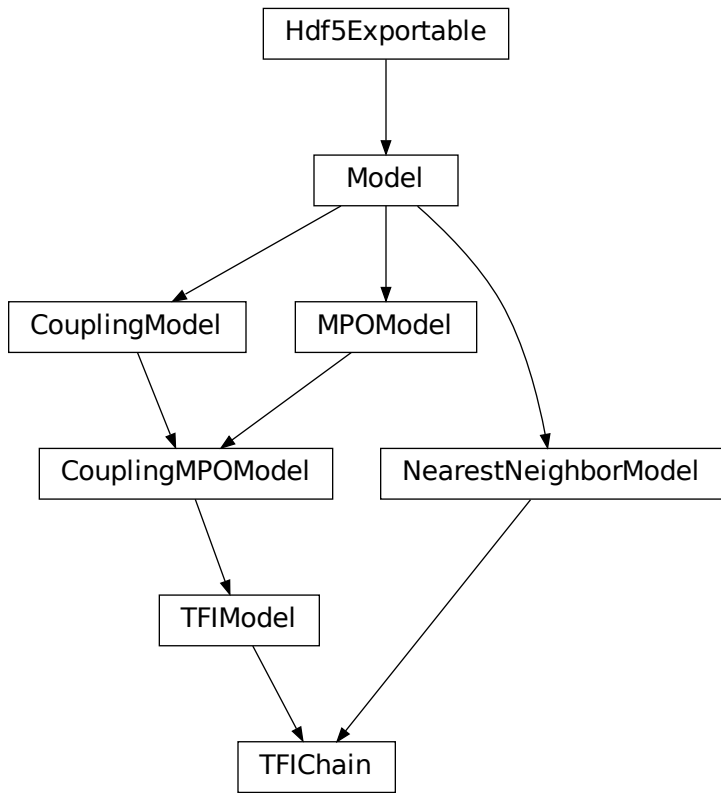
Table 103 – continued from previous page

<i>fermions_spinless</i>	Spinless fermions with hopping and interaction.
<i>hubbard</i>	Bosonic and fermionic Hubbard models.
<i>hofstadter</i>	Cold atomic (Harper-)Hofstadter model on a strip or cylinder.
<i>haldane</i>	Bosonic and fermionic Haldane models.
<i>toric_code</i>	Kitaev’s exactly solvable toric code model.

7.9.3 tf_ising

- full name: `tenpy.models.tf_ising`
- parent module: `tenpy.models`
- type: module

Classes



<i>TFIChain</i> (model_params)	The <code>TFIModel</code> on a Chain, suitable for TEBD.
continues on next page	

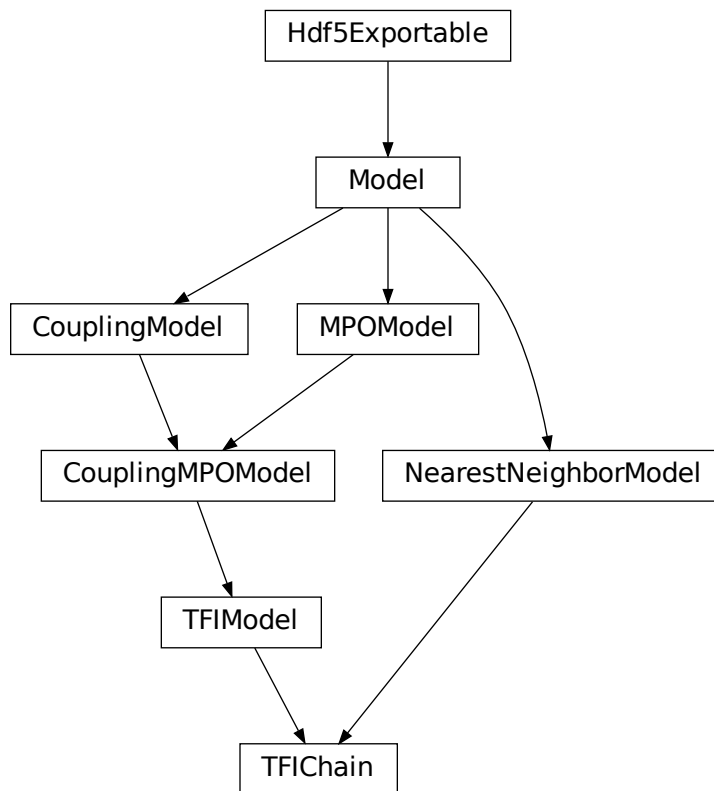
Table 104 – continued from previous page

TFIModel(model_params)	Transverse field Ising model on a general lattice.
------------------------	--

TFIChain

- full name: `tenpy.models.tf_ising.TFIChain`
- parent module: `tenpy.models.tf_ising`
- type: class

Inheritance Diagram



Methods

<code>TFIChain.__init__(model_params)</code>	Initialize self.
<code>TFIChain.add_coupling(strength, u1, op1, u2, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>TFIChain.add_coupling_term(strength, i, j, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>TFIChain.add_local_term(strength, term[, ...])</code>	Add a single term to <i>self</i> .
<code>TFIChain.add_onsite(strength, u, opname[, ...])</code>	Add onsite terms to <code>onsite_terms</code> .
<code>TFIChain.add_onsite_term(strength, i, op[, ...])</code>	Add an onsite term on a given MPS site.
<code>TFIChain.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>TFIChain.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>TFIChain.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>TFIChain.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>TFIChain.calc_H_MPO_from_bond([tol_zero])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>TFIChain.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>TFIChain.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>TFIChain.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>TFIChain.coupling_strength_add_ext_flux(dx)</code>	Add an external flux to the coupling strength.
<code>TFIChain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>TFIChain.from_MPOModel(mpo_model)</code>	Initialize a NearestNeighborModel from a model class defining an MPO.
<code>TFIChain.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>TFIChain.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>TFIChain.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>TFIChain.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>TFIChain.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>TFIChain.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>TFIChain.test_sanity()</code>	Sanity check, raises ValueErrors, if something is wrong.
<code>TFIChain.trivial_like_NNModel()</code>	Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.tf_ising.TFIChain(model_params)`

Bases: `tenpy.models.tf_ising.TFIModel`, `tenpy.models.model.NearestNeighborModel`

The TFIModel on a Chain, suitable for TEBD.

See the TFIModel for the documentation of parameters.

add_coupling (*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*, *raise_op2_left=False*, *category=None*, *plus_hc=False*)
Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\text{dim}-1}} \text{strength}[\text{shift}(\vec{x})] * OP_0 * OP_1$, where $OP_0 := \text{lat.unit_cell}[u_0].\text{get_op}(op_0)$ acts on the site $(x_0, \dots, x_{\{\text{dim}-1\}}, u_1)$,

and `OP1 := lat.unit_cell[u1].get_op(op1)` acts on the site $(x_0+dx[0], \dots, x_{\{dim-1\}}+dx[dim-1], u1)$. Possible combinations $x_0, \dots, x_{\{dim-1\}}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* / *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* / *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.

- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for *coupling_terms*. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category=None*, *plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to *onsite_terms* or *coupling_terms*, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for *onsite_terms* or *coupling_terms*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category=None*, *plus_hc=False*)

Add onsite terms to *onsite_terms*.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x₀*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to *onsite_terms*; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar / array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a Site *lat.unit_cell[u]* out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in *lat.unit_cell[u]*.
- **category** (*str*) – Descriptive name used as key for *onsite_terms*. Defaults to *opname*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

[**add_coupling\(\)**](#) Add a terms acting on two sites.

[**add_onsite_term\(\)**](#) Add a single term without summing over *vecx*.

add_onsite_term (*strength*, *i*, *op*, *category=None*, *plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms ()

Sum of all `coupling_terms`.

all_onsite_terms ()

Sum of all `onsite_terms`.

bond_energies (*psi*)

Calculate bond energies $\langle \text{psi} | H_{\text{bond}} | \text{psi} \rangle$.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

calc_H_MPO (*tol_zero=1e-15*)

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_MPO_from_bond (*tol_zero=1e-15*)

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm $< \text{tol_zero}$ are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_bond (*tol_zero=1e-15*)

calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters **tol_zero** (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises ValueError : if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters *tol_zero* (*float*) – Arrays with norm < *tol_zero* are considered to be zero.

Returns *H_bond* – Bond terms as required by the constructor of `NearestNeighborModel`.

Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises ValueError : if the Hamiltonian contains longer-range terms.:

calc_H_onsite (*tol_zero=1e-15*)

Calculate *H_onsite* from *self.onsite_terms*.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- *H_onsite* (list of *np.ndarray*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar* | *array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase *phi* when hopping around the cylinder.

Returns *strength* – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the x -direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase ϕ given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

classmethod from_MPOModel (*mpo_model*)

Initialize a NearestNeighborModel from a model class defining an MPO.

This is especially usefull in combination with `MPOModel.group_sites()`.

Parameters **mpo_model** (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The `SpinChainNNN2` has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a `NearestNeighborModel` from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod `from_hdf5(hdf5_loader, h5gr, subpath)`

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which is represent the object to be constructed.
- **subpath** (`str`) – The *name* of `h5gr` with a `' / '` in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

group_sites (`n=2, grouped_sites=None`)

Modify *self* in place to group sites.

Group each *n* sites together using the `GroupedSite`. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (`int`) – Number of sites to be grouped together.
- **grouped_sites** (`None` | list of `GroupedSite`) – The sites grouped together.

Returns `grouped_sites` – The sites grouped together.

Return type list of `GroupedSite`

init_lattice (`model_params`)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full `Lattice` instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters `model_params` (`dict`) – The model parameters given to `__init__`.

Returns `lat` – An initialized lattice.

Return type `Lattice`

Options

option `CouplingMPOModel.lattice: str | Lattice`

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) Lattice instance. In the latter case, no further parameters are read out.

option `CouplingMPOModel.bc_MPS: str`

Boundary conditions for the MPS.

option `CouplingMPOModel.order: str`

The order of sites within the lattice for non-trivial lattices, e.g. `'default'`, `'snake'`, see `ordering()`. Only used if *lattice* is a string.

option `CouplingMPOModel.L: int`

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option `CouplingMPOModel.Lx`: **int**

option `CouplingMPOModel.Ly`: **int**

The length in x- and y-direction; only read out for 2D lattices. For "infinite" *bc_MPS*, the system is infinite in x-direction and *Lx* is the number of “rings” in the infinite MPS unit cell, while *Ly* gives the circumference around the cylinder or width of the rung for a ladder (depending on *bc_y*).

option `CouplingMPOModel.bc_y`: **str**

"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x`: **str**

"open" | "periodic". Can be used to force “periodic” boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for *bc_MPS*="finite" and "periodic" for *bc_MPS*="infinite". If you are not aware of the consequences, you should probably *not* use “periodic” boundary conditions. (The MPS is still “open”, so this will introduce long-range couplings between the first and last sites of the MPS!)

init_sites (*model_params*)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by *init_lattice()* to get the *Site* for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept *conserve*=None to disable using quantum numbers. Many models in TeNPy read out the *conserve* model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters *model_params* (*dict*) – The model parameters given to `__init__`.

Returns *sites* – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) *Site*

init_terms (*model_params*)

Add the onsite and coupling terms to the model; subclasses should implement this.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

test_sanity ()

Sanity check, raises ValueErrors, if something is wrong.

trivial_like_NNModel ()

Return a NearestNeighborModel with same lattice, but trivial (H=0) bonds.

Module description

Prototypical example of a quantum model: the transverse field Ising model.

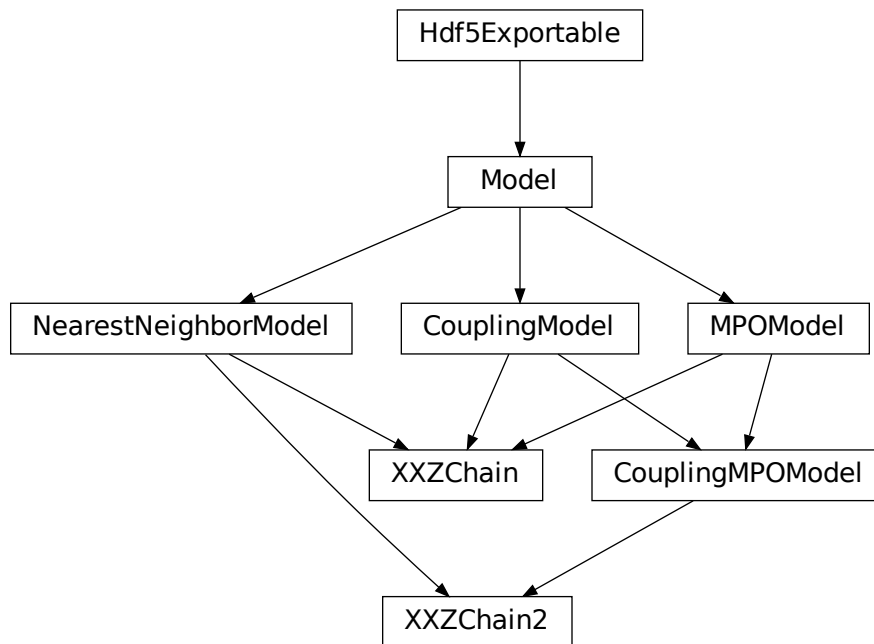
Like the `XXZChain`, the transverse field Ising chain `TFIChain` is contained in the more general `SpinChain`; the idea is more to serve as a pedagogical example for a ‘model’.

We choose the field along z to allow to conserve the parity, if desired.

7.9.4 xxz_chain

- full name: `tenpy.models.xxz_chain`
- parent module: `tenpy.models`
- type: module

Classes

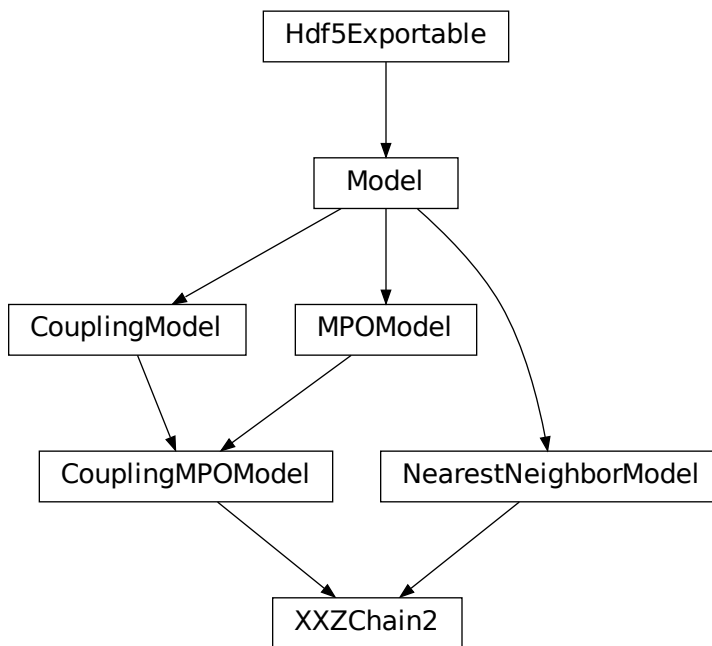


<code>XXZChain(model_params)</code>	Spin-1/2 XXZ chain with Sz conservation.
<code>XXZChain2(model_params)</code>	Another implementation of the Spin-1/2 XXZ chain with Sz conservation.

XXZChain2

- full name: `tenpy.models.xxz_chain.XXZChain2`
- parent module: `tenpy.models.xxz_chain`
- type: class

Inheritance Diagram



Methods

<code>XXZChain2.__init__(model_params)</code>	Initialize self.
<code>XXZChain2.add_coupling(strength, u1, op1, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>XXZChain2.add_coupling_term(strength, i, j, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>XXZChain2.add_local_term(strength, term[, ...])</code>	Add a single term to <i>self</i> .
<code>XXZChain2.add_onsite(strength, u, opname[, ...])</code>	Add onsite terms to <code>onsite_terms</code> .
<code>XXZChain2.add_onsite_term(strength, i, op[, ...])</code>	Add an onsite term on a given MPS site.

continues on next page

Table 107 – continued from previous page

<code>XXZChain2.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>XXZChain2.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>XXZChain2.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>XXZChain2.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>XXZChain2.calc_H_MPO_from_bond([tol_zero])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>XXZChain2.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>XXZChain2.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>XXZChain2.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>XXZChain2.coupling_strength_add_ext_flux([flux])</code>	Add an external flux to the coupling strength.
<code>XXZChain2.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>XXZChain2.from_MPOModel(mpo_model)</code>	Initialize a <code>NearestNeighborModel</code> from a model class defining an MPO.
<code>XXZChain2.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>XXZChain2.group_sites([n, grouped_sites])</code>	Modify <code>self</code> in place to group sites.
<code>XXZChain2.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>XXZChain2.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>XXZChain2.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>XXZChain2.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <code>self</code> into a HDF5 file.
<code>XXZChain2.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>XXZChain2.trivial_like_NNModel()</code>	Return a <code>NearestNeighborModel</code> with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.xxz_chain.XXZChain2` (*model_params*)

Bases: `tenpy.models.model.CouplingMPOModel`, `tenpy.models.model.NearestNeighborModel`

Another implementation of the Spin-1/2 XXZ chain with Sz conservation.

This implementation takes the same parameters as the `XXZChain`, but is implemented based on the `CouplingMPOModel`.

Parameters `model_params` (dict | Config) – See `XXZChain`

init_sites (*model_params*)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by `init_lattice()` to get the *Site* for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept `conserve=None` to disable using quantum numbers. Many models in TeNPy read out the *conserve* model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters `model_params` (*dict*) – The model parameters given to `__init__`.

Returns `sites` – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) *Site*

init_terms (*model_params*)

Add the onsite and coupling terms to the model; subclasses should implement this.

add_coupling (*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*,
raise_op2_left=False, *category=None*, *plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{dim-1}} strength[shift(\vec{x})] * OP0 * OP1$, where $OP0 := lat.unit_cell[u0].get_op(op0)$ acts on the site $(x_0, \dots, x_{dim-1}, u1)$, and $OP1 := lat.unit_cell[u1].get_op(op1)$ acts on the site $(x_0+dx[0], \dots, x_{dim-1}+dx[dim-1], u1)$. Possible combinations x_0, \dots, x_{dim-1} are determined from the boundary conditions in [possible_couplings\(\)](#).

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* | *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* | *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.

- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪ Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

add_onsite() Add terms acting on one site only.

MultiCouplingModel.add_multi_coupling_term() for terms on more than two sites.

add_coupling_term() Add a single term without summing over *vecx*.

add_coupling_term (*strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False*)

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category=None*, *plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category=None*, *plus_hc=False*)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x₀*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to `onsite_terms`; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar / array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a `lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.

- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

add_coupling() Add a terms acting on two sites.

add_onsite_term() Add a single term without summing over *vecx*.

add_onsite_term (*strength*, *i*, *op*, *category=None*, *plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms ()

Sum of all `coupling_terms`.

all_onsite_terms ()

Sum of all `onsite_terms`.

bond_energies (*psi*)

Calculate bond energies $\langle \text{psi} | H_{\text{bond}} | \text{psi} \rangle$.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

calc_H_MPO (*tol_zero=1e-15*)

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_MPO_from_bond (*tol_zero=1e-15*)

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm $< \text{tol_zero}$ are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_bond (*tol_zero=1e-15*)

calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters `tol_zero` (*float*) – Arrays with norm $< tol_zero$ are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_on-site (*tol_zero=1e-15*)

Calculate `H_on-site` from `self.on-site_terms`.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_on-site_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- `H_on-site` (list of *npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an

infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase ϕ when hopping around the cylinder.

Returns strength – The strength array to be used as `strength` in `add_coupling()` with the given `dx`.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the x -direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase ϕ given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (`factor=2`)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters factor (`int`) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

classmethod from_MPOModel (`mpo_model`)

Initialize a `NearestNeighborModel` from a model class defining an MPO.

This is especially useful in combination with `MPOModel.group_sites()`.

Parameters mpo_model (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The `SpinChainNNN2` has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a NearestNeighborModel from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod `from_hdf5` (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n=2*, *grouped_sites=None*)

Modify *self* in place to group sites.

Group each *n* sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

init_lattice (*model_params*)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full *Lattice* instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters **model_params** (*dict*) – The model parameters given to `__init__`.

Returns *lat* – An initialized lattice.

Return type *Lattice*

Options

option `CouplingMPOModel.lattice: str | Lattice`

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) Lattice instance. In the latter case, no further parameters are read out.

option `CouplingMPOModel.bc_MPS: str`

Boundary conditions for the MPS.

option `CouplingMPOModel.order: str`

The order of sites within the lattice for non-trivial lattices, e.g. 'default', 'snake', see `ordering()`. Only used if `lattice` is a string.

option `CouplingMPOModel.L: int`

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option `CouplingMPOModel.Lx: int`

option `CouplingMPOModel.Ly: int`

The length in x- and y-direction; only read out for 2D lattices. For "infinite" `bc_MPS`, the system is infinite in x-direction and `Lx` is the number of “rings” in the infinite MPS unit cell, while `Ly` gives the circumference around the cylinder or width of the rung for a ladder (depending on `bc_y`).

option `CouplingMPOModel.bc_y: str`

"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x: str`

"open" | "periodic". Can be used to force “periodic” boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for `bc_MPS="finite"` and "periodic" for `bc_MPS="infinite"`. If you are not aware of the consequences, you should probably *not* use “periodic” boundary conditions. (The MPS is still “open”, so this will introduce long-range couplings between the first and last sites of the MPS!)

save_hdf5 (`hdf5_saver`, `h5gr`, `subpath`)

Export `self` into a HDF5 file.

This method saves all the data it needs to reconstruct `self` with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (`Hdf5Saver`) – Instance of the saving engine.
- **h5gr** (`:class`Group``) – HDF5 group which is supposed to represent `self`.
- **subpath** (`str`) – The name of `h5gr` with a '/' in the end.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

trivial_like_NNModel ()

Return a `NearestNeighborModel` with same lattice, but trivial ($H=0$) bonds.

Module description

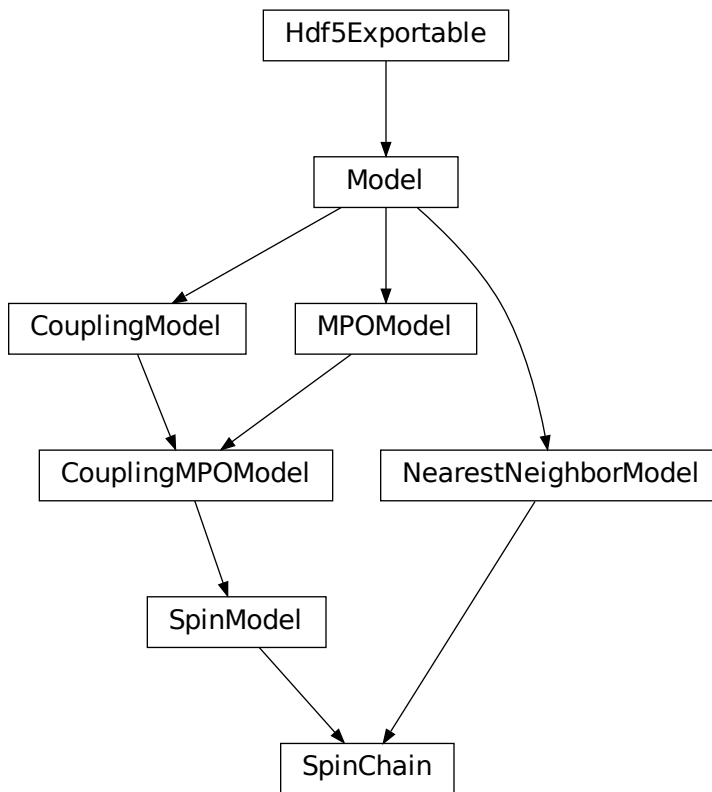
Prototypical example of a 1D quantum model: the spin-1/2 XXZ chain.

The XXZ chain is contained in the more general *SpinChain*; the idea of this module is more to serve as a pedagogical example for a model.

7.9.5 spins

- full name: `tenpy.models.spins`
- parent module: `tenpy.models`
- type: module

Classes

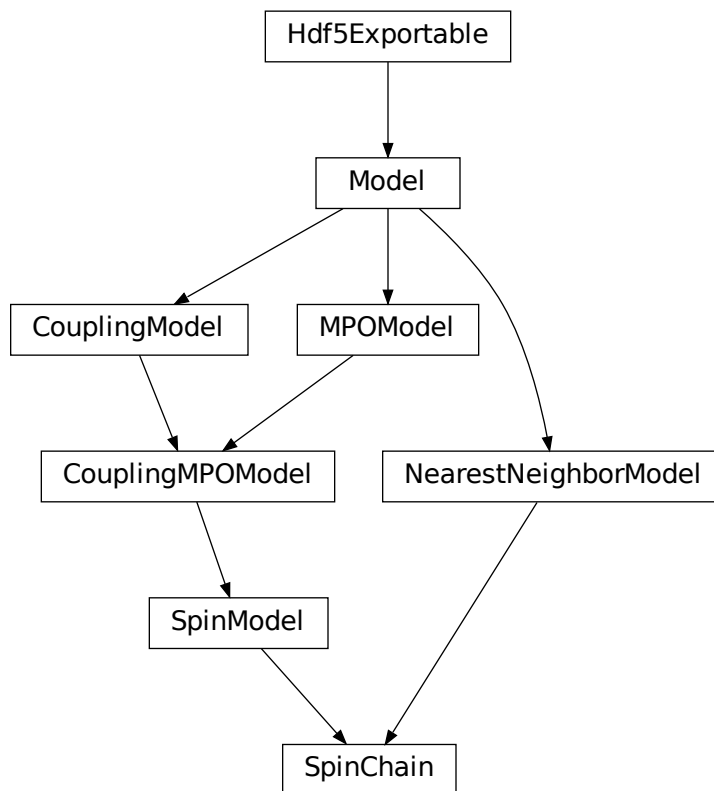


<code>SpinChain(model_params)</code>	The <code>SpinModel</code> on a Chain, suitable for TEBD.
<code>SpinModel(model_params)</code>	Spin-S sites coupled by nearest neighbour interactions.

SpinChain

- full name: `tenpy.models.spins.SpinChain`
- parent module: `tenpy.models.spins`
- type: class

Inheritance Diagram



Methods

<code>SpinChain.__init__(model_params)</code>	Initialize self.
<code>SpinChain.add_coupling(strength, u1, op1, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>SpinChain.add_coupling_term(strength, i, j, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>SpinChain.add_local_term(strength, term[, ...])</code>	Add a single term to <i>self</i> .

continues on next page

Table 109 – continued from previous page

<code>SpinChain.add_onsite(strength, u, opname[, ...])</code>	Add onsite terms to <code>onsite_terms</code> .
<code>SpinChain.add_onsite_term(strength, i, op[, ...])</code>	Add an onsite term on a given MPS site.
<code>SpinChain.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>SpinChain.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>SpinChain.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>SpinChain.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>SpinChain.calc_H_MPO_from_bond([tol_zero])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>SpinChain.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>SpinChain.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>SpinChain.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>SpinChain.coupling_strength_add_ext_flux(flux)</code>	Add an external flux to the coupling strength.
<code>SpinChain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>SpinChain.from_MPOModel(mpo_model)</code>	Initialize a <code>NearestNeighborModel</code> from a model class defining an MPO.
<code>SpinChain.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>SpinChain.group_sites([n, grouped_sites])</code>	Modify <code>self</code> in place to group sites.
<code>SpinChain.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>SpinChain.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>SpinChain.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>SpinChain.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <code>self</code> into a HDF5 file.
<code>SpinChain.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>SpinChain.trivial_like_NNModel()</code>	Return a <code>NearestNeighborModel</code> with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.spins.SpinChain(model_params)`

Bases: `tenpy.models.spins.SpinModel`, `tenpy.models.model.NearestNeighborModel`

The `SpinModel` on a Chain, suitable for TEBD.

See the `SpinModel` for the documentation of parameters.

add_coupling(*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*, *raise_op2_left=False*, *category=None*, *plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\text{dim}-1}} \text{strength}[\text{shift}(\vec{x})] * OP0 * OP1$, where $OP0 := \text{lat.unit_cell}[u0].\text{get_op}(op0)$ acts on the site $(x_0, \dots, x_{\{\text{dim}-1\}})$, $u1$, and $OP1 := \text{lat.unit_cell}[u1].\text{get_op}(op1)$ acts on the site $(x_0+dx[0], \dots, x_{\{\text{dim}-1\}}+dx[\text{dim}-1], u1)$. Possible combinations $x_0, \dots, x_{\{\text{dim}-1\}}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first

entry `strength[0, 0, ...]` of `strength` is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments `str_on_first` and `raise_op2_left` will be removed in version 1.0.0.

Parameters

- **strength** (*scalar / array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str / None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If `None`, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided `op_string` should also act on the first site. This option should be chosen as `True` for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the `op_string` to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of `op1` or `op2` acts first on a given state). We follow the convention that `op2` acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when `op2` appears left of `op1` (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.
- **plus_hc** (*bool*) – If `True`, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪ Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **`strength(float)`** – The strength of the coupling term.
- **`j(i,)`** – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **`op2(op1,)`** – Names of the involved operators.
- **`op_string(str)`** – The operator to be inserted between *i* and *j*.

- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form "`{op1}_i {op2}_j`".
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength, term, category=None, plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname, lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example `[x, y, u]` for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength, u, opname, category=None, plus_hc=False*)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index $(x_0, \dots, x_{\{\text{dim}-1\}}, u)$,

The necessary terms are just added to `onsite_terms`; doesn't rebuild the MPO.

Parameters

- **strength** (*scalar | array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a `lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

[`add_coupling\(\)`](#) Add a terms acting on two sites.

[`add_onsite_term\(\)`](#) Add a single term without summing over *vecx*.

add_onsite_term (*strength, i, op, category=None, plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.

- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms ()
Sum of all `coupling_terms`.

all_onsite_terms ()
Sum of all `onsite_terms`.

bond_energies (*psi*)
Calculate bond energies `<psi|H_bond|psi>`.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

calc_H_MPO (*tol_zero=1e-15*)
Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_MPO_from_bond (*tol_zero=1e-15*)
Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm `< tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_bond (*tol_zero=1e-15*)
calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters **tol_zero** (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError`: if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)
Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm `< tol_zero` are considered to be zero.

Returns **H_bond** – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_onsite (*tol_zero=1e-15*)

Calculate *H_onsite* from *self.onsite_terms*.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- **H_onsite** (*list of npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase *phi* when hopping around the cylinder.

Returns **strength** – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let’s say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the *FermionSite*. The cylinder axis is the *x*-direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase *phi* given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↳ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (*factor*=2)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

classmethod from_MPOModel (*mpo_model*)

Initialize a NearestNeighborModel from a model class defining an MPO.

This is especially useful in combination with `MPOModel.group_sites()`.

Parameters **mpo_model** (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The *SpinChainNNN2* has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a `NearestNeighborModel` from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.

- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n*=2, *grouped_sites*=None)

Modify *self* in place to group sites.

Group each *n* sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (None | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

init_lattice (*model_params*)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full *Lattice* instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters *model_params* (*dict*) – The model parameters given to `__init__`.

Returns *lat* – An initialized lattice.

Return type *Lattice*

Options

option *CouplingMPOModel.lattice*: *str* | *Lattice*

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) *Lattice* instance. In the latter case, no further parameters are read out.

option *CouplingMPOModel.bc_MPS*: *str*

Boundary conditions for the MPS.

option *CouplingMPOModel.order*: *str*

The order of sites within the lattice for non-trivial lattices, e.g. `'default'`, `'snake'`, see *ordering()*. Only used if *lattice* is a string.

option *CouplingMPOModel.L*: *int*

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option *CouplingMPOModel.Lx*: *int*

option *CouplingMPOModel.Ly*: *int*

The length in x- and y-direction; only read out for 2D lattices. For `"infinite"` *bc_MPS*, the system is infinite in x-direction and *Lx* is the number of “rings” in the infinite MPS unit cell, while *Ly* gives the circumference around the cylinder or width of the rung for a ladder (depending on *bc_y*).

option `CouplingMPOModel.bc_y: str`
"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x: str`
"open" | "periodic". Can be used to force "periodic" boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for `bc_MPS="finite"` and "periodic" for `bc_MPS="infinite"`. If you are not aware of the consequences, you should probably *not* use "periodic" boundary conditions. (The MPS is still "open", so this will introduce long-range couplings between the first and last sites of the MPS!)

init_sites (*model_params*)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by `init_lattice()` to get the *Site* for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept `conserve=None` to disable using quantum numbers. Many models in TeNPy read out the *conserve* model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters `model_params (dict)` – The model parameters given to `__init__`.

Returns `sites` – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) *Site*

init_terms (*model_params*)

Add the onsite and coupling terms to the model; subclasses should implement this.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

trivial_like_NNModel ()

Return a `NearestNeighborModel` with same lattice, but trivial ($H=0$) bonds.

Module description

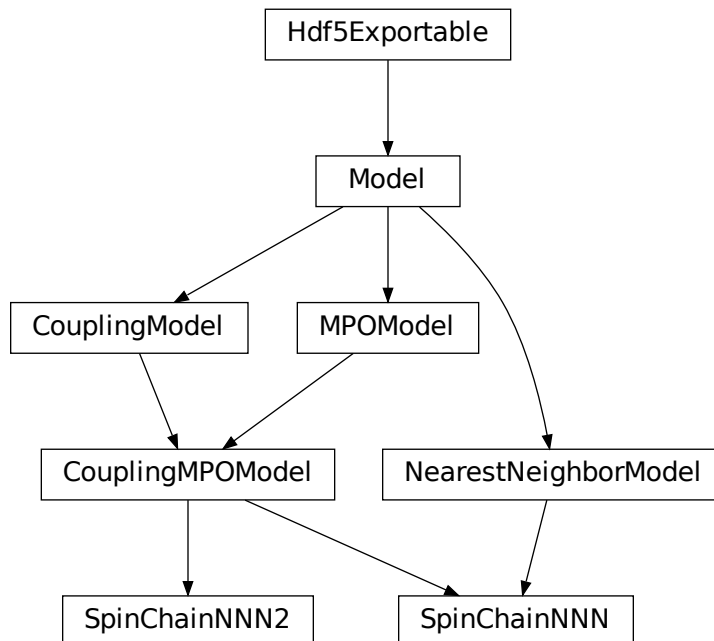
Nearest-neighbour spin-S models.

Uniform lattice of spin-S sites, coupled by nearest-neighbour interactions.

7.9.6 spins_nnn

- full name: `tenpy.models.spins_nnn`
- parent module: `tenpy.models`
- type: module

Classes



<code>SpinChainNNN(model_params)</code>	Spin-S sites coupled by (next-)nearest neighbour interactions on a <i>GroupedSite</i> .
<code>SpinChainNNN2(model_params)</code>	Spin-S sites coupled by next-nearest neighbour interactions.

Module description

Next-Nearest-neighbour spin-S models.

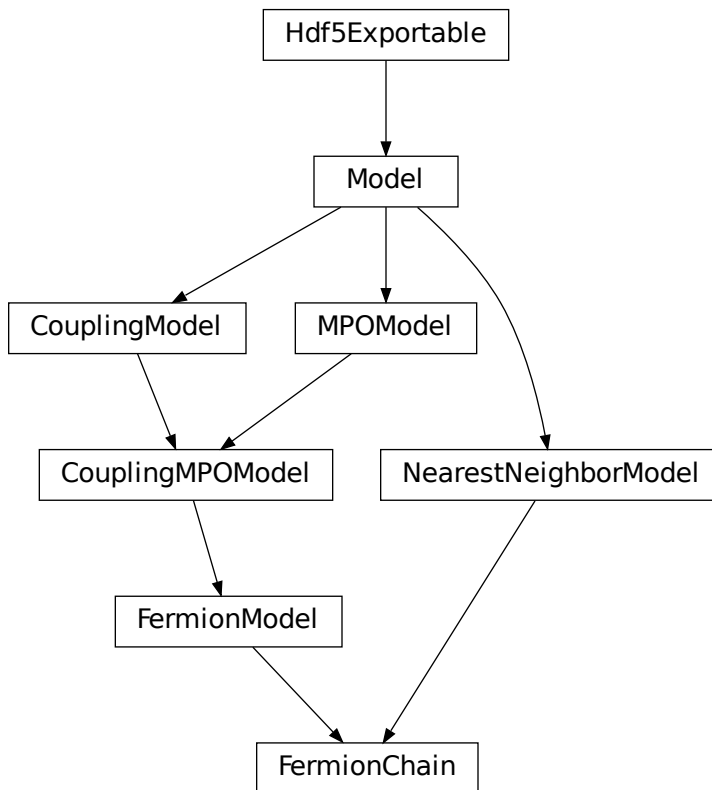
Uniform lattice of spin-S sites, coupled by next-nearest-neighbour interactions. We have two variants implementing the same hamiltonian. The `SpinChainNNN` uses the `GroupedSite` to keep it a `NearestNeighborModel` suitable for TEBD, while the `SpinChainNNN2` just involves longer-range couplings in the MPO. The latter is preferable for pure DMRG calculations and avoids having to add each of the short range couplings twice for the grouped sites.

Note that you can also get a `NearestNeighborModel` for TEBD from the latter by using `group_sites()` and `from_MPOModel()`. An example for such a case is given in the file `examples/c_tebd.py`.

7.9.7 fermions_spinless

- full name: `tenpy.models.fermions_spinless`
- parent module: `tenpy.models`
- type: module

Classes

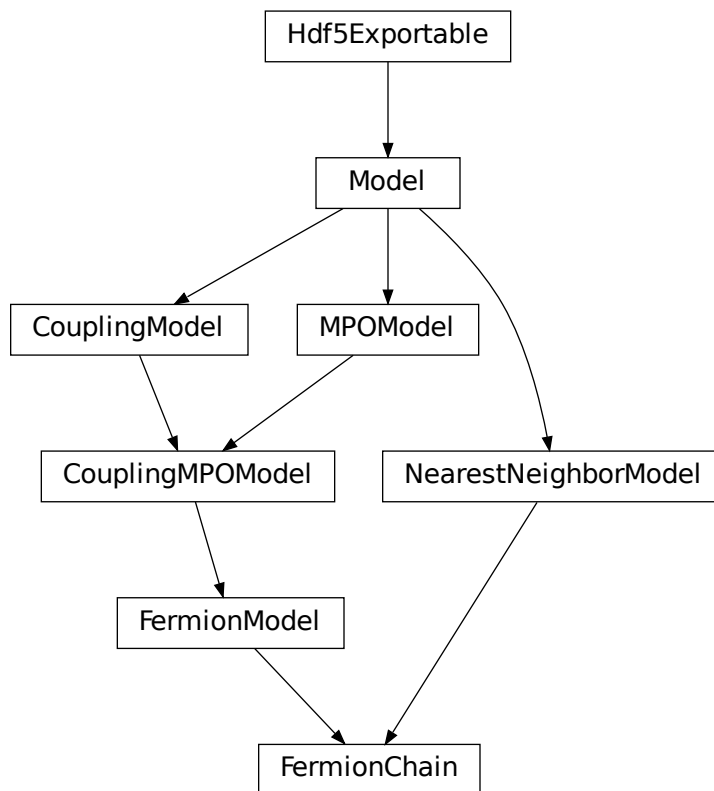


<code>FermionChain(model_params)</code>	The <code>FermionModel</code> on a Chain, suitable for TEBD.
<code>FermionModel(model_params)</code>	Spinless fermions with particle number conservation.

FermionChain

- full name: `tenpy.models.fermions_spinless.FermionChain`
- parent module: `tenpy.models.fermions_spinless`
- type: class

Inheritance Diagram



Methods

<code>FermionChain.__init__(model_params)</code>	Initialize <i>self</i> .
<code>FermionChain.add_coupling(strength, u1, op1, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>FermionChain.add_coupling_term(strength, i, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>FermionChain.add_local_term(strength, term)</code>	Add a single term to <i>self</i> .
<code>FermionChain.add_onsite(strength, u, op_name)</code>	Add onsite terms to <code>onsite_terms</code> .
<code>FermionChain.add_onsite_term(strength, i, op)</code>	Add an onsite term on a given MPS site.
<code>FermionChain.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>FermionChain.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>FermionChain.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>FermionChain.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>FermionChain.calc_H_MPO_from_bond([tol_zero])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>FermionChain.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>FermionChain.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>FermionChain.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>FermionChain.coupling_strength_add_ext_flux([flux])</code>	Add an external flux to the coupling strength.
<code>FermionChain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>FermionChain.from_MPOModel(mpo_model)</code>	Initialize a NearestNeighborModel from a model class defining an MPO.
<code>FermionChain.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>FermionChain.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>FermionChain.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>FermionChain.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>FermionChain.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>FermionChain.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>FermionChain.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>FermionChain.trivial_like_NNModel()</code>	Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.fermions_spinless.FermionChain(model_params)`

Bases: `tenpy.models.fermions_spinless.FermionModel`, `tenpy.models.model.NearestNeighborModel`

The FermionModel on a Chain, suitable for TEBD.

See the FermionModel for the documentation of parameters.

add_coupling(*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*,
raise_op2_left=False, *category=None*, *plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\dim-1}} \text{strength}[\text{shift}(\vec{x})] * OP0 * OP1$, where $OP0 := \text{lat.unit_cell}[u0].\text{get_op}(op0)$ acts on the site $(x_0, \dots, x_{\dim-1}, u1)$, and $OP1 := \text{lat.unit_cell}[u1].\text{get_op}(op1)$ acts on the site $(x_0+dx[0], \dots, x_{\dim-1}+dx[\dim-1], u1)$. Possible combinations $x_0, \dots, x_{\dim-1}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* | *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* | *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form "`{op1}_i {op2}_j`".
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪ Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category=None*, *plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category=None*, *plus_hc=False*)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x₀*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to `onsite_terms`; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar / array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a Site `lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

[**add_coupling\(\)**](#) Add a terms acting on two sites.

`add_onsite_term()` Add a single term without summing over *vecx*.

`add_onsite_term(strength, i, op, category=None, plus_hc=False)`

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **`strength`** (*float*) – The strength of the term.
- **`i`** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **`op`** (*str*) – Name of the involved operator.
- **`category`** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **`plus_hc`** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

`all_coupling_terms()`

Sum of all `coupling_terms`.

`all_onsite_terms()`

Sum of all `onsite_terms`.

`bond_energies(psi)`

Calculate bond energies $\langle \text{psi} | H_{\text{bond}} | \text{psi} \rangle$.

Parameters **`psi`** (MPS) – The MPS for which the bond energies should be calculated.

Returns **`E_bond`** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

`calc_H_MPO(tol_zero=1e-15)`

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **`tol_zero`** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **`H_MPO`** – MPO representation of the Hamiltonian.

Return type MPO

`calc_H_MPO_from_bond(tol_zero=1e-15)`

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **`tol_zero`** (*float*) – Arrays with norm $< \text{tol_zero}$ are considered to be zero.

Returns **`H_MPO`** – MPO representation of the Hamiltonian.

Return type MPO

`calc_H_bond(tol_zero=1e-15)`

calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters **`tol_zero`** (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **`H_bond`** – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters *tol_zero* (*float*) – Arrays with norm $< tol_zero$ are considered to be zero.

Returns *H_bond* – Bond terms as required by the constructor of `NearestNeighborModel`.

Legs are ['p0', 'p0*', 'p1', 'p1*']

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_onsite (*tol_zero=1e-15*)

Calculate *H_onsite* from *self.onsite_terms*.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters *tol_zero* (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- *H_onsite* (list of *npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase *phi* when hopping around the cylinder.

Returns *strength* – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the x -direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase ϕ given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

`enlarge_mps_unit_cell` (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters `factor` (*int*) – The new number of sites in the MPS unit cell will be increased from N_{sites} to $\text{factor} \times N_{\text{sites_per_ring}}$. Since MPS unit cells are repeated in the x -direction in our convention, the lattice shape goes from (L_x, L_y, \dots, L_u) to $(L_x \times \text{factor}, L_y, \dots, L_u)$.

`classmethod from_MPOModel` (*mpo_model*)

Initialize a `NearestNeighborModel` from a model class defining an MPO.

This is especially useful in combination with `MPOModel.group_sites()`.

Parameters `mpo_model` (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The `SpinChainNNN2` has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a `NearestNeighborModel` from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod `from_hdf5` (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which represents the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n=2*, *grouped_sites=None*)

Modify *self* in place to group sites.

Group each *n* sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

init_lattice (*model_params*)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full *Lattice* instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters *model_params* (*dict*) – The model parameters given to `__init__`.

Returns *lat* – An initialized lattice.

Return type *Lattice*

Options

option `CouplingMPOModel.lattice:` *str* | *Lattice*

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) *Lattice* instance. In the latter case, no further parameters are read out.

option `CouplingMPOModel.bc_MPS:` *str*

Boundary conditions for the MPS.

option `CouplingMPOModel.order:` *str*

The order of sites within the lattice for non-trivial lattices, e.g. 'default', 'snake', see `ordering()`. Only used if *lattice* is a string.

option `CouplingMPOModel.L:` *int*

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option `CouplingMPOModel.Lx`: `int`

option `CouplingMPOModel.Ly`: `int`

The length in x- and y-direction; only read out for 2D lattices. For "infinite" `bc_MPS`, the system is infinite in x-direction and `Lx` is the number of “rings” in the infinite MPS unit cell, while `Ly` gives the circumference around the cylinder or width of the rung for a ladder (depending on `bc_y`).

option `CouplingMPOModel.bc_y`: `str`

"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x`: `str`

"open" | "periodic". Can be used to force “periodic” boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for `bc_MPS="finite"` and "periodic" for `bc_MPS="infinite"`. If you are not aware of the consequences, you should probably *not* use “periodic” boundary conditions. (The MPS is still “open”, so this will introduce long-range couplings between the first and last sites of the MPS!)

`init_sites` (`model_params`)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by `init_lattice()` to get the `Site` for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept `conserve=None` to disable using quantum numbers. Many models in TeNPy read out the `conserve` model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters `model_params` (`dict`) – The model parameters given to `__init__`.

Returns `sites` – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) `Site`

`init_terms` (`model_params`)

Add the onsite and coupling terms to the model; subclasses should implement this.

`save_hdf5` (`hdf5_saver`, `h5gr`, `subpath`)

Export `self` into a HDF5 file.

This method saves all the data it needs to reconstruct `self` with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- `hdf5_saver` (`Hdf5Saver`) – Instance of the saving engine.
- `h5gr` (`:class`Group``) – HDF5 group which is supposed to represent `self`.
- `subpath` (`str`) – The *name* of `h5gr` with a '/' in the end.

`test_sanity` ()

Sanity check, raises `ValueErrors`, if something is wrong.

`trivial_like_NNModel` ()

Return a `NearestNeighborModel` with same lattice, but trivial (`H=0`) bonds.

Module description

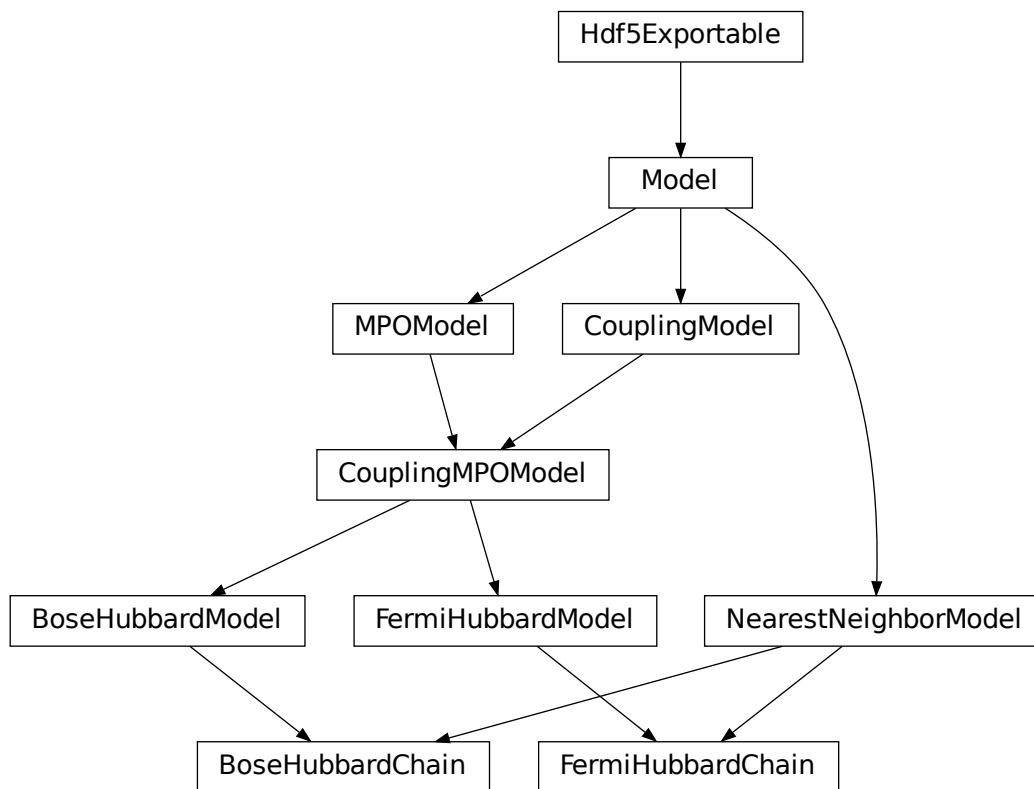
Spinless fermions with hopping and interaction.

Todo: add further terms (e.g. $c^\dagger c^\dagger + \text{h.c.}$) to the Hamiltonian.

7.9.8 hubbard

- full name: `tenpy.models.hubbard`
- parent module: `tenpy.models`
- type: module

Classes



`BoseHubbardChain(model_params)`

The `BoseHubbardModel` on a Chain, suitable for
TEBD.

continues on next page

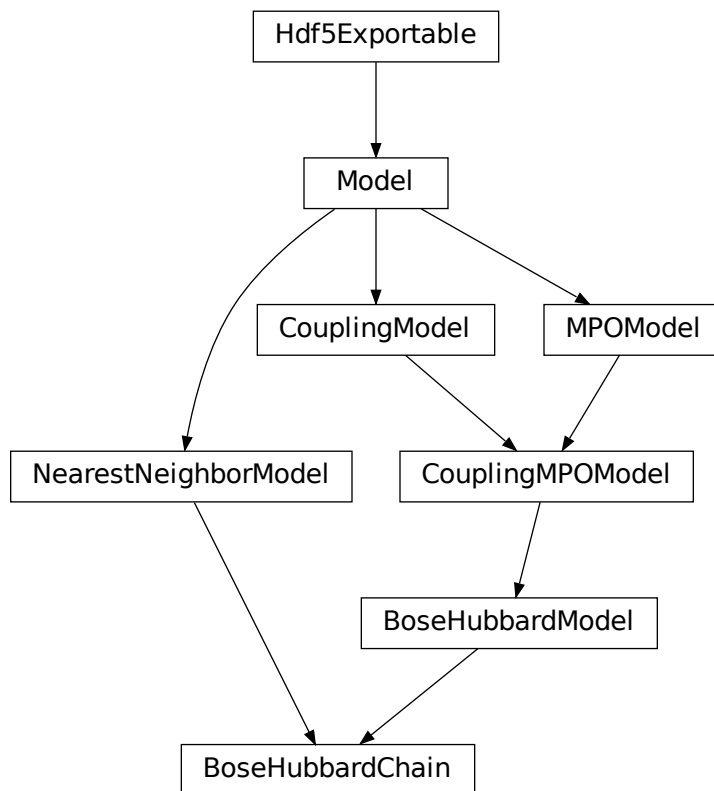
Table 113 – continued from previous page

<code>BoseHubbardModel(model_params)</code>	Spinless Bose-Hubbard model.
<code>FermiHubbardChain(model_params)</code>	The <code>FermiHubbardModel</code> on a Chain, suitable for TEBD.
<code>FermiHubbardModel(model_params)</code>	Spin-1/2 Fermi-Hubbard model.

BoseHubbardChain

- full name: `tenpy.models.hubbard.BoseHubbardChain`
- parent module: `tenpy.models.hubbard`
- type: class

Inheritance Diagram



Methods

<code>BoseHubbardChain.__init__(model_params)</code>	Initialize self.
<code>BoseHubbardChain.add_coupling(strength, u1, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>BoseHubbardChain.add_coupling_term(strength, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>BoseHubbardChain.add_local_term(strength, term)</code>	Add a single term to <i>self</i> .
<code>BoseHubbardChain.add_onsite(strength, u, opname)</code>	Add onsite terms to <code>onsite_terms</code> .
<code>BoseHubbardChain.add_onsite_term(strength, i, op)</code>	Add an onsite term on a given MPS site.
<code>BoseHubbardChain.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>BoseHubbardChain.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>BoseHubbardChain.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>BoseHubbardChain.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>BoseHubbardChain.calc_H_MPO_from_bond([tol_zero])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>BoseHubbardChain.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>BoseHubbardChain.calc_H_bond_from_MPO([tol_zero])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>BoseHubbardChain.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <code>self.onsite_terms</code> .
<code>BoseHubbardChain.coupling_strength_add_ext_flux(...)</code>	Add an external flux to the coupling strength.
<code>BoseHubbardChain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>BoseHubbardChain.from_MPOModel(mpo_model)</code>	Initialize a NearestNeighborModel from a model class defining an MPO.
<code>BoseHubbardChain.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>BoseHubbardChain.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>BoseHubbardChain.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>BoseHubbardChain.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>BoseHubbardChain.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>BoseHubbardChain.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>BoseHubbardChain.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>BoseHubbardChain.trivial_like_NNModel()</code>	Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.hubbard.BoseHubbardChain` (*model_params*)

Bases: `tenpy.models.hubbard.BoseHubbardModel`, `tenpy.models.model.NearestNeighborModel`

The BoseHubbardModel on a Chain, suitable for TEBD.

See the `BoseHubbardModel` for the documentation of parameters.

add_coupling(*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*,
raise_op2_left=False, *category=None*, *plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\dim-1}} \text{strength}[\text{shift}(\vec{x})] * OP0 * OP1$, where $OP0 := \text{lat.unit_cell}[u0].\text{get_op}(op0)$ acts on the site $(x_0, \dots, x_{\dim-1}, u1)$, and $OP1 := \text{lat.unit_cell}[u1].\text{get_op}(op1)$ acts on the site $(x_0+dx[0], \dots, x_{\dim-1}+dx[\dim-1], u1)$. Possible combinations $x_0, \dots, x_{\dim-1}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* | *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* | *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category=None*, *plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category=None*, *plus_hc=False*)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x₀*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to `onsite_terms`; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar | array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a `lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.

- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

add_coupling() Add a terms acting on two sites.

add_onsite_term() Add a single term without summing over *vecx*.

add_onsite_term(*strength*, *i*, *op*, *category=None*, *plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms()

Sum of all `coupling_terms`.

all_onsite_terms()

Sum of all `onsite_terms`.

bond_energies (*psi*)

Calculate bond energies $\langle \text{psi} | H_{\text{bond}} | \text{psi} \rangle$.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

calc_H_MPO (*tol_zero=1e-15*)

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_MPO_from_bond (*tol_zero=1e-15*)

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with norm $< \text{tol_zero}$ are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_bond (*tol_zero=1e-15*)

calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are `['p0', 'p0*', 'p1', 'p1*']`

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters `tol_zero` (*float*) – Arrays with norm `< tol_zero` are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are `['p0', 'p0*', 'p1', 'p1*']`

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_onsite (*tol_zero=1e-15*)

Calculate `H_onsite` from `self.onsite_terms`.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_onsite_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- `H_onsite` (list of *npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an

infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase ϕ when hopping around the cylinder.

Returns **strength** – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the *x*-direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase ϕ given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (*factor*=2)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor***N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx***factor*, *Ly*, ..., *Lu*).

classmethod from_MPOModel (*mpo_model*)

Initialize a `NearestNeighborModel` from a model class defining an MPO.

This is especially usefull in combination with `MPOModel.group_sites()`.

Parameters **mpo_model** (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The `SpinChainNNN2` has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a NearestNeighborModel from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod `from_hdf5` (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n=2*, *grouped_sites=None*)

Modify *self* in place to group sites.

Group each *n* sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

init_lattice (*model_params*)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full *Lattice* instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters **model_params** (*dict*) – The model parameters given to `__init__`.

Returns *lat* – An initialized lattice.

Return type *Lattice*

Options

option `CouplingMPOModel.lattice: str | Lattice`

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) Lattice instance. In the latter case, no further parameters are read out.

option `CouplingMPOModel.bc_MPS: str`

Boundary conditions for the MPS.

option `CouplingMPOModel.order: str`

The order of sites within the lattice for non-trivial lattices, e.g. 'default', 'snake', see `ordering()`. Only used if `lattice` is a string.

option `CouplingMPOModel.L: int`

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option `CouplingMPOModel.Lx: int`

option `CouplingMPOModel.Ly: int`

The length in x- and y-direction; only read out for 2D lattices. For "infinite" `bc_MPS`, the system is infinite in x-direction and `Lx` is the number of “rings” in the infinite MPS unit cell, while `Ly` gives the circumference around the cylinder or width of the rung for a ladder (depending on `bc_y`).

option `CouplingMPOModel.bc_y: str`

"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x: str`

"open" | "periodic". Can be used to force “periodic” boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for `bc_MPS="finite"` and "periodic" for `bc_MPS="infinite"`. If you are not aware of the consequences, you should probably *not* use “periodic” boundary conditions. (The MPS is still “open”, so this will introduce long-range couplings between the first and last sites of the MPS!)

init_sites (*model_params*)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by `init_lattice()` to get the *Site* for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept `conserve=None` to disable using quantum numbers. Many models in TeNPy read out the *conserve* model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters `model_params` (*dict*) – The model parameters given to `__init__`.

Returns `sites` – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) *Site*

init_terms (*model_params*)

Add the onsite and coupling terms to the model; subclasses should implement this.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

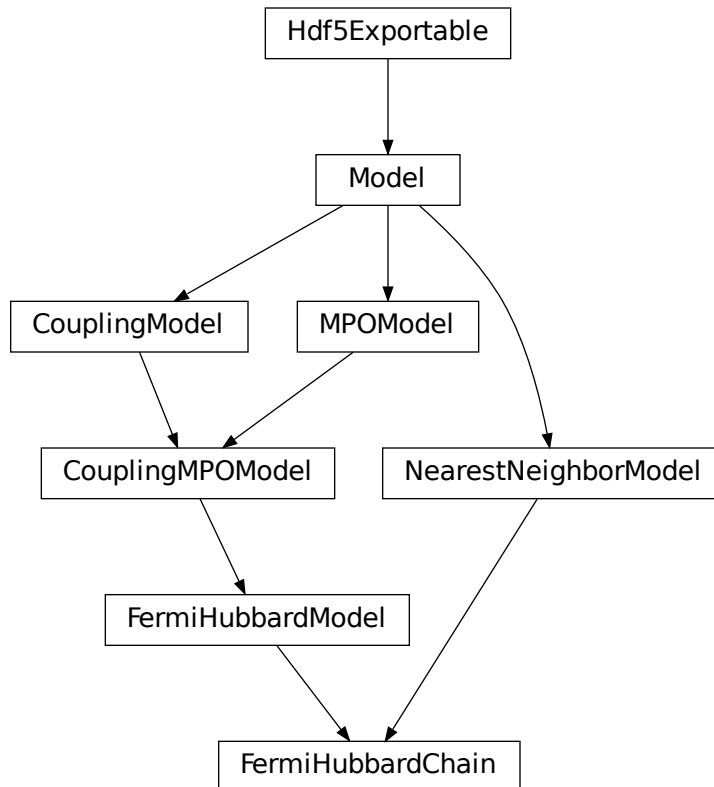
- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

test_sanity()

Sanity check, raises ValueErrors, if something is wrong.

trivial_like_NNModel()Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.**FermiHubbardChain**

- full name: `tenpy.models.hubbard.FermiHubbardChain`
- parent module: `tenpy.models.hubbard`
- type: class

Inheritance Diagram

Methods

<code>FermiHubbardChain.__init__(model_params)</code>	Initialize self.
<code>FermiHubbardChain.add_coupling(strength, u1, ...)</code>	Add twosite coupling terms to the Hamiltonian, summing over lattice sites.
<code>FermiHubbardChain.add_coupling_term(...[, ...])</code>	Add a two-site coupling term on given MPS sites.
<code>FermiHubbardChain.add_local_term(strength, term)</code>	Add a single term to <i>self</i> .
<code>FermiHubbardChain.add_onsite(strength, u, opname)</code>	Add onsite terms to <code>onsite_terms</code> .
<code>FermiHubbardChain.add_onsite_term(strength, ...)</code>	Add an onsite term on a given MPS site.
<code>FermiHubbardChain.all_coupling_terms()</code>	Sum of all <code>coupling_terms</code> .
<code>FermiHubbardChain.all_onsite_terms()</code>	Sum of all <code>onsite_terms</code> .
<code>FermiHubbardChain.bond_energies(psi)</code>	Calculate bond energies $\langle \text{psi} H_{\text{bond}} \text{psi} \rangle$.
<code>FermiHubbardChain.calc_H_MPO([tol_zero])</code>	Calculate MPO representation of the Hamiltonian.
<code>FermiHubbardChain.calc_H_MPO_from_bond([...])</code>	Calculate the MPO Hamiltonian from the bond Hamiltonian.
<code>FermiHubbardChain.calc_H_bond([tol_zero])</code>	calculate H_{bond} from <code>coupling_terms</code> and <code>onsite_terms</code> .
<code>FermiHubbardChain.calc_H_bond_from_MPO([...])</code>	Calculate the bond Hamiltonian from the MPO Hamiltonian.
<code>FermiHubbardChain.calc_H_onsite([tol_zero])</code>	Calculate H_{onsite} from <i>self.onsite_terms</i> .
<code>FermiHubbardChain.coupling_strength_add_ext_flux(...)</code>	Add an external flux to the coupling strength.
<code>FermiHubbardChain.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>FermiHubbardChain.from_MPOModel(mpo_model)</code>	Initialize a NearestNeighborModel from a model class defining an MPO.
<code>FermiHubbardChain.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>FermiHubbardChain.group_sites([n, grouped_sites])</code>	Modify <i>self</i> in place to group sites.
<code>FermiHubbardChain.init_lattice(model_params)</code>	Initialize a lattice for the given model parameters.
<code>FermiHubbardChain.init_sites(model_params)</code>	Define the local Hilbert space and operators; needs to be implemented in subclasses.
<code>FermiHubbardChain.init_terms(model_params)</code>	Add the onsite and coupling terms to the model; subclasses should implement this.
<code>FermiHubbardChain.save_hdf5(hdf5_saver, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>FermiHubbardChain.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>FermiHubbardChain.trivial_like_NNModel()</code>	Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.

class `tenpy.models.hubbard.FermiHubbardChain` (*model_params*)

Bases: `tenpy.models.hubbard.FermiHubbardModel`, `tenpy.models.model.NearestNeighborModel`

The `FermiHubbardModel` on a Chain, suitable for TEBD.

See the `FermiHubbardModel` for the documentation of parameters.

add_coupling(*strength*, *u1*, *op1*, *u2*, *op2*, *dx*, *op_string=None*, *str_on_first=True*,
raise_op2_left=False, *category=None*, *plus_hc=False*)

Add twosite coupling terms to the Hamiltonian, summing over lattice sites.

Represents couplings of the form $\sum_{x_0, \dots, x_{\dim-1}} \text{strength}[\text{shift}(\vec{x})] * OP0 * OP1$, where $OP0 := \text{lat.unit_cell}[u0].\text{get_op}(op0)$ acts on the site $(x_0, \dots, x_{\dim-1}, u1)$, and $OP1 := \text{lat.unit_cell}[u1].\text{get_op}(op1)$ acts on the site $(x_0+dx[0], \dots, x_{\dim-1}+dx[\dim-1], u1)$. Possible combinations $x_0, \dots, x_{\dim-1}$ are determined from the boundary conditions in `possible_couplings()`.

The coupling *strength* may vary spatially if the given *strength* is a numpy array. The correct shape of this array is the *coupling_shape* returned by `tenpy.models.lattice.possible_couplings()` and depends on the boundary conditions. The `shift(...)` depends on *dx*, and is chosen such that the first entry `strength[0, 0, ...]` of *strength* is the prefactor for the first possible coupling fitting into the lattice if you imagine open boundary conditions.

The necessary terms are just added to `coupling_terms`; this function does not rebuild the MPO.

Deprecated since version 0.4.0: The arguments *str_on_first* and *raise_op2_left* will be removed in version 1.0.0.

Parameters

- **strength** (*scalar* | *array*) – Prefactor of the coupling. May vary spatially (see above). If an array of smaller size is provided, it gets tiled to the required shape.
- **u1** (*int*) – Picks the site `lat.unit_cell[u1]` for OP1.
- **op1** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u1]` for OP1.
- **u2** (*int*) – Picks the site `lat.unit_cell[u2]` for OP2.
- **op2** (*str*) – Valid operator name of an onsite operator in `lat.unit_cell[u2]` for OP2.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between OP1 and OP2. For a 1D lattice, a single int is also fine.
- **op_string** (*str* | *None*) – Name of an operator to be used between the OP1 and OP2 sites. Typical use case is the phase for a Jordan-Wigner transformation. The operator should be defined on all sites in the unit cell. If *None*, auto-determine whether a Jordan-Wigner string is needed, using `op_needs_JW()`.
- **str_on_first** (*bool*) – Whether the provided *op_string* should also act on the first site. This option should be chosen as *True* for Jordan-Wigner strings. When handling Jordan-Wigner strings we need to extend the *op_string* to also act on the ‘left’, first site (in the sense of the MPS ordering of the sites given by the lattice). In this case, there is a well-defined ordering of the operators in the physical sense (i.e. which of *op1* or *op2* acts first on a given state). We follow the convention that *op2* acts first (in the physical sense), independent of the MPS ordering. Deprecated.
- **raise_op2_left** (*bool*) – Raise an error when *op2* appears left of *op1* (in the sense of the MPS ordering given by the lattice). Deprecated.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form `"{op1}_i {op2}_j"`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

Examples

When initializing a model, you can add a term $J \sum_{\langle i,j \rangle} S_i^z S_j^z$ on all nearest-neighbor bonds of the lattice like this:

```
>>> J = 1. # the strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(J, u1, 'Sz', u2, 'Sz', dx)
```

The strength can be an array, which gets tiled to the correct shape. For example, in a 1D *Chain* with an even number of sites and periodic (or infinite) boundary conditions, you can add alternating strong and weak couplings with a line like:

```
>>> self.add_coupling([1.5, 1.], 0, 'Sz', 0, 'Sz', dx)
```

Make sure to use the *plus_hc* argument if necessary, e.g. for hoppings:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx, plus_hc=True)
```

Alternatively, you can add the hermitian conjugate terms explicitly. The correct way is to complex conjugate the strength, take the hermitian conjugate of the operators and swap the order (including a swap $u1 \leftrightarrow u2$), and use the opposite direction $-dx$, i.e. the *h.c.* of `add_coupling(t, u1, 'A', u2, 'B', dx)` is `add_coupling(np.conj(t), u2, hc('B'), u1, hc('A'), -dx)`, where *hc* takes the hermitian conjugate of the operator names, see `get_hc_op_name()`. For spin-less fermions (*FermionSite*), this would be

```
>>> t = 1. # hopping strength
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(t), u2, 'Cd', u1, 'C', -dx) # h.c.
```

With spin-full fermions (*SpinHalfFermions*), it could be:

```
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(t, u1, 'Cdu', u2, 'Cd', dx) # Cdagger_up C_down
...     self.add_coupling(np.conj(t), u2, 'Cdd', u1, 'Cu', -dx) # h.c.
↪Cdagger_down C_up
```

Note that the Jordan-Wigner strings for the fermions are added automatically!

See also:

`add_onsite()` Add terms acting on one site only.

`MultiCouplingModel.add_multi_coupling_term()` for terms on more than two sites.

`add_coupling_term()` Add a single term without summing over *vecx*.

`add_coupling_term(strength, i, j, op_i, op_j, op_string='Id', category=None, plus_hc=False)`

Add a two-site coupling term on given MPS sites.

Wrapper for `self.coupling_terms[category].add_coupling_term(...)`.

Warning: This function does not handle Jordan-Wigner strings! You might want to use `add_local_term()` instead.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i*,) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.
- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.
- **category** (*str*) – Descriptive name used as key for `coupling_terms`. Defaults to a string of the form “{op1}_i {op2}_j”.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

add_local_term (*strength*, *term*, *category=None*, *plus_hc=False*)

Add a single term to *self*.

The represented term is *strength* times the product of the operators given in *terms*. Each operator is specified by the name and the site it acts on; the latter given by a lattice index, see [Lattice](#).

Depending on the length of *term*, it can add an onsite term or a coupling term to `onsite_terms` or `coupling_terms`, respectively.

Parameters

- **strength** (*float/complex*) – The prefactor of the term.
- **term** (*list of (str, array_like)*) – List of tuples (*opname*, *lat_idx*) where *opname* is a string describing the operator acting on the site given by the lattice index *lat_idx*. Here, *lat_idx* is for example [*x*, *y*, *u*] for a 2D lattice, with *u* being the index within the unit cell.
- **category** – Descriptive name used as key for `onsite_terms` or `coupling_terms`.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

add_onsite (*strength*, *u*, *opname*, *category=None*, *plus_hc=False*)

Add onsite terms to `onsite_terms`.

Adds $\sum_{\vec{x}} \text{strength}[\vec{x}] * OP$ to the represented Hamiltonian, where the operator $OP = \text{lat.unit_cell}[u].\text{get_op}(\text{opname})$ acts on the site given by a lattice index (*x₀*, ..., *x_{dim-1}*, *u*),

The necessary terms are just added to `onsite_terms`; doesn’t rebuild the MPO.

Parameters

- **strength** (*scalar | array*) – Prefactor of the onsite term. May vary spatially. If an array of smaller size is provided, it gets tiled to the required shape.
- **u** (*int*) – Picks a `lat.unit_cell[u]` out of the unit cell.
- **opname** (*str*) – valid operator name of an onsite operator in `lat.unit_cell[u]`.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *opname*.

- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the terms is added automatically.

See also:

add_coupling() Add a terms acting on two sites.

add_onsite_term() Add a single term without summing over *vecx*.

add_onsite_term(*strength*, *i*, *op*, *category=None*, *plus_hc=False*)

Add an onsite term on a given MPS site.

Wrapper for `self.onsite_terms[category].add_onsite_term(...)`.

Parameters

- **strength** (*float*) – The strength of the term.
- **i** (*int*) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (*str*) – Name of the involved operator.
- **category** (*str*) – Descriptive name used as key for `onsite_terms`. Defaults to *op*.
- **plus_hc** (*bool*) – If *True*, the hermitian conjugate of the term is added automatically.

all_coupling_terms()

Sum of all `coupling_terms`.

all_onsite_terms()

Sum of all `onsite_terms`.

bond_energies (*psi*)

Calculate bond energies $\langle \text{psi} | H_{\text{bond}} | \text{psi} \rangle$.

Parameters **psi** (MPS) – The MPS for which the bond energies should be calculated.

Returns **E_bond** – List of bond energies: for finite bc, `E_Bond[i]` is the energy of bond *i*, *i*+1. (i.e. we omit bond 0 between sites *L*-1 and 0); for infinite bc `E_bond[i]` is the energy of bond *i*-1, *i*.

Return type 1D ndarray

calc_H_MPO (*tol_zero=1e-15*)

Calculate MPO representation of the Hamiltonian.

Uses `onsite_terms` and `coupling_terms` to build an MPO graph (and then an MPO).

Parameters **tol_zero** (*float*) – Prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_MPO_from_bond (*tol_zero=1e-15*)

Calculate the MPO Hamiltonian from the bond Hamiltonian.

Parameters **tol_zero** (*float*) – Arrays with `norm < tol_zero` are considered to be zero.

Returns **H_MPO** – MPO representation of the Hamiltonian.

Return type MPO

calc_H_bond (*tol_zero=1e-15*)

calculate `H_bond` from `coupling_terms` and `onsite_terms`.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are `['p0', 'p0*', 'p1', 'p1*']`

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_bond_from_MPO (*tol_zero=1e-15*)

Calculate the bond Hamiltonian from the MPO Hamiltonian.

Parameters `tol_zero` (*float*) – Arrays with norm $< tol_zero$ are considered to be zero.

Returns `H_bond` – Bond terms as required by the constructor of `NearestNeighborModel`.
Legs are `['p0', 'p0*', 'p1', 'p1*']`

Return type list of *Array*

:raises `ValueError` : if the Hamiltonian contains longer-range terms.:

calc_H_on-site (*tol_zero=1e-15*)

Calculate `H_on-site` from `self.on-site_terms`.

Deprecated since version 0.4.0: This function will be removed in 1.0.0. Replace calls to this function by `self.all_on-site_terms().remove_zeros(tol_zero).to_Arrays(self.lat.mps_sites())`. You might also want to take `explicit_plus_hc` into account.

Parameters `tol_zero` (*float*) – prefactors with `abs(strength) < tol_zero` are considered to be zero.

Returns

- `H_on-site` (list of *npc.Array*)
- onsite terms of the Hamiltonian. If `explicit_plus_hc` is `True`, – Hermitian conjugates of the onsite terms will be included.

coupling_strength_add_ext_flux (*strength, dx, phase*)

Add an external flux to the coupling strength.

When performing DMRG on a “cylinder” geometry, it might be useful to put an “external flux” through the cylinder. This means that a particle hopping around the cylinder should pick up a phase given by the external flux [Resta1997]. This is also called “twisted boundary conditions” in literature. This function adds a complex phase to the *strength* array on some bonds, such that particles hopping in positive direction around the cylinder pick up $\exp(+i \text{ phase})$.

Warning: For the sign of *phase* it is important that you consistently use the creation operator as *op1* and the annihilation operator as *op2* in `add_coupling()`.

Parameters

- **strength** (*scalar | array*) – The strength to be used in `add_coupling()`, when no external flux would be present.
- **dx** (*iterable of int*) – Translation vector (of the unit cell) between *op1* and *op2* in `add_coupling()`.
- **phase** (*iterable of float*) – The phase of the external flux for hopping in each direction of the lattice. E.g., if you want flux through the cylinder on which you have an

infinite MPS, you should give `phase=[0, phi]` such that particles pick up a phase ϕ when hopping around the cylinder.

Returns **strength** – The strength array to be used as *strength* in `add_coupling()` with the given *dx*.

Return type complex array

Examples

Let's say you have an infinite MPS on a cylinder, and want to add nearest-neighbor hopping of fermions with the `FermionSite`. The cylinder axis is the *x*-direction of the lattice, so to put a flux through the cylinder, you want particles hopping *around* the cylinder to pick up a phase ϕ given by the external flux.

```
>>> strength = 1. # hopping strength without external flux
>>> phi = np.pi/4 # determines the external flux strength
>>> strength_with_flux = self.coupling_strength_add_ext_flux(strength, dx, [0,
↪ phi])
>>> for u1, u2, dx in self.lat.pairs['nearest_neighbors']:
...     self.add_coupling(strength_with_flux, u1, 'Cd', u2, 'C', dx)
...     self.add_coupling(np.conj(strength_with_flux), u2, 'Cd', u1, 'C', -dx)
```

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

This has to be done after finishing initialization and can not be reverted.

Parameters **factor** (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor***N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx***factor*, *Ly*, ..., *Lu*).

classmethod from_MPOModel (*mpo_model*)

Initialize a `NearestNeighborModel` from a model class defining an MPO.

This is especially usefull in combination with `MPOModel.group_sites()`.

Parameters **mpo_model** (`MPOModel`) – A model instance implementing the MPO. Does not need to be a `NearestNeighborModel`, but should only have nearest-neighbor couplings.

Examples

The `SpinChainNNN2` has next-nearest-neighbor couplings and thus only implements an MPO:

```
>>> from tenpy.models.spins_nnn import SpinChainNNN2
>>> nnn_chain = SpinChainNNN2({'L': 20})
parameter 'L'=20 for SpinChainNNN2
>>> print(isinstance(nnn_chain, NearestNeighborModel))
False
>>> print("range before grouping:", nnn_chain.H_MPO.max_range)
range before grouping: 2
```

By grouping each two neighboring sites, we can bring it down to nearest neighbors.

```
>>> nnn_chain.group_sites(2)
>>> print("range after grouping:", nnn_chain.H_MPO.max_range)
range after grouping: 1
```

Yet, TEBD will not yet work, as the model doesn't define H_{bond} . However, we can initialize a NearestNeighborModel from the MPO:

```
>>> nnn_chain_for_tebd = NearestNeighborModel.from_MPOModel(nnn_chain)
```

classmethod `from_hdf5` (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

group_sites (*n=2*, *grouped_sites=None*)

Modify *self* in place to group sites.

Group each *n* sites together using the *GroupedSite*. This might allow to do TEBD with a Trotter decomposition, or help the convergence of DMRG (in case of too long range interactions).

This has to be done after finishing initialization and can not be reverted.

Parameters

- **n** (*int*) – Number of sites to be grouped together.
- **grouped_sites** (*None* | list of *GroupedSite*) – The sites grouped together.

Returns *grouped_sites* – The sites grouped together.

Return type list of *GroupedSite*

init_lattice (*model_params*)

Initialize a lattice for the given model parameters.

This function reads out the model parameter *lattice*. This can be a full *Lattice* instance, in which case it is just returned without further action. Alternatively, the *lattice* parameter can be a string giving the name of one of the predefined lattices, which then gets initialized. Depending on the dimensionality of the lattice, this requires different model parameters.

Parameters **model_params** (*dict*) – The model parameters given to `__init__`.

Returns *lat* – An initialized lattice.

Return type *Lattice*

Options

option `CouplingMPOModel.lattice: str | Lattice`

The name of a lattice pre-defined in TeNPy to be initialized. Alternatively, a (possibly self-defined) Lattice instance. In the latter case, no further parameters are read out.

option `CouplingMPOModel.bc_MPS: str`

Boundary conditions for the MPS.

option `CouplingMPOModel.order: str`

The order of sites within the lattice for non-trivial lattices, e.g. 'default', 'snake', see `ordering()`. Only used if `lattice` is a string.

option `CouplingMPOModel.L: int`

The length in x-direction; only read out for 1D lattices. For an infinite system the length of the unit cell.

option `CouplingMPOModel.Lx: int`

option `CouplingMPOModel.Ly: int`

The length in x- and y-direction; only read out for 2D lattices. For "infinite" `bc_MPS`, the system is infinite in x-direction and `Lx` is the number of “rings” in the infinite MPS unit cell, while `Ly` gives the circumference around the cylinder or width of the rung for a ladder (depending on `bc_y`).

option `CouplingMPOModel.bc_y: str`

"cylinder" | "ladder"; only read out for 2D lattices. The boundary conditions in y-direction.

option `CouplingMPOModel.bc_x: str`

"open" | "periodic". Can be used to force “periodic” boundaries for the lattice, i.e., for the couplings in the Hamiltonian, even if the MPS is finite. Defaults to "open" for `bc_MPS="finite"` and "periodic" for `bc_MPS="infinite"`. If you are not aware of the consequences, you should probably *not* use “periodic” boundary conditions. (The MPS is still “open”, so this will introduce long-range couplings between the first and last sites of the MPS!)

init_sites (*model_params*)

Define the local Hilbert space and operators; needs to be implemented in subclasses.

This function gets called by `init_lattice()` to get the *Site* for the lattice unit cell.

Note: Initializing the sites requires to define the conserved quantum numbers. All pre-defined sites accept `conserve=None` to disable using quantum numbers. Many models in TeNPy read out the *conserve* model parameter, which can be set to "best" to indicate the optimal parameters.

Parameters `model_params` (*dict*) – The model parameters given to `__init__`.

Returns `sites` – The local sites of the lattice, defining the local basis states and operators.

Return type (tuple of) *Site*

init_terms (*model_params*)

Add the onsite and coupling terms to the model; subclasses should implement this.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

test_sanity()

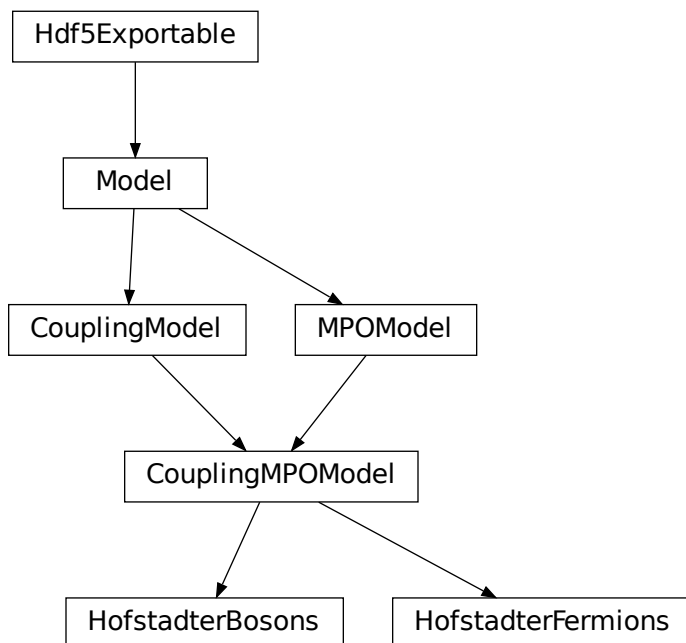
Sanity check, raises ValueErrors, if something is wrong.

trivial_like_NNModel()Return a NearestNeighborModel with same lattice, but trivial ($H=0$) bonds.**Module description**

Bosonic and fermionic Hubbard models.

7.9.9 hofstadter

- full name: `tenpy.models.hofstadter`
- parent module: `tenpy.models`
- type: module

Classes

<code>HofstadterBosons(model_params)</code>	Bosons on a square lattice with magnetic flux.
<code>HofstadterFermions(model_params)</code>	Fermions on a square lattice with magnetic flux.

Functions

<code>gauge_hopping(model_params)</code>	Compute hopping amplitudes for the Hofstadter models based on a gauge choice.
--	---

gauge_hopping

- full name: `tenpy.models.hofstadter.gauge_hopping`
- parent module: `tenpy.models.hofstadter`
- type: function

`tenpy.models.hofstadter.gauge_hopping(model_params)`

Compute hopping amplitudes for the Hofstadter models based on a gauge choice.

In the Hofstadter model, the magnetic field enters as an Aharonov-Bohm phase. This phase is dependent on a choice of gauge, which simultaneously defines a ‘magnetic unit cell’ (MUC).

The magnetic unit cell is the smallest set of lattice plaquettes that encloses an integer number of flux quanta. It can be user-defined by setting `mx` and `my`, but for common gauge choices is computed based on the flux density.

The gauge choices are:

- ‘`landau_x`’: Landau gauge along the x-axis. The magnetic unit cell will have shape $(mx, 1)$. For flux densities p/q , `mx` will default to q . Example: at a flux density $1/3$, the magnetic unit cell will have shape $(3, 1)$, so it encloses exactly 1 flux quantum.
- ‘`landau_y`’: Landau gauge along the y-axis. The magnetic unit cell will have shape $(1, my)$. For flux densities p/q , `my` will default to q . Example: at a flux density $3/7$, the magnetic unit cell will have shape $(1, 7)$, so it encloses exactly 3 flux quanta.
- ‘`symmetric`’: symmetric gauge. The magnetic unit cell will have shape (mx, my) , with $mx = my$. For flux densities p/q , `mx` and `my` will default to q . Example: at a flux density $4/9$, the magnetic unit cell will have shape $(9, 9)$.

Parameters

- **gauge** (`'landau_x' | 'landau_y' | 'symmetric'`) – Choice of the gauge, see table above.
- **my** (`mx`,) – Dimensions of the magnetic unit cell in terms of lattice sites. None defaults to the minimal choice compatible with `gauge` and `phi_pq`.
- **Jy** (`Jx`,) – ‘Bare’ hopping amplitudes (without phase). Without any flux we have `hop_x` = `-Jx` and `hop_y` = `-Jy`.
- **phi_pq** (`tuple (int, int)`) – Magnetic flux as a fraction p/q , defined as (p, q)

Returns `hop_x, hop_y` – Hopping amplitudes to be used as prefactors for $c_{x,y}^\dagger c_{x+1,y}$ (`hop_x`) and $c_{x,y}^\dagger c_{x,y+1}$ (`hop_y`), respectively, with the necessary phases for the gauge.

Return type float | array

Module description

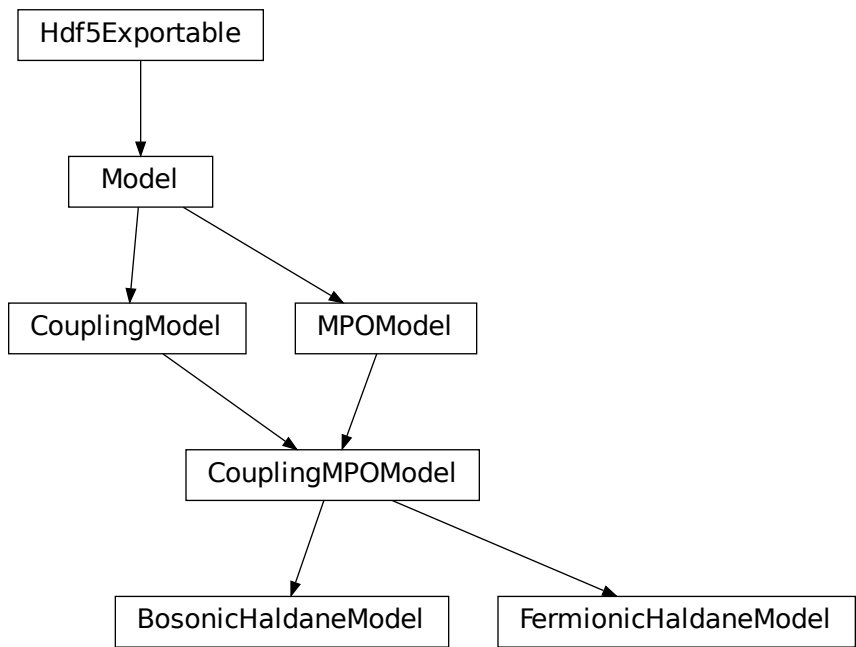
Cold atomic (Harper-)Hofstadter model on a strip or cylinder.

Todo: WARNING: These models are still under development and not yet tested for correctness. Use at your own risk! Replicate known results to confirm models work correctly. Long term: implement different lattices. Long term: implement variable hopping strengths J_x, J_y .

7.9.10 haldane

- full name: `tenpy.models.haldane`
- parent module: `tenpy.models`
- type: module

Classes



<code>BosonicHaldaneModel(model_params)</code>	Hardcore bosonic Haldane model.
<code>FermionicHaldaneModel(model_params)</code>	Spinless fermionic Haldane model.

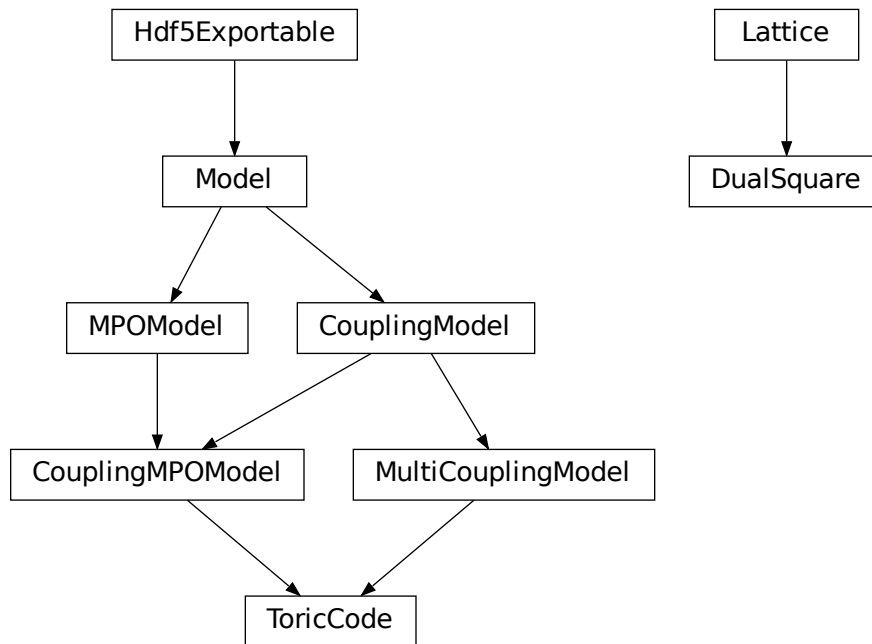
Module description

Bosonic and fermionic Haldane models.

7.9.11 toric_code

- full name: `tenpy.models.toric_code`
- parent module: `tenpy.models`
- type: module

Classes

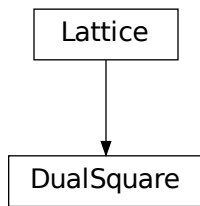


<code>DualSquare(Lx, Ly, sites, **kwargs)</code>	The dual lattice of the square lattice (again square).
<code>ToricCode(model_params)</code>	Toric code model.

DualSquare

- full name: `tenpy.models.toric_code.DualSquare`
- parent module: `tenpy.models.toric_code`
- type: class

Inheritance Diagram



Methods

<code>DualSquare.__init__(Lx, Ly, sites, **kwargs)</code>	Initialize self.
<code>DualSquare.count_neighbors([u, key])</code>	Count e.g.
<code>DualSquare.coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a coupling.
<code>DualSquare.enlarge_mps_unit_cell([factor])</code>	Repeat the unit cell for infinite MPS boundary conditions; in place.
<code>DualSquare.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>DualSquare.lat2mps_idx(lat_idx)</code>	Translate lattice indices (x_0, \dots, x_{D-1}) , u to MPS index i .
<code>DualSquare.mps2lat_idx(i)</code>	Translate MPS index i to lattice indices $(x_0, \dots, x_{\text{dim}-1})$, u .
<code>DualSquare.mps2lat_values(A[, axes, u])</code>	Reshape/reorder A to replace an MPS index by lattice indices.
<code>DualSquare.mps2lat_values_masked(A[, axes, ...])</code>	Reshape/reorder an array A to replace an MPS index by lattice indices.
<code>DualSquare.mps_idx_fix_u([u])</code>	return an index array of MPS indices for which the site within the unit cell is u .
<code>DualSquare.mps_lat_idx_fix_u([u])</code>	Similar as <code>mps_idx_fix_u()</code> , but return also the corresponding lattice indices.
<code>DualSquare.mps_sites()</code>	Return a list of sites for all MPS indices.
<code>DualSquare.multi_coupling_shape(dx)</code>	Calculate correct shape of the <i>strengths</i> for a multi_coupling.
<code>DualSquare.number_nearest_neighbors([u])</code>	Deprecated.
<code>DualSquare.number_next_nearest_neighbors([u])</code>	Deprecated.
<code>DualSquare.ordering(order)</code>	Provide possible orderings of the N lattice sites.

continues on next page

Table 120 – continued from previous page

<code>DualSquare.plot_basis(ax[, origin, shade])</code>	Plot arrows indicating the basis vectors of the lattice.
<code>DualSquare.plot_bc_identified(ax[, ...])</code>	Mark two sites identified by periodic boundary conditions.
<code>DualSquare.plot_coupling(ax[, coupling, wrap])</code>	Plot lines connecting nearest neighbors of the lattice.
<code>DualSquare.plot_order(ax[, order, textkwargs])</code>	Plot a line connecting sites in the specified “order” and text labels enumerating them.
<code>DualSquare.plot_sites(ax[, markers])</code>	Plot the sites of the lattice with markers.
<code>DualSquare.position(lat_idx)</code>	return ‘space’ position of one or multiple sites.
<code>DualSquare.possible_couplings(u1, u2, dx)</code>	Find possible MPS indices for two-site couplings.
<code>DualSquare.possible_multi_couplings(ops)</code>	Generalization of <code>possible_couplings()</code> to couplings with more than 2 sites.
<code>DualSquare.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>DualSquare.site(i)</code>	return <i>Site</i> instance corresponding to an MPS index <i>i</i>
<code>DualSquare.test_sanity()</code>	Sanity check.

Class Attributes and Properties

<code>DualSquare.boundary_conditions</code>	Human-readable list of boundary conditions from <code>bc</code> and <code>bc_shift</code> .
<code>DualSquare.dim</code>	The dimension of the lattice.
<code>DualSquare.nearest_neighbors</code>	
<code>DualSquare.next_nearest_neighbors</code>	
<code>DualSquare.next_next_nearest_neighbors</code>	
<code>DualSquare.order</code>	Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

class `tenpy.models.toric_code.DualSquare` (*Lx*, *Ly*, *sites*, ****kwargs**)

Bases: `tenpy.models.lattice.Lattice`

The dual lattice of the square lattice (again square).

The sites in this lattice correspond to the vertical and horizontal (nearest neighbor) bonds of a common *Square* lattice with the same dimensions *Lx*, *Ly*.

Parameters

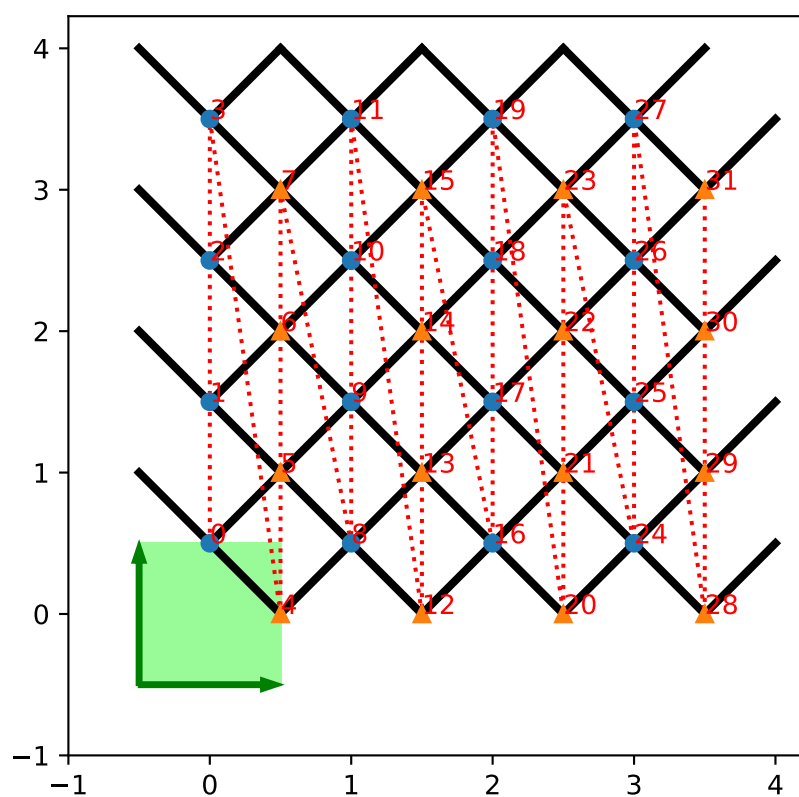
- **Ly** (*Lx*,) – Dimensions of the original lattice. This lattice has $2*Lx*Ly$ sites.
- **sites** (*Site*) – The sites for the horizontal (first entry) and vertical (second entry) bonds.
- ****kwargs** – Additional keyword arguments given to the `Lattice`. *basis*, *pos* and *pairs* are set accordingly.

ordering (*order*)

Provide possible orderings of the *N* lattice sites.

The following orders are defined in this method compared to `tenpy.models.lattice.Lattice.ordering()`:

<i>order</i>	equivalent <i>priority</i>	equivalent <i>snake_winding</i>
'default'	(0, 2, 1)	(False, False, False)



property boundary_conditions

Human-readable list of boundary conditions from `bc` and `bc_shift`.

Returns boundary_conditions – List of "open" or "periodic", one entry for each direction of the lattice.

Return type list of str

count_neighbors (*u=0, key='nearest_neighbors'*)

Count e.g. the number of nearest neighbors for a site in the bulk.

Parameters

- **u** (*int*) – Specifies the site in the unit cell, for which we should count the number of neighbors (or whatever *key* specifies).
- **key** (*str*) – Key of `pairs` to select what to count.

Returns number – Number of nearest neighbors (or whatever *key* specified) for the *u*-th site in the unit cell, somewhere in the bulk of the lattice. Note that it might not be the correct value at the edges of a lattice with open boundary conditions.

Return type int

coupling_shape (*dx*)

Calculate correct shape of the *strengths* for a coupling.

Parameters dx (*tuple of int*) – Translation vector in the lattice for a coupling of two operators. Corresponds to *dx* argument of `tenpy.models.model.CouplingModel.add_multi_coupling()`.

Returns

- **coupling_shape** (*tuple of int*) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **shift_lat_indices** (*array*) – Translation vector from origin to the lower left corner of box spanned by *dx*.

property dim

The dimension of the lattice.

enlarge_mps_unit_cell (*factor=2*)

Repeat the unit cell for infinite MPS boundary conditions; in place.

Parameters factor (*int*) – The new number of sites in the MPS unit cell will be increased from *N_sites* to *factor***N_sites_per_ring*. Since MPS unit cells are repeated in the *x*-direction in our convention, the lattice shape goes from (*Lx*, *Ly*, ..., *Lu*) to (*Lx***factor*, *Ly*, ..., *Lu*).

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns obj – Newly generated class instance containing the required data.

Return type cls

lat2mps_idx (*lat_idx*)

Translate lattice indices (x_0, \dots, x_{D-1}, u) to MPS index i .

Parameters **lat_idx** (*array_like* [$\dots, dim+1$]) – The last dimension corresponds to lattice indices (x_0, \dots, x_{D-1}, u). All lattice indices should be positive and smaller than the corresponding entry in `self.shape`. Exception: for “infinite” *bc_MPS*, an x_0 outside indicates shifts accross the boundary.

Returns **i** – MPS index/indices corresponding to *lat_idx*. Has the same shape as *lat_idx* without the last dimension.

Return type *array_like*

mps2lat_idx (*i*)

Translate MPS index i to lattice indices (x_0, \dots, x_{dim-1}, u).

Parameters **i** (*int* | *array_like of int*) – MPS index/indices.

Returns **lat_idx** – First dimensions like i , last dimension has `len dim + 1` and contains the lattice indices `((x_0, ..., x_{dim-1}, u))` corresponding to i . For i accross the MPS unit cell and “infinite” *bc_MPS*, we shift x_0 accordingly.

Return type *array*

mps2lat_values (*A, axes=0, u=None*)

Reshape/reorder *A* to replace an MPS index by lattice indices.

Parameters

- **A** (*ndarray*) – Some values. Must have `A.shape[axes] = self.N_sites` if u is None, or `A.shape[axes] = self.N_cells` if u is an int.
- **axes** (*(iterable of) int*) – chooses the axis which should be replaced.
- **u** (*None* | *int*) – Optionally choose a subset of MPS indices present in the axes of *A*, namely the indices corresponding to `self.unit_cell[u]`, as returned by `mps_idx_fix_u()`. The resulting array will not have the additional dimension(s) of u .

Returns **res_A** – Reshaped and reordered versions of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index j maps to lattice site (x_0, x_1, x_2) , then `res_A[..., x0, x1, x2, ...] = A[..., j, ...]`.

Return type *ndarray*

Examples

Say you measure expectation values of an onsite term for an MPS, which gives you an 1D array *A*, where *A[i]* is the expectation value of the site given by `self.mps2lat_idx(i)`. Then this function gives you the expectation values ordered by the lattice:

```
>>> print(lat.shape, A.shape)
(10, 3, 2) (60,)
>>> A_res = lat.mps2lat_values(A)
>>> A_res.shape
(10, 3, 2)
>>> A_res[lat.mps2lat_idx(5)] == A[5]
True
```

If you have a correlation function `C[i, j]`, it gets just slightly more complicated:


```
>>> print(lat.shape, C.shape)
(10, 3, 2) (60, 60)
>>> lat.mps2lat_values(C, axes=[0, 1]).shape
(10, 3, 2, 10, 3, 2)
```

If the unit cell consists of different physical sites, an onsite operator might be defined only on one of the sites in the unit cell. Then you can use `mps_idx_fix_u()` to get the indices of sites it is defined on, measure the operator on these sites, and use the argument `u` of this function.

```
>>> u = 0
>>> idx_subset = lat.mps_idx_fix_u(u)
>>> A_u = A[idx_subset]
>>> A_u_res = lat.mps2lat_values(A_u, u=u)
>>> A_u_res.shape
(10, 3)
>>> np.all(A_res[:, :, u] == A_u_res[:, :])
True
```

Todo: make sure this function is used for expectation values...

mps2lat_values_masked (*A*, *axes=-1*, *mps_inds=None*, *include_u=None*)

Reshape/reorder an array *A* to replace an MPS index by lattice indices.

This is a generalization of `mps2lat_values()` allowing for the case of an arbitrary set of MPS indices present in each axis of *A*.

Parameters

- **A** (*ndarray*) – Some values.
- **axes** ((*iterable of int*)) – Chooses the axis of *A* which should be replaced. If multiple axes are given, you also need to give multiple index arrays as *mps_inds*.
- **mps_inds** ((*list of 1D ndarray*)) – Specifies for each *axis* in *axes*, for which MPS indices we have values in the corresponding *axis* of *A*. Defaults to `[np.arange(A.shape[ax]) for ax in axes]`. For indices accross the MPS unit cell and “infinite” *bc_MPS*, we shift *x_0* accordingly.
- **include_u** ((*list of bool*)) – Specifies for each *axis* in *axes*, whether the *u* index of the lattice should be included into the output array *res_A*. Defaults to `len(self.unit_cell) > 1`.

Returns *res_A* – Reshaped and reordered copy of *A*. Such that MPS indices along the specified axes are replaced by lattice indices, i.e., if MPS index *j* maps to lattice site (*x0*, *x1*, *x2*), then `res_A[..., x0, x1, x2, ...] = A[..., mps_inds[j], ...]`.

Return type `np.ma.MaskedArray`

mps_idx_fix_u (*u=None*)

return an index array of MPS indices for which the site within the unit cell is *u*.

If you have multiple sites in your unit-cell, an onsite operator is in general not defined for all sites. This functions returns an index array of the mps indices which belong to sites given by `self.unit_cell[u]`.

Parameters *u* (*None* / *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns `mps_idx` – MPS indices for which `self.site(i)` is `self.unit_cell[u]`.
Ordered ascending.

Return type array

`mps_lat_idx_fix_u` (*u=None*)

Similar as `mps_idx_fix_u()`, but return also the corresponding lattice indices.

Parameters *u* (*None* | *int*) – Selects a site of the unit cell. *None* (default) means all sites.

Returns

- **`mps_idx`** (array) – MPS indices *i* for which `self.site(i)` is `self.unit_cell[u]`.
- **`lat_idx`** (2D array) – The row *j* contains the lattice index (without *u*) corresponding to `mps_idx[j]`.

`mps_sites` ()

Return a list of sites for all MPS indices.

Equivalent to `[self.site(i) for i in range(self.N_sites)]`.

This should be used for *sites* of 1D tensor networks (MPS, MPO,...).

`multi_coupling_shape` (*dx*)

Calculate correct shape of the *strengths* for a multi_coupling.

Parameters *dx* (2D array, shape (N_ops, *dim*)) – `dx[i, :]` is the translation vector in the lattice for the *i*-th operator. Corresponds to the *dx* of each operator given in the argument *ops* of `tenpy.models.model.MultiCouplingModel.add_multi_coupling()`.

Returns

- **`coupling_shape`** (tuple of int) – Len *dim*. The correct shape for an array specifying the coupling strength. *lat_indices* has only rows within this shape.
- **`shift_lat_indices`** (array) – Translation vector from origin to the lower left corner of box spanned by *dx*. (Unlike for `coupling_shape()` it can also contain entries > 0)

`number_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

`number_next_nearest_neighbors` (*u=0*)

Deprecated.

Deprecated since version 0.5.0: Use `count_neighbors()` instead.

property order

Defines an ordering of the lattice sites, thus mapping the lattice to a 1D chain.

Each row of the array contains the lattice indices for one site, the order of the rows thus specifies a path through the lattice, along which an MPS will wind through the lattice.

You can visualize the order with `plot_order()`.

`plot_basis` (*ax, origin=0.0, 0.0, shade=None, **kwargs*)

Plot arrows indicating the basis vectors of the lattice.

Parameters

- **`ax`** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **`**kwargs`** – Keyword arguments for `ax.arrow`.

plot_bc_identified (*ax*, *direction*=-1, *origin*=None, *cylinder_axis*=False, ***kwargs*)

Mark two sites identified by periodic boundary conditions.

Works only for lattice with a 2-dimensional basis.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **direction** (*int*) – The direction of the lattice along which we should mark the identified sites. If None, mark it along all directions with periodic boundary conditions.
- **cylinder_axis** (*bool*) – Whether to plot the cylinder axis as well.
- **origin** (*None* | *np.ndarray*) – The origin starting from where we mark the identified sites. Defaults to the first entry of `unit_cell_positions`.
- ****kwargs** – Keyword arguments for the used `ax.plot`.

plot_coupling (*ax*, *coupling*=None, *wrap*=False, ***kwargs*)

Plot lines connecting nearest neighbors of the lattice.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **coupling** (*list of (u1, u2, dx)*) – By default (None), use `self.pairs['nearest_neighbors']`. Specifies the connections to be plotted; iterating over lattice indices (*i0, i1, ...*), we plot a connection from the site (*i0, i1, ..., u1*) to the site (*i0+dx[0], i1+dx[1], ..., u2*), taking into account the boundary conditions.
- **wrap** (*bool*) – If True, wrap
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_order (*ax*, *order*=None, *textkwargs*={}, ***kwargs*)

Plot a line connecting sites in the specified “order” and text labels enumerating them.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **order** (*None* | *2D array (self.N_sites, self.dim+1)*) – The order as returned by `ordering()`; by default (None) use `order`.
- **textkwargs** (*None* | *dict*) – If not None, we add text labels enumerating the sites in the plot. The dictionary can contain keyword arguments for `ax.text()`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

plot_sites (*ax*, *markers*=['o', '^', 's', 'p', 'h', 'D'], ***kwargs*)

Plot the sites of the lattice with markers.

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **markers** (*list*) – List of values for the keyword *marker* of `ax.plot()` to distinguish the different sites in the unit cell, a site *u* in the unit cell is plotted with a marker `markers[u % len(markers)]`.
- ****kwargs** – Further keyword arguments given to `ax.plot()`.

position (*lat_idx*)

return ‘space’ position of one or multiple sites.

Parameters `lat_idx` (ndarray, (... , dim+1)) – Lattice indices.

Returns `pos` – The position of the lattice sites specified by `lat_idx` in real-space.

Return type ndarray, (... , dim)

possible_couplings (`u1`, `u2`, `dx`)

Find possible MPS indices for two-site couplings.

For periodic boundary conditions (`bc[a] == False`) the index `x_a` is taken modulo `Ls[a]` and runs through `range(Ls[a])`. For open boundary conditions, `x_a` is limited to $0 \leq x_a < Ls[a]$ and $0 \leq x_a + dx[a] < lat.Ls[a]$.

Parameters

- `u2` (`u1`,) – Indices within the unit cell; the `u1` and `u2` of `add_coupling()`
- `dx` (array) – Length `dim`. The translation in terms of basis vectors for the coupling.

Returns

- `mps1`, `mps2` (array) – For each possible two-site coupling the MPS indices for the `u1` and `u2`.
- `lat_indices` (2D int array) – Rows of `lat_indices` correspond to rows of `mps_ijkl` and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- `coupling_shape` (tuple of int) – Len `dim`. The correct shape for an array specifying the coupling strength. `lat_indices` has only rows within this shape.

possible_multi_couplings (`ops`)

Generalization of `possible_couplings()` to couplings with more than 2 sites.

Parameters `ops` (list of (opname, dx, u)) – Same as the argument `ops` of `add_multi_coupling()`.

Returns

- `mps_ijkl` (2D int array) – Each row contains MPS indices `i,j,k,l,...` for each of the operators positions. The positions are defined by `dx` (`j,k,l,...` relative to `i`) and boundary conditions of `self` (how much the `box` for given `dx` can be shifted around without hitting a boundary - these are the different rows).
- `lat_indices` (2D int array) – Rows of `lat_indices` correspond to rows of `mps_ijkl` and contain the lattice indices of the “lower left corner” of the box containing the coupling.
- `coupling_shape` (tuple of int) – Len `dim`. The correct shape for an array specifying the coupling strength. `lat_indices` has only rows within this shape.

save_hdf5 (`hdf5_saver`, `h5gr`, `subpath`)

Export `self` into a HDF5 file.

This method saves all the data it needs to reconstruct `self` with `from_hdf5()`.

Specifically, it saves `unit_cell`, `Ls`, `unit_cell_positions`, `basis`, `boundary_conditions`, pairs under their name, `bc_MPS` as “boundary_conditions_MPS”, and `order` as “order_for_MPS”. Moreover, it saves `dim` and `N_sites` as HDF5 attributes.

Parameters

- `hdf5_saver` (`Hdf5Saver`) – Instance of the saving engine.
- `h5gr` (:class`Group`) – HDF5 group which is supposed to represent `self`.
- `subpath` (str) – The name of `h5gr` with a ‘/’ in the end.

```

site(i)
    return Site instance corresponding to an MPS index i

test_sanity()
    Sanity check.

    Raises ValueErrors, if something is wrong.

```

Module description

Kitaev’s exactly solvable toric code model.

As we put the model on a cylinder, the name “toric code” is a bit misleading, but it is the established name for this model...

7.10 networks

- full name: `tenpy.networks`
- parent module: `tenpy`
- type: module

Module description

Definitions of tensor networks like MPS and MPO.

Here, ‘tensor network’ refers just to the (partial) contraction of tensors. For example an MPS represents the contraction along the ‘virtual’ legs/bonds of its B .

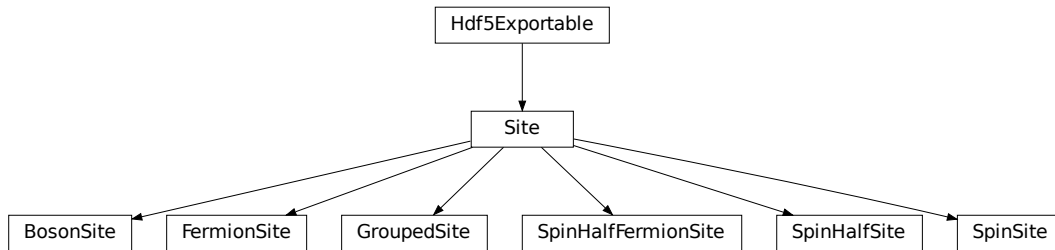
Submodules

<code>site</code>	Defines a class describing the local physical Hilbert space.
<code>mps</code>	This module contains a base class for a Matrix Product State (MPS).
<code>mpo</code>	Matrix product operator (MPO).
<code>terms</code>	Classes to store a collection of operator names and sites they act on, together with prefactors.
<code>purification_mps</code>	This module contains an MPS class representing an density matrix by purification.

7.10.1 site

- full name: `tenpy.networks.site`
- parent module: `tenpy.networks`
- type: module

Classes

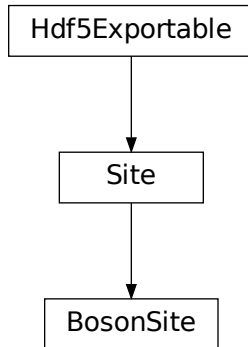


<code>BosonSite</code> ([Nmax, conserve, filling])	Create a <i>Site</i> for up to <i>Nmax</i> bosons.
<code>FermionSite</code> ([conserve, filling])	Create a <i>Site</i> for spin-less fermions.
<code>GroupedSite</code> (sites[, labels, charges])	Group two or more <i>Site</i> into a larger one.
<code>Site</code> (leg[, state_labels])	Collects necessary information about a single local site of a lattice.
<code>SpinHalfFermionSite</code> ([cons_N, cons_Sz, filling])	Create a <i>Site</i> for spinful (spin-1/2) fermions.
<code>SpinHalfSite</code> ([conserve])	Spin-1/2 site.
<code>SpinSite</code> ([S, conserve])	General Spin S site.

BosonSite

- full name: `tenpy.networks.site.BosonSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>BosonSite.__init__([Nmax, conserve, filling])</code>	Initialize self.
<code>BosonSite.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>BosonSite.change_charge([new_leg_charge, ...])</code>	Change the charges of the site (in place).
<code>BosonSite.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>BosonSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>BosonSite.get_op(name)</code>	Return operator of given name.
<code>BosonSite.multiply_op_names(names)</code>	Multiply operator names together.
<code>BosonSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>BosonSite.remove_op(name)</code>	Remove an added operator.
<code>BosonSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>BosonSite.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>BosonSite.state_index(label)</code>	Return index of a basis state from its label.
<code>BosonSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>BosonSite.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>BosonSite.valid_opname(name)</code>	Check whether 'name' labels a valid onsite-operator.

Class Attributes and Properties

<code>BosonSite.dim</code>	Dimension of the local Hilbert space.
<code>BosonSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.BosonSite` (*Nmax=1, conserve='N', filling=0.0*)

Bases: `tenpy.networks.site.Site`

Create a *Site* for up to *Nmax* bosons.

Local states are `vac`, `1`, `2`, `...`, `Nc`. (Exception: for parity conservation, we sort as `vac`, `2`, `4`, `...`, `1`, `3`, `5`, `...`.)

operator	description
<code>Id</code> , <code>JW</code>	Identity \mathbb{I}
<code>B</code>	Annihilation operator b
<code>Bd</code>	Creation operator b^\dagger
<code>N</code>	Number operator $n = b^\dagger b$
<code>NN</code>	n^2
<code>dN</code>	$\delta n := n - \text{filling}$
<code>dNdN</code>	$(\delta n)^2$
<code>P</code>	Parity $Id - 2(n \bmod 2)$.

<i>conserve</i>	<i>qmod</i>	<i>excluded onsite operators</i>
'N'	[1]	–
'parity'	[2]	–
None	[]	–

Parameters

- **Nmax** (*int*) – Cutoff defining the maximum number of bosons per site. The default `Nmax=1` describes hard-core bosons.
- **conserve** (*str*) – Defines what is conserved, see table above.
- **filling** (*float*) – Average filling. Used to define `dN`.

conserve

Defines what is conserved, see table above.

Type *str*

filling

Average filling. Used to define `dN`.

Type *float*

add_op (*name, op, need_JW=False, hc=None*)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.

- **op** (`np.ndarray` | `Array`) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to `Array`. `LegCharges` have to be `[leg, leg.conj()]`. We set labels 'p', 'p*'.
- **need_JW** (`bool`) – Whether the operator needs a Jordan-Wigner string. If `True`, add `name` to `need_JW_string`.
- **hc** (`None` | `False` | `str`) – The name for the hermitian conjugate operator, to be used for `hc_ops`. By default (`None`), try to auto-determine it. If `False`, disable adding antries to `hc_ops`.

change_charge (`new_leg_charge=None, permute=None`)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (`LegCharge` | `None`) – The new charges to be used. If `None`, use trivial charges.
- **permute** (`ndarray` | `None`) – The permutation applied to the physical leg, which gets used to adjust `state_labels` and `perm`. If you sorted the previous leg with `perm_qind`, `new_leg_charge = leg.sort()`, use `old_leg.perm_flat_from_perm_qind(perm_qind)`. Ignored if `None`.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (`hdf5_loader, h5gr, subpath`)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which is represent the object to be constructed.
- **subpath** (`str`) – The *name* of `h5gr` with a '/' in the end.

Returns obj – Newly generated class instance containing the required data.

Return type `cls`

get_hc_op_name (`name`)

Return the hermitian conjugate of a given operator.

Parameters name (`str`) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as `get_op()` does.

Returns hc_op_name – Operator name for the hermi such that `get_op()` of

Return type `str`

get_op (`name`)

Return operator of given name.

Parameters name (`str`) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns op – The operator given by `name`, with labels 'p', 'p*'. If name already was an `np.ndarray`, it's directly returned.

Return type `np.ndarray`

multiply_op_names (*names*)

Multiply operator names together.

Join the operator names in *names* such that *get_op* returns the product of the corresponding operators.

Parameters *names* (*list of str*) – List of valid operator labels.

Returns **combined_opname** – A valid operator name *Operatorname* representing the product of operators in *names*.

Return type *str*

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters *name* (*str*) – The name of the operator, as in *get_op()*.

Returns **needs_JW** – Whether the operator needs a Jordan-Wigner string, judging from *need_JW_string*.

Return type *bool*

remove_op (*name*)

Remove an added operator.

Parameters *name* (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

state_index (*label*)

Return index of a basis state from its label.

Parameters *label* (*int | string*) – either the index directly or a label (string) set before.

Returns **state_index** – the index of the basis state associated with the label.

Return type *int*

state_indices (*labels*)

Same as *state_index()*, but for multiple labels.

test_sanity()

Sanity check, raises ValueErrors, if something is wrong.

valid_opname(name)

Check whether 'name' labels a valid onsite-operator.

Parameters **name** (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

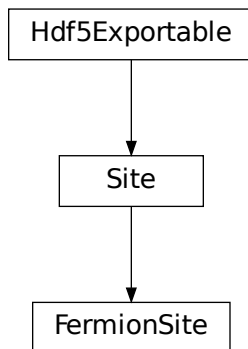
Returns **valid** – True if *name* is a valid argument to *get_op()*.

Return type **bool**

FermionSite

- full name: `tenpy.networks.site.FermionSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>FermionSite.__init__([conserve, filling])</code>	Initialize self.
<code>FermionSite.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>FermionSite.change_charge([new_leg_charge, ...])</code>	Change the charges of the site (in place).
<code>FermionSite.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>FermionSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>FermionSite.get_op(name)</code>	Return operator of given name.
<code>FermionSite.multiply_op_names(names)</code>	Multiply operator names together.

continues on next page

Table 126 – continued from previous page

<code>FermionSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>FermionSite.remove_op(name)</code>	Remove an added operator.
<code>FermionSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>FermionSite.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>FermionSite.state_index(label)</code>	Return index of a basis state from its label.
<code>FermionSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>FermionSite.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>FermionSite.valid_opname(name)</code>	Check whether ‘name’ labels a valid onsite-operator.

Class Attributes and Properties

<code>FermionSite.dim</code>	Dimension of the local Hilbert space.
<code>FermionSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.FermionSite` (*conserve='N', filling=0.5*)

Bases: `tenpy.networks.site.Site`

Create a *Site* for spin-less fermions.

Local states are empty and full.

Warning: Using the Jordan-Wigner string (JW) is crucial to get correct results, otherwise you just describe hardcore bosons! Further details in *Fermions and the Jordan-Wigner transformation*.

operator	description
Id	Identity \mathbb{I}
JW	Sign for the Jordan-Wigner string.
C	Annihilation operator c (up to ‘JW’-string left of it)
Cd	Creation operator c^\dagger (up to ‘JW’-string left of it)
N	Number operator $n = c^\dagger c$
dN	$\delta n := n - \text{filling}$
dNdN	$(\delta n)^2$

<i>conserve</i>	qmod	<i>excluded</i> onsite operators
'N'	[1]	–
'parity'	[2]	–
None	[]	–

Parameters

- **conserve** (*str*) – Defines what is conserved, see table above.
- **filling** (*float*) – Average filling. Used to define dN.

conserve

Defines what is conserved, see table above.

Type `str`

filling

Average filling. Used to define `dN`.

Type `float`

add_op (*name*, *op*, *need_JW=False*, *hc=None*)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (`np.ndarray` | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. *LegCharges* have to be [*leg*, *leg.conj()*]. We set labels 'p', 'p*'.
 If *op* is a *LegCharge*, we use *leg* and *leg.conj()* to get the labels.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If *True*, add *name* to *need_JW_string*.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for *hc_ops*. By default (*None*), try to auto-determine it. If *False*, disable adding antries to *hc_ops*.

change_charge (*new_leg_charge=None*, *permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (*LegCharge* | *None*) – The new charges to be used. If *None*, use trivial charges.
- **permute** (*ndarray* | *None*) – The permutation applied to the physical leg, which gets used to adjust *state_labels* and *perm*. If you sorted the previous leg with *perm_qind*, *new_leg_charge = leg.sort()*, use *old_leg.perm_flat_from_perm_qind(perm_qind)*. Ignored if *None*.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

get_hc_op_name (*name*)

Return the hermitian conjugate of a given operator.

Parameters **name** (*str*) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as *get_op()* does.

Returns *hc_op_name* – Operator name for the hermi such that *get_op()* of

Return type `str`

get_op (*name*)

Return operator of given name.

Parameters **name** (*str*) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns **op** – The operator given by *name*, with labels 'p', 'p*'. If name already was an `np.ndarray`, it's directly returned.

Return type `np.ndarray`

multiply_op_names (*names*)

Multiply operator names together.

Join the operator names in *names* such that *get_op* returns the product of the corresponding operators.

Parameters **names** (*list of str*) – List of valid operator labels.

Returns **combined_opname** – A valid operator name *Operatorname* representing the product of operators in *names*.

Return type `str`

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters **name** (*str*) – The name of the operator, as in *get_op()*.

Returns **needs_JW** – Whether the operator needs a Jordan-Wigner string, judging from *need_JW_string*.

Return type `bool`

remove_op (*name*)

Remove an added operator.

Parameters **name** (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.

- **h5gr** (`:class`Group``) – HDF5 group which is supposed to represent *self*.
- **subpath** (`str`) – The *name* of *h5gr* with a `' / '` in the end.

state_index (`label`)

Return index of a basis state from its label.

Parameters **label** (`int` | `string`) – either the index directly or a label (string) set before.

Returns **state_index** – the index of the basis state associated with the label.

Return type `int`

state_indices (`labels`)

Same as `state_index()`, but for multiple labels.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

valid_opname (`name`)

Check whether ‘name’ labels a valid onsite-operator.

Parameters **name** (`str`) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

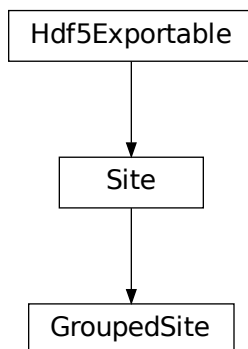
Returns **valid** – True if *name* is a valid argument to `get_op()`.

Return type `bool`

GroupedSite

- full name: `tenpy.networks.site.GroupedSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>GroupedSite.__init__(sites[, labels, charges])</code>	Initialize self.
<code>GroupedSite.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>GroupedSite.change_charge([new_leg_charge, ...])</code>	Change the charges of the site (in place).
<code>GroupedSite.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>GroupedSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>GroupedSite.get_op(name)</code>	Return operator of given name.
<code>GroupedSite.kroneckerproduct(ops)</code>	Return the Kronecker product $op_0 \otimes op_1$ of local operators.
<code>GroupedSite.multiply_op_names(names)</code>	Multiply operator names together.
<code>GroupedSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>GroupedSite.remove_op(name)</code>	Remove an added operator.
<code>GroupedSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>GroupedSite.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>GroupedSite.state_index(label)</code>	Return index of a basis state from its label.
<code>GroupedSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>GroupedSite.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>GroupedSite.valid_opname(name)</code>	Check whether ‘name’ labels a valid onsite-operator.

Class Attributes and Properties

<code>GroupedSite.dim</code>	Dimension of the local Hilbert space.
<code>GroupedSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.GroupedSite` (*sites*, *labels=None*, *charges='same'*)

Bases: `tenpy.networks.site.Site`

Group two or more `Site` into a larger one.

A typical use-case is that you want a `NearestNeighborModel` for TEBD although you have next-nearest neighbor interactions: you just double your local Hilbertspace to consist of two original sites. Note that this is a ‘hack’ at the cost of other things (e.g., measurements of ‘local’ operators) getting more complicated/computationally expensive.

If the individual sites indicate fermionic operators (with entries in `need_JW_string`), we construct the new onsite operators of *site1* to include the JW string of *site0*, i.e., we use the Kronecker product of `[JW, op]` instead of `[Id, op]` if necessary (but always `[op, Id]`). In that way the onsite operators of this `DoubleSite` automatically fulfill the expected commutation relations. See also *Fermions and the Jordan-Wigner transformation*.

Parameters

- **sites** (list of `Site`) – The individual sites being grouped together. Copied before use if `charges != 'same'`.
- **labels** – Include the Kronecker product of the each onsite operator *op* on `sites[i]` and identities on other sites with the name `opname+labels[i]`. Similarly, set state labels for `' '.join(state[i]+'_'+labels[i])`. Defaults to `[str(i) for i in range(n_sites)]`, which for example grouping two `SpinSites` gives operators name

like "Sz0" and sites labels like 'up_0 down_1'.

- **charges** ('same' | 'drop' | 'independent') – How to handle charges, defaults to 'same'. 'same' means that all *sites* have the same *ChargeInfo*, and the total charge is the sum of the charges on the individual *sites*. 'independent' means that the *sites* have possibly different *ChargeInfo*, and the charges are conserved separately, i.e., we have *n_sites* conserved charges. For 'drop', we drop any charges, such that the remaining legcharges are trivial.

n_sites

The number of sites grouped together, i.e. `len(sites)`.

Type `int`

sites

The sites grouped together into self.

Type list of *Site*

labels

The labels using which the single-site operators are added during construction.

Type list of `str`

kroneckerproduct (*ops*)

Return the Kronecker product $op0 \otimes op1$ of local operators.

Parameters **ops** (list of *Array*) – One operator (or operator name) on each of the ungrouped sites. Each operator should have labels ['p', 'p*'].

Returns **prod** – Kronecker product $ops[0] \otimes ops[1] \otimes \dots$, with labels ['p', 'p*'].

Return type *Array*

add_op (*name, op, need_JW=False, hc=None*)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (*np.ndarray* | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. LegCharges have to be [*leg*, *leg.conj()*]. We set labels 'p', 'p*'.
 If *op* is a *LegCharge*, we use its *leg* and *leg.conj()* to set the labels.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If *True*, add *name* to *need_JW_string*.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for *hc_ops*. By default (*None*), try to auto-determine it. If *False*, disable adding antries to *hc_ops*.

change_charge (*new_leg_charge=None, permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (*LegCharge* | *None*) – The new charges to be used. If *None*, use trivial charges.
- **permute** (*ndarray* | *None*) – The permutation applied to the physical leg, which gets used to adjust *state_labels* and *perm*. If you sorted the previ-

ous leg with `perm_qind`, `new_leg_charge = leg.sort()`, use `old_leg.perm_flat_from_perm_qind(perm_qind)`. Ignored if None.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`**get_hc_op_name** (*name*)

Return the hermitian conjugate of a given operator.

Parameters **name** (*str*) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as `get_op()` does.

Returns `hc_op_name` – Operator name for the hermi such that `get_op()` of

Return type `str`**get_op** (*name*)

Return operator of given name.

Parameters **name** (*str*) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns `op` – The operator given by *name*, with labels `'p'`, `'p*'`. If name already was an `np.ndarray`, it's directly returned.

Return type `np.ndarray`**multiply_op_names** (*names*)

Multiply operator names together.

Join the operator names in *names* such that `get_op` returns the product of the corresponding operators.

Parameters **names** (*list of str*) – List of valid operator labels.

Returns `combined_opname` – A valid operator name `Operatorname` representing the product of operators in *names*.

Return type `str`**property onsite_ops**

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters **name** (*str*) – The name of the operator, as in `get_op()`.

Returns `needs_JW` – Whether the operator needs a Jordan-Wigner string, judging from `need_JW_string`.

Return type `bool`

remove_op (*name*)
Remove an added operator.

Parameters `name` (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)
Rename an added operator.

Parameters

- `old_name` (*str*) – The old name of the operator.
- `new_name` (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)
Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- `hdf5_saver` (*Hdf5Saver*) – Instance of the saving engine.
- `h5gr` (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- `subpath` (*str*) – The *name* of *h5gr* with a '/' in the end.

state_index (*label*)
Return index of a basis state from its label.

Parameters `label` (*int* | *string*) – either the index directly or a label (string) set before.

Returns `state_index` – the index of the basis state associated with the label.

Return type `int`

state_indices (*labels*)
Same as `state_index()`, but for multiple labels.

test_sanity ()
Sanity check, raises `ValueErrors`, if something is wrong.

valid_opname (*name*)
Check whether 'name' labels a valid onsite-operator.

Parameters `name` (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

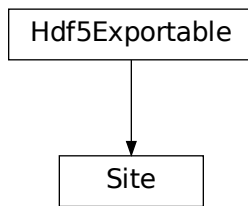
Returns `valid` – True if *name* is a valid argument to `get_op()`.

Return type `bool`

Site

- full name: `tenpy.networks.site.Site`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>Site.__init__(leg[, state_labels])</code>	Initialize self.
<code>Site.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>Site.change_charge([new_leg_charge, per-mute])</code>	Change the charges of the site (in place).
<code>Site.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>Site.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>Site.get_op(name)</code>	Return operator of given name.
<code>Site.multiply_op_names(names)</code>	Multiply operator names together.
<code>Site.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>Site.remove_op(name)</code>	Remove an added operator.
<code>Site.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>Site.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>Site.state_index(label)</code>	Return index of a basis state from its label.
<code>Site.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>Site.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>Site.valid_opname(name)</code>	Check whether 'name' labels a valid onsite-operator.

Class Attributes and Properties

<code>Site.dim</code>	Dimension of the local Hilbert space.
<code>Site.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.Site` (*leg*, *state_labels=None*, ***site_ops*)

Bases: `tenpy.tools.hdf5_io.Hdf5Exportable`

Collects necessary information about a single local site of a lattice.

This class defines what the local basis states are: it provides the *leg* defining the charges of the physical leg for this site. Moreover, it stores (local) on-site operators, which are directly available as attribute, e.g., `self.Sz` is the Sz operator for the *SpinSite*. Alternatively, operators can be obtained with `get_op()`. The operator names `Id` and `JW` are reserved for the identity and Jordan-Wigner strings.

Warning: The order of the local basis can change depending on the charge conservation! This is a *necessary* feature since we need to sort the basis by charges for efficiency. We use the *state_labels* and *perm* to keep track of these permutations.

Parameters

- **leg** (*LegCharge*) – Charges of the physical states, to be used for the physical leg of MPS.
- **state_labels** (*None* | *list of str*) – Optionally a label for each local basis states. *None* entries are ignored / not set.
- ****site_ops** – Additional keyword arguments of the form `name=op` given to `add_op()`. The identity operator `'Id'` is automatically included. If no `'JW'` for the Jordan-Wigner string is given, `'JW'` is set as an alias to `'Id'`.

leg

Charges of the local basis states.

Type *LegCharge*

state_labels

(Optional) labels for the local basis states.

Type `{str: int}`

opnames

Labels of all onsite operators (i.e. `self.op` exists if `'op'` in `self.opnames`). Note that `get_op()` allows arbitrary concatenations of them.

Type *set*

need_JW_string

Labels of all onsite operators that need a Jordan-Wigner string. Used in `op_needs_JW()` to determine whether an operator anticommutes or commutes with operators on other sites.

Type *set*

ops

Onsite operators are added directly as attributes to `self`. For example after `self.add_op('Sz', Sz)` you can use `self.Sz` for the Sz operator. All onsite operators have labels `'p'`, `'p*'`.

Type *Array*

perm
Index permutation of the physical leg compared to *conserve=None*, i.e. `OP_conserved = OP_nonconserved[np.ix_(perm, perm)]` and `perm[state_labels_conserved["some_state"]] == state_labels_nonconserved["some_state"]`.

Type 1D array

JW_exponent
Exponents of the 'JW' operator, such that `self.JW.to_ndarray() = np.diag(np.exp(1.j*np.pi* JW_exponent))`

Type 1D array

hc_ops
Mapping from operator names to their hermitian conjugates. Use `get_hc_op_name()` to obtain entries.

Type `dict(str->str)`

Examples

The following generates a site for spin-1/2 with Sz conservation. Note that $S_x = (S_p + S_m) / 2$ violates Sz conservation and is thus not a valid on-site operator.

```
>>> chinfo = npc.ChargeInfo([1], ['Sz'])
>>> ch = npc.LegCharge.from_qflat(chinfo, [1, -1])
>>> Sp = [[0, 1.], [0, 0]]
>>> Sm = [[0, 0], [1., 0]]
>>> Sz = [[0.5, 0], [0, -0.5]]
>>> site = Site(ch, ['up', 'down'], Splus=Sp, Sminus=Sm, Sz=Sz)
>>> print(site.Splus.to_ndarray())
array([[ 0.,  1.],
       [ 0.,  0.]])
>>> print(site.get_op('Sminus').to_ndarray())
array([[ 0.,  0.],
       [ 1.,  0.]])
>>> print(site.get_op('Splus Sminus').to_ndarray())
array([[ 1.,  0.],
       [ 0.,  0.]])
```

change_charge (*new_leg_charge=None*, *permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (`LegCharge` | `None`) – The new charges to be used. If `None`, use trivial charges.
- **permute** (`ndarray` | `None`) – The permutation applied to the physical leg, which gets used to adjust `state_labels` and `perm`. If you sorted the previous leg with `perm_qind`, `new_leg_charge = leg.sort()`, use `old_leg.perm_flat_from_perm_qind(perm_qind)`. Ignored if `None`.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

property dim

Dimension of the local Hilbert space.

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

add_op (*name, op, need_JW=False, hc=None*)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (*np.ndarray* | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. LegCharges have to be `[leg, leg.conj()]`. We set labels 'p', 'p*'.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If *True*, add *name* to *need_JW_string*.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for *hc_ops*. By default (*None*), try to auto-determine it. If *False*, disable adding antries to *hc_ops*.

rename_op (*old_name, new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

remove_op (*name*)

Remove an added operator.

Parameters **name** (*str*) – The name of the operator to be removed.

state_index (*label*)

Return index of a basis state from its label.

Parameters **label** (*int* | *string*) – either the index directly or a label (string) set before.

Returns **state_index** – the index of the basis state associated with the label.

Return type *int*

state_indices (*labels*)

Same as *state_index()*, but for multiple labels.

get_op (*name*)

Return operator of given name.

Parameters **name** (*str*) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns **op** – The operator given by *name*, with labels 'p', 'p*'. If name already was an *np* Array, it's directly returned.

Return type *np_conserved*

get_hc_op_name (*name*)

Return the hermitian conjugate of a given operator.

Parameters **name** (*str*) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as `get_op()` does.

Returns **hc_op_name** – Operator name for the hermi such that `get_op()` of

Return type *str*

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters **name** (*str*) – The name of the operator, as in `get_op()`.

Returns **needs_JW** – Whether the operator needs a Jordan-Wigner string, judging from `need_JW_string`.

Return type *bool*

valid_opname (*name*)

Check whether 'name' labels a valid onsite-operator.

Parameters **name** (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

Returns **valid** – True if *name* is a valid argument to `get_op()`.

Return type *bool*

multiply_op_names (*names*)

Multiply operator names together.

Join the operator names in *names* such that `get_op` returns the product of the corresponding operators.

Parameters **names** (*list of str*) – List of valid operator labels.

Returns **combined_opname** – A valid operator name Operatorname representing the product of operators in *names*.

Return type *str*

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns **obj** – Newly generated class instance containing the required data.

Return type *cls*

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

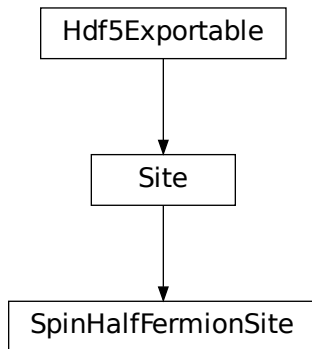
- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.

- `h5gr (:class`Group`)` – HDF5 group which is supposed to represent *self*.
- `subpath (str)` – The *name* of *h5gr* with a `' / '` in the end.

SpinHalfFermionSite

- full name: `tenpy.networks.site.SpinHalfFermionSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>SpinHalfFermionSite.__init__([cons_N, ...])</code>	Initialize self.
<code>SpinHalfFermionSite.add_op(name, op[, ...])</code>	Add one on-site operators.
<code>SpinHalfFermionSite.change_charge([...])</code>	Change the charges of the site (in place).
<code>SpinHalfFermionSite.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>SpinHalfFermionSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>SpinHalfFermionSite.get_op(name)</code>	Return operator of given name.
<code>SpinHalfFermionSite.multiply_op_names(names)</code>	Multiply operator names together.
<code>SpinHalfFermionSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>SpinHalfFermionSite.remove_op(name)</code>	Remove an added operator.

continues on next page

Table 132 – continued from previous page

<code>SpinHalfFermionSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>SpinHalfFermionSite.save_hdf5(hdf5_saver, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>SpinHalfFermionSite.state_index(label)</code>	Return index of a basis state from its label.
<code>SpinHalfFermionSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>SpinHalfFermionSite.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>SpinHalfFermionSite.valid_opname(name)</code>	Check whether ‘name’ labels a valid onsite-operator.

Class Attributes and Properties

<code>SpinHalfFermionSite.dim</code>	Dimension of the local Hilbert space.
<code>SpinHalfFermionSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.SpinHalfFermionSite` (`cons_N='N'`, `cons_Sz='Sz'`, `filling=1.0`)

Bases: `tenpy.networks.site.Site`

Create a *Site* for spinful (spin-1/2) fermions.

Local states are: `empty` (vacuum), `up` (one spin-up electron), `down` (one spin-down electron), and `full` (both electrons)

Local operators can be built from creation operators.

Warning: Using the Jordan-Wigner string (JW) in the correct way is crucial to get correct results, otherwise you just describe hardcore bosons!

operator	description
<code>Id</code>	Identity \mathbb{I}
<code>JW</code>	Sign for the Jordan-Wigner string $(-1)^{n_{\uparrow}+n_{\downarrow}}$
<code>JWu</code>	Partial sign for the Jordan-Wigner string $(-1)^{n_{\uparrow}}$
<code>JWd</code>	Partial sign for the Jordan-Wigner string $(-1)^{n_{\downarrow}}$
<code>Cu</code>	Annihilation operator spin-up c_{\uparrow} (up to ‘JW’-string on sites left of it).
<code>Cdu</code>	Creation operator spin-up c_{\uparrow}^{\dagger} (up to ‘JW’-string on sites left of it).
<code>Cd</code>	Annihilation operator spin-down c_{\downarrow} (up to ‘JW’-string on sites left of it). Includes <code>JWu</code> such that it anti-commutes onsite with <code>Cu</code> , <code>Cdu</code> .
<code>Cdd</code>	Creation operator spin-down c_{\downarrow}^{\dagger} (up to ‘JW’-string on sites left of it). Includes <code>JWu</code> such that it anti-commutes onsite with <code>Cu</code> , <code>Cdu</code> .
<code>Nu</code>	Number operator $n_{\uparrow} = c_{\uparrow}^{\dagger}c_{\uparrow}$
<code>Nd</code>	Number operator $n_{\downarrow} = c_{\downarrow}^{\dagger}c_{\downarrow}$
<code>NuNd</code>	Dotted number operators $n_{\uparrow}n_{\downarrow}$
<code>Ntot</code>	Total number operator $n_t = n_{\uparrow} + n_{\downarrow}$
<code>dN</code>	Total number operator compared to the filling $\Delta n = n_t - filling$
<code>Sx</code> , <code>Sy</code> , <code>Sz</code>	Spin operators $S^{x,y,z}$, in particular $S^z = \frac{1}{2}(n_{\uparrow} - n_{\downarrow})$
<code>Sp</code> , <code>Sm</code>	Spin flips $S^{\pm} = S^x \pm iS^y$, e.g. $S^+ = c_{\uparrow}^{\dagger}c_{\downarrow}$

The spin operators are defined as $S^\gamma = (c_\uparrow^\dagger, c_\downarrow^\dagger) \sigma^\gamma (c_\uparrow, c_\downarrow)^T$, where σ^γ are spin-1/2 matrices (i.e. half the pauli matrices).

<i>cons_N</i>	<i>cons_Sz</i>	qmod	<i>excluded onsite operators</i>
'N'	'Sz'	[1, 1]	Sx, Sy
'N'	'parity'	[1, 2]	–
'N'	None	[1]	–
'parity'	'Sz'	[2, 1]	Sx, Sy
'parity'	'parity'	[2, 2]	–
'parity'	None	[2]	–
None	'Sz'	[1]	Sx, Sy
None	'parity'	[2]	–
None	None	[]	–

Todo: Check if Jordan-Wigner strings for 4x4 operators are correct.

Parameters

- **cons_N** ('N' | 'parity' | None) – Whether particle number is conserved, c.f. table above.
- **cons_Sz** ('Sz' | 'parity' | None) – Whether spin is conserved, c.f. table above.
- **filling** (*float*) – Average filling. Used to define dN.

cons_N

Whether particle number is conserved, c.f. table above.

Type 'N' | 'parity' | None

cons_Sz

Whether spin is conserved, c.f. table above.

Type 'Sz' | 'parity' | None

filling

Average filling. Used to define dN.

Type *float*

add_op (name, op, need_JW=False, hc=None)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (np.ndarray | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. LegCharges have to be [leg, leg.conj()]. We set labels 'p', 'p*'.
 If *Array* is a list of operators, the operators are added sequentially.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If *True*, add *name* to need_JW_string.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for hc_ops. By default (*None*), try to auto-determine it. If *False*, disable adding antries to hc_ops.

change_charge (*new_leg_charge=None, permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (*LegCharge | None*) – The new charges to be used. If *None*, use trivial charges.
- **permute** (*ndarray | None*) – The permutation applied to the physical leg, which gets used to adjust *state_labels* and *perm*. If you sorted the previous leg with *perm_qind*, *new_leg_charge = leg.sort()*, use *old_leg.perm_flat_from_perm_qind(perm_qind)*. Ignored if *None*.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Returns obj – Newly generated class instance containing the required data.

Return type *cls*

get_hc_op_name (*name*)

Return the hermitian conjugate of a given operator.

Parameters name (*str*) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as *get_op()* does.

Returns hc_op_name – Operator name for the hermi such that *get_op()* of

Return type *str*

get_op (*name*)

Return operator of given name.

Parameters name (*str*) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns op – The operator given by *name*, with labels *'p'*, *'p*'*. If name already was an *np.ndarray*, it's directly returned.

Return type *np.conservated*

multiply_op_names (*names*)

Multiply operator names together.

Join the operator names in *names* such that *get_op* returns the product of the corresponding operators.

Parameters names (*list of str*) – List of valid operator labels.

Returns combined_opname – A valid operator name Operatorname representing the product of operators in *names*.

Return type *str*

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters *name* (*str*) – The name of the operator, as in `get_op()`.

Returns `needs_JW` – Whether the operator needs a Jordan-Wigner string, judging from `need_JW_string`.

Return type `bool`

remove_op (*name*)

Remove an added operator.

Parameters *name* (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

state_index (*label*)

Return index of a basis state from its label.

Parameters *label* (*int* | *string*) – either the index directly or a label (string) set before.

Returns `state_index` – the index of the basis state associated with the label.

Return type `int`

state_indices (*labels*)

Same as `state_index()`, but for multiple labels.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

valid_opname (*name*)

Check whether 'name' labels a valid onsite-operator.

Parameters *name* (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

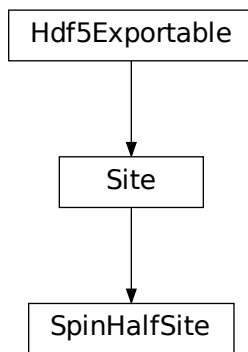
Returns `valid` – True if *name* is a valid argument to `get_op()`.

Return type `bool`

SpinHalfSite

- full name: `tenpy.networks.site.SpinHalfSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>SpinHalfSite.__init__([conserve])</code>	Initialize self.
<code>SpinHalfSite.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>SpinHalfSite.change_charge([new_leg_charge, ...])</code>	Change the charges of the site (in place).
<code>SpinHalfSite.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>SpinHalfSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>SpinHalfSite.get_op(name)</code>	Return operator of given name.
<code>SpinHalfSite.multiply_op_names(names)</code>	Multiply operator names together.
<code>SpinHalfSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>SpinHalfSite.remove_op(name)</code>	Remove an added operator.
<code>SpinHalfSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>SpinHalfSite.save_hdf5(hdf5_saver, subpath, h5gr)</code>	Export <i>self</i> into a HDF5 file.
<code>SpinHalfSite.state_index(label)</code>	Return index of a basis state from its label.
<code>SpinHalfSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.

continues on next page

Table 134 – continued from previous page

<code>SpinHalfSite.test_sanity()</code>	Sanity check, raises ValueErrors, if something is wrong.
<code>SpinHalfSite.valid_opname(name)</code>	Check whether 'name' labels a valid onsite-operator.

Class Attributes and Properties

<code>SpinHalfSite.dim</code>	Dimension of the local Hilbert space.
<code>SpinHalfSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.SpinHalfSite` (*conserve*='Sz')

Bases: `tenpy.networks.site.Site`

Spin-1/2 site.

Local states are up (0) and down (1). Local operators are the usual spin-1/2 operators, e.g. $S_z = \begin{bmatrix} 0.5 & 0. \\ 0. & -0.5 \end{bmatrix}$, $S_x = 0.5 \cdot \text{sigma}_x$ for the Pauli matrix *sigma_x*.

operator	description
Id, JW	Identity \mathbb{I}
Sx, Sy, Sz	Spin components $S^{x,y,z}$, equal to half the Pauli matrices.
Sigmax, Sigmay, Sigmaz	Pauli matrices $\sigma^{x,y,z}$
Sp, Sm	Spin flips $S^\pm = S^x \pm iS^y$

<i>conserve</i>	qmod	<i>excluded</i> onsite operators
'Sz'	[1]	Sx, Sy, Sigmax, Sigmay
'parity'	[2]	–
None	[]	–

Parameters *conserve* (*str*) – Defines what is conserved, see table above.

conserve

Defines what is conserved, see table above.

Type *str*

add_op (*name*, *op*, *need_JW*=False, *hc*=None)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (`np.ndarray` | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. LegCharges have to be `[leg, leg.conj()]`. We set labels 'p', 'p*'.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If True, add *name* to `need_JW_string`.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for `hc_ops`. By default (None), try to auto-determine it. If False, disable adding antries to `hc_ops`.

change_charge (*new_leg_charge=None, permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (*LegCharge | None*) – The new charges to be used. If *None*, use trivial charges.
- **permute** (*ndarray | None*) – The permutation applied to the physical leg, which gets used to adjust *state_labels* and *perm*. If you sorted the previous leg with *perm_qind*, *new_leg_charge = leg.sort()*, use *old_leg.perm_flat_from_perm_qind(perm_qind)*. Ignored if *None*.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Returns obj – Newly generated class instance containing the required data.

Return type *cls*

get_hc_op_name (*name*)

Return the hermitian conjugate of a given operator.

Parameters name (*str*) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as *get_op()* does.

Returns hc_op_name – Operator name for the hermi such that *get_op()* of

Return type *str*

get_op (*name*)

Return operator of given name.

Parameters name (*str*) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns op – The operator given by *name*, with labels *'p'*, *'p*'*. If name already was an *np.ndarray*, it's directly returned.

Return type *np.conservated*

multiply_op_names (*names*)

Multiply operator names together.

Join the operator names in *names* such that *get_op* returns the product of the corresponding operators.

Parameters names (*list of str*) – List of valid operator labels.

Returns combined_opname – A valid operator name Operatorname representing the product of operators in *names*.

Return type *str*

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters *name* (*str*) – The name of the operator, as in `get_op()`.

Returns `needs_JW` – Whether the operator needs a Jordan-Wigner string, judging from `need_JW_string`.

Return type `bool`

remove_op (*name*)

Remove an added operator.

Parameters *name* (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

state_index (*label*)

Return index of a basis state from its label.

Parameters *label* (*int* | *string*) – either the index directly or a label (string) set before.

Returns `state_index` – the index of the basis state associated with the label.

Return type `int`

state_indices (*labels*)

Same as `state_index()`, but for multiple labels.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

valid_opname (*name*)

Check whether 'name' labels a valid onsite-operator.

Parameters *name* (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

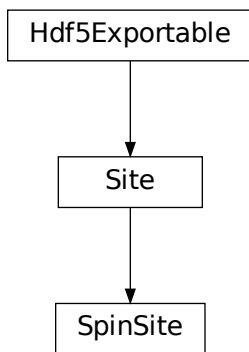
Returns `valid` – True if *name* is a valid argument to `get_op()`.

Return type `bool`

SpinSite

- full name: `tenpy.networks.site.SpinSite`
- parent module: `tenpy.networks.site`
- type: class

Inheritance Diagram



Methods

<code>SpinSite.__init__([S, conserve])</code>	Initialize self.
<code>SpinSite.add_op(name, op[, need_JW, hc])</code>	Add one on-site operators.
<code>SpinSite.change_charge([new_leg_charge, permute])</code>	Change the charges of the site (in place).
<code>SpinSite.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>SpinSite.get_hc_op_name(name)</code>	Return the hermitian conjugate of a given operator.
<code>SpinSite.get_op(name)</code>	Return operator of given name.
<code>SpinSite.multiply_op_names(names)</code>	Multiply operator names together.
<code>SpinSite.op_needs_JW(name)</code>	Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.
<code>SpinSite.remove_op(name)</code>	Remove an added operator.
<code>SpinSite.rename_op(old_name, new_name)</code>	Rename an added operator.
<code>SpinSite.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>SpinSite.state_index(label)</code>	Return index of a basis state from its label.
<code>SpinSite.state_indices(labels)</code>	Same as <code>state_index()</code> , but for multiple labels.
<code>SpinSite.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.
<code>SpinSite.valid_opname(name)</code>	Check whether 'name' labels a valid onsite-operator.

Class Attributes and Properties

<code>SpinSite.dim</code>	Dimension of the local Hilbert space.
<code>SpinSite.onsite_ops</code>	Dictionary of on-site operators for iteration.

class `tenpy.networks.site.SpinSite` ($S=0.5$, `conserve='Sz'`)

Bases: `tenpy.networks.site.Site`

General Spin S site.

There are $2S+1$ local states range from down (0) to up ($2S+1$), corresponding to $S_z = -S, -S+1, \dots, S-1, S$. Local operators are the spin-S operators, e.g. $S_z = [[0.5, 0.], [0., -0.5]]$, $S_x = 0.5 \times \text{sigma}_x$ for the Pauli matrix *sigma_x*.

operator	description
Id, JW	Identity \mathbb{I}
S_x, S_y, S_z	Spin components $S^{x,y,z}$, equal to half the Pauli matrices.
S_p, S_m	Spin flips $S^\pm = S^x \pm iS^y$

<i>conserve</i>	qmod	<i>excluded onsite operators</i>
'Sz'	[1]	S_x, S_y
'parity'	[2]	–
None	[]	–

Parameters `conserve` (*str*) – Defines what is conserved, see table above.

S

The $2S+1$ states range from $m = -S, -S+1, \dots +S$.

Type {0.5, 1, 1.5, 2, ..}

conserve

Defines what is conserved, see table above.

Type *str*

add_op (*name, op, need_JW=False, hc=None*)

Add one on-site operators.

Parameters

- **name** (*str*) – A valid python variable name, used to label the operator. The name under which *op* is added as attribute to self.
- **op** (`np.ndarray` | *Array*) – A matrix acting on the local hilbert space representing the local operator. Dense numpy arrays are automatically converted to *Array*. *LegCharges* have to be `[leg, leg.conj()]`. We set labels 'p', 'p*'.
 If *op* is a *LegCharge* object, it will be converted to a matrix and the labels will be set accordingly.
- **need_JW** (*bool*) – Whether the operator needs a Jordan-Wigner string. If *True*, add *name* to *need_JW_string*.
- **hc** (*None* | *False* | *str*) – The name for the hermitian conjugate operator, to be used for *hc_ops*. By default (*None*), try to auto-determine it. If *False*, disable adding antries to *hc_ops*.

change_charge (*new_leg_charge=None, permute=None*)

Change the charges of the site (in place).

Parameters

- **new_leg_charge** (`LegCharge` | `None`) – The new charges to be used. If `None`, use trivial charges.
- **permute** (`ndarray` | `None`) – The permutation applied to the physical leg, which gets used to adjust `state_labels` and `perm`. If you sorted the previous leg with `perm_qind`, `new_leg_charge = leg.sort()`, use `old_leg.perm_flat_from_perm_qind(perm_qind)`. Ignored if `None`.

property dim

Dimension of the local Hilbert space.

classmethod from_hdf5 (`hdf5_loader`, `h5gr`, `subpath`)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which is represent the object to be constructed.
- **subpath** (`str`) – The *name* of `h5gr` with a `' / '` in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

get_hc_op_name (`name`)

Return the hermitian conjugate of a given operator.

Parameters **name** (`str`) – The name of the operator to be returned. Multiple operators separated by whitespace are interpreted as an operator product, exactly as `get_op()` does.

Returns `hc_op_name` – Operator name for the hermi such that `get_op()` of

Return type `str`

get_op (`name`)

Return operator of given name.

Parameters **name** (`str`) – The name of the operator to be returned. In case of multiple operator names separated by whitespace, we multiply them together to a single on-site operator (with the one on the right acting first).

Returns `op` – The operator given by `name`, with labels `'p'`, `'p*'`. If name already was an `np.ndarray`, it's directly returned.

Return type `np.ndarray`

multiply_op_names (`names`)

Multiply operator names together.

Join the operator names in `names` such that `get_op` returns the product of the corresponding operators.

Parameters **names** (`list of str`) – List of valid operator labels.

Returns `combined_opname` – A valid operator name `Operatorname` representing the product of operators in `names`.

Return type `str`

property onsite_ops

Dictionary of on-site operators for iteration.

Single operators are accessible as attributes.

op_needs_JW (*name*)

Whether an (composite) onsite operator is fermionic and needs a Jordan-Wigner string.

Parameters *name* (*str*) – The name of the operator, as in `get_op()`.

Returns `needs_JW` – Whether the operator needs a Jordan-Wigner string, judging from `need_JW_string`.

Return type `bool`

remove_op (*name*)

Remove an added operator.

Parameters *name* (*str*) – The name of the operator to be removed.

rename_op (*old_name*, *new_name*)

Rename an added operator.

Parameters

- **old_name** (*str*) – The old name of the operator.
- **new_name** (*str*) – The new name of the operator.

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The name of *h5gr* with a '/' in the end.

state_index (*label*)

Return index of a basis state from its label.

Parameters *label* (*int* | *string*) – either the index directly or a label (string) set before.

Returns `state_index` – the index of the basis state associated with the label.

Return type `int`

state_indices (*labels*)

Same as `state_index()`, but for multiple labels.

test_sanity ()

Sanity check, raises `ValueErrors`, if something is wrong.

valid_opname (*name*)

Check whether 'name' labels a valid onsite-operator.

Parameters *name* (*str*) – Label for the operator. Can be multiple operator(labels) separated by whitespace, indicating that they should be multiplied together.

Returns `valid` – True if *name* is a valid argument to `get_op()`.

Return type `bool`

Functions

<code>group_sites(sites[, n, labels, charges])</code>	Given a list of sites, group each n sites together.
<code>multi_sites_combine_charges(sites[, ...])</code>	Adjust the charges of the given sites (in place) such that they can be used together.

group_sites

- full name: `tenpy.networks.site.group_sites`
- parent module: `tenpy.networks.site`
- type: function

`tenpy.networks.site.group_sites(sites, n=2, labels=None, charges='same')`

Given a list of sites, group each n sites together.

Parameters

- **sites** (list of `Site`) – The sites to be grouped together.
- **n** (`int`) – We group each n consecutive sites from `sites` together in a `GroupedSite`.
- **charges** (`labels,`) – See `GroupedSites`.

Returns `grouped_sites` – The grouped sites. Has length $(\text{len}(\text{sites}) - 1) // n + 1$.

Return type list of `GroupedSite`

multi_sites_combine_charges

- full name: `tenpy.networks.site.multi_sites_combine_charges`
- parent module: `tenpy.networks.site`
- type: function

`tenpy.networks.site.multi_sites_combine_charges(sites, same_charges=[])`

Adjust the charges of the given sites (in place) such that they can be used together.

When we want to contract tensors corresponding to different `Site` instances, these sites need to share a single `ChargeInfo`. This function adjusts the charges of these sites such that they can be used together.

Parameters

- **sites** (list of `Site`) – The sites to be combined. Modified **in place**.
- **same_charges** (`[[int, int|str), (int, int|str), ...], ...]`) – Defines which charges actually are the same, i.e. their quantum numbers are added up. Each charge is specified by a tuple $(s, i) = (int, int|str)$, where s gives the index of the site within `sites` and i the index or name of the charge in the `ChargeInfo` of this site.

Returns `perms` – For each site the permutation performed on the physical leg to sort by charges.

Return type list of ndarray

Examples

```

>>> ferm = SpinHalfFermionSite(cons_N='N', cons_Sz='Sz')
>>> spin = SpinSite(1.0, 'Sz')
>>> ferm.leg.chinfo is spin.leg.chinfo
False
>>> print(spin.leg)
+1
0 [[-1]
1 [ 1]]
2

>>> multi_sites_combine_charges([ferm, spin], same_charges=[[0, 'Sz'], (1, 0)])
[array([0, 1, 2, 3]), array([0, 1])]
>>> # no permutations where needed
>>> ferm.leg.chinfo is spin.leg.chinfo
True
>> ferm.leg.chinfo.names
['N', 'Sz']
>>> print(spin.leg)
+1
0 [[ 0 -1]
1 [ 0  1]]
2

```

Module description

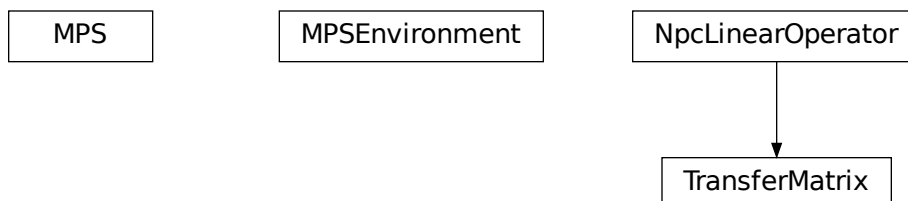
Defines a class describing the local physical Hilbert space.

The *Site* is the prototype, read it's docstring.

7.10.2 mps

- full name: `tenpy.networks.mps`
- parent module: `tenpy.networks`
- type: module

Classes



<code>MPS(sites, Bs, SVs[, bc, form, norm])</code>	A Matrix Product State, finite (MPS) or infinite (iMPS).
<code>MPSEnvironment(bra, ket[, init_LP, init_RP, ...])</code>	Stores partial contractions of $\langle bra Op ket \rangle$ for local operators Op .
<code>TransferMatrix(bra, ket[, shift_bra, ...])</code>	Transfer matrix of two MPS (bra & ket).

MPSEnvironment

- full name: `tenpy.networks.mps.MPSEnvironment`
- parent module: `tenpy.networks.mps`
- type: class

Inheritance Diagram

MPSEnvironment

Methods

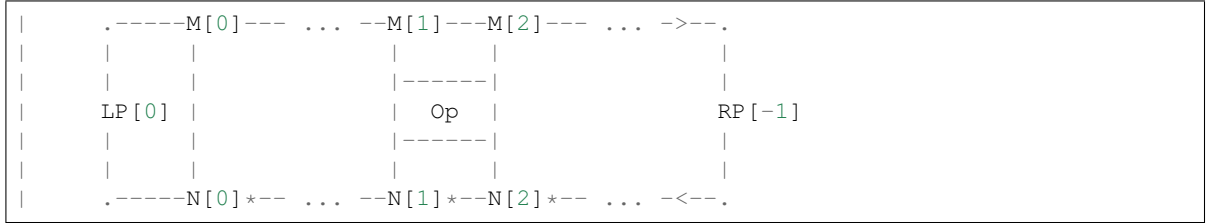
<code>MPSEnvironment.__init__(bra, ket[, init_LP, ...])</code>	Initialize self.
<code>MPSEnvironment.del_LP(i)</code>	Delete stored part strictly to the left of site i .
<code>MPSEnvironment.del_RP(i)</code>	Delete stored part strictly to the right of site i .
<code>MPSEnvironment.expectation_value(ops[, ...])</code>	Expectation value $\langle bra ops ket \rangle$ of (n-site) operator(s).
<code>MPSEnvironment.full_contraction(i0)</code>	Calculate the overlap by a full contraction of the network.
<code>MPSEnvironment.get_LP(i[, store])</code>	Calculate LP at given site from nearest available one (including i).
<code>MPSEnvironment.get_LP_age(i)</code>	Return number of physical sites in the contractions of <code>get_LP(i)</code> .
<code>MPSEnvironment.get_RP(i[, store])</code>	Calculate RP at given site from nearest available one (including i).
<code>MPSEnvironment.get_RP_age(i)</code>	Return number of physical sites in the contractions of <code>get_RP(i)</code> .
<code>MPSEnvironment.get_initialization_data()</code>	Return data for (re-)initialization.
<code>MPSEnvironment.init_LP(i)</code>	Build initial left part LP.
<code>MPSEnvironment.init_RP(i)</code>	Build initial right part RP for an MPS/MPOEnvironment.
<code>MPSEnvironment.set_LP(i, LP, age)</code>	Store part to the left of site i .
<code>MPSEnvironment.set_RP(i, RP, age)</code>	Store part to the right of site i .
<code>MPSEnvironment.test_sanity()</code>	Sanity check, raises ValueErrors, if something is wrong.


```
class tenpy.networks.mps.MPSEnvironment (bra, ket, init_LP=None, init_RP=None,
                                         age_LP=0, age_RP=0)
```

Bases: `object`

Stores partial contractions of $\langle bra|Op|ket \rangle$ for local operators Op .

The network for a contraction $\langle bra|Op|ket \rangle$ of a local operator Op , say exemplary at sites $i, i+1$ looks like:



Of course, we can also calculate the overlap $\langle braket \rangle$ by using the special case $Op = Id$.

We use the following label convention (where arrows indicate $qconj$):



To avoid recalculations of the whole network e.g. in the DMRG sweeps, we store the contractions up to some site index in this class. For `bc='finite', 'segment'`, the very left and right part `LP[0]` and `RP[-1]` are trivial and don't change, but for `bc='infinite'` they are might be updated (by inserting another unit cell to the left/right).

The MPS *bra* and *ket* have to be in canonical form. All the environments are constructed without the singular values on the open bond. In other words, we contract left-canonical *A* to the left parts *LP* and right-canonical *B* to the right parts *RP*. Thus, the special case `ket=bra` should yield identity matrices for *LP* and *RP*.

Parameters

- **bra** (MPS) – The MPS to project on. Should be given in usual ‘ket’ form; we call `conj()` on the matrices directly. Stored in place, without making copies. If necessary to match charges, we call `gauge_total_charge()`.
- **ket** (MPO | None) – The MPS on which the local operator acts. Stored in place, without making copies. If None, use *bra*.
- **init_LP** (None | `Array`) – Initial very left part *LP*. If None, build trivial one with `init_LP()`.
- **init_RP** (None | `Array`) – Initial very right part *RP*. If None, build trivial one with `init_RP()`.
- **age_LP** (`int`) – The number of physical sites involved into the contraction yielding *firstLP*.
- **age_RP** (`int`) – The number of physical sites involved into the contraction yielding *lastRP*.

L

Number of physical sites involved into the Environment, i.e. the least common multiple of `bra.L` and `ket.L`.

Type `int`

bra, ket

The two MPS for the contraction.

Type `MPS`

dtype

The data type.

Type `type`

_finite

Whether the boundary conditions of the MPS are finite.

Type `bool`

_LP

Left parts of the environment, len L . `LP[i]` contains the contraction strictly left of site i (or `None`, if we don't have it calculated).

Type list of `{None | Array}`

_RP

Right parts of the environment, len L . `RP[i]` contains the contraction strictly right of site i (or `None`, if we don't have it calculated).

Type list of `{None | Array}`

_LP_age

Used for book-keeping, how large the DMRG system grew: `_LP_age[i]` stores the number of physical sites involved into the contraction network which yields `self._LP[i]`.

Type list of `int | None`

_RP_age

Used for book-keeping, how large the DMRG system grew: `_RP_age[i]` stores the number of physical sites involved into the contraction network which yields `self._RP[i]`.

Type list of `int | None`

test_sanity()

Sanity check, raises `ValueErrors`, if something is wrong.

init_LP(i)

Build initial left part LP.

Parameters `i (int)` – Build LP left of site i .

Returns `init_LP` – Identity contractible with the νL leg of `ket.get_B(i)`, labels `'vR*'`, `'vR'`.

Return type `Array`

init_RP(i)

Build initial right part RP for an MPS/MPOEnvironment.

Parameters `i (int)` – Build RP right of site i .

Returns `init_RP` – Identity contractible with the νR leg of `ket.get_B(i)`, labels `'vL*'`, `'vL'`.

Return type `Array`

get_LP(i, store=True)

Calculate LP at given site from nearest available one (including i).

The returned `LP_i` corresponds to the following contraction, where the M 's and the N 's are in the 'A' form:

```

|      .-----M[0]--- ... --M[i-1]--->-   'vR'
|      |               |
|      LP[0]           |
|      |               |
|      .-----N[0]*-- ... --N[i-1]*--<-   'vR*'

```

Parameters

- **i** (*int*) – The returned *LP* will contain the contraction *strictly* left of site *i*.
- **store** (*bool*) – Wheter to store the calculated *LP* in *self* (*True*) or discard them (*False*).

Returns **LP_i** – Contraction of everything left of site *i*, with labels 'vR*', 'vR' for *bra*, *ket*.

Return type *Array*

get_RP (*i*, *store=True*)

Calculate RP at given site from nearest available one (including *i*).

The returned **RP_i** corresponds to the following contraction, where the M's and the N's are in the 'B' form:

```

|      'vL'  ->---M[i+1]-- ... --M[L-1]----.
|      |               |               |
|      |               |               RP[-1]
|      |               |
|      'vL*' -<---N[i+1]*- ... --N[L-1]*----.

```

Parameters

- **i** (*int*) – The returned *RP* will contain the contraction *strictly* right of site *i*.
- **store** (*bool*) – Wheter to store the calculated *RP* in *self* (*True*) or discard them (*False*).

Returns **RP_i** – Contraction of everything left of site *i*, with labels 'vL*', 'vL' for *bra*, *ket*.

Return type *Array*

get_LP_age (*i*)

Return number of physical sites in the contractions of **get_LP**(*i*).

Might be *None*.

get_RP_age (*i*)

Return number of physical sites in the contractions of **get_RP**(*i*).

Might be *None*.

set_LP (*i*, *LP*, *age*)

Store part to the left of site *i*.

set_RP (*i*, *RP*, *age*)

Store part to the right of site *i*.

del_LP (*i*)

Delete stored part strictly to the left of site *i*.

del_RP (*i*)

Delete storde part scrictly to the right of site *i*.

get_initialization_data()
Return data for (re-)initialization.

The returned parameters are collected in a dictionary with the following names.

Returns

- **init_LP, init_RP** (*Array*) – *LP* on the left of site 0 and *RP* on the right of site $L-1$, which can be used as *init_LP* and *init_RP* for the initialization of a new environment.
- **age_LP, age_RP** (*int*) – The number of physical sites involved into the contraction yielding *init_LP* and *init_RP*, respectively.

full_contraction (*i0*)

Calculate the overlap by a full contraction of the network.

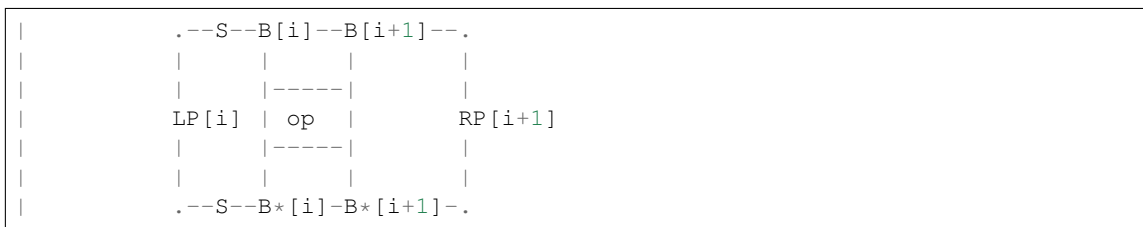
The full contraction of the environments gives the overlap $\langle \text{bra} | \text{ket} \rangle$, taking into account `MPS.norm` of both *bra* and *ket*. For this purpose, this function contracts `get_LP(i0+1, store=False)` and `get_RP(i0, store=False)` with appropriate singular values in between.

Parameters *i0* (*int*) – Site index.

expectation_value (*ops, sites=None, axes=None*)

Expectation value $\langle \text{bra} | \text{ops} | \text{ket} \rangle$ of (*n*-site) operator(s).

Calculates *n*-site expectation values of operators sandwiched between *bra* and *ket*. For examples the contraction for a two-site operator on site *i* would look like:



Here, the *B* are taken from *ket*, the *B** from *bra*. The call structure is the same as for `MPS.expectation_value()`.

Parameters

- **ops** ((list of) { *Array* | *str* }) – The operators, for which the expectation value should be taken. All operators should all have the same number of legs (namely $2n$). If less than `len(sites)` operators are given, we repeat them periodically. Strings (like 'Id', 'Sz') are translated into single-site operators defined by *sites*.
- **sites** (*list*) – List of site indices. Expectation values are evaluated there. If *None* (default), the entire chain is taken (clipping for finite b.c.)
- **axes** (*None* | (*list of str*, *list of str*)) – Two lists of each *n* leg labels giving the physical legs of the operator used for contraction. The first *n* legs are contracted with conjugated *B*, the second *n* legs with the non-conjugated *B*. *None* defaults to (['p'], ['p*']) for single site ($n=1$), or (['p0', 'p1', ..., 'p{n-1}'], ['p0*', 'p1*', ..., 'p{n-1}*']) for $n > 1$.

Returns **exp_vals** – Expectation values, `exp_vals[i] = $\langle \text{bra} | \text{ops}[i] | \text{ket} \rangle$` , where `ops[i]` acts on site(s) *j*, *j*+1, ..., *j*+{*n*-1} with *j*=*sites*[*i*].

Return type 1D ndarray

Examples

One site examples (n=1):

```
>>> env.expectation_value('Sz')
[Sz0, Sz1, ..., Sz{L-1}]
>>> env.expectation_value(['Sz', 'Sx'])
[Sz0, Sx1, Sz2, Sx3, ... ]
>>> env.expectation_value('Sz', sites=[0, 3, 4])
[Sz0, Sz3, Sz4]
```

Two site example (n=2), assuming homogeneous sites:

```
>>> SzSx = npc.outer(psi.sites[0].Sz.replace_labels(['p', 'p*'], ['p0', 'p0*
↳']),
                    psi.sites[1].Sx.replace_labels(['p', 'p*'], ['p1', 'p1*
↳']))
>>> env.expectation_value(SzSx)
[Sz0Sx1, Sz1Sx2, Sz2Sx3, ... ] # with len L-1 for finite bc, or L for_
↳infinite
```

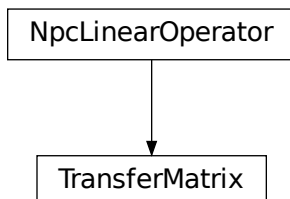
Example measuring $\langle \text{bra} | \text{SzSx} | \text{ket} \rangle$ on each second site, for inhomogeneous sites:

```
>>> SzSx_list = [npc.outer(psi.sites[i].Sz.replace_labels(['p', 'p*'], ['p0',
↳'p0*']),
                        psi.sites[i+1].Sx.replace_labels(['p', 'p*'], ['p1
↳', 'p1*']))
...
...         for i in range(0, psi.L-1, 2)]
>>> env.expectation_value(SzSx_list, range(0, psi.L-1, 2))
[Sz0Sx1, Sz2Sx3, Sz4Sx5, ...]
```

TransferMatrix

- full name: `tenpy.networks.mps.TransferMatrix`
- parent module: `tenpy.networks.mps`
- type: class

Inheritance Diagram



Methods

<code>TransferMatrix.__init__(bra, ket[, ...])</code>	Initialize self.
<code>TransferMatrix.adjoint()</code>	Return the hermitian conjugate of <i>self</i>
<code>TransferMatrix.eigenvectors([num_ev, ...])</code>	Find (dominant) eigenvector(s) of self using <code>scipy.sparse</code> .
<code>TransferMatrix.initial_guess([diag])</code>	Return a diagonal matrix as initial guess for the eigenvector.
<code>TransferMatrix.matvec(vec)</code>	Given <i>vec</i> as an <code>np.ndarray</code> , apply the transfer matrix.
<code>TransferMatrix.to_matrix()</code>	Contract <i>self</i> to a matrix.

Class Attributes and Properties

<code>TransferMatrix.acts_on</code>

class `tenpy.networks.mps.TransferMatrix`(*bra*, *ket*, *shift_bra*=0, *shift_ket*=None, *transpose*=False, *charge_sector*=0, *form*='B')

Bases: `tenpy.linalg.sparse.NpcLinearOperator`

Transfer matrix of two MPS (bra & ket).

For an iMPS in the thermodynamic limit, we often need to find the ‘dominant *RP*’ (and *LP*). This mean nothing else than to take the transfer matrix of the unit cell and find the (right/left) eigenvector with the largest (magnitude) eigenvalue, since it will dominate $(TM)^n RP$ (or $LP(TM)^n$) in the limit $n \rightarrow \infty$ - whatever the initial *RP* is. This class provides exactly that functionality with `eigenvectors()`.

Given two MPS, we define the transfer matrix as:

```
|
|  ---M[i]---M[i+1]- ... --M[i+L]---
|      |           |           |
|  ---N[j]*---N[j+1]* ... --N[j+L]*---
```

Here the *M* denotes the matrices of the bra and *N* the ones of the ket, respectively. To view it as a *matrix*, we combine the left and right indices to pipes:

```
| (vL.vL*) ->-TM->- (vR.vR*) acting on (vL.vL*) ->-RP
```

Note that we keep all *M* and *N* as copies.

Deprecated since version 0.6.0: The default for *shift_ket* was the value of *shift_bra*, this will be changed to 0.

Parameters

- **bra** (*MPS*) – The MPS which is to be (complex) conjugated.
- **ket** (*MPS*) – The MPS which is not (complex) conjugated.
- **shift_bra** (*int*) – We start the *N* of the bra at site *shift_bra* (i.e. the *j* in the above network).
- **shift_ket** (*int* | *None*) – We start the *M* of the ket at site *shift_ket* (i.e. the *i* in the above network). *None* is deprecated, default will be changed to 0 in the future.
- **transpose** (*bool*) – Whether *self.matvec* acts on *RP* (False) or *LP* (True).

- **charge_sector** (None | charges | 0) – Selects the charge sector of the vector onto which the Linear operator acts. None stands for *all* sectors, 0 stands for the zero-charge sector. Defaults to 0, i.e., **assumes** the dominant eigenvector is in charge sector 0.
- **form** ('B' | 'A' | 'C' | 'G' | 'Th' | None | tuple(float, float)) – In which canonical form we take the M and N matrices.

L

Number of physical sites involved in the transfer matrix, i.e. the least common multiple of $bra.L$ and $ket.L$.

Type int

shift_bra

We start the N of the bra at site $shift_bra$.

Type int

shift_ket

We start the M of the ket at site $shift_ket$. None defaults to $shift_bra$.

Type int | None

transpose

Whether $self.matvec$ acts on RP (True) or LP (False).

Type bool

qtotal

Total charge of the transfer matrix (which is gauged away in $matvec$).

Type charges

form

In which canonical form (all of) the M and N matrices are.

Type tuple(float, float) | None

flat_linop

Class lifting $matvec()$ to ndarrays in order to use $speigs()$.

Type *FlatLinearOperator*

pipe

Pipe corresponding to $'(vL.vL*)'$ for $transpose=False$ or to $'(vR.vR*)'$ for $transpose=True$.

Type *LegPipe*

label_split

$['vL', 'vL*']$ if $transpose=False$ or $['vR', 'vR*']$ if $transpose=True$.

_bra_N

Complex conjugated matrices of the bra, transposed for fast $matvec$.

Type list of $np.array$

_ket_M

The matrices of the ket, transposed for fast $matvec$.

Type list of $np.array$

matvec (vec)

Given vec as an $np.array$, apply the transfer matrix.

Parameters `vec` (*Array*) – Vector to act on with the transfermatrix. If not *transposed*, `vec` is the right part *RP* of an environment, with legs ' (vL.vL*) ' in a pipe or splitted. If *transposed*, the left part *LP* of an environment with legs ' (vR*.vR) '.

Returns `mat_vec` – The transfer matrix acted on `vec`, in the same form as given.

Return type *Array*

initial_guess (*diag=1.0*)

Return a diagonal matrix as initial guess for the eigenvector.

Parameters `diag` (*float | 1D ndarray*) – Should be 1. for the identity or some singular values squared.

Returns `mat` – A 2D array with `diag` on the diagonal such that `matvec()` can act on it.

Return type *Array*

eigenvectors (*num_ev=1, max_num_ev=None, max_tol=1e-12, which='LM', v0=None, **kwargs*)

Find (dominant) eigenvector(s) of self using `scipy.sparse`.

If no charge_sector was selected, we look in *all* charge sectors.

Parameters

- **num_ev** (*int*) – Number of eigenvalues/vectors to look for.
- **max_num_ev** (*int*) – `scipy.sparse.linalg.speigs()` sometimes raises a `NoConvergenceError` for small `num_ev`, which might be avoided by increasing `num_ev`. As a work-around, we try it again in the case of an error, just with larger `num_ev` up to `max_num_ev`. None defaults to `num_ev + 2`.
- **max_tol** (*float*) – After the first `NoConvergenceError` we increase the `tol` argument to that value.
- **which** (*str*) – Which eigenvalues to look for, see `scipy.sparse.linalg.speigs`.
- ****kwargs** – Further keyword arguments given to `speigs()`.

Returns

- **eta** (*1D ndarray*) – The eigenvalues, sorted according to *which*.
- **w** (list of *Array*) – The eigenvectors corresponding to *eta*, as `np.array` with `LegPipe`.

adjoint ()

Return the hermitian conjugate of *self*

If *self* is hermitian, subclasses *can* choose to implement this to define the adjoint operator of *self*.

to_matrix ()

Contract *self* to a matrix.

If *self* represents an operator with very small shape, e.g. because the MPS bond dimension is very small, an algorithm might choose to contract *self* to a single tensor.

Returns `matrix` – Contraction of the represented operator.

Return type *Array*

Functions

<code>build_initial_state(size, states, filling[, ...])</code>	Build an “initial state” list.
--	--------------------------------

build_initial_state

- full name: `tenpy.networks.mps.build_initial_state`
- parent module: `tenpy.networks.mps`
- type: function

`tenpy.networks.mps.build_initial_state` (*size, states, filling, mode='random', seed=None*)

Build an “initial state” list.

Uses two iterables (‘states’ and ‘filling’) to determine how to fill the state. The two lists should have the same length as every element in ‘filling’ gives the filling fraction for the corresponding state in ‘states’.

Example

`size = 6, states = [0, 1, 2], filling = [1./3, 2./3, 0.]` `n_states = size * filling = [2, 4, 0]` ==> Two sites will get state 0, 4 sites will get state 1, 0 sites will get state 2.

Todo: Make more general: it should be possible to specify states as strings.

Parameters

- **size** (*int*) – length of state
- **states** (*iterable*) – Containing the possible local states
- **filling** (*iterable*) – Fraction of the total number of sites to get a certain state. If infinite fractions (e.g. 1/3) are needed, one should supply a fraction (1./3.)
- **mode** (*str* | *None*) – State filling pattern. Only ‘random’ is implemented
- **seed** (*int* | *None*) – Seed for random number generators

Returns `initial_state` (*list*)

Return type the initial state

Raises

- **ValueError** – If fractional fillings are incommensurate with system size.
- **AssertionError** – If the total filling is not equal to 1, or the length of *filling* does not equal the length of *states*.

Module description

This module contains a base class for a Matrix Product State (MPS).

An MPS looks roughly like this:

```
|  -- B[0] -- B[1] -- B[2] -- ...
|      |      |      |
|      |      |      |
```

We use the following label convention for the B (where arrows indicate $qconj$):

```
|  vL ->- B ->- vR
|          |
|          ^
|          p
```

We store one 3-leg tensor $_B[i]$ with labels 'vL', 'vR', 'p' for each of the L sites $0 \leq i < L$. Additionally, we store $L+1$ singular value arrays $_S[ib]$ on each bond $0 \leq ib \leq L$, independent of the boundary conditions. $_S[ib]$ gives the singular values on the bond $i-1, i$. However, be aware that e.g. `chi` returns only the dimensions of the `nontrivial_bonds` depending on the boundary conditions.

The matrices and singular values always represent a normalized state (i.e. `np.linalg.norm(psi._S[ib]) == 1` up to roundoff errors), but (for finite MPS) we keep track of the norm in `norm` (which is respected by `overlap()`, ...).

Valid MPS boundary conditions (not to confuse with `bc_coupling` of `tenpy.models.model.CouplingModel`) are the following:

<i>bc</i>	description
'finite'	Finite MPS, $G_0 \ s_1 \ G_1 \ \dots \ s_{\{L-1\}} \ G_{\{L-1\}}$. This is achieved by using a trivial left and right bond $s[0] = s[-1] = \text{np.array}([1.])$.
'segment'	Generalization of 'finite', describes an MPS embedded in left and right environments. The left environment is described by <code>chi[0]</code> orthonormal states which are weighted by the singular values $s[0]$. Similar, $s[L]$ weight some right orthonormal states. You can think of the left and right states to be generated by additional MPS, such that the overall structure is something like $\dots s_L s_L [s_0 G_0 s_1 G_1 \dots s_{\{L-1\}} G_{\{L-1\}} s_{\{L\}}] R s R s R \dots$ (where we save the part in the brackets $[\dots]$).
'infinite'	infinite MPS (iMPS): we save a 'MPS unit cell' $[s_0 G_0 s_1 G_1 \dots s_{\{L-1\}} G_{\{L-1\}}]$ which is repeated periodically, identifying all indices modulo <code>self.L</code> . In particular, the last bond L is identified with 0. (The MPS unit cell can differ from a lattice unit cell). bond is identified with the first one.

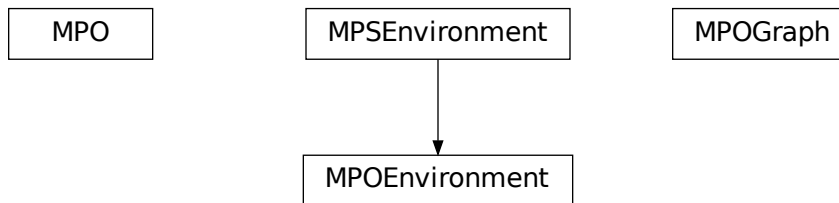
An MPS can be in different 'canonical forms' (see [Vidal2004], [Schollwoeck2011]). To take care of the different canonical forms, algorithms should use functions like `get_theta()`, `get_B()` and `set_B()` instead of accessing them directly, as they return the B in the desired form (which can be chosen as an argument). The values of the tuples for the form correspond to the exponent of the singular values on the left and right. To keep track of a "mixed" canonical form $A \ A \ A \ s \ B \ B$, we save the tuples for each site of the MPS in `MPS.form`.

<i>form</i>	<i>tuple</i>	<i>description</i>
'B'	(0, 1)	right canonical: $_B[i] = \text{-- Gamma}[i] \text{-- s}[i+1]$ -- The default form, which algorithms assume.
'C'	(0.5, 0.5)	symmetric form: $_B[i] = \text{-- s}[i]*0.5 \text{-- Gamma}[i] \text{-- s}[i+1]*0.5$ --
'A'	(1, 0)	left canonical: $_B[i] = \text{-- s}[i] \text{-- Gamma}[i] \text{--}$.
'G'	(0, 0)	Save only $_B[i] = \text{-- Gamma}[i] \text{--}$.
'Th'	(1, 1)	Form of a local wave function <i>theta</i> with singular value on both sides. <code>psi.get_B(i, 'Th')</code> is equivalent to <code>psi.get_theta(i, n=1)</code> .
None	None	General non-canonical form. Valid form for initialization, but you need to call <code>canonical_form()</code> (or similar) before using algorithms.

7.10.3 mpo

- full name: `tenpy.networks.mpo`
- parent module: `tenpy.networks`
- type: module

Classes

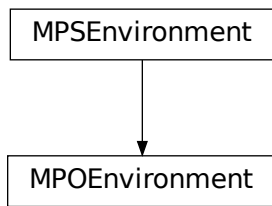


<code>MPO(sites, Ws[, bc, IdL, IdR, max_range, ...])</code>	Matrix product operator, finite (MPO) or infinite (iMPO).
<code>MPOEnvironment(bra, H, ket[, init_LP, ...])</code>	Stores partial contractions of $\langle bra H ket \rangle$ for an MPO H .
<code>MPOGraph(sites[, bc, max_range])</code>	Representation of an MPO by a graph, based on a 'finite state machine'.

MPOEnvironment

- full name: `tenpy.networks.mpo.MPOEnvironment`
- parent module: `tenpy.networks.mpo`
- type: class

Inheritance Diagram



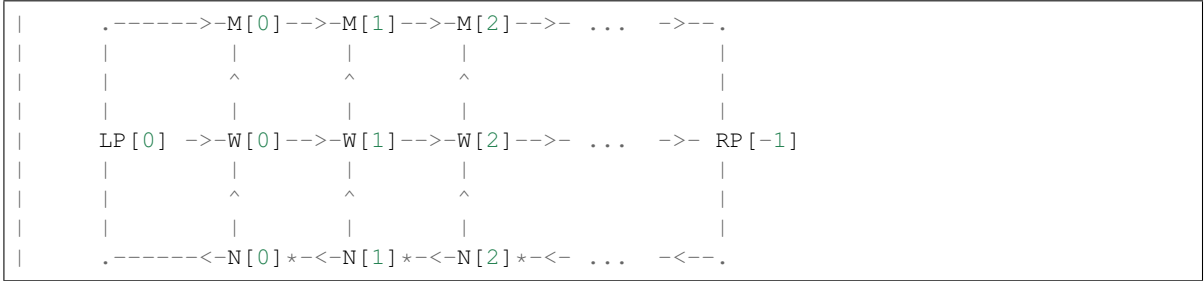
Methods

<code>MPOEnvironment.__init__(bra, H, ket[, ...])</code>	Initialize self.
<code>MPOEnvironment.del_LP(i)</code>	Delete stored part strictly to the left of site i .
<code>MPOEnvironment.del_RP(i)</code>	Delete stored part strictly to the right of site i .
<code>MPOEnvironment.expectation_value(ops[, ...])</code>	Expectation value $\langle \text{bra} \text{ops} \text{ket} \rangle$ of (n-site) operator(s).
<code>MPOEnvironment.full_contraction(i0)</code>	Calculate the energy by a full contraction of the network.
<code>MPOEnvironment.get_LP(i[, store])</code>	Calculate LP at given site from nearest available one (including i).
<code>MPOEnvironment.get_LP_age(i)</code>	Return number of physical sites in the contractions of <code>get_LP(i)</code> .
<code>MPOEnvironment.get_RP(i[, store])</code>	Calculate RP at given site from nearest available one (including i).
<code>MPOEnvironment.get_RP_age(i)</code>	Return number of physical sites in the contractions of <code>get_RP(i)</code> .
<code>MPOEnvironment.get_initialization_data()</code>	Return data for (re-)initialization.
<code>MPOEnvironment.init_LP(i)</code>	Build initial left part LP.
<code>MPOEnvironment.init_RP(i)</code>	Build initial right part RP for an MPS/MPOEnvironment.
<code>MPOEnvironment.set_LP(i, LP, age)</code>	Store part to the left of site i .
<code>MPOEnvironment.set_RP(i, RP, age)</code>	Store part to the right of site i .
<code>MPOEnvironment.test_sanity()</code>	Sanity check, raises <code>ValueErrors</code> , if something is wrong.

```
class tenpy.networks.mpo.MPOEnvironment (bra, H, ket, init_LP=None, init_RP=None,
                                         age_LP=0, age_RP=0)
    Bases: tenpy.networks.mps.MPSEnvironment
```

Stores partial contractions of $\langle bra|H|ket \rangle$ for an MPO H .

The network for a contraction $\langle bra|H|ket \rangle$ of an MPO H between two MPS looks like:



We use the following label convention (where arrows indicate $qconj$):



To avoid recalculations of the whole network e.g. in the DMRG sweeps, we store the contractions up to some site index in this class. For `bc='finite'`, `'segment'`, the very left and right part `LP[0]` and `RP[-1]` are trivial and don't change in the DMRG algorithm, but for `iDMRG` (`bc='infinite'`) they are also updated (by inserting another unit cell to the left/right).

The MPS *bra* and *ket* have to be in canonical form. All the environments are constructed without the singular values on the open bond. In other words, we contract left-canonical *A* to the left parts *LP* and right-canonical *B* to the right parts *RP*.

Parameters

- **bra** (MPS) – The MPS to project on. Should be given in usual ‘ket’ form; we call `conj()` on the matrices directly.
- **H** (MPO) – The MPO sandwiched between *bra* and *ket*. Should have ‘`IdL`’ and ‘`IdR`’ set on the first and last bond.
- **ket** (MPS) – The MPS on which *H* acts. May be identical with *bra*.
- **init_LP** (None | `Array`) – Initial very left part LP. If None, build trivial one with `:meth`init_LP``.
- **init_RP** (None | `Array`) – Initial very right part RP. If None, build trivial one with `init_RP()`.
- **age_LP** (`int`) – The number of physical sites involved into the contraction yielding *firstLP*.
- **age_RP** (`int`) – The number of physical sites involved into the contraction yielding *lastRP*.

H

The MPO sandwiched between *bra* and *ket*.

Type MPO

`test_sanity()`

Sanity check, raises `ValueErrors`, if something is wrong.

`init_LP(i)`

Build initial left part LP.

Parameters `i` (*int*) – Build `LP` left of site `i`.

Returns `init_LP` – Identity contractible with the `vL` leg of `.ket.get_B(i)`, multiplied with a unit vector nonzero in `H.IdL[i]`, with labels `'vR*'`, `'wR'`, `'vR'`.

Return type *Array*

init_RP (`i`)

Build initial right part `RP` for an MPS/MPOEnvironment.

Parameters `i` (*int*) – Build `RP` right of site `i`.

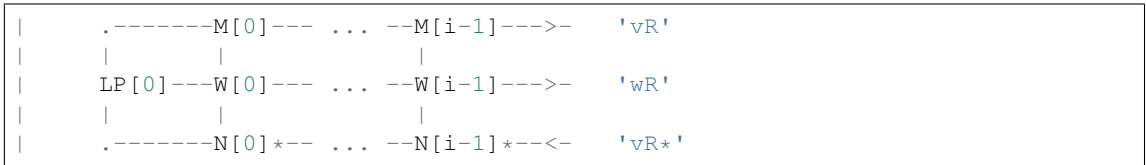
Returns `init_RP` – Identity contractible with the `vR` leg of `self.get_B(i)`, multiplied with a unit vector nonzero in `H.IdR[i]`, with labels `'vL*'`, `'wL'`, `'vL'`.

Return type *Array*

get_LP (`i`, `store=True`)

Calculate `LP` at given site from nearest available one (including `i`).

The returned `LP_i` corresponds to the following contraction, where the `M`'s and the `N`'s are in the 'A' form:



Parameters

- `i` (*int*) – The returned `LP` will contain the contraction *strictly* left of site `i`.
- `store` (*bool*) – Wheter to store the calculated `LP` in `self` (`True`) or discard them (`False`).

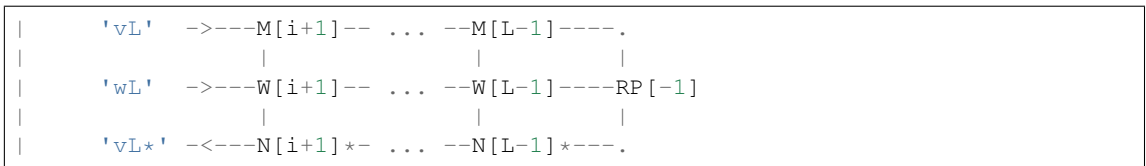
Returns `LP_i` – Contraction of everything left of site `i`, with labels `'vR*'`, `'wR'`, `'vR'` for `bra`, `H`, `ket`.

Return type *Array*

get_RP (`i`, `store=True`)

Calculate `RP` at given site from nearest available one (including `i`).

The returned `RP_i` corresponds to the following contraction, where the `M`'s and the `N`'s are in the 'B' form:



Parameters

- `i` (*int*) – The returned `RP` will contain the contraction *strictly* right of site `i`.
- `store` (*bool*) – Wheter to store the calculated `RP` in `self` (`True`) or discard them (`False`).

Returns `RP_i` – Contraction of everything right of site `i`, with labels `'vL*'`, `'wL'`, `'vL'` for `bra`, `H`, `ket`.

Return type `Array`

full_contraction (*i0*)

Calculate the energy by a full contraction of the network.

The full contraction of the environments gives the value $\langle \text{bra} | H | \text{ket} \rangle / (\text{norm}(|\text{bra}\rangle) * \text{norm}(|\text{ket}\rangle))$, i.e. if *bra* is *ket* and normalized, the total energy. For this purpose, this function contracts `get_LP(i0+1, store=False)` and `get_RP(i0, store=False)`.

Parameters *i0* (*int*) – Site index.

del_LP (*i*)

Delete stored part strictly to the left of site *i*.

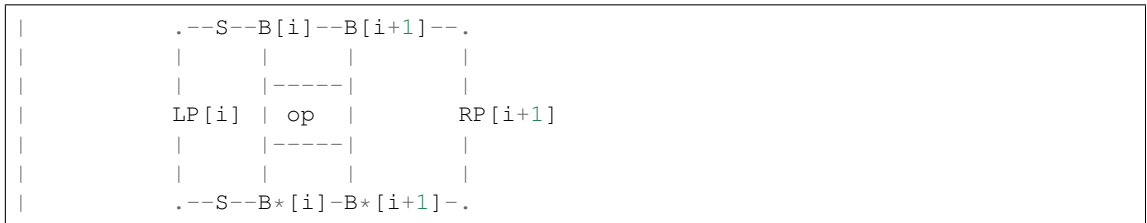
del_RP (*i*)

Delete stored part strictly to the right of site *i*.

expectation_value (*ops*, *sites=None*, *axes=None*)

Expectation value $\langle \text{bra} | \text{ops} | \text{ket} \rangle$ of (n-site) operator(s).

Calculates n-site expectation values of operators sandwiched between bra and ket. For examples the contraction for a two-site operator on site *i* would look like:



Here, the *B* are taken from *ket*, the *B** from *bra*. The call structure is the same as for `MPS.expectation_value()`.

Parameters

- **ops** ((list of) { `Array` | `str` }) – The operators, for which the expectation value should be taken. All operators should all have the same number of legs (namely $2n$). If less than `len(sites)` operators are given, we repeat them periodically. Strings (like 'Id', 'Sz') are translated into single-site operators defined by *sites*.
- **sites** (*list*) – List of site indices. Expectation values are evaluated there. If `None` (default), the entire chain is taken (clipping for finite b.c.)
- **axes** (`None` | (*list of str*, *list of str*)) – Two lists of each *n* leg labels giving the physical legs of the operator used for contraction. The first *n* legs are contracted with conjugated *B*, the second *n* legs with the non-conjugated *B*. `None` defaults to (`['p']`, `['p*']`) for single site ($n=1$), or (`['p0', 'p1', ..., 'p{n-1}']`, `['p0*', 'p1*', ..., 'p{n-1}*']`) for $n > 1$.

Returns **exp_vals** – Expectation values, `exp_vals[i] = $\langle \text{bra} | \text{ops}[i] | \text{ket} \rangle$` , where `ops[i]` acts on site(s) *j*, *j*+1, ..., *j*+{*n*-1} with *j*=*sites*[*i*].

Return type 1D ndarray

Examples

One site examples ($n=1$):

```
>>> env.expectation_value('Sz')
[Sz0, Sz1, ..., Sz{L-1}]
>>> env.expectation_value(['Sz', 'Sx'])
[Sz0, Sx1, Sz2, Sx3, ... ]
>>> env.expectation_value('Sz', sites=[0, 3, 4])
[Sz0, Sz3, Sz4]
```

Two site example (n=2), assuming homogeneous sites:

```
>>> SzSx = npc.outer(psi.sites[0].Sz.replace_labels(['p', 'p*'], ['p0', 'p0*
↳']),
                    psi.sites[1].Sx.replace_labels(['p', 'p*'], ['p1', 'p1*
↳']))
>>> env.expectation_value(SzSx)
[Sz0Sx1, Sz1Sx2, Sz2Sx3, ... ] # with len L-1 for finite bc, or L for_
↳infinite
```

Example measuring $\langle \text{bra} | \text{SzSx} | \text{ket} \rangle$ on each second site, for inhomogeneous sites:

```
>>> SzSx_list = [npc.outer(psi.sites[i].Sz.replace_labels(['p', 'p*'], ['p0',
↳ 'p0*']),
                        psi.sites[i+1].Sx.replace_labels(['p', 'p*'], ['p1
↳ ', 'p1*']))
...
for i in range(0, psi.L-1, 2)]
>>> env.expectation_value(SzSx_list, range(0, psi.L-1, 2))
[Sz0Sx1, Sz2Sx3, Sz4Sx5, ...]
```

get_LP_age(i)

Return number of physical sites in the contractions of get_LP(i).

Might be None.

get_RP_age(i)

Return number of physical sites in the contractions of get_RP(i).

Might be None.

get_initialization_data()

Return data for (re-)initialization.

The returned parameters are collected in a dictionary with the following names.

Returns

- **init_LP, init_RP** (*Array*) – *LP* on the left of site 0 and *RP* on the right of site $L-1$, which can be used as *init_LP* and *init_RP* for the initialization of a new environment.
- **age_LP, age_RP** (*int*) – The number of physical sites involved into the contraction yielding *init_LP* and *init_RP*, respectively.

set_LP(i, LP, age)

Store part to the left of site *i*.

set_RP(i, RP, age)

Store part to the right of site *i*.

MPOGraph

- full name: `tenpy.networks.mpo.MPOGraph`
- parent module: `tenpy.networks.mpo`
- type: class

Inheritance Diagram

MPOGraph

Methods

<code>MPOGraph.__init__(sites[, bc, max_range])</code>	Initialize self.
<code>MPOGraph.add(i, keyL, keyR, opname, strength)</code>	Insert an edge into the graph.
<code>MPOGraph.add_missing_IdL_IdR([insert_all_id])</code>	Add missing identity ('Id') edges connecting 'IdL'-'>'IdL' and ``'IdR'-'>'IdR'.
<code>MPOGraph.add_string(i, j, key[, opname, ...])</code>	Insert a bunch of edges for an 'operator string' into the graph.
<code>MPOGraph.build_MPO([Ws_qtotal])</code>	Build the MPO represented by the graph (<i>self</i>).
<code>MPOGraph.from_term_list(term_list, sites, bc)</code>	Initialize from a list of operator terms and prefactors.
<code>MPOGraph.from_terms(onsite_terms, ...[, ...])</code>	Initialize an <i>MPOGraph</i> from OnsiteTerms and CouplingTerms.
<code>MPOGraph.has_edge(i, keyL, keyR)</code>	True if there is an edge from <i>keyL</i> on bond (i-1, i) to <i>keyR</i> on bond (i, i+1).
<code>MPOGraph.test_sanity()</code>	Sanity check, raises ValueErrors, if something is wrong.

Class Attributes and Properties

<code>MPOGraph.L</code>	Number of physical sites; for infinite boundaries the length of the unit cell.
-------------------------	--

class `tenpy.networks.mpo.MPOGraph` (*sites*, *bc*='finite', *max_range*=None)

Bases: `object`

Representation of an MPO by a graph, based on a 'finite state machine'.

This representation is used for building `H_MPO` from the interactions. The idea is to view the MPO as a kind of 'finite state machine'. The **states** or **keys** of this finite state machine live on the MPO bonds *between* the *Ws*. They label the indices of the virtul bonds of the MPOs, i.e., the indices on legs *wL* and *wR*. They can be anything hash-able like a `str`, `int` or a tuple of them.

The **edges** of the graph are the entries `W[keyL, keyR]`, which itself are onsite operators on the local Hilbert

space. The indices *keyL* and *keyR* correspond to the legs 'wL', 'wR' of the MPO. The entry `W[keyL, keyR]` connects the state *keyL* on bond $(i-1, i)$ with the state *keyR* on bond $(i, i+1)$.

The keys 'IdL' (for 'identity left') and 'IdR' (for 'identity right') are reserved to represent only 'Id' (=identity) operators to the left and right of the bond, respectively.

Todo: might be useful to add a “cleanup” function which removes operators cancelling each other and/or unused states. Or better use a ‘compress’ of the MPO?

Parameters

- **sites** (list of `Site`) – Local sites of the Hilbert space.
- **bc** (`{'finite', 'infinite'}`) – MPO boundary conditions.
- **max_range** (`int | np.inf | None`) – Maximum range of hopping/interactions (in unit of sites) of the MPO. `None` for unknown.

sites

Defines the local Hilbert space for each site.

Type list of `Site`

chinfo

The nature of the charge.

Type `ChargeInfo`

bc

MPO boundary conditions.

Type `{'finite', 'infinite'}`

max_range

Maximum range of hopping/interactions (in unit of sites) of the MPO. `None` for unknown.

Type `int | np.inf | None`

states

`states[i]` gives the possible keys at the virtual bond $(i-1, i)$ of the MPO. $L+1$ entries.

Type list of set of keys

graph

For each site *i* a dictionary `{keyL: {keyR: [(opname, strength)]}}` with *keyL* in `states[i]` and *keyR* in `states[i+1]`.

Type list of dict of dict of list of tuples

_grid_legs

The charges for the MPO

Type `None | list of LegCharge`

classmethod from_terms (*onsite_terms*, *coupling_terms*, *sites*, *bc*, *insert_all_id=True*)

Initialize an *MPOGraph* from *OnsiteTerms* and *CouplingTerms*.

Parameters

- **onsite_terms** (*OnsiteTerms*) – Onsite terms to be added to the new *MPOGraph*.
- **coupling_terms** (*CouplingTerms | MultiCouplingTerms*) – Coupling terms to be added to the new *MPOGraph*.

- **sites** (list of *Site*) – Local sites of the Hilbert space.
- **bc** ('finite' | 'infinite') – MPO boundary conditions.
- **insert_all_id**(*bool*) – Whether to insert identities such that *IdL* and *IdR* are defined on each bond. See `add_missing_IdL_IdR()`.

Returns **graph** – Initialized with the given terms.

Return type *MPOGraph*

See also:

`from_term_list()` equivalent for other representation terms.

classmethod **from_term_list** (*term_list*, *sites*, *bc*, *insert_all_id=True*)

Initialize form a list of operator terms and prefactors.

Parameters

- **term_list** (*TermList*) – Terms to be added to the *MPOGraph*.
- **sites** (list of *Site*) – Local sites of the Hilbert space.
- **bc** ('finite' | 'infinite') – MPO boundary conditions.
- **insert_all_id**(*bool*) – Whether to insert identities such that *IdL* and *IdR* are defined on each bond. See `add_missing_IdL_IdR()`.

Returns **graph** – Initialized with the given terms.

Return type *MPOGraph*

See also:

`from_terms()` equivalent for other representation of terms.

test_sanity ()

Sanity check, raises *ValueErrors*, if something is wrong.

property **L**

Number of physical sites; for infinite boundaries the length of the unit cell.

add (*i*, *keyL*, *keyR*, *opname*, *strength*, *check_op=True*, *skip_existing=False*)

Insert an edge into the graph.

Parameters

- **i** (*int*) – Site index at which the edge of the graph is to be inserted.
- **keyL** (*hashable*) – The state at bond (i-1, i) to connect from.
- **keyR** (*hashable*) – The state at bond (i, i+1) to connect to.
- **opname** (*str*) – Name of the operator.
- **strength** (*str*) – Prefactor of the operator to be inserted.
- **check_op** (*bool*) – Whether to check that ‘opname’ exists on the given *site*.
- **skip_existing** (*bool*) – If *True*, skip adding the graph node if it exists (with same keys and *opname*).

add_string (*i, j, key, opname='Id', check_op=True, skip_existing=True*)

Insert a bunch of edges for an ‘operator string’ into the graph.

Terms like $S_i^z S_j^z$ actually stand for $S_i^z \otimes \prod_{i < k < j} \mathbb{I}_k \otimes S_j^z$. This function adds the \mathbb{I} terms to the graph.

Parameters

- **j** (*i, j*) – An edge is inserted on all bonds between *i* and *j*, $i < j$. *j* can be larger than *L*, in which case the operators are supposed to act on different MPS unit cells.
- **key** (*hashable*) – The state at bond (i-1, i) to connect from and on bond (j-1, j) to connect to. Also used for the intermediate states. No operator is inserted on a site $i < k < j$ if `has_edge(k, key, key)`.
- **opname** (*str*) – Name of the operator to be used for the string. Useful for the Jordan-Wigner transformation to fermions.
- **skip_existing** (*bool*) – Whether existing graph nodes should be skipped.

Returns `label_j` – The *key* on the left of site *j* to connect to. Usually the same as the parameter *key*, except if $j - i > \text{self.L}$, in which case we use the additional labels `(key, 1)`, `(key, 2)`, ... to generate couplings over multiple unit cells.

Return type `hashable`

add_missing_IdL_IdR (*insert_all_id=True*)

Add missing identity (‘Id’) edges connecting ‘IdL’->‘IdL’ and ‘IdR’->‘IdR’.

This function should be called *after* all other operators have been inserted.

Parameters `insert_all_id` (*bool*) – If `True`, insert ‘Id’ edges on *all* bonds. If `False` and boundary conditions are finite, only insert ‘IdL’->‘IdL’ to the left of the rightmost existing ‘IdL’ and ‘IdR’->‘IdR’ to the right of the leftmost existing ‘IdR’. The latter avoid “dead ends” in the MPO, but some functions (like *make_WI*) expect ‘IdL’/‘IdR’ to exist on all bonds.

has_edge (*i, keyL, keyR*)

True if there is an edge from *keyL* on bond (i-1, i) to *keyR* on bond (i, i+1).

build_MPO (*Ws_qtotal=None*)

Build the MPO represented by the graph (*self*).

Parameters `Ws_qtotal` (*None | (list of) charges*) – The *qtotal* for each of the *Ws* to be generated, default (`None`) means 0 charge. A single *qtotal* holds for each site.

Returns `mpo` – the MPO which self represents.

Return type `MPO`

Functions

<code>grid_insert_ops(site, grid)</code>	Replaces entries representing operators in a grid of <code>W[i]</code> with <code>npc.Arrays</code> .
<code>make_W_II(t, A, B, C, D)</code>	<code>W_II</code> approx to <code>exp(t H)</code> from MPO parts (A, B, C, D).

grid_insert_ops

- full name: `tenpy.networks.mpo.grid_insert_ops`
- parent module: `tenpy.networks.mpo`
- type: function

`tenpy.networks.mpo.grid_insert_ops(site, grid)`

Replaces entries representing operators in a grid of $W[i]$ with `np.ndarray`s.

Parameters

- **site** (`site`) – The site on which the grid acts.
- **grid** (list of list of *entries*) – Represents a single matrix W of an MPO, i.e. the lists correspond to the legs 'vL', 'vR', and entries to onsite operators acting on the given *site*. *entries* may be `None`, `Array`, a single string or of the form `[('opname', strength), ...]`, where 'opname' labels an operator in the *site*.

Returns grid – Copy of *grid* with entries `[('opname', strength), ...]` replaced by `sum([strength*site.get_op('opname') for opname, strength in entry])` and entries 'opname' replaced by `site.get_op('opname')`.

Return type list of list of `{None | Array}`

make_W_II

- full name: `tenpy.networks.mpo.make_W_II`
- parent module: `tenpy.networks.mpo`
- type: function

`tenpy.networks.mpo.make_W_II(t, A, B, C, D)`

W_{II} approx to $\exp(tH)$ from MPO parts (A, B, C, D).

Get the W_{II} approximation of [Zaletel2015].

In the paper, we have two formal parameter “ $\phi_{r/c}$ ” which satisfies $\phi_r^2 = \phi_c^2 = 0$. To implement this, we temporarily extend the virtual Hilbert space with two hard-core bosons “br, bl”. The components of Eqn (11) can be computed for each index of the virtual row/column independently. The matrix exponential is done in the hard-core extended Hilbert space.

Parameters

- **t** (`float`) – The time step per application of the propagator. Should be imaginary for real time evolution!
- **B, C, D** (`A,`) – Blocks of the MPO tensor to be exponentiated, as defined in [Zaletel2015]. Legs 'wL', 'wR', 'p', 'p*'; legs projected to a single IdL/IdR can be dropped.

Module description

Matrix product operator (MPO).

An MPO is the generalization of an MPS to operators. Graphically:



So each ‘matrix’ has two physical legs p , p^* instead of just one, i.e. the entries of the ‘matrices’ are local operators. Valid boundary conditions of an MPO are the same as for an MPS (i.e. ‘finite’ | ‘segment’ | ‘infinite’). (In general, you can view the MPO as an MPS with larger physical space and bring it into canonical form. However, unlike for an MPS, this doesn’t simplify calculations. Thus, an MPO has no *form*.)

We use the following label convention for the W (where arrows indicate *qconj*):



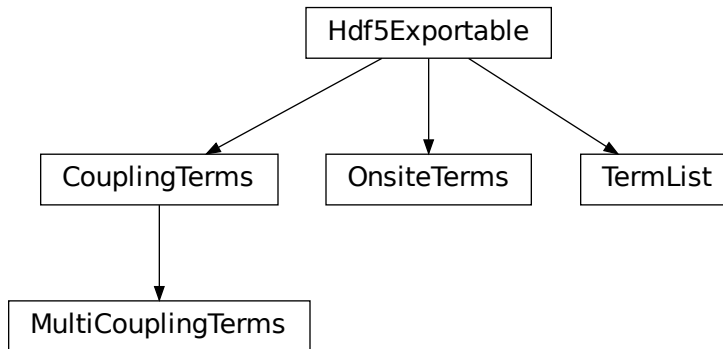
If an MPO describes a sum of local terms (e.g. most Hamiltonians), some bond indices correspond to ‘only identities to the left/right’. We store these indices in *IdL* and *IdR* (if there are such indices).

Similar as for the MPS, a bond index i is *left* of site i , i.e. between sites $i-1$ and i .

7.10.4 terms

- full name: `tenpy.networks.terms`
- parent module: `tenpy.networks`
- type: module

Classes

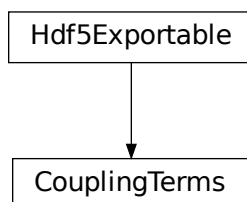


<i>CouplingTerms</i> (L)	Operator names, site indices and strengths representing two-site coupling terms.
<i>MultiCouplingTerms</i> (L)	Operator names, site indices and strengths representing general M -site coupling terms.
<i>OnsiteTerms</i> (L)	Operator names, site indices and strengths representing onsite terms.
<i>TermList</i> (terms, strength)	A list of terms (=operator names and sites they act on) and associated strengths.

CouplingTerms

- full name: `tenpy.networks.terms.CouplingTerms`
- parent module: `tenpy.networks.terms`
- type: class

Inheritance Diagram



Methods

<code>CouplingTerms.__init__(L)</code>	Initialize self.
<code>CouplingTerms.add_coupling_term(strength, i, ...)</code>	Add a two-site coupling term on given MPS sites.
<code>CouplingTerms.add_to_graph(graph)</code>	Add terms from <code>coupling_terms</code> to an <code>MPOGraph</code> .
<code>CouplingTerms.coupling_term_handle_JW(...)</code>	Helping function to call before <code>add_multi_coupling_term()</code> .
<code>CouplingTerms.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>CouplingTerms.max_range()</code>	Determine the maximal range in <code>coupling_terms</code> .
<code>CouplingTerms.plot_coupling_terms(ax, lat[, ...])</code>	Plot coupling terms into a given lattice.
<code>CouplingTerms.remove_zeros([tol_zero])</code>	Remove entries close to 0 from <code>coupling_terms</code> .
<code>CouplingTerms.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.
<code>CouplingTerms.to_TermList()</code>	Convert <code>onsite_terms</code> into a <code>TermList</code> .
<code>CouplingTerms.to_nn_bond_Arrays(sites)</code>	Convert the <code>coupling_terms</code> into <code>Arrays</code> on nearest neighbor bonds.

class `tenpy.networks.terms.CouplingTerms(L)`

Bases: `tenpy.tools.hdf5_io.Hdf5Exportable`

Operator names, site indices and strengths representing two-site coupling terms.

Parameters `L (int)` – Number of sites.

L

Number of sites.

Type `int`

coupling_terms

Filled by `add_coupling_term()`. Nested dictionaries of the form `{i: {'opname_i', 'opname_string': {j: {'opname_j': strength}}}}`. Note that always $i < j$, but entries with $j \geq L$ are allowed for `bc_MPS == 'infinite'`, in which case they indicate couplings between different iMPS unit cells.

Type `dict of dict`

max_range()

Determine the maximal range in `coupling_terms`.

Returns `max_range` – The maximum of $j - i$ for the i, j occuring in a term of `coupling_terms`.

Return type `int`

add_coupling_term(strength, i, j, op_i, op_j, op_string='Id')

Add a two-site coupling term on given MPS sites.

Parameters

- **strength (float)** – The strength of the coupling term.
- **j (i,)** – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_{\text{sites}}$ and $i < j$, i.e., `op_i` acts “left” of `op_j`. If $j \geq N_{\text{sites}}$, it indicates couplings between unit cells of an infinite MPS.

- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.

coupling_term_handle_JW (*strength*, *term*, *sites*, *op_string*=None)

Helping function to call before `add_multi_coupling_term()`.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **term** ([*(str, int)*, *(str, int)*]) – List of two tuples (*op*, *i*) where *i* is the MPS index of the site the operator named *op* acts on.
- **sites** (list of *Site*) – Defines the local Hilbert space for each site. Used to check whether the operators need Jordan-Wigner strings.
- **op_string** (None | *str*) – Operator name to be used as operator string *between* the operators, or None if the Jordan Wigner string should be figured out.

Returns Arguments for `MultiCouplingTerms.add_multi_coupling_term()` such that the added term corresponds to the parameters of this function.

Return type *strength*, *i*, *j*, *op_i*, *op_j*, *op_string*

plot_coupling_terms (*ax*, *lat*, *style_map*='default', *common_style*={'linestyle': '--'}, *text*=None, *text_pos*=0.4)

“Plot coupling terms into a given lattice.

This function plots the `coupling_terms`

Parameters

- **ax** (`matplotlib.axes.Axes`) – The axes on which we should plot.
- **lat** (*Lattice*) – The lattice for plotting the couplings, most probably the `M.lat` of the corresponding model `M`, see `lat`.
- **style_map** (*function* | None) – Function which get’s called with arguments *i*, *j*, *op_i*, *op_string*, *op_j*, *strength* for each two-site coupling and should return a keyword-dictionary with the desired plot-style for this coupling. By default (None), the *linewidth* is given by the absolute value of *strength*, and the *linecolor* depends on the phase of *strength* (using the *hsv* colormap).
- **common_style** (*dict*) – Common style, which overwrites values of the dictionary returned by *style_map*. A 'label' is only used for the first plotted line.
- **text** (*format_string* | None) – If not None, we add text labeling the couplings in the plot. Available keywords are *i*, *j*, *op_i*, *op_string*, *op_j*, *strength* as well as *strength_abs*, *strength_angle*, *strength_real*.
- **text_pos** (*float*) – Specify where to put the text on the line between *i* (0.0) and *j* (1.0), e.g. 0.5 is exactly in the middle between *i* and *j*.

See also:

`tenpy.models.lattice.Lattice.plot_sites()` plot the sites of the lattice.

add_to_graph (*graph*)

Add terms from `coupling_terms` to an `MPOGraph`.

Parameters **graph** (`MPOGraph`) – The graph into which the terms from `coupling_terms` should be added.

to_nn_bond_Arrays (*sites*)

Convert the *coupling_terms* into Arrays on nearest neighbor bonds.

Parameters *sites* (list of *Site*) – Defines the local Hilbert space for each site. Used to translate the operator names into *Array*.

Returns *H_bond* – The *coupling_terms* rewritten as $\sum_i H_bond[i]$ for MPS indices *i*. *H_bond*[*i*] acts on sites (*i*-1, *i*), None represents 0. Legs of each *H_bond*[*i*] are ['p0', 'p0*', 'p1', 'p1*'].

Return type list of {*Array* | None}

remove_zeros (*tol_zero=1e-15*)

Remove entries close to 0 from *coupling_terms*.

Parameters *tol_zero* (*float*) – Entries in *coupling_terms* with *strength* < *tol_zero* are considered to be zero and removed.

to_TermList ()

Convert *onsite_terms* into a *TermList*.

Returns *term_list* – Representation of the terms as a list of terms.

Return type *TermList*

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

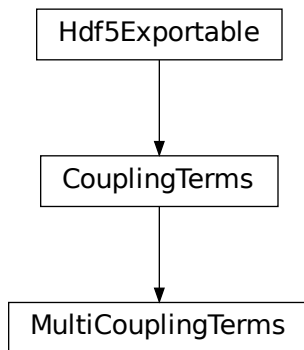
Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

MultiCouplingTerms

- full name: `tenpy.networks.terms.MultiCouplingTerms`
- parent module: `tenpy.networks.terms`
- type: class

Inheritance Diagram



Methods

<code>MultiCouplingTerms.__init__(L)</code>	Initialize self.
<code>MultiCouplingTerms.add_coupling_term(...[, ...])</code>	Add a two-site coupling term on given MPS sites.
<code>MultiCouplingTerms.add_multi_coupling_term(...)</code>	Add a multi-site coupling term.
<code>MultiCouplingTerms.add_to_graph(graph[, _i, ...])</code>	Add terms from <code>coupling_terms</code> to an <code>MPOGraph</code> .
<code>MultiCouplingTerms.coupling_term_handle_JW(...)</code>	Helping function to call before <code>add_multi_coupling_term()</code> .
<code>MultiCouplingTerms.from_hdf5(hdf5_loader, ...)</code>	Load instance from a HDF5 file.
<code>MultiCouplingTerms.max_range()</code>	Determine the maximal range in <code>coupling_terms</code> .
<code>MultiCouplingTerms.multi_coupling_term_handle_JW(...)</code>	Helping function to call before <code>add_multi_coupling_term()</code> .
<code>MultiCouplingTerms.plot_coupling_terms(ax, lat)</code>	“Plot coupling terms into a given lattice.
<code>MultiCouplingTerms.remove_zeros([tol_zero, _d0])</code>	Remove entries close to 0 from <code>coupling_terms</code> .
<code>MultiCouplingTerms.save_hdf5(hdf5_saver, ...)</code>	Export <i>self</i> into a HDF5 file.

continues on next page

Table 151 – continued from previous page

<code>MultiCouplingTerms.to_TermList()</code>	Convert onsite_terms into a <i>TermList</i> .
<code>MultiCouplingTerms.to_nn_bond_Arrays(sites)</code>	Convert the coupling_terms into Arrays on nearest neighbor bonds.

class `tenpy.networks.terms.MultiCouplingTerms(L)`

Bases: `tenpy.networks.terms.CouplingTerms`

Operator names, site indices and strengths representing general M -site coupling terms.

Generalizes the `coupling_terms` of `CouplingTerms` to M -site couplings. The structure of the nested dictionary `coupling_terms` is similar, but we allow an arbitrary recursion depth of the dictionary.

Parameters `L (int)` – Number of sites.

L

Number of sites.

Type `int`

coupling_terms

Nested dictionaries of the following form:

```
{i: {'opname_i', 'opname_string_ij':
    {j: {'opname_j', 'opname_string_jk':
        {k: {'opname_k', 'opname_string_kl':
            ...
            {l: {'opname_l':
                strength
            } }
        ...
        } }
    } }
```

For a M -site coupling, this involves a nesting depth of $2 \times M$ dictionaries. Note that always $i < j < k < \dots < l$, but entries with $j, k, l \geq L$ are allowed for the case of `bc_MPS == 'infinite'`, when they indicate couplings between different iMPS unit cells.

Type `dict of dict`

add_multi_coupling_term(`strength, ijk, ops_ijk, op_string='Id'`)

Add a multi-site coupling term.

Parameters

- **strength** (`float`) – The strength of the coupling term.
- **ijk** (`list of int`) – The MPS indices of the sites on which the operators acts. With $i, j, k, \dots = ijk$, we require that they are ordered ascending, $i < j < k < \dots$ and that $0 \leq i < N_{\text{sites}}$. Indices $\geq N_{\text{sites}}$ indicate couplings between different unit cells of an infinite MPS.
- **ops_ijk** (`list of str`) – Names of the involved operators on sites i, j, k, \dots
- **op_string** (`(list of) str`) – Names of the operator to be inserted between the operators, e.g., `op_string[0]` is inserted between i and j . A single name holds for all in-between segments.

multi_coupling_term_handle_JW(`strength, term, sites, op_string=None`)

Helping function to call before `add_multi_coupling_term()`.

Handle/figure out Jordan-Wigner strings if needed.

Parameters

- **strength** (*float*) – The strength of the term.
- **term** (*list of (str, int)*) – List of tuples (*op_i*, *i*) where *i* is the MPS index of the site the operator named *op_i* acts on. We **require** the operators to be sorted (strictly ascending) by sites. If necessary, call `order_combine_term()` beforehand.
- **sites** (*list of Site*) – Defines the local Hilbert space for each site. Used to check whether the operators need Jordan-Wigner strings.
- **op_string** (*None | str*) – Operator name to be used as operator string *between* the operators, or *None* if the Jordan Wigner string should be figured out.

Returns Arguments for `MultiCouplingTerms.add_multi_coupling_term()` such that the added term corresponds to the parameters of this function.

Return type `strength, ijl, ops_ijkl, op_string`

max_range()

Determine the maximal range in `coupling_terms`.

Returns `max_range` – The maximum of $j - i$ for the i, j occuring in a term of `coupling_terms`.

Return type `int`

add_to_graph (*graph, _i=None, _dl=None, _label_left=None*)

Add terms from `coupling_terms` to an MPOGraph.

Parameters

- **graph** (*MPOGraph*) – The graph into which the terms from `coupling_terms` should be added.
- **_dl, _label_left** (*_i,*) – Should not be given; only needed for recursion.

remove_zeros (*tol_zero=1e-15, _d0=None*)

Remove entries close to 0 from `coupling_terms`.

Parameters

- **tol_zero** (*float*) – Entries in `coupling_terms` with $strength < tol_zero$ are considered to be zero and removed.
- **_d0** (*None*) – Should not be given; only needed for recursion.

to_TermList()

Convert `onsite_terms` into a `TermList`.

Returns `term_list` – Representation of the terms as a list of terms.

Return type `TermList`

add_coupling_term (*strength, i, j, op_i, op_j, op_string='Id'*)

Add a two-site coupling term on given MPS sites.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **j** (*i,*) – The MPS indices of the two sites on which the operator acts. We require $0 \leq i < N_sites$ and $i < j$, i.e., *op_i* acts “left” of *op_j*. If $j \geq N_sites$, it indicates couplings between unit cells of an infinite MPS.

- **op2** (*op1*,) – Names of the involved operators.
- **op_string** (*str*) – The operator to be inserted between *i* and *j*.

coupling_term_handle_JW (*strength*, *term*, *sites*, *op_string*=None)

Helping function to call before `add_multi_coupling_term()`.

Parameters

- **strength** (*float*) – The strength of the coupling term.
- **term** ([*(str, int)*, (*str, int*)]) – List of two tuples (*op*, *i*) where *i* is the MPS index of the site the operator named *op* acts on.
- **sites** (list of *Site*) – Defines the local Hilbert space for each site. Used to check whether the operators need Jordan-Wigner strings.
- **op_string** (None | *str*) – Operator name to be used as operator string *between* the operators, or None if the Jordan Wigner string should be figured out.

Returns Arguments for `MultiCouplingTerms.add_multi_coupling_term()` such that the added term corresponds to the parameters of this function.

Return type *strength*, *i*, *j*, *op_i*, *op_j*, *op_string*

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

plot_coupling_terms (*ax*, *lat*, *style_map*='default', *common_style*={'linestyle': '--'}, *text*=None, *text_pos*=0.4)

“Plot coupling terms into a given lattice.

This function plots the `coupling_terms`

Parameters

- **ax** (*matplotlib.axes.Axes*) – The axes on which we should plot.
- **lat** (*Lattice*) – The lattice for plotting the couplings, most probably the *M.lat* of the corresponding model *M*, see *lat*.
- **style_map** (*function* | None) – Function which get's called with arguments *i*, *j*, *op_i*, *op_string*, *op_j*, *strength* for each two-site coupling and should return a keyword-dictionary with the desired plot-style for this coupling. By default (None), the *linewidth* is given by the absolute value of *strength*, and the *linecolor* depends on the phase of *strength* (using the *hsv* colormap).
- **common_style** (*dict*) – Common style, which overwrites values of the dictionary returned by *style_map*. A 'label' is only used for the first plotted line.
- **text** (*format_string* | None) – If not None, we add text labeling the couplings in the plot. Available keywords are *i*, *j*, *op_i*, *op_string*, *op_j*, *strength* as well as *strength_abs*, *strength_angle*, *strength_real*.

- **text_pos** (*float*) – Specify where to put the text on the line between i (0.0) and j (1.0), e.g. 0.5 is exactly in the middle between i and j .

See also:

`tenpy.models.lattice.Lattice.plot_sites()` plot the sites of the lattice.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

to_nn_bond_Arrays (*sites*)

Convert the `coupling_terms` into Arrays on nearest neighbor bonds.

Parameters *sites* (list of *Site*) – Defines the local Hilbert space for each site. Used to translate the operator names into *Array*.

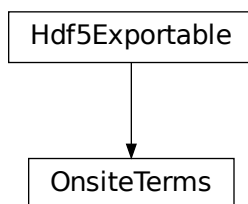
Returns **H_bond** – The `coupling_terms` rewritten as `sum_i H_bond[i]` for MPS indices i . `H_bond[i]` acts on sites $(i-1, i)$, `None` represents 0. Legs of each `H_bond[i]` are ['p0', 'p0*', 'p1', 'p1*'].

Return type list of {*Array* | `None`}

OnsiteTerms

- full name: `tenpy.networks.terms.OnsiteTerms`
- parent module: `tenpy.networks.terms`
- type: class

Inheritance Diagram



Methods

<code>OnsiteTerms.__init__(L)</code>	Initialize self.
<code>OnsiteTerms.add_onsite_term(strength, i, op)</code>	Add a onsite term on a given MPS site.
<code>OnsiteTerms.add_to_graph(graph)</code>	Add terms from <code>onsite_terms</code> to an <code>MPOGraph</code> .
<code>OnsiteTerms.add_to_nn_bond_Arrays(H_bond, ...)</code>	Add <code>self.onsite_terms</code> into nearest-neighbor bond arrays.
<code>OnsiteTerms.from_hdf5(hdf5_loader, h5gr, sub-path)</code>	Load instance from a HDF5 file.
<code>OnsiteTerms.remove_zeros([tol_zero])</code>	Remove entries close to 0 from <code>onsite_terms</code> .
<code>OnsiteTerms.save_hdf5(hdf5_saver, h5gr, sub-path)</code>	Export <i>self</i> into a HDF5 file.
<code>OnsiteTerms.to_Arrays(sites)</code>	Convert the <code>onsite_terms</code> into a list of <code>np_conserved</code> Arrays.
<code>OnsiteTerms.to_TermList()</code>	Convert <code>onsite_terms</code> into a <i>TermList</i> .

class `tenpy.networks.terms.OnsiteTerms(L)`

Bases: `tenpy.tools.hdf5_io.Hdf5Exportable`

Operator names, site indices and strengths representing onsite terms.

Represents a sum of onsite terms where the operators are only given by their name (in the form of a string). What the operator represents is later given by a list of *Site* with `get_op()`.

Parameters `L (int)` – Number of sites.

L

Number of sites.

Type `int`

onsite_terms

Filled by meth:`add_onsite_term`. For each index *i* a dictionary `{'opname': strength}` defining the onsite terms.

Type list of dict

add_onsite_term (`strength, i, op`)

Add a onsite term on a given MPS site.

Parameters

- **strength** (`float`) – The strength of the term.
- **i** (`int`) – The MPS index of the site on which the operator acts. We require $0 \leq i < L$.
- **op** (`str`) – Name of the involved operator.

add_to_graph (`graph`)

Add terms from `onsite_terms` to an `MPOGraph`.

Parameters `graph (MPOGraph)` – The graph into which the terms from `onsite_terms` should be added.

to_Arrays (`sites`)

Convert the `onsite_terms` into a list of `np_conserved` Arrays.

Parameters `sites` (list of `Site`) – Defines the local Hilbert space for each site. Used to translate the operator names into `Array`.

Returns `onsite_arrays` – Onsite terms represented by `self`. Entry `i` of the list lives on `sites[i]`.

Return type list of `Array`

remove_zeros (`tol_zero=1e-15`)

Remove entries close to 0 from `onsite_terms`.

Parameters `tol_zero` (`float`) – Entries in `onsite_terms` with `strength < tol_zero` are considered to be zero and removed.

add_to_nn_bond_Arrays (`H_bond, sites, finite, distribute=0.5, 0.5`)

Add `self.onsite_terms` into nearest-neighbor bond arrays.

Parameters

- **H_bond** (list of `{Array | None}`) – The coupling_terms rewritten as `sum_i H_bond[i]` for MPS indices `i`. `H_bond[i]` acts on sites `(i-1, i)`, `None` represents 0. Legs of each `H_bond[i]` are `['p0', 'p0*', 'p1', 'p1*']`. Modified *in place*.
- **sites** (list of `Site`) – Defines the local Hilbert space for each site. Used to translate the operator names into `Array`.
- **distribute** (`(float, float)`) – How to split the onsite terms (in the bulk) into the bond terms to the left (`distribute[0]`) and right (`distribute[1]`).
- **finite** (`bool`) – Boundary conditions of the MPS, `MPS.finite`. If finite, we distribute the onsite term of the

to_TermList ()

Convert `onsite_terms` into a `TermList`.

Returns `term_list` – Representation of the terms as a list of terms.

Return type `TermList`

classmethod from_hdf5 (`hdf5_loader, h5gr, subpath`)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (`Hdf5Loader`) – Instance of the loading engine.
- **h5gr** (`Group`) – HDF5 group which is represent the object to be constructed.
- **subpath** (`str`) – The *name* of `h5gr` with a `'/'` in the end.

Returns `obj` – Newly generated class instance containing the required data.

Return type `cls`

save_hdf5 (`hdf5_saver, h5gr, subpath`)

Export `self` into a HDF5 file.

This method saves all the data it needs to reconstruct `self` with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute `'format'`.

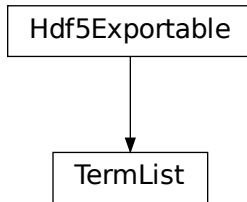
Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

TermList

- full name: `tenpy.networks.terms.TermList`
- parent module: `tenpy.networks.terms`
- type: class

Inheritance Diagram



Methods

<code>TermList.__init__(terms, strength)</code>	Initialize self.
<code>TermList.from_hdf5(hdf5_loader, h5gr, subpath)</code>	Load instance from a HDF5 file.
<code>TermList.order_combine(sites)</code>	Order and combine operators in each term.
<code>TermList.save_hdf5(hdf5_saver, h5gr, subpath)</code>	Export <i>self</i> into a HDF5 file.
<code>TermList.to_OnsiteTerms_CouplingTerms(sites)</code>	Convert to <i>OnsiteTerms</i> and <i>CouplingTerms</i> .

class `tenpy.networks.terms.TermList` (*terms, strength*)

Bases: `tenpy.tools.hdf5_io.Hdf5Exportable`

A list of terms (=operator names and sites they act on) and associated strengths.

A representation of terms, similar as *OnsiteTerms*, *CouplingTerms* and *MultiCouplingTerms*.

This class does not store operator strings between the sites. Jordan-Wigner strings of fermions are added during conversion to (Multi)CouplingTerms.

Parameters

- **terms** (*list of list of (str, int)*) – List of terms where each *term* is a list of tuples (*opname*, *i*) of an operator name and a site *i* it acts on. For Fermions, the order is the order in the mathematic sense, i.e., the right-most/last operator in the list acts last.
- **strengths** (*list of float/complex*) – For each term in *terms* an associated pref-

actor or strength (e.g. expectation value).

terms

List of terms where each *term* is a tuple (opname, i) of an operator name and a site *i* it acts on.

Type list of list of (str, int)

strengths

For each term in *terms* an associated prefactor or strength (e.g. expectation value).

Type 1D ndarray

to_OnsiteTerms_CouplingTerms (*sites*)

Convert to *OnsiteTerms* and *CouplingTerms*

Performs Jordan-Wigner transformation for fermionic operators.

Parameters *sites* (list of *Site*) – Defines the local Hilbert space for each site. Used to check whether the operators need Jordan-Wigner strings. The length is used as *L* for the *onsite_terms* and *coupling_terms*.

Returns

- **onsite_terms** (*OnsiteTerms*) – Onsite terms.
- **coupling_terms** (*CouplingTerms* | *MultiCouplingTerms*) – Coupling terms. If *self* contains terms involving more than two operators, a *MultiCouplingTerms* instance, otherwise just *CouplingTerms*.

order_combine (*sites*)

Order and combine operators in each term.

Parameters *sites* (list of *Site*) – Defines the local Hilbert space for each site. Used to check whether the operators anticommute (= whether they need Jordan-Wigner strings) and for multiplication rules.

See also:

order_and_combine_term() does it for a single term.

classmethod from_hdf5 (*hdf5_loader*, *h5gr*, *subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with *save_hdf5()*.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a '/' in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

save_hdf5 (*hdf5_saver*, *h5gr*, *subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with *from_hdf5()*.

This implementation saves the content of `__dict__` with *save_dict_content()*, storing the format under the attribute 'format'.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a *' / '* in the end.

Functions

<code>order_combine_term</code> (term, sites)	Combine operators in a term to one terms per site.
---	--

order_combine_term

- full name: `tenpy.networks.terms.order_combine_term`
- parent module: `tenpy.networks.terms`
- type: function

`tenpy.networks.terms.order_combine_term`(term, sites)
Combine operators in a term to one terms per site.

Takes in a term of operators and sites they acts on, commutes operators to order them by site and combines operators acting on the same site with `multiply_op_names()`.

Parameters

- **term** (*a list of (opname_i, i) tuples*) – Represents a product of onsite operators with site indices *i* they act on. Needs not to be ordered and can have multiple entries acting on the same site.
- **sites** (list of *Site*) – Defines the local Hilbert space for each site. Used to check whether the operators anticommute (= whether they need Jordan-Wigner strings) and for multiplication rules.

Returns

- **combined_term** – Equivalent to *term* but with at most one operator per site.
- **overall_sign** (*+1 | -1 | 0*) – Comes from the (anti-)commutation relations. When the operators in *term* are multiplied from left to right, and then multiplied by *overall_sign*, the result is the same operator as the product of *combined_term* from left to right.

Module description

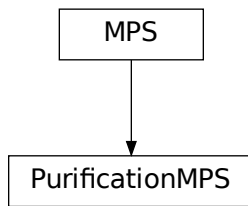
Classes to store a collection of operator names and sites they act on, together with prefactors.

This modules collects classes which are not strictly speaking tensor networks but represent “terms” acting on them. Each term is given by a collection of (onsite) operator names and indices of the sites it acts on. Moreover, we associate a *strength* to each term, which corresponds to the prefactor when specifying e.g. a Hamiltonian.

7.10.5 purification_mps

- full name: `tenpy.networks.purification_mps`
- parent module: `tenpy.networks`
- type: module

Classes



<code>PurificationMPS(sites, Bs, SVs[, bc, form, norm])</code>	An MPS representing a finite-temperature ensemble using purification.
--	---

Module description

This module contains an MPS class representing an density matrix by purification.

Usually, an MPS represents a pure state, i.e. the density matrix is $\rho = |\psi\rangle\langle\psi|$, describing observables as $\langle O \rangle = \text{Tr}(O|\psi\rangle\langle\psi|) = \langle\psi|O|\psi\rangle$. Clearly, if $|\psi\rangle$ is the ground state of a Hamiltonian, this is the density matrix at $T=0$.

At finite temperatures $T > 0$, we want to describe a non-pure density matrix $\rho = \exp(-H/T)$. This can be achieved by the so-called purification: in addition to the physical space P , we introduce a second ‘auxiliar’ space Q and define the density matrix of the physical system as $\rho = \text{Tr}_Q(|\phi\rangle\langle\phi|)$, where $|\phi\rangle$ is a pure state in the combined physical and auxiliar system.

For $T = \infty$, the density matrix ρ_∞ is the identity matrix. In other words, expectation values are sums over all possible states $\langle O \rangle = \text{Tr}_P(\rho_\infty O) = \text{Tr}_P(O)$. Saying that each `:` on top is to be connected with the corresponding `:` on the bottom, the trace is simply a contraction:



Clearly, we get the same result, if we insert an identity operator, written as MPO, on the top and bottom:



We use the following label convention:



You can view the *MPO* as an MPS by combining the p and q leg and defining every physical operator to act trivial on the q leg. In expectation values, you would then sum over over the q legs, which is exactly what we need. In other words, the choice $B = \delta_{p,q}$ with trivial (length-1) virtual bonds yields infinite temperature expectation values for operators action only on the p legs!

Now, you go a step further and also apply imaginary time evolution (acting only on p legs) to the initial infinite temperature state. For example, the normalized state $|\psi\rangle \propto \exp(-\beta/2H)|\phi\rangle$ yields expectation values

$$\langle O \rangle = \text{Tr}(\exp(-\beta H)O) / \text{Tr}(\exp(-\beta H)) \propto \langle \phi | \exp(-\beta/2H) O \exp(-\beta/2H) | \phi \rangle.$$

An additional real-time evolution allows to calculate time correlation functions:

$$\langle A(t)B(0) \rangle \propto \langle \phi | \exp(-\beta H/2) \exp(+iHt) A \exp(-iHt) B \exp(-\beta H/2) | \phi \rangle$$

Time evolution algorithms (TEBD and MPO application) are adjusted in the module `purification`.

See also [Karrasch2013] for additional tricks! One of their crucial observations is, that one can apply arbitrary unitaries on the auxiliary space (i.e. the q) without changing the result. This can actually be used to reduce the necessary virtual bond dimensions: From the definition, it is easy to see that if we apply $\exp(-iHt)$ to the p legs of $|\phi\rangle$, and $\exp(+iHt)$ to the q legs, they just cancel out! (They commute with $\exp(-\beta H/2)$...) If the state is modified (e.g. by applying A or B to calculate correlation functions), this is not true any more. However, we still can find unitaries, which are ‘optimal’ in the sense of reducing the entanglement of the MPS/MPO to the minimal value. For a discussion of *Disentangler*s (implemented in `disentangler`s), see [Hauschild2018].

Note: The classes `MPSEnvironment` and `TransferMatrix` should also work for the `PurificationMPS` defined here. For example, you can use `expectation_value()` for the expectation value of operators between different `PurificationMPS`. However, this makes only sense if the *same* disentangler was applied to the *bra* and *ket* `PurificationMPS`.

Note: The literature (e.g. section 7.2 of [Schollwoeck2011] or [Karrasch2013]) suggests to use a *singlet* as a maximally entangled state. Here, we use instead the identity $\delta_{p,q}$, since it is easier to generalize for p running over more than two indices, and allows a simple use of charge conservation with the above *qconj* convention. Moreover, we don’t split the physical and auxiliary space into separate sites, which makes TEBD as costly as $O(d^6 \chi^3)$.

Todo: One can also look at the canonical ensembles by defining the conserved quantities differently, see Barthel (2016), [arXiv:1607.01696](https://arxiv.org/abs/1607.01696) for details. Idea: usual charges on p , trivial charges on q ; fix total charge to desired value. I think it should suffice to implement another *from_infiniteT*.

7.11 tools

- full name: `tenpy.tools`
- parent module: `tenpy`
- type: module

Module description

A collection of tools: mostly short yet quite useful functions.

Some functions are explicitly imported in other parts of the library, others might just be useful when using the library. Common to all tools is that they are not just useful for a single algorithm but fairly general.

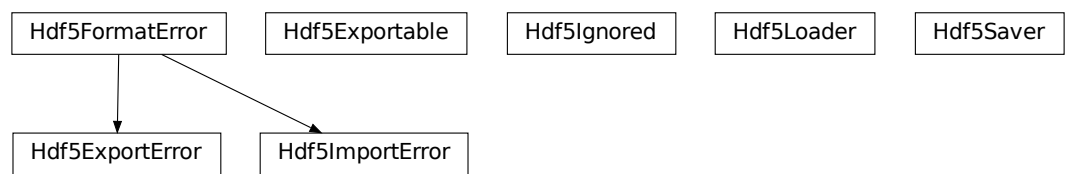
Submodules

<code>hdf5_io</code>	Tools to save and load data (from TeNPy) to disk.
<code>params</code>	Tools to handle config options/parameters for algorithms.
<code>misc</code>	Miscellaneous tools, somewhat random mix yet often helpful.
<code>math</code>	Different math functions needed at some point in the library.
<code>fit</code>	tools to fit to an algebraic decay.
<code>string</code>	Tools for handling strings.
<code>process</code>	Tools to read out total memory usage and get/set the number of threads.
<code>optimization</code>	Optimization options for this library.

7.11.1 hdf5_io

- full name: `tenpy.tools.hdf5_io`
- parent module: `tenpy.tools`
- type: module

Classes

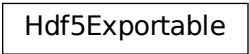


<i>Hdf5Exportable</i>	Interface specification for a class to be exportable to our HDF5 format.
<i>Hdf5Ignored</i> ([name])	Placeholder for a dataset/group to be ignored during both loading and saving.
<i>Hdf5Loader</i> (h5group[, ignore_unknown])	Class to load and import object from a HDF5 file.
<i>Hdf5Saver</i> (h5group[, format_selection])	Engine to save simple enough objects into a HDF5 file.

Hdf5Exportable

- full name: `tenpy.tools.hdf5_io.Hdf5Exportable`
- parent module: `tenpy.tools.hdf5_io`
- type: class

Inheritance Diagram



Methods

<code>Hdf5Exportable.__init__</code>	Initialize self.
<code>Hdf5Exportable.from_hdf5(hdf5_loader, h5gr, ...)</code>	Load instance from a HDF5 file.
<code>Hdf5Exportable.save_hdf5(hdf5_saver, h5gr, ...)</code>	Export <i>self</i> into a HDF5 file.

```
class tenpy.tools.hdf5_io.Hdf5Exportable
    Bases: object
```


Interface specification for a class to be exportable to our HDF5 format.

To allow a class to be exported to HDF5 with `save_to_hdf5()`, it only needs to implement the `save_hdf5()` method as documented below. To allow import, a class should implement the classmethod `from_hdf5()`. During the import, the class already needs to be defined; loading can only initialize instances, not define classes.

The implementation given works for sufficiently simple (sub-)classes, for which all data is stored in `__dict__`. In particular, this works for python-defined classes which simply store data using `self.data = data` in their methods.

save_hdf5 (*hdf5_saver, h5gr, subpath*)

Export *self* into a HDF5 file.

This method saves all the data it needs to reconstruct *self* with `from_hdf5()`.

This implementation saves the content of `__dict__` with `save_dict_content()`, storing the format under the attribute `'format'`.

Parameters

- **hdf5_saver** (*Hdf5Saver*) – Instance of the saving engine.
- **h5gr** (*:class`Group`*) – HDF5 group which is supposed to represent *self*.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

classmethod from_hdf5 (*hdf5_loader, h5gr, subpath*)

Load instance from a HDF5 file.

This method reconstructs a class instance from the data saved with `save_hdf5()`.

Parameters

- **hdf5_loader** (*Hdf5Loader*) – Instance of the loading engine.
- **h5gr** (*Group*) – HDF5 group which is represent the object to be constructed.
- **subpath** (*str*) – The *name* of *h5gr* with a `'/'` in the end.

Returns *obj* – Newly generated class instance containing the required data.

Return type *cls*

Hdf5Ignored

- full name: `tenpy.tools.hdf5_io.Hdf5Ignored`
- parent module: `tenpy.tools.hdf5_io`
- type: class

Inheritance Diagram



```
graph TD; Hdf5Ignored[Hdf5Ignored];
```

Methods

Hdf5Ignored.__init__([name])	Initialize self.
------------------------------	------------------

class `tenpy.tools.hdf5_io.Hdf5Ignored` (*name*='unknown')

Bases: `object`

Placeholder for a dataset/group to be ignored during both loading and saving.

Objects of this type are not saved. Moreover, if a saved dataset/group has the *type* attribute matching *REPR_IGNORED*, instance of this class are returned instead of loading the data.

Parameters **name** (*str*) – The name of the dataset during loading; just for reference.

name

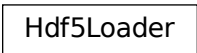
See above.

Type *str*

Hdf5Loader

- full name: `tenpy.tools.hdf5_io.Hdf5Loader`
- parent module: `tenpy.tools.hdf5_io`
- type: class

Inheritance Diagram



```
graph TD; Hdf5Loader[Hdf5Loader];
```

Methods

<code>Hdf5Loader.__init__(h5group[, ignore_unknown])</code>	ig-	Initialize self.
<code>Hdf5Loader.find_class(module, classname)</code>		Get the class of the qualified <i>classname</i> in a given python <i>module</i> .
<code>Hdf5Loader.get_attr(h5gr, attr_name)</code>		Return attribute <code>h5gr.attrs[attr_name]</code> , if existent.
<code>Hdf5Loader.load([path])</code>		Load a Python <i>object</i> from the dataset.
<code>Hdf5Loader.load_dataset(h5gr, type_info, subpath)</code>		Load a h5py <i>Dataset</i> and convert it into the desired type.
<code>Hdf5Loader.load_dict(h5gr, type_info, subpath)</code>		Load a dictionary in the format according to <i>type_info</i> .
<code>Hdf5Loader.load_dtype(h5gr, type_info, subpath)</code>		Load a <i>numpy.dtype</i> .
<code>Hdf5Loader.load_general_dict(h5gr, ...)</code>		Load a dictionary with general keys.
<code>Hdf5Loader.load_hdf5exportable(h5gr, ...)</code>		Load an instance of a userdefined class.
<code>Hdf5Loader.load_ignored(h5gr, type_info, subpath)</code>		Ignore the group to be loaded.
<code>Hdf5Loader.load_list(h5gr, type_info, subpath)</code>		Load a list.
<code>Hdf5Loader.load_none(h5gr, type_info, subpath)</code>		Load the <i>None</i> object from a dataset.
<code>Hdf5Loader.load_range(h5gr, type_info, subpath)</code>		Load a range.
<code>Hdf5Loader.load_set(h5gr, type_info, subpath)</code>		Load a set.
<code>Hdf5Loader.load_simple_dict(h5gr, type_info, ...)</code>		Load a dictionary with simple keys.
<code>Hdf5Loader.load_tuple(h5gr, type_info, subpath)</code>		Load a tuple.
<code>Hdf5Loader.memorize_load(h5gr, obj)</code>		Store objects already loaded in the <i>memo_load</i> .

Class Attributes and Properties

<code>Hdf5Loader.dispatch_load</code>

class `tenpy.tools.hdf5_io.Hdf5Loader` (*h5group*, *ignore_unknown=True*)

Bases: `object`

Class to load and import object from a HDF5 file.

The intended use of this class is through `load_from_hdf5()`, which is simply an alias for `Hdf5Loader(h5group).load(path)`.

It can load data exported with `save_to_hdf5()` or the *Hdf5Saver*, respectively.

The basic structure of this class is similar as the *Unpickler* from `pickle`.

See *Saving to disk: input/output* for a specification of what can be saved and what the resulting datastructure is.

Parameters

- **h5group** (*Group*) – The HDF5 group (or file) where to save the data.

- **ignore_unknown** (*bool*) – Whether to just warn (True) or raise an Error (False) if a class to be loaded is not found.

h5group

The HDF5 group (or HDF5 [File](#)) where to save the data.

Type [Group](#)

ignore_unknown

Whether to just warn (True) or raise an Error (False) if a class to be loaded is not found.

Type [bool](#)

dispatch_load

Mapping from one of the global REPR_* variables to (unbound) methods *f* of this class. The method is called as *f*(self, h5gr, type_info, subpath). The call to *f* should load and return an object *obj* from the h5py [Group](#) or [Dataset](#) *h5gr*; and memorize the loaded *obj* with [memorize_load\(\)](#). *subpath* is just the name of *h5gr* with a guaranteed ' / ' in the end. *type_info* is often the REPR_* variable of the type or some other information about the type, which allows to use a single dispatch_load function for different datatypes.

Type [dict](#)

memo_load

A dictionary to remember all the objects which we already loaded from [h5group](#). The dictionary key is a h5py group- or dataset id; the value is the loaded object. See [memorize_load\(\)](#).

Type [dict](#)

load (*path=None*)

Load a Python [object](#) from the dataset.

See [load_from_hdf5\(\)](#) for more details.

Parameters *path* (None | str | Reference) – Path within [h5group](#) to be used for loading.
Defaults to the name of [h5group](#) itself.

Returns *obj* – The Python object loaded from [h5group](#) (specified by *path*).

Return type [object](#)

memorize_load (*h5gr, obj*)

Store objects already loaded in the [memo_load](#).

This allows to avoid copies, if the same dataset appears multiple times in the hdf5 group of *obj*. Examples can be shared [LegCharge](#) objects or even shared [Array](#).

To handle cyclic references correctly, this function should be called *before* loading data from subgroups with new calls of [load\(\)](#).

static get_attr (*h5gr, attr_name*)

Return attribute *h5gr.attrs[attr_name]*, if existent.

Raises [Hdf5ImportError](#) – If the attribute does not exist.

static find_class (*module, classname*)

Get the class of the qualified *classname* in a given python *module*.

Imports the module.

load_none (*h5gr, type_info, subpath*)

Load the None object from a dataset.

load_dataset (*h5gr, type_info, subpath*)

Load a h5py [Dataset](#) and convert it into the desired type.

load_list (*h5gr, type_info, subpath*)
Load a list.

load_set (*h5gr, type_info, subpath*)
Load a set.

load_tuple (*h5gr, type_info, subpath*)
Load a tuple.

load_dict (*h5gr, type_info, subpath*)
Load a dictionary in the format according to *type_info*.

load_general_dict (*h5gr, type_info, subpath*)
Load a dictionary with general keys.

load_simple_dict (*h5gr, type_info, subpath*)
Load a dictionary with simple keys.

load_range (*h5gr, type_info, subpath*)
Load a range.

load_dtype (*h5gr, type_info, subpath*)
Load a `numpy.dtype`.


load_hdf5exportable (*h5gr, type_info, subpath*)
Load an instance of a userdefined class.

load_ignored (*h5gr, type_info, subpath*)
Ignore the group to be loaded.

Hdf5Saver

- full name: `tenpy.tools.hdf5_io.Hdf5Saver`
- parent module: `tenpy.tools.hdf5_io`
- type: class

Inheritance Diagram



```

classDiagram
    class Hdf5Saver
  
```

Hdf5Saver

Methods

<code>Hdf5Saver.__init__(h5group[, mat_selection])</code>	for-	Initialize self.
<code>Hdf5Saver.create_group_for_obj(path, obj)</code>		Create an HDF5 group <code>self.h5group[path]</code> to store <i>obj</i> .
<code>Hdf5Saver.memorize_save(h5gr, obj)</code>		Store objects already saved in the <code>memo_save</code> .
<code>Hdf5Saver.save(obj[, path])</code>		Save <i>obj</i> in <code>self.h5group[path]</code> .
<code>Hdf5Saver.save_dataset(obj, path, type_repr)</code>		Save <i>obj</i> as a hdf5 dataset; in dispatch table.
<code>Hdf5Saver.save_dict(obj, path, type_repr)</code>		Save the dictionary <i>obj</i> ; in dispatch table.
<code>Hdf5Saver.save_dict_content(obj, h5gr, subpath)</code>		Save contents of a dictionary <i>obj</i> in the existing <i>h5gr</i> .
<code>Hdf5Saver.save_dtype(obj, path, type_repr)</code>		Save a <code>dtype</code> object; in dispatch table.
<code>Hdf5Saver.save_ignored(obj, path, type_repr)</code>		Don't save the <code>Hdf5Ignored</code> object; just return <code>None</code> .
<code>Hdf5Saver.save_iterable(obj, path, type_repr)</code>		Save an iterable <i>obj</i> like a list, tuple or set; in dispatch table.
<code>Hdf5Saver.save_iterable_content(obj, h5gr, ...)</code>		Save contents of an iterable <i>obj</i> in the existing <i>h5gr</i> .
<code>Hdf5Saver.save_none(obj, path, type_repr)</code>		Save the <code>None</code> object as a string (dataset); in dispatch table.
<code>Hdf5Saver.save_range(obj, path, type_repr)</code>		Save a range object; in dispatch table.

Class Attributes and Properties

<code>Hdf5Saver.dispatch_save</code>

class `tenpy.tools.hdf5_io.Hdf5Saver` (*h5group*, *format_selection=None*)

Bases: `object`

Engine to save simple enough objects into a HDF5 file.

The intended use of this class is through `save_to_hdf5()`, which is simply an alias for `Hdf5Saver(h5group).save(obj, path)`.

It exports python objects to a HDF5 file such that they can be loaded with the `Hdf5Loader`, or a call to `load_from_hdf5()`, respectively.

The basic structure of this class is similar as the *Pickler* from `pickle`.

See *Saving to disk: input/output* for a specification of what can be saved and what the resulting datastructure is.

Parameters

- **h5group** (`Group`) – The HDF5 group (or `HDF5 File`) where to save the data.
- **format_selection** (`dict`) – This dictionary allows to set a output format selection for user-defined `Hdf5Exportable.save_hdf5()` implementations. For example, `LegCharge` checks it for the key "LegCharge".

h5group

The HDF5 group (or `HDF5 File`) where to save the data.

Type `Group`

dispatch_save

Mapping from a type *keytype* to methods *f* of this class. The method is called as `f(self, obj,`

`path, type_repr`). The call to `f` should save the object `obj` in `self.h5group[path]`, call `memorize_save()`, and set `h5gr.attr[ATTR_TYPE] = type_repr` to a string `type_repr` in order to allow loading with the dispatcher in `Hdf5Loader.dispatch_save[type_repr]`.

Type dict

memo_save

A dictionary to remember all the objects which we already stored to `h5group`. The dictionary key is the object id; the value is a two-tuple of the hdf5 group or dataset where an object was stored, and the object itself. See `memorize_save()`.

Type dict

format_selection

This dictionary allows to set a output format selection for user-defined `Hdf5Exportable.save_hdf5()` implementations. For example, `LegCharge` checks it for the key "LegCharge".

Type dict

save (*obj*, *path*='/')

Save *obj* in `self.h5group[path]`.

Parameters

- **obj** (*object*) – The object (=data) to be saved.
- **path** (*str*) – Path within `h5group` under which the *obj* should be saved. To avoid unwanted overwriting of important data, the group/object should not yet exist, except if *path* is the default `'/'`.

Returns `h5gr` – The h5py group or dataset in which *obj* was saved.

Return type `Group|Dataset`

create_group_for_obj (*path*, *obj*)

Create an HDF5 group `self.h5group[path]` to store *obj*.

Also handle ending of path with `'/'`, and memorize *obj* in `memo_save`.

Parameters

- **path** (*str*) – Path within `h5group` under which the *obj* should be saved. To avoid unwanted overwriting of important data, the group/object should not yet exist, except if *path* is the default `'/'`.
- **obj** (*object*) – The object (=data) to be saved.

Returns

- **h5group** (`Group`) – Newly created h5py (sub)group `self.h5group[path]`, unless *path* is `'/'`, in which case it is simply the existing `self.h5group['/']`.
- **subpath** (*str*) – The *group.name* ending with `'/'`, such that other names can be appended to get the path for subgroups or datasets in the group.

:raises `ValueError`: if `self.h5group[path]` already existed and *path* is not `'/'`.

memorize_save (*h5gr*, *obj*)

Store objects already saved in the `memo_save`.

This allows to avoid copies, if the same python object appears multiple times in the data of *obj*. Examples can be shared `LegCharge` objects or even shared `Array`. Using the memo also avoids crashes from cyclic references, e.g., when a list contains a reference to itself.

Parameters

- **h5gr** (*Group* | *Dataset*) – The h5py group or dataset in which *obj* was saved.
- **obj** (*object*) – The object saved.

save_none (*obj*, *path*, *type_repr*)

Save the None object as a string (dataset); in dispatch table.

save_dataset (*obj*, *path*, *type_repr*)

Save *obj* as a hdf5 dataset; in dispatch table.

save_iterable (*obj*, *path*, *type_repr*)

Save an iterable *obj* like a list, tuple or set; in dispatch table.

save_iterable_content (*obj*, *h5gr*, *subpath*)

Save contents of an iterable *obj* in the existing *h5gr*.

Parameters

- **obj** (*dict*) – The data to be saved
- **h5gr** (*Group*) – h5py Group under which the keys and values of *obj* should be saved.
- **subpath** (*str*) – Name of h5gr with ' / ' in the end.

save_dict (*obj*, *path*, *type_repr*)

Save the dictionary *obj*; in dispatch table.

save_dict_content (*obj*, *h5gr*, *subpath*)

Save contents of a dictionary *obj* in the existing *h5gr*.

The format depends on whether the dictionary *obj* has simple keys valid for hdf5 path components (see [*valid_hdf5_path_component\(\)*](#)) or not. For simple keys: directly use the keys as path. For non-simple keys: save list of keys und "keys" and list of values und "values".

Parameters

- **obj** (*dict*) – The data to be saved
- **h5gr** (*Group*) – h5py Group under which the keys and values of *obj* should be saved.
- **subpath** (*str*) – Name of h5gr with ' / ' in the end.

Returns *type_repr* – Indicates whether the data was saved in the format for a dictionary with simple keys or general keys, see comment above.

Return type REPR_DICT_SIMPLE | REPR_DICT_GENERAL

save_range (*obj*, *path*, *type_repr*)

Save a range object; in dispatch table.

save_dtype (*obj*, *path*, *type_repr*)

Save a *dtype* object; in dispatch table.

save_ignored (*obj*, *path*, *type_repr*)

Don't save the Hdf5Ignored object; just return None.

Exceptions

<code>Hdf5ExportError</code>	This exception is raised when something went wrong during export to hdf5.
<code>Hdf5FormatError</code>	Common base class for errors regarding our HDF5 format.
<code>Hdf5ImportError</code>	This exception is raised when something went wrong during import from hdf5.

Hdf5ExportError

- full name: `tenpy.tools.hdf5_io.Hdf5ExportError`
- parent module: `tenpy.tools.hdf5_io`
- type: exception

exception `tenpy.tools.hdf5_io.Hdf5ExportError`

This exception is raised when something went wrong during export to hdf5.

Hdf5FormatError

- full name: `tenpy.tools.hdf5_io.Hdf5FormatError`
- parent module: `tenpy.tools.hdf5_io`
- type: exception

exception `tenpy.tools.hdf5_io.Hdf5FormatError`

Common base class for errors regarding our HDF5 format.

Hdf5ImportError

- full name: `tenpy.tools.hdf5_io.Hdf5ImportError`
- parent module: `tenpy.tools.hdf5_io`
- type: exception

exception `tenpy.tools.hdf5_io.Hdf5ImportError`

This exception is raised when something went wrong during import from hdf5.

Functions

<code>load(filename)</code>	Load data from file with given <i>filename</i> .
<code>load_from_hdf5(h5group[, path, ignore_unknown])</code>	Load an object from hdf5 file or group.
<code>save(data, filename[, mode])</code>	Save <i>data</i> to file with given <i>filename</i> .
<code>save_to_hdf5(h5group, obj[, path])</code>	Save an object <i>obj</i> into a hdf5 file or group.
<code>valid_hdf5_path_component(name)</code>	Determine if <i>name</i> is a valid HDF5 path component.

load

- full name: `tenpy.tools.hdf5_io.load`
- parent module: `tenpy.tools.hdf5_io`
- type: function

`tenpy.tools.hdf5_io.load(filename)`
Load data from file with given *filename*.

Guess the type of the file from the filename ending, see `save()` for possible endings.

Parameters `filename` (*str*) – The name of the file to load.

Returns `data` – The object loaded from the file.

Return type `obj`

load_from_hdf5

- full name: `tenpy.tools.hdf5_io.load_from_hdf5`
- parent module: `tenpy.tools.hdf5_io`
- type: function

`tenpy.tools.hdf5_io.load_from_hdf5(h5group, path=None, ignore_unknown=True)`
Load an object from hdf5 file or group.

Roughly equivalent to `obj = h5group[path][...]`, but handle more complicated objects saved as hdf5 groups and/or datasets with `save_to_hdf5()`. For example, dictionaries are handled recursively. See [Saving to disk: input/output](#) for a specification of what can be saved/loaded and what the corresponding datastructure is.

Parameters

- **h5group** (*Group*) – The HDF5 group (or *h5py File*) to be loaded.
- **path** (*None | str | Reference*) – Path within *h5group* to be used for loading. Defaults to the *h5group* itself specified.
- **ignore_unknown** (*bool*) – Whether to just warn (*True*) or raise an *Error* (*False*) if a class to be loaded is not found.

Returns `obj` – The Python object loaded from *h5group* (specified by *path*).

Return type `object`

save

- full name: `tenpy.tools.hdf5_io.save`
- parent module: `tenpy.tools.hdf5_io`
- type: function

`tenpy.tools.hdf5_io.save(data, filename, mode='w')`
Save *data* to file with given *filename*.

This function guesses the type of the file from the filename ending. Supported endings:

ending	description
.pkl	Pickle without compression
.pklz	Pickle with gzip compression.
.hdf5	Hdf5 file (using <i>h5py</i>).

Parameters

- **filename** (*str*) – The name of the file where to save the data.
- **mode** (*str*) – File mode for opening the file. 'w' for write (discard existing file), 'a' for append (add data to existing file). See `open()` for more details.

save_to_hdf5

- full name: `tenpy.tools.hdf5_io.save_to_hdf5`
- parent module: `tenpy.tools.hdf5_io`
- type: function

`tenpy.tools.hdf5_io.save_to_hdf5(h5group, obj, path='/')`
 Save an object *obj* into a hdf5 file or group.

Roughly equivalent to `h5group[path] = obj`, but handle different types of *obj*. For example, dictionaries are handled recursively. See *Saving to disk: input/output* for a specification of what can be saved and what the resulting datastructure is.

Parameters

- **h5group** (*Group*) – The HDF5 group (or *h5py File*) to which *obj* should be saved.
- **obj** (*object*) – The object (=data) to be saved.
- **path** (*str*) – Path within *h5group* under which the *obj* should be saved. To avoid unwanted overwriting of important data, the group/object should not yet exist, except if *path* is the default `'/'`.

Returns *h5obj* – The *h5py* group or dataset under which *obj* was saved.

Return type `Group|Dataset`

valid_hdf5_path_component

- full name: `tenpy.tools.hdf5_io.valid_hdf5_path_component`
- parent module: `tenpy.tools.hdf5_io`
- type: function

`tenpy.tools.hdf5_io.valid_hdf5_path_component(name)`
 Determine if *name* is a valid HDF5 path component.

Conditions: String, no `'/'`, and overall name `!= '.'`.

Module description

Tools to save and load data (from TeNPy) to disk.

Note: This module is maintained in the repository https://github.com/tenpy/hdf5_io.git

See *Saving to disk: input/output* for a motivation and specification of the HDF5 format implemented below. .. online at https://tenpy.readthedocs.io/en/latest/intro/input_output.html

The functions `save()` and `load()` are convenience functions for saving and loading quite general python objects (like dictionaries) to/from files, guessing the file type (and hence protocol for reading/writing) from the file ending.

On top of that, this function provides support for saving python objects to [HDF5] files with the `Hdf5Saver` and `Hdf5Loader` classes and the wrapper functions `save_to_hdf5()`, `load_from_hdf5()`.

Note: To use the export/import features to HDF5, you need to install the `h5py` python package (and hence some version of the HDF5 library).

Global module constants used for our HDF5 format

Names of HDF5 attributes:

```
tenpy.tools.hdf5_io.ATTR_TYPE = 'type'
    Attribute name for type of the saved object, should be one of the REPR_*
tenpy.tools.hdf5_io.ATTR_CLASS = 'class'
    Attribute name for the class name of an HDF5Exportable
tenpy.tools.hdf5_io.ATTR_MODULE = 'module'
    Attribute name for the module where ATTR_CLASS can be retrieved
tenpy.tools.hdf5_io.ATTR_LEN = 'len'
    Attribute name for the length of iterables, e.g, list, tuple
tenpy.tools.hdf5_io.ATTR_FORMAT = 'format'
    indicates the ATTR_TYPE format used by Hdf5Exportable
```

Names for the ATTR_TYPE attribute:

```
tenpy.tools.hdf5_io.REPR_HDF5EXPORTABLE = 'instance'
    saved object is instance of a user-defined class following the Hdf5Exportable style.
tenpy.tools.hdf5_io.REPR_ARRAY = 'array'
    saved object represents a numpy array
tenpy.tools.hdf5_io.REPR_INT = 'int'
    saved object represents a (python) int
tenpy.tools.hdf5_io.REPR_FLOAT = 'float'
    saved object represents a (python) float
tenpy.tools.hdf5_io.REPR_STR = 'str'
    saved object represents a (python unicode) string
tenpy.tools.hdf5_io.REPR_COMPLEX = 'complex'
    saved object represents a complex number
```

```

tenpy.tools.hdf5_io.REPR_INT64 = 'np.int64'
    saved object represents a np.int64

tenpy.tools.hdf5_io.REPR_FLOAT64 = 'np.float64'
    saved object represents a np.float64

tenpy.tools.hdf5_io.REPR_INT32 = 'np.int32'
    saved object represents a np.int32

tenpy.tools.hdf5_io.REPR_FLOAT32 = 'np.float32'
    saved object represents a np.float32

tenpy.tools.hdf5_io.REPR_BOOL = 'bool'
    saved object represents a boolean

tenpy.tools.hdf5_io.REPR_NONE = 'None'
    saved object is None

tenpy.tools.hdf5_io.REPR_RANGE = 'range'
    saved object is a range

tenpy.tools.hdf5_io.REPR_LIST = 'list'
    saved object represents a list

tenpy.tools.hdf5_io.REPR_TUPLE = 'tuple'
    saved object represents a tuple

tenpy.tools.hdf5_io.REPR_SET = 'set'
    saved object represents a set

tenpy.tools.hdf5_io.REPR_DICT_GENERAL = 'dict'
    saved object represents a dict with complicated keys

tenpy.tools.hdf5_io.REPR_DICT_SIMPLE = 'simple_dict'
    saved object represents a dict with simple keys

tenpy.tools.hdf5_io.REPR_DTYPE = 'dtype'
    saved object represents a np.dtype

tenpy.tools.hdf5_io.REPR_IGNORED = 'ignore'
    ignore the object/dataset during loading and saving

tenpy.tools.hdf5_io.TYPES_FOR_HDF5_DATASETS = ((<class 'numpy.ndarray'>, 'array'), (<class
    tuple of (type, type_repr) which h5py can save as datasets; one entry for each type.

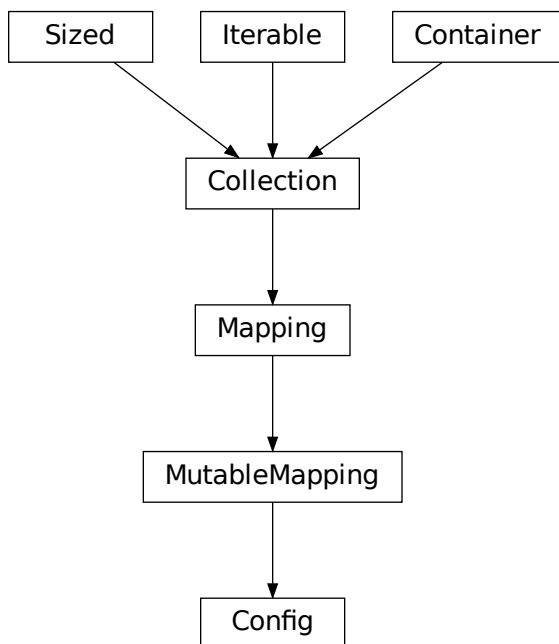
```

Todo: For memory caching with big MPO environments, we need a Hdf5Cacher clearing the memo's every now and then (triggered by what?).

7.11.2 params

- full name: `tenpy.tools.params`
- parent module: `tenpy.tools`
- type: module

Classes



<code>Config(config, name)</code>	Dict-like wrapper class for parameter/configuration dictionaries.
-----------------------------------	---

Functions

<code>asConfig(config, name)</code>	Convert a dict-like <i>config</i> to a <code>Config</code> .
<code>get_parameter(params, key, default, descr[, ...])</code>	Read out a parameter from the dictionary and/or provide default values.
<code>unused_parameters(params[, warn])</code>	Returns a set of the parameters which have not been read out with <i>get_parameters</i> .

asConfig

- full name: `tenpy.tools.params.asConfig`
- parent module: `tenpy.tools.params`
- type: function

`tenpy.tools.params.asConfig(config, name)`

Convert a dict-like *config* to a `Config`.

Parameters

- **config** (`dict`|`Config`) – If this is a `Config`, just return it. Otherwise, create a `Config` from it and return that.
- **name** (`str`) – Name to be used for the `Config`.

Returns `config` – Either directly *config* or `Config(config, name)`.

Return type `Config`

get_parameter

- full name: `tenpy.tools.params.get_parameter`
- parent module: `tenpy.tools.params`
- type: function

`tenpy.tools.params.get_parameter(params, key, default, descr, asarray=False)`

Read out a parameter from the dictionary and/or provide default values.

This function provides a similar functionality as `params.get(key, default)`. *Unlike dict.get* this function writes the default value into the dictionary (i.e. in other words it's more similar to `params.setdefault(key, default)`).

This allows the user to save the modified dictionary as meta-data, which gives a concrete record of the actually used parameters and simplifies reproducing the results and restarting simulations.

Moreover, a special entry with the key `'verbose'` in the *params* can trigger this function to also print the used value. A higher *verbose* level implies more output. If *verbose* ≥ 100 , it is printed every time it's used. If *verbose* ≥ 2 , it's printed for the first time it's used. and for *verbose* ≥ 1 , non-default values are printed the first time they are used. otherwise only for the first use.

Internally, whether a parameter was used is saved in the set `params['_used_param']`. This is used in `unused_parameters()` to print a warning if the key wasn't used at the end of the algorithm, to detect mis-spelled parameters.

Parameters

- **params** (`dict`) – A dictionary of the parameters as provided by the user. If *key* is not a valid key, `params[key]` is set to *default*.
- **key** (`string`) – The key for the parameter which should be read out from the dictionary.
- **default** – The default value for the parameter.
- **descr** (`str`) – A short description for verbose output, like `'TEBD'`, `'XXZ_model'`, `'truncation'`.
- **asarray** (`bool`) – If `True`, convert the result to a numpy array with `np.asarray(...)` before returning.

Returns `params[key]` if the key is in `params`, otherwise *default*. Converted to a numpy array, if *asarray*.

Return type `value`

Examples

In the algorithm Engine gets a dictionary of parameters. Beside doing other stuff, it calls `tenpy.models.model.NearestNeighborModel.calc_U_bond()` with the dictionary as argument, which looks similar like:

```
>>> def model_calc_U(U_param):
>>>     dt = get_parameter(U_param, 'dt', 0.01, 'TEBD')
>>>     # ... calculate exp(-i * dt * H) ....
```

Then, when you call *time_evolution* without any parameters, it just uses the default value:

```
>>> tenpy.algorithms.tebd.time_evolution(..., dict()) # uses dt=0.01
```

If you provide the special keyword 'verbose' you can trigger this function to print the used parameter values:

```
>>> tenpy.algorithms.tebd.time_evolution(..., dict(verbose=1))
parameter 'dt'=0.01 (default) for TEBD
```

Of course you can also provide the parameter to use a non-default value:

```
>>> tenpy.algorithms.tebd.time_evolution(..., dict(dt=0.1, verbose=1))
parameter 'dt'=0.1 for TEBD
```

unused_parameters

- full name: `tenpy.tools.params.unused_parameters`
- parent module: `tenpy.tools.params`
- type: function

`tenpy.tools.params.unused_parameters(params, warn=None)`

Returns a set of the parameters which have not been read out with *get_parameters*.

This function might be useful to check for typos in the parameter keys.

Parameters

- **params** (*dict*) – A dictionary of parameters which was given to (functions using) *get_parameter()*
- **warn** (*None* | *str*) – If given, print a warning “unused parameter for {warn!s}: {unused_keys!s}”.

Returns `unused_keys` – The set of keys of the params which was not used

Return type `set`

Module description

Tools to handle config options/parameters for algorithms.

See the doc-string of `Config` for details.

7.11.3 misc

- full name: `tenpy.tools.misc`
- parent module: `tenpy.tools`
- type: module

Functions

<code>add_with_None_0(a, b)</code>	Return $a + b$, treating <i>None</i> as zero.
<code>any_nonzero(params, keys[, verbose_msg])</code>	Check for any non-zero or non-equal entries in some parameters.
<code>anynan(a)</code>	check whether any entry of a ndarray <i>a</i> is 'NaN'.
<code>argsort(a[, sort])</code>	wrapper around <code>np.argsort</code> to allow sorting ascending/descending and by magnitude.
<code>atleast_2d_pad(a[, pad_item])</code>	Transform <i>a</i> into a 2D array, filling missing places with <i>pad_item</i> .
<code>build_initial_state(size, states, filling[, ...])</code>	
<code>chi_list(chi_max[, dchi, nsweeps, verbose])</code>	
<code>inverse_permutation(perm)</code>	reverse sorting indices.
<code>lexsort(a[, axis])</code>	wrapper around <code>np.lexsort</code> : allow for trivial case $a.shape[0] = 0$ without sorting
<code>list_to_dict_list(l)</code>	Given a list <i>l</i> of objects, construct a lookup table.
<code>pad(a[, w_l, v_l, w_r, v_r, axis])</code>	Pad an array along a given <i>axis</i> .
<code>setup_executable(mod, run_defaults[, ...])</code>	Read command line arguments and turn into useable dicts.
<code>to_array(a[, shape])</code>	Convert <i>a</i> to a numpy array and tile to matching dimension/shape.
<code>to_iterable(a)</code>	If <i>a</i> is a not iterable or a string, return <code>[a]</code> , else return <i>a</i> .
<code>to_iterable_of_len(a, L)</code>	If <i>a</i> is a non-string iterable of length <i>L</i> , return <i>a</i> , otherwise return <code>[a]*L</code> .
<code>transpose_list_list(D[, pad])</code>	Returns a list of lists <i>T</i> , such that $T[i][j] = D[j][i]$.
<code>zero_if_close(a[, tol])</code>	set real and/or imaginary part to 0 if their absolute value is smaller than <i>tol</i> .

add_with_None_0

- full name: `tenpy.tools.misc.add_with_None_0`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.add_with_None_0(a, b)`

Return $a + b$, treating *None* as zero.

Parameters *b* (*a*,) – The two things to be added, or *None*.

Returns $a + b$, except if *a* or *b* is *None*, in which case the other variable is returned.

Return type `sum`

any_nonzero

- full name: `tenpy.tools.misc.any_nonzero`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.any_nonzero(params, keys, verbose_msg=None)`

Check for any non-zero or non-equal entries in some parameters.

Parameters

- **params** (*dict* | *Config*) – A dictionary of parameters, or a *Config* instance.
- **keys** (*list of {key | tuple of keys}*) – For a single key, check `params[key]` for non-zero entries. For a tuple of keys, all the `params[key]` have to be equal (as numpy arrays).
- **verbose_msg** (*None* | *str*) – If `params['verbose'] >= 1`, we print *verbose_msg* before checking, and a short notice with the *key*, if a non-zero entry is found.

Returns *match* – False, if all `params[key]` are zero or *None* and True, if any of the `params[key]` for single *key* in *keys*, or if any of the entries for a tuple of *keys*

Return type `bool`

anynan

- full name: `tenpy.tools.misc.anynan`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.anynan(a)`

check whether any entry of a ndarray *a* is 'NaN'.

argsort

- full name: `tenpy.tools.misc.argsort`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.argsort` (*a*, *sort=None*, ***kwargs*)

wrapper around `np.argsort` to allow sorting ascending/descending and by magnitude.

Parameters

- **a** (*array_like*) – The array to sort.
- **sort** ('m>', 'm<', '>', '<', None) – Specify how the arguments should be sorted.

<i>sort</i>	<i>order</i>
'm>', 'LM'	Largest magnitude first
'm<', 'SM'	Smallest magnitude first
'>', 'LR', 'LA'	Largest real part first
'<', 'SR', 'SA'	Smallest real part first
'LI'	Largest imaginary part first
'Si'	Smallest imaginary part first
None	numpy default: same as '<'

- ****kwargs** – Further keyword arguments given directly to `numpy.argsort()`.

Returns *index_array* – Same shape as *a*, such that `a[index_array]` is sorted in the specified way.

Return type ndarray, int

atleast_2d_pad

- full name: `tenpy.tools.misc.atleast_2d_pad`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.atleast_2d_pad` (*a*, *pad_item=0*)

Transform *a* into a 2D array, filling missing places with *pad_item*.

Given a list of lists, turn it to a 2D array (pad with 0), or turn a 1D list to 2D.

Parameters *a* (*list of lists*) – to be converted into ad 2D array.

Returns *a_2D* – *a* converted into a numpy array.

Return type 2D ndarray

Examples

```
>>> atleast_2d_pad([3, 4, 0])
array([[3, 4, 0]])
```

```
>>> atleast_2d_pad([[3, 4],[1, 6, 7]])
array([[ 3.,  4.,  0.],
       [ 1.,  6.,  7.]])
```

build_initial_state

- full name: `tenpy.tools.misc.build_initial_state`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.build_initial_state` (*size, states, filling, mode='random', seed=None*)

chi_list

- full name: `tenpy.tools.misc.chi_list`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.chi_list` (*chi_max, dchi=20, nsweeps=20, verbose=0*)

inverse_permutation

- full name: `tenpy.tools.misc.inverse_permutation`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.inverse_permutation` (*perm*)
reverse sorting indices.

Sort functions (as `LegCharge.sort()`) return a (1D) permutation *perm* array, such that `sorted_array = old_array[perm]`. This function inverts the permutation *perm*, such that `old_array = sorted_array[inverse_permutation(perm)]`.

Parameters *perm* (1D array_like) – The permutation to be reversed.
Assumes that it is a permutation with unique indices. If it is,
`inverse_permutation(inverse_permutation(perm)) == perm`.

Returns *inv_perm* – The inverse permutation of *perm* such that `inv_perm[perm[j]] = j = perm[inv_perm[j]]`.

Return type 1D array (`int`)

lexsort

- full name: `tenpy.tools.misc.lexsort`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.lexsort(a, axis=-1)`
 wrapper around `np.lexsort`: allow for trivial case `a.shape[0] == 0` without sorting

list_to_dict_list

- full name: `tenpy.tools.misc.list_to_dict_list`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.list_to_dict_list(l)`
 Given a list *l* of objects, construct a lookup table.

This function will handle duplicate entries in *l*.

Parameters *l* (*iterable of iterable of immutable*) – A list of objects that can be converted to tuples to be used as keys for a dictionary.

Returns **lookup** – A dictionary with (key, value) pairs `(key): [i1, i2, ...]` where *i1*, *i2*, ... are the indices where *key* is found in *l*: i.e. `key == tuple(l[i1]) == tuple(l[i2]) == ...`

Return type `dict`

pad

- full name: `tenpy.tools.misc.pad`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.pad(a, w_l=0, v_l=0, w_r=0, v_r=0, axis=0)`
 Pad an array along a given *axis*.

Parameters

- **a** (*ndarray*) – the array to be padded
- **w_l** (*int*) – the width to be padded in the front
- **v_l** (*dtype*) – the value to be inserted before *a*
- **w_r** (*int*) – the width to be padded after the last index
- **v_r** (*dtype*) – the value to be inserted after *a*
- **axis** (*int*) – the axis along which to pad

Returns **padded** – a copy of *a* with enlarged *axis*, padded with the given values.

Return type `ndarray`

setup_executable

- full name: `tenpy.tools.misc.setup_executable`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.setup_executable(mod, run_defaults, identifier_list=None)`

Read command line arguments and turn into useable dicts.

Uses default values defined at: - model class for `model_par` - here for `sim_par` - executable file for `run_par`
Alternatively, a `model_defaults` dictionary and `identifier_list` can be supplied without the model

NB: for `setup_executable` to work with a model class, the model class needs to define two things:

- `defaults`, a static (class level) dictionary with (key, value) pairs that have the name of the parameter (as string) as key, and the default value as value.
- `identifier`, a static (class level) list or other iterable with the names of the parameters to be used in filename identifiers.

Parameters

- **mod** (*model | dict*) – Model class (or instance) OR a dictionary containing model defaults
- **run_defaults** (*dict*) – default values for executable file parameters
- **identifier_list** (*iterable, optional*) – variables

Returns containing all parameters. args | namespace with raw arguments for some backwards compatibility with executables.

Return type `model_par, sim_par, run_par` (dicts)

to_array

- full name: `tenpy.tools.misc.to_array`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.to_array(a, shape=None)`

Convert *a* to an numpy array and tile to matching dimension/shape.

This function provides similar functionality as `numpy.broadcast`, but not quite the same: Only scalars are broadcasted to higher dimensions, for a non-scalar, we require the number of dimension to match. If the shape does not match, we repeat periodically, e.g. we tile $(3, 4) \rightarrow (6, 16)$, but $(4, 4) \rightarrow (6, 16)$ will raise an error.

Parameters

- **a** (*scalar | array_like*) – The input to be converted to an array. A scalar is reshaped to the desired dimension.
- **shape** (*tuple of {None | int}*) – The desired shape of the array. An entry `None` indicates arbitrary len ≥ 1 . For int entries, tile the array periodically to fit the len.

Returns `a_array` – A copy of *a* converted to a numpy ndarray of desired dimension and shape.

Return type ndarray

to_iterable

- full name: `tenpy.tools.misc.to_iterable`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.to_iterable(a)`

If *a* is a not iterable or a string, return `[a]`, else return *a*.

to_iterable_of_len

- full name: `tenpy.tools.misc.to_iterable_of_len`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.to_iterable_of_len(a, L)`

If *a* is a non-string iterable of length *L*, return *a*, otherwise return `[a]*L`.

Raises `ValueError` if *a* is already an iterable of different length.

transpose_list_list

- full name: `tenpy.tools.misc.transpose_list_list`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.transpose_list_list(D, pad=None)`

Returns a list of lists *T*, such that $T[i][j] = D[j][i]$.

Parameters

- *D* (*list of list*) – to be transposed
- *pad* – Used to fill missing places, if *D* is not rectangular.

Returns *T* – transposed, rectangular version of *D*. constructed such that $T[i][j] = D[j][i]$ if $i < \text{len}(D[j])$ else *pad*

Return type list of lists

zero_if_close

- full name: `tenpy.tools.misc.zero_if_close`
- parent module: `tenpy.tools.misc`
- type: function

`tenpy.tools.misc.zero_if_close(a, tol=1e-15)`

set real and/or imaginary part to 0 if their absolute value is smaller than *tol*.

Parameters

- *a* (*ndarray*) – numpy array to be rounded
- *tol* (*float*) – the threshold which values to consider as ‘0’.

Module description

Miscellaneous tools, somewhat random mix yet often helpful.

7.11.4 math

- full name: `tenpy.tools.math`
- parent module: `tenpy.tools`
- type: module

Functions

<code>entropy(p[, n])</code>	Calculate the entropy of a distribution.
<code>gcd(a, b)</code>	Computes the greatest common divisor (GCD) of two numbers.
<code>gcd_array(a)</code>	Return the greatest common divisor of all of entries in <i>a</i>
<code>lcm(a, b)</code>	Returns the least common multiple (LCM) of two positive numbers.
<code>matvec_to_array(H)</code>	transform an linear operator with a <i>matvec</i> method into a dense numpy array.
<code>perm_sign(p)</code>	Given a permutation <i>p</i> of numbers, returns its sign.
<code>qr_li(A[, cutoff])</code>	QR decomposition with cutoff to discard nearly linear dependent columns in <i>Q</i> .
<code>rq_li(A[, cutoff])</code>	RQ decomposition with cutoff to discard nearly linear dependent columns in <i>Q</i> .
<code>speigs(A, k, *args, **kwargs)</code>	Wrapper around <code>scipy.sparse.linalg.eigs()</code> , lifting the restriction <code>k < rank(A) - 1</code> .
<code>speigsh(A, k, *args, **kwargs)</code>	Wrapper around <code>scipy.sparse.linalg.eigsh()</code> , lifting the restriction <code>k < rank(A) - 1</code> .

entropy

- full name: `tenpy.tools.math.entropy`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.entropy(p, n=1)`

Calculate the entropy of a distribution.

Assumes that *p* is a normalized distribution (`np.sum(p) == 1.`).

Parameters

- **p** (*1D array*) – A normalized distribution.
- **n** (*1 | float | np.inf*) – Selects the entropy, see below.

Returns **entropy** – Shannon-entropy – $\sum_i p_i \log(p_i)$ (*n*=1) or Renyi-entropy $\frac{1}{1-n} \log(\sum_i p_i^n)$ (*n* != 1) of the distribution *p*.

Return type `float`

gcd

- full name: `tenpy.tools.math.gcd`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.gcd(a, b)`

Computes the greatest common divisor (GCD) of two numbers.

Return 0 if both a, b are zero, otherwise always return a non-negative number.

gcd_array

- full name: `tenpy.tools.math.gcd_array`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.gcd_array(a)`

Return the greatest common divisor of all of entries in *a*

lcm

- full name: `tenpy.tools.math.lcm`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.lcm(a, b)`

Returns the least common multiple (LCM) of two positive numbers.

matvec_to_array

- full name: `tenpy.tools.math.matvec_to_array`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.matvec_to_array(H)`

transform an linear operator with a *matvec* method into a dense numpy array.

Parameters *H* (*linear operator*) – should have *shape*, *dtype* attributes and a *matvec* method.

Returns *H_dense* – a dense array version of *H*.

Return type ndarray, shape (H.dim, H.dim)

perm_sign

- full name: `tenpy.tools.math.perm_sign`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.perm_sign(p)`

Given a permutation p of numbers, returns its sign. (+1 or -1)

Assumes that all the elements are distinct, if not, you get crap.

Examples

```
>>> for p in itertools.permutations(range(3)):
...     print('{p!s}: {sign!s}'.format(p=p, sign=perm_sign(p)))
(0, 1, 2): 1
(0, 2, 1): -1
(1, 0, 2): -1
(1, 2, 0): 1
(2, 0, 1): 1
(2, 1, 0): -1
```

qr_li

- full name: `tenpy.tools.math.qr_li`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.qr_li(A, cutoff=1e-15)`

QR decomposition with cutoff to discard nearly linear dependent columns in Q .

Perform a QR decomposition with pivoting, discard columns where $R[i, i] < \text{cutoff}$, reverse the permutation from pivoting and perform another QR decomposition to ensure that R is upper right.

Parameters A (`numpy.ndarray`) – Matrix to be decomposed as $A = Q \cdot R$

Returns Q, R – Decomposition of A into isometry $Q^d Q = I$ and upper right R with diagonal entries larger than *cutoff*.

Return type `numpy.ndarray`

rq_li

- full name: `tenpy.tools.math.rq_li`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.rq_li(A, cutoff=1e-15)`

RQ decomposition with cutoff to discard nearly linear dependent columns in Q .

Uses `qr_li()` on tranpose of A . Note that R is nonzero in the lowest left corner; R has entries below the diagonal for non-square R .

Parameters **A** (`numpy.ndarray`) – Matrix to be decomposed as $A = Q \cdot R$

Returns **R, Q** – Decomposition of A into isometry Q $Q^d = I$ and upper right R with diagonal entries larger than *cutoff*. If $M, N = A.shape$, then $R.shape = M, K$ and $Q.shape = K, N$ with $K \leq \min(M, N)$.

Return type `numpy.ndarray`

speigs

- full name: `tenpy.tools.math.speigs`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.speigs(A, k, *args, **kwargs)`

Wrapper around `scipy.sparse.linalg.eigs()`, lifting the restriction $k < \text{rank}(A) - 1$.

Parameters

- **A** ($M \times M$ ndarray or like `scipy.sparse.linalg.LinearOperator`) – the (square) linear operator for which the eigenvalues should be computed.
- **k** (`int`) – the number of eigenvalues to be computed.
- ***args** – Further arguments directly given to `scipy.sparse.linalg.eigs()`
- ****kwargs** – Further keyword arguments directly given to `scipy.sparse.linalg.eigs()`

Returns

- **w** (`ndarray`) – array of $\min(k, A.shape[0])$ eigenvalues
- **v** (`ndarray`) – array of $\min(k, A.shape[0])$ eigenvectors, $v[:, i]$ is the i -th eigenvector. Only returned if `kwargs['return_eigenvectors'] == True`.

speigsh

- full name: `tenpy.tools.math.speigsh`
- parent module: `tenpy.tools.math`
- type: function

`tenpy.tools.math.speigsh(A, k, *args, **kwargs)`

Wrapper around `scipy.sparse.linalg.eigsh()`, lifting the restriction $k < \text{rank}(A) - 1$.

Parameters

- **A** ($M \times M$ ndarray or like `scipy.sparse.linalg.LinearOperator`) – The (square) hermitian linear operator for which the eigenvalues should be computed.
- **k** (`int`) – The number of eigenvalues to be computed.
- ***args** – Further arguments directly given to `scipy.sparse.linalg.eigsh()`.
- ****kwargs** – Further keyword arguments directly given to `scipy.sparse.linalg.eigsh()`.

Returns

- **w** (`ndarray`) – Array of $\min(k, A.shape[0])$ eigenvalues.

- **v** (*ndarray*) – Array of $\min(k, A.\text{shape}[0])$ eigenvectors, $v[:, i]$ is the i -th eigenvector. Only returned if `kwargs['return_eigenvectors'] == True`.

Module description

Different math functions needed at some point in the library.

```
tenpy.tools.math.LeviCivita3 = array([[ 0, 0, 0], [ 0, 0, 1], [ 0, -1, 0]], [[ 0, 0, -1],  
    Levi-Civita Symbol of int type
```

7.11.5 fit

- full name: `tenpy.tools.fit`
- parent module: `tenpy.tools`
- type: module

Functions

<code>alg_decay(x, a, b, c)</code>	define the algebraic decay.
<code>alg_decay_fit(x, y[, npts, power_range, ...])</code>	Fit y to the form $a \cdot x^{**(-b)} + c$.
<code>alg_decay_fit_res(log_b, x, y)</code>	Returns the residue of an algebraic decay fit of the form $x^{**(-np.exp(log_b))}$.
<code>alg_decay_fits(x, ys[, npts, power_range, ...])</code>	Fit arrays of y 's to the form $a * x^{**(-b)} + c$.
<code>fit_with_sum_of_exp(f, n[, N])</code>	Approximate a decaying function f with a sum of exponentials.
<code>lin_fit_res(x, y)</code>	Returns the least-square residue of a linear fit y vs x .
<code>linear_fit(x, y)</code>	Perform a linear fit of y to $ax + b$.
<code>plot_alg_decay_fit(plot_module, x, y, fit_par)</code>	Given x , y , and <code>fit_par</code> (output from <code>alg_decay_fit</code>), produces a plot of the algebraic decay fit.
<code>sum_of_exp(lambdas, prefactors, x)</code>	Evaluate $\sum_i \text{prefactor}[i] * \text{lambda}[i] ** x$ for different x .

alg_decay

- full name: `tenpy.tools.fit.alg_decay`
- parent module: `tenpy.tools.fit`
- type: function

```
tenpy.tools.fit.alg_decay(x, a, b, c)  
    define the algebraic decay.
```

alg_decay_fit

- full name: `tenpy.tools.fit.alg_decay_fit`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.alg_decay_fit(x, y, npts=5, power_range=0.01, 4.0, power_mesh=[60, 10])`

Fit y to the form $a \cdot x^{**(-b)} + c$.

Returns a triplet $[a, b, c]$.

`npts` specifies the maximum number of points to fit. If `npts < len(x)`, then `alg_decay_fit()` will only fit to the last `npts` points. `power_range` is a tuple that gives that restricts the possible ranges for `b`. `power_mesh` is a list of numbers, which specifies how fine to search for the optimal `b`. E.g., if `power_mesh = [60, 10]`, then it'll first divide the `power_range` into 60 intervals, and then divide those intervals by 10.

alg_decay_fit_res

- full name: `tenpy.tools.fit.alg_decay_fit_res`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.alg_decay_fit_res(log_b, x, y)`

Returns the residue of an algebraic decay fit of the form $x^{**(-np.exp(log_b))}$.

alg_decay_fits

- full name: `tenpy.tools.fit.alg_decay_fits`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.alg_decay_fits(x, ys, npts=5, power_range=0.01, 4.0, power_mesh=[60, 10])`

Fit arrays of y 's to the form $a * x^{**(-b)} + c$.

Returns arrays of $[a, b, c]$.

fit_with_sum_of_exp

- full name: `tenpy.tools.fit.fit_with_sum_of_exp`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.fit_with_sum_of_exp(f, n, N=50)`

Approximate a decaying function f with a sum of exponentials.

MPOs can naturally represent long-range interactions with an exponential decay. A common technique for other (e.g. powerlaw) long-range interactions is to approximate them by sums of exponentials and to include them into the MPOs. This function allows to do that.

The algorithm/implementation follows the appendix of [Murg2010].

Parameters

- **f** (*function*) – Decaying function to be approximated. Needs to accept a 1D numpy array *x*
- **n** (*int*) – Number of exponentials to be used.
- **N** (*int*) – Number of points at which to evaluate/fit *f*; we evaluate and fit *f* at the points $x = \text{np.arange}(1, N+1)$.

Returns **lambdas, prefactors** – Such that $f(k) \approx \sum_i x_i \lambda_i^k$ for (integer) $1 \leq k \leq N$. The function `sum_of_exp()` evaluates this for given *x*.

Return type 1D arrays

lin_fit_res

- full name: `tenpy.tools.fit.lin_fit_res`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.lin_fit_res(x, y)`
Returns the least-square residue of a linear fit *y* vs *x*.

linear_fit

- full name: `tenpy.tools.fit.linear_fit`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.linear_fit(x, y)`
Perform a linear fit of *y* to *ax + b*.
Returns *a*, *b*, *res*.

plot_alg_decay_fit

- full name: `tenpy.tools.fit.plot_alg_decay_fit`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.plot_alg_decay_fit(plot_module, x, y, fit_par, xfunc=None, kwargs={}, plot_fit_args={})`

Given *x*, *y*, and *fit_par* (output from `alg_decay_fit`), produces a plot of the algebraic decay fit.

plot_module is `matplotlib.pyplot`, or a subplot. *x*, *y* are the data (real, 1-dimensional `np.ndarray`) *fit_par* is a triplet of numbers [*a*, *b*, *c*] that describes and algebraic decay (see `alg_decay()`). *xfunc* is an optional parameter that scales the *x*-axis in the resulting plot. *kwargs* is a dictionary, whoses key/items are passed to the plot function. *plot_fit_args* is a dictionary that controls how the fit is shown.

sum_of_exp

- full name: `tenpy.tools.fit.sum_of_exp`
- parent module: `tenpy.tools.fit`
- type: function

`tenpy.tools.fit.sum_of_exp(lambdas, prefactors, x)`

Evaluate $\sum_i \text{prefactor}[i] * \text{lambda}[i]**x$ for different x .

See `fit_sum_of_exp()` for more details.

Module description

tools to fit to an algebraic decay.

7.11.6 string

- full name: `tenpy.tools.string`
- parent module: `tenpy.tools`
- type: module

Functions

<code>is_non_string_iterable(x)</code>	Check if x is a non-string iterable, (e.g., list, tuple, dictionary, <code>np.ndarray</code>)
<code>to_mathematica_lists(a)</code>	convert nested a to string readable by mathematica using curly brackets <code>'{\...}'</code> .
<code>vert_join(strlist[, valign, halign, delim])</code>	Join strings with multilines vertically such that they appear next to each other.

is_non_string_iterable

- full name: `tenpy.tools.string.is_non_string_iterable`
- parent module: `tenpy.tools.string`
- type: function

`tenpy.tools.string.is_non_string_iterable(x)`

Check if x is a non-string iterable, (e.g., list, tuple, dictionary, `np.ndarray`)

to_mathematica_lists

- full name: `tenpy.tools.string.to_mathematica_lists`
- parent module: `tenpy.tools.string`
- type: function

`tenpy.tools.string.to_mathematica_lists(a)`
convert nested *a* to string readable by mathematica using curly brackets '{...}'.

vert_join

- full name: `tenpy.tools.string.vert_join`
- parent module: `tenpy.tools.string`
- type: function

`tenpy.tools.string.vert_join(strlist, valign='t', halign='l', delim='')`
Join strings with multilines vertically such that they appear next to each other.

Parameters

- **strlist** (*list of str*) – the strings to be joined vertically
- **valign** ('t', 'c', 'b') – vertical alignment of the strings: top, center, or bottom
- **halign** ('l', 'c', 'r') – horizontal alignment of the strings: left, center, or right
- **delim** (*str*) – field separator between the strings

Returns **joined** – a string where the strings of strlist are aligned vertically

Return type `str`

Examples

```
>>> print vert_join(['a\nsample\nmultiline\nstring', str(np.arange(9).reshape(3, 3))],
...                 delim=' | ')
a          | [[0 1 2]
sample     |  [3 4 5]
multiline  |  [6 7 8]]
string
```

Module description

Tools for handling strings.

7.11.7 process

- full name: `tenpy.tools.process`
- parent module: `tenpy.tools`
- type: module

Functions

<code>load_omp_library([libs, verbose])</code>	Tries to load openMP library.
<code>memory_usage()</code>	Return memory usage of the running python process.
<code>mkl_get_nthreads()</code>	wrapper around MKL <code>get_max_threads</code> .
<code>mkl_set_nthreads(n)</code>	wrapper around MKL <code>set_num_threads</code> .
<code>omp_get_nthreads()</code>	wrapper around OpenMP <code>get_max_threads</code> .
<code>omp_set_nthreads(n)</code>	wrapper around OpenMP <code>set_nthreads</code> .

load_omp_library

- full name: `tenpy.tools.process.load_omp_library`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.load_omp_library(libs=['libiomp5.so', None, 'libgomp.so.1'], verbose=True)`

Tries to load openMP library.

Parameters

- **libs** – list of possible library names we should try to load (with `ctypes.CDLL`).
- **verbose** (*bool*) – wheter to print the name of the loaded library.

Returns `omp` – OpenMP shared library if found, otherwise `None`. Once it was successfully imported, no re-imports are tried.

Return type `CDLL` | `None`

memory_usage

- full name: `tenpy.tools.process.memory_usage`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.memory_usage()`
Return memory usage of the running python process.

You can `pip install psutil` if you get only `-1..`

Returns `mem` – Currently used memory in megabytes. `-1.` if no way to read out.

Return type *float*

mkl_get_nthreads

- full name: `tenpy.tools.process.mkl_get_nthreads`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.mkl_get_nthreads()`
wrapper around MKL `get_max_threads`.

Returns `max_threads` – The maximum number of threads used by MKL. `-1` if unable to read out.

Return type `int`

mkl_set_nthreads

- full name: `tenpy.tools.process.mkl_set_nthreads`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.mkl_set_nthreads(n)`
wrapper around MKL `set_num_threads`.

Parameters `n (int)` – the number of threads to use

Returns `success` – whether the shared library was found and set.

Return type `bool`

omp_get_nthreads

- full name: `tenpy.tools.process.omp_get_nthreads`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.omp_get_nthreads()`
wrapper around OpenMP `get_max_threads`.

Returns `max_threads` – The maximum number of threads used by OpenMP (and thus MKL). `-1` if unable to read out.

Return type `int`

omp_set_nthreads

- full name: `tenpy.tools.process.omp_set_nthreads`
- parent module: `tenpy.tools.process`
- type: function

`tenpy.tools.process.omp_set_nthreads(n)`
wrapper around OpenMP `set_nthreads`.

Parameters `n (int)` – the number of threads to use

Returns `success` – whether the shared library was found and set.

Return type `bool`

Module description

Tools to read out total memory usage and get/set the number of threads.

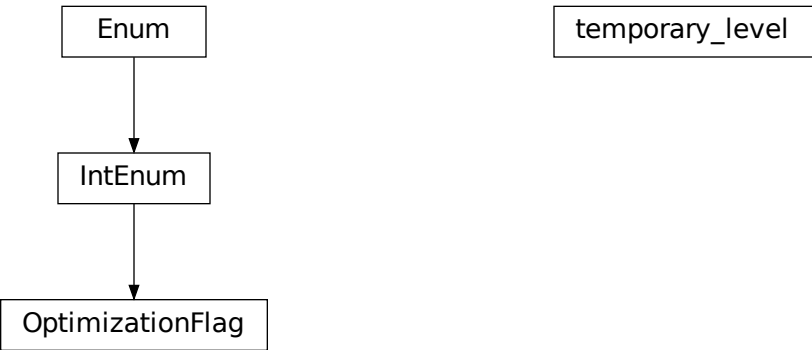
If your python is compiled against MKL (e.g. if you use *anaconda* as recommended in `INSTALL`), it will by default use as many threads as CPU cores are available. If you run a job on a cluster, you should limit this to the number of cores you reserved – otherwise your colleagues might get angry... A simple way to achieve this is to set a suitable environment variable before calling your python program, e.g. on the linux bash `export OMP_NUM_THREADS=4` for 4 threads. (MKL used OpenMP and thus respects its settings.)

Alternatively, this module provides `omp_get_nthreads()` and `omp_set_nthreads()`, which give their best to get and set the number of threads at runtime, while still being failsafe if the shared OpenMP library is not found. In the latter case, you might also try the equivalent `mkl_get_nthreads()` and `mkl_set_nthreads()`.

7.11.8 optimization

- full name: `tenpy.tools.optimization`
- parent module: `tenpy.tools`
- type: module

Classes

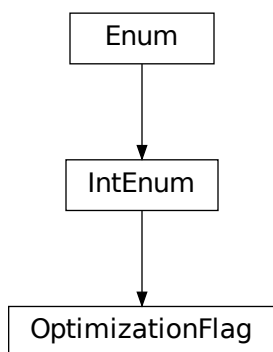


<code>OptimizationFlag</code>	Options for the global ‘optimization level’ used for dynamical optimizations.
<code>temporary_level(temporary_level)</code>	Context manager to temporarily set the optimization level to a different value.

OptimizationFlag

- full name: `tenpy.tools.optimization.OptimizationFlag`
- parent module: `tenpy.tools.optimization`
- type: class

Inheritance Diagram



Class Attributes and Properties

<code>OptimizationFlag.default</code>
<code>OptimizationFlag.none</code>
<code>OptimizationFlag.safe</code>
<code>OptimizationFlag.skip_arg_checks</code>

class `tenpy.tools.optimization.OptimizationFlag`

Bases: `enum.IntEnum`

Options for the global ‘optimization level’ used for dynamical optimizations.

Whether we optimize dynamically is decided by comparison of the global “optimization level” with one of the following flags. A higher level *includes* all the previous optimizations.

Level	Flag	Description
0	none	Don’t do any optimizations, i.e., run many sanity checks. Used for testing.
1	default	Skip really unnecessary sanity checks, but also don’t try any optional optimizations if they might give an overhead.
2	safe	Activate safe optimizations in algorithms, even if they might give a small overhead. Example: Try to compress the MPO representing the hamiltonian.
3	skip_arg_checks	Unsafe! Skip (some) class sanity tests and (function) argument checks.

Warning: When unsafe optimizations are enabled, errors will not be detected that easily, debugging is much harder, and you might even get segmentation faults in the compiled parts. Use this kind of optimization only for code which you successfully ran before with (very) similar parameters and disabled optimizations! Enable this optimization only during the parts of the code where it is really necessary. Check whether it actually helps - if it doesn't, keep the optimization disabled!

temporary_level

- full name: `tenpy.tools.optimization.temporary_level`
- parent module: `tenpy.tools.optimization`
- type: class

Inheritance Diagram

temporary_level

Methods

<code>temporary_level.__init__(temporary_level)</code>	Initialize self.
--	------------------

class `tenpy.tools.optimization.temporary_level` (*temporary_level*)

Bases: `object`

Context manager to temporarily set the optimization level to a different value.

Parameters `temporary_level` (*int* | *OptimizationFlag* | *str* | *None*) – The optimization level to be set during the context. *None* defaults to the current value of the optimization level.

temporary_level

The optimization level to be set during the context.

Type `None` | `OptimizationFlag`

_old_level

Optimization level to be restored at the end of the context manager.

Type *OptimizationFlag*

Examples

It is recommended to use this context manager in a `with` statement:

```
# optimization level default
with temporary_level(OptimizationFlag.safe):
    do_some_stuff() # temporarily have Optimization level `safe`
    # you can even change the optimization level to something else:
    set_level(OptimizationFlag.skip_args_check)
    do_some_really_heavy_stuff()
# here we are back to the optimization level as before the ``with ...`` statement
```

Functions

<code>get_level()</code>	Return the global optimization level.
<code>optimize([level_compare])</code>	Called by algorithms to check whether it should (try to) do some optimizations.
<code>set_level([level])</code>	Set the global optimization level.
<code>to_OptimizationFlag(level)</code>	Convert strings and int to a valid OptimizationFlag.
<code>use_cython([func, replacement, check_doc])</code>	Decorator to replace a function with a Cython-equivalent from <code>_npc_helper.pyx</code> .

get_level

- full name: `tenpy.tools.optimization.get_level`
- parent module: `tenpy.tools.optimization`
- type: function

`tenpy.tools.optimization.get_level()`
Return the global optimization level.

optimize

- full name: `tenpy.tools.optimization.optimize`
- parent module: `tenpy.tools.optimization`
- type: function

`tenpy.tools.optimization.optimize(level_compare=<OptimizationFlag.default: 1>)`
Called by algorithms to check whether it should (try to) do some optimizations.

Parameters `level_compare` (`OptimizationFlag`) – At which level to start optimization, i.e., how safe the suggested optimization is.

Returns `optimize` – True if the algorithms should try to optimize, i.e., whether the global “optimization level” is equal or higher than the level to compare to.

Return type `bool`

set_level

- full name: `tenpy.tools.optimization.set_level`
- parent module: `tenpy.tools.optimization`
- type: function

`tenpy.tools.optimization.set_level(level=1)`
Set the global optimization level.

Parameters `level` (`int` | `OptimizationFlag` | `str` | `None`) – The new global optimization level to be set. `None` defaults to keeping the current level.

to_OptimizationFlag

- full name: `tenpy.tools.optimization.to_OptimizationFlag`
- parent module: `tenpy.tools.optimization`
- type: function

`tenpy.tools.optimization.to_OptimizationFlag(level)`
Convert strings and int to a valid `OptimizationFlag`.
`None` defaults to the current level.

use_cython

- full name: `tenpy.tools.optimization.use_cython`
- parent module: `tenpy.tools.optimization`
- type: function

`tenpy.tools.optimization.use_cython(func=None, replacement=None, check_doc=True)`
Decorator to replace a function with a Cython-equivalent from `_npc_helper.pyx`.

This is a [decorator](#), which is supposed to be used in front of function definitions with an `@` sign, for example:

```
@use_cython
def my_slow_function(a):
    "some example function with slow python loops"
    result = 0.
    for i in range(a.shape[0]):
        for j in range(a.shape[1]):
            #... heavy calculations ...
            result += np.cos(a[i, j]**2) * (i + j)
    return result
```

This decorator indicates that there is a [Cython](#) implementation in the file `tenpy/linalg/_npc_helper.pyx`, which should have the same signature (i.e. same arguments and return values) as the decorated function, and can be used as a replacement for the decorated function. However, if the cython code could not be compiled on your system (or if the environment variable `TENPY_OPTIMIZE` is set to negative values, or the environment variable `TENPY_NO_CYTHON` is “true”), we just pass the previous function.

Note: In case that the decorator is used for a class method, the corresponding Cython version needs to have an `@cython.binding(True)`.

Parameters

- **func** (*function*) – The defined function
- **replacement** (*string* | *None*) – The name of the function defined in `tenpy/linalg/_npc_helper.pyx` which should replace the decorated function. *None* defaults to the name of the decorated function, e.g., in the above example `my_slow_function`.
- **check_doc** (*bool*) – If *True*, we check that the cython version of the function has the exact same doc string (up to a possible first line containing the function signature) to exclude typos and inconsistent versions.

Returns `replacement_func` – The function replacing the decorated function `func`. If the cython code can not be loaded, this is just `func`, otherwise it's the cython version specified by `replacement`.

Return type `function`

Module description

Optimization options for this library.

Let me start with a *quote* of “Micheal Jackson” (a programmer, not the musician):

```
First rule of optimization: "Don't do it."
Second rule of optimization (for experts only): "Don't do it yet."
Third rule of optimization: "Profile before optimizing."
```

Luckily, following the third optimization rule, namely profiling code, is fairly simple in python, see the [documentation](#). If you have a python skript running your code, you can simply call it with `python -m "cProfile" -s "tottime" your_skript.py`. Alternatively, save the profiling statistics with `python -m "cProfile" -o "profile_data.stat" your_skript.py` and run these few lines of python code:

```
import pstats
p = pstats.Pstats("profile_data.stat")
p.sort_stats('cumtime') # sort by 'cumtime' column
p.print_stats(30)      # prints first 30 entries
```

That being said, I actually did profile and optimize (parts of) the library; and there are a few knobs you can turn to tweak the most out of this library, explained in the following.

- 1) Simply install the ‘bottleneck’ python package, which allows to optimize slow parts of numpy, most notably ‘NaN’ checking.
- 2) Figure out which numpy/scipy/python you are using. As explained in [Installation instructions](#), we recommend to use the Python distributed provided by Intel or Anaconda. They ship with numpy and scipy which use Intels MKL library, such that e.g. `np.tensordot` is parallelized to use multiple cores.
- 3) In case you didn't do that yet: some parts of the library are written in both python and Cython with the same interface, so you can simply compile the Cython code, as explained in [Installation instructions](#). Then everything should work the same way from a user perspective, while internally the faster, pre-compiled cython code from `tenpy/linalg/_npc_helper.pyx` is used. This should also be a safe thing to do. The replacement of the optimized functions is done by the decorator `use_cython()`.
- 4) One of the great things about python is its dynamical nature - anything can be done at runtime. In that spirit, this module allows to set a global “optimization level” which can be changed *dynamically* (i.e., during runtime) with `set_level()`. The library will then try some extra optimization, most notably skip sanity checks of arguments. The possible choices for this global level are given by the [OptimizationFlag](#). The default initial value for the global optimization level can be adjusted by the environment variable `TENPY_OPTIMIZE`.

Warning: When this optimizing is enabled, we skip (some) sanity checks. Thus, errors will not be detected that easily, and debugging is much harder! We recommend to use this kind of optimization only for code which you successfully have run before with (very) similar parameters! Enable this optimization only during the parts of the code where it is really necessary. The context manager `temporary_level` can help with that. Check whether it actually helps - if it doesn't, keep the optimization disabled! Some parts of the library already do that as well (e.g. DMRG after the first sweep).

- 5) You might want to try some different compile time options for the cython code, set in the `setup.py` in the top directory of the repository. Since the `setup.py` reads out the `TENPY_OPTIMIZE` environment variable, you can simply use an `export TENPY_OPTIMIZE=3` (in your bash/terminal) right before compilation. An `export TENPY_OPTIMIZE=0` activates profiling hooks instead.

Warning: This increases the probability of getting segmentation faults and anyway might not help that much; in the crucial parts of the cython code, these optimizations are already applied. We do *not* recommend using this!

```
tenpy.tools.optimization.bottleneck = None
tenpy.tools.optimization.have_cython_functions = False
    bool whether the import of the cython file tenpy/linalg/_npc_helper.pyx succeeded.

    The value is set in the first call of use_cython().
```

7.12 version

- full name: `tenpy.version`
- parent module: `tenpy`
- type: module

Module description

Access to version of this library.

The version is provided in the standard python format `major.minor.revision` as string. Use `pkg_resources.parse_version` before comparing versions.

```
tenpy.version.version = '0.7.1'
    current release version as a string

tenpy.version.released = True
    whether this is a released version or modified

tenpy.version.short_version = 'v0.7.1'
    same as version, but with 'v' in front

tenpy.version.git_revision = '506268db713a329325860672e4fb5e18b3fd1f74'
    the hash of the last git commit (if available)

tenpy.version.full_version = '0.7.1'
    if not released additional info with part of git revision
```

```
tenpy.version.version_summary = 'tenpy 0.7.1 (not compiled), \ngit revision 506268db713a329'
summary of the tenpy, python, numpy and scipy versions used
```

INDICES AND TABLES

- [genindex](#)
- [modindex](#)
- [cfg-config-index](#)
- [cfg-option-index](#)
- [search](#)

BIBLIOGRAPHY

- [TeNPyNotes] “Efficient numerical simulations with Tensor Networks: Tensor Network Python (TeNPy)” J. Hauschild, F. Pollmann, SciPost Phys. Lect. Notes 5 (2018), [arXiv:1805.00055](#), [doi:10.21468/SciPostPhysLectNotes.5](#)
- [TeNPySource] <https://github.com/tenpy/tenpy>
- [TeNPyDoc] Online documentation, <https://tenpy.readthedocs.io/>
- [TeNPyForum] Community forum for discussions, FAQ and announcements, <https://tenpy.johannes-hauschild.de>
- [Cirac2009] “Renormalization and tensor product states in spin chains and lattices” J. I. Cirac and F. Verstraete, Journal of Physics A: Mathematical and Theoretical, 42, 50 (2009) [arXiv:0910.1130](#) [doi:10.1088/1751-8113/42/50/504004](#)
- [Verstraete2009] “Matrix Product States, Projected Entangled Pair States, and variational renormalization group methods for quantum spin systems” F. Verstraete and V. Murg and J.I. Cirac, Advances in Physics 57 2, 143-224 (2009) [arXiv:0907.2796](#) [doi:10.1080/14789940801912366](#)
- [Schollwoeck2011] “The density-matrix renormalization group in the age of matrix product states” U. Schollwoeck, Annals of Physics 326, 96 (2011), [arXiv:1008.3477](#) [doi:10.1016/j.aop.2010.09.012](#)
- [Stoudenmire2011] “Studying Two Dimensional Systems With the Density Matrix Renormalization Group” E.M. Stoudenmire, Steven R. White, Ann. Rev. of Cond. Mat. Physics, 3: 111-128 (2012), [arXiv:1105.1374](#) [doi:10.1146/annurev-conmatphys-020911-125018](#)
- [Eisert2013] “Entanglement and tensor network states” J. Eisert, Modeling and Simulation 3, 520 (2013) [arXiv:1308.3318](#)
- [Orus2014] “A Practical Introduction to Tensor Networks: Matrix Product States and Projected Entangled Pair States” R. Orus, Annals of Physics 349, 117-158 (2014) [arXiv:1306.2164](#) [doi:10.1016/j.aop.2014.06.013](#)
- [Hubig2019] “Time-evolution methods for matrix-product states” S. Paeckel, T. Köhler, A. Swoboda, S. R. Manmana, U. Schollwöck, C. Hubig, [arXiv:1901.05824](#)
- [White1992] “Density matrix formulation for quantum renormalization groups” S. White, Phys. Rev. Lett. 69, 2863 (1992) [doi:10.1103/PhysRevLett.69.2863](#), S. White, Phys. Rev. B 48, 10345 (1992) [doi:10.1103/PhysRevB.48.10345](#)
- [Vidal2004] “Efficient Simulation of One-Dimensional Quantum Many-Body Systems” G. Vidal, Phys. Rev. Lett. 93, 040502 (2004), [arXiv:quant-ph/0310089](#) [doi:10.1103/PhysRevLett.93.040502](#)
- [White2005] “Density matrix renormalization group algorithms with a single center site” S. White, Phys. Rev. B 72, 180403(R) (2005), [arXiv:cond-mat/0508709](#) [doi:10.1103/PhysRevB.72.180403](#)
- [Vidal2007] “Entanglement Renormalization” G. Vidal, Phys. Rev. Lett. 99, 220405 (2007), [arXiv:cond-mat/0512165](#), [doi:10.1103/PhysRevLett.99.220405](#)

- [McCulloch2008] “Infinite size density matrix renormalization group, revisited” I. P. McCulloch, [arXiv:0804.2509](#)
- [Singh2009] “Tensor network decompositions in the presence of a global symmetry” S. Singh, R. Pfeifer, G. Vidal, Phys. Rev. A 82, 050301(R), [arXiv:0907.2994](#) [doi:10.1103/PhysRevA.82.050301](#)
- [Stoudenmire2010] “Minimally Entangled Typical Thermal State Algorithms” E.M. Stoudenmire, Steven R. White, 2010 New J. Phys. 12, 055026, [arXiv:1002.1305](#) [doi:10.1088/1367-2630/12/5/055026](#)
- [Singh2010] “Tensor network states and algorithms in the presence of a global U(1) symmetry” S. Singh, R. Pfeifer, G. Vidal, Phys. Rev. B 83, 115125, [arXiv:1008.4774](#) [doi:10.1103/PhysRevB.83.115125](#)
- [Haegeman2011] “Time-Dependent Variational Principle for Quantum Lattices” J. Haegeman, J. I. Cirac, T. J. Osborne, I. Pizorn, H. Verschelde, F. Verstraete, Phys. Rev. Lett. 107, 070601 (2011), [arXiv:1103.0936](#) [doi:10.1103/PhysRevLett.107.070601](#)
- [Karrasch2013] “Reducing the numerical effort of finite-temperature density matrix renormalization group calculations” C. Karrasch, J. H. Bardarson, J. E. Moore, New J. Phys. 15, 083031 (2013), [arXiv:1303.3942](#) [doi:10.1088/1367-2630/15/8/083031](#)
- [Zaletel2015] “Time-evolving a matrix product state with long-ranged interactions” M. P. Zaletel, R. S. K. Mong, C. Karrasch, J. E. Moore, F. Pollmann, Phys. Rev. B 91, 165112 (2015), [arXiv:1407.1832](#) [doi:10.1103/PhysRevB.91.165112](#)
- [Hubig2015] “Strictly single-site DMRG algorithm with subspace expansion” C. Hubig, I. P. McCulloch, U. Schollwoeck, F. A. Wolf, Phys. Rev. B 91, 155115 (2015), [arXiv:1501.05504](#) [doi:10.1103/PhysRevB.91.155115](#)
- [Haegeman2016] “Unifying time evolution and optimization with matrix product states” J. Haegeman, C. Lubich, I. Oseledets, B. Vandereycken, F. Verstraete, Phys. Rev. B 94, 165116 (2016), [arXiv:1408.5056](#) [doi:10.1103/PhysRevB.94.165116](#)
- [Hauschild2018] “Finding purifications with minimal entanglement” J. Hauschild, E. Leviatan, J. H. Bardarson, E. Altman, M. P. Zaletel, F. Pollmann, Phys. Rev. B 98, 235163 (2018), [arXiv:1711.01288](#) [doi:10.1103/PhysRevB.98.235163](#)
- [Suzuki1991] “General theory of fractal path integrals with applications to many-body theories and statistical physics”, M. Suzuki, Journal of Mathematical Physics 32, 400 (1991); [doi:10.1063/1.529425](#)
- [Resta1997] “Quantum-Mechanical Position Operator in Extended Systems” R. Resta, Phys. Rev. Lett. 80, 1800 (1997) [doi:10.1103/PhysRevLett.80.1800](#)
- [Murg2010] “Matrix product operator representations” V. Murg, J.I. Cirac, B. Pirvu, F. Verstraete, New J. Phys. 12 025012 (2010), [arXiv:0804.3976](#), [doi:10.1088/1367-2630/12/2/025012](#)
- [Neupert2011] “Fractional quantum Hall states at zero magnetic field” T. Neupert, L. Santos, C. Chamon, and C. Mudry, Phys. Rev. Lett. 106, 236804 (2011), [arXiv:1012.4723](#) [doi:10.1103/PhysRevLett.106.236804](#)
- [Yang2012] “Topological flat band models with arbitrary Chern numbers” Shuo Yang, Zheng-Cheng Gu, Kai Sun, and S. Das Sarma, Phys. Rev. B 86, 241112(R) (2012), [arXiv:1205.5792](#), [doi:10.1103/PhysRevB.86.241112](#)
- [CincioVidal2013] “Characterizing Topological Order by Studying the Ground States on an Infinite Cylinder” L. Cincio, G. Vidal, Phys. Rev. Lett. 110, 067208 (2013), [arXiv:1208.2623](#) [doi:10.1103/PhysRevLett.110.067208](#)
- [Schuch2013] “Condensed Matter Applications of Entanglement Theory” N. Schuch, Quantum Information Processing. Lecture Notes of the 44th IFF Spring School (2013) [arXiv:1306.5551](#)
- [PollmannTurner2012] “Detection of symmetry-protected topological phases in one dimension” F. Pollmann, A. Turner, Phys. Rev. B 86, 125441 (2012), [arXiv:1204.0704](#) [doi:10.1103/PhysRevB.86.125441](#)
- [Grushin2015] “Characterization and stability of a fermionic $\nu=1/3$ fractional Chern insulator” A. G. Grushin, J. Motruk, M. P. Zaletel, and F. Pollmann, Phys. Rev. B 91, 035136 (2015), [arXiv:1407.6985](#) [doi:10.1103/PhysRevB.91.035136](#)

- [Barthel2020] “Optimized Lie–Trotter–Suzuki decompositions for two and three non-commuting terms” T. Barthel, Y. Zhang, *Annals of Physics* 418, 168165 (2020), [arXiv:1901.04974](https://arxiv.org/abs/1901.04974) doi:10.1016/j.aop.2020.168165
- [git] “git version control system”, <https://git-scm.com> A software which we use to keep track of changes in the source code.
- [conda] “conda package manger”, <https://docs.conda.io/en/latest/> A package and environment management system that allows to easily install (multiple version of) various software, and in particular python packages like TeNPy.
- [pip] “pip - the Python Package installer”, <https://pip.pypa.io/en/stable/> Traditional way to handle installed python packages with `pip install ...` and `pip uninstall ...` on the command line.
- [matplotlib] “Matplotlib”, <https://matplotlib.org/> A Python 2D plotting library. Some TeNPy functions expect `matplotlib.axes.Axes` as arguments to plot into.
- [HDF5] “Hierarchical Data Format 5 (R)”, <https://portal.hdfgroup.org/display/HDF5/HDF5> A file format and library for saving data (including metadata). We use it through the python interface of the *h5py* <<https://docs.h5py.org/en/stable/>>, see *Saving to disk: input/output*.

PYTHON MODULE INDEX

t

- tenpy, 131
- tenpy.algorithms, 132
 - tenpy.algorithms.dmrq, 170
 - tenpy.algorithms.exact_diag, 196
 - tenpy.algorithms.mpo_evolution, 190
 - tenpy.algorithms.mps_common, 145
 - tenpy.algorithms.network_contractor, 192
 - tenpy.algorithms.purification, 189
 - tenpy.algorithms.tdvp, 174
 - tenpy.algorithms.tebd, 137
 - tenpy.algorithms.truncation, 136
- tenpy.linalg, 196
 - tenpy.linalg.charges, 250
 - tenpy.linalg.lanczos, 275
 - tenpy.linalg.np_conserved, 227
 - tenpy.linalg.random_matrix, 255
 - tenpy.linalg.sparse, 273
 - tenpy.linalg.svd_robust, 252
- tenpy.models, 275
 - tenpy.models.fermions_spinless, 439
 - tenpy.models.haldane, 463
 - tenpy.models.hofstadter, 462
 - tenpy.models.hubbard, 460
 - tenpy.models.lattice, 367
 - tenpy.models.model, 393
 - tenpy.models.spins, 427
 - tenpy.models.spins_nnn, 428
 - tenpy.models.tf_ising, 405
 - tenpy.models.toric_code, 473
 - tenpy.models.xx_z_chain, 416
- tenpy.networks, 473
 - tenpy.networks.mpo, 530
 - tenpy.networks.mps, 518
 - tenpy.networks.purification_mps, 545
 - tenpy.networks.site, 507
 - tenpy.networks.terms, 544
- tenpy.tools, 547
 - tenpy.tools.fit, 579
 - tenpy.tools.hdf5_io, 560
 - tenpy.tools.math, 576
 - tenpy.tools.misc, 572
 - tenpy.tools.optimization, 588
 - tenpy.tools.params, 565
 - tenpy.tools.process, 583
 - tenpy.tools.string, 580
 - tenpy.version, 589

CONFIG INDEX

B

BoseHubbardModel, ??
BosonicHaldaneModel, ??

C

Config, ??
CouplingMPOModel, ??

D

DMRG, ??
DMRGEngine, ??

E

ExpMPOEvolution, ??

F

FermiHubbardModel, ??
FermionicHaldaneModel, ??
FermionModel, ??

H

HofstadterBosons, ??
HofstadterFermions, ??

L

Lanczos, ??
LanczosEvolution, ??

M

Mixer, ??
MPS_compress (*master*), ??
MPS_compress, ??
MPS_compress, ??

R

RandomUnitaryEvolution, ??

S

SingleSiteDMRGEngine, ??
SpinChainNNN, ??
SpinChainNNN2, ??

SpinModel, ??

Sweep, ??

T

TDVP, ??
TEBD, ??
TFIModel, ??
ToricCode, ??
truncation, ??
TwoSiteDMRGEngine, ??

V

VariationalApplyMPO, ??
VariationalCompression, ??

X

XXZChain, ??

Z

zip_up, ??

CONFIG OPTION INDEX

BoseHubbardModel

`bc_MPS` (*multiple definitions*), 437
`bc_MPS` (*FermionChain.init_lattice*), 437
`bc_MPS` (*FermionModel.init_lattice*), ??
`bc_MPS` (*BosonicHaldaneModel.init_lattice*), ??
`bc_MPS` (*FermionicHaldaneModel.init_lattice*), ??
`bc_MPS` (*HofstadterBosons.init_lattice*), ??
`bc_MPS` (*HofstadterFermions.init_lattice*), ??
`bc_MPS` (*BoseHubbardChain.init_lattice*), 449
`bc_MPS` (*BoseHubbardModel.init_lattice*), ??
`bc_MPS` (*FermiHubbardChain.init_lattice*), 459
`bc_MPS` (*FermiHubbardModel.init_lattice*), ??
`bc_MPS` (*CouplingMPOModel.init_lattice*), ??
`bc_MPS` (*SpinChain.init_lattice*), 425
`bc_MPS` (*SpinModel.init_lattice*), ??
`bc_MPS` (*SpinChainNNN.init_lattice*), ??
`bc_MPS` (*SpinChainNNN2.init_lattice*), ??
`bc_MPS` (*TFIChain.init_lattice*), 403
`bc_MPS` (*TFIModel.init_lattice*), ??
`bc_MPS` (*ToricCode.init_lattice*), ??
`bc_MPS` (*XXZChain2.init_lattice*), 415
`bc_x` (*multiple definitions*), 438
`bc_x` (*FermionChain.init_lattice*), 438
`bc_x` (*FermionModel.init_lattice*), ??
`bc_x` (*BosonicHaldaneModel.init_lattice*), ??
`bc_x` (*FermionicHaldaneModel.init_lattice*), ??
`bc_x` (*HofstadterBosons.init_lattice*), ??
`bc_x` (*HofstadterFermions.init_lattice*), ??
`bc_x` (*BoseHubbardChain.init_lattice*), 449
`bc_x` (*BoseHubbardModel.init_lattice*), ??
`bc_x` (*FermiHubbardChain.init_lattice*), 459
`bc_x` (*FermiHubbardModel.init_lattice*), ??
`bc_x` (*CouplingMPOModel.init_lattice*), ??
`bc_x` (*SpinChain.init_lattice*), 426
`bc_x` (*SpinModel.init_lattice*), ??
`bc_x` (*SpinChainNNN.init_lattice*), ??
`bc_x` (*SpinChainNNN2.init_lattice*), ??
`bc_x` (*TFIChain.init_lattice*), 404
`bc_x` (*TFIModel.init_lattice*), ??
`bc_x` (*ToricCode.init_lattice*), ??
`bc_x` (*XXZChain2.init_lattice*), 415
`bc_y` (*multiple definitions*), 438
`bc_y` (*FermionChain.init_lattice*), 438
`bc_y` (*FermionModel.init_lattice*), ??
`bc_y` (*BosonicHaldaneModel.init_lattice*), ??
`bc_y` (*FermionicHaldaneModel.init_lattice*), ??
`bc_y` (*HofstadterBosons.init_lattice*), ??
`bc_y` (*HofstadterFermions.init_lattice*), ??
`bc_y` (*BoseHubbardChain.init_lattice*), 449
`bc_y` (*BoseHubbardModel.init_lattice*), ??
`bc_y` (*FermiHubbardChain.init_lattice*), 459
`bc_y` (*FermiHubbardModel.init_lattice*), ??
`bc_y` (*CouplingMPOModel.init_lattice*), ??
`bc_y` (*SpinChain.init_lattice*), 425
`bc_y` (*SpinModel.init_lattice*), ??
`bc_y` (*SpinChainNNN.init_lattice*), ??
`bc_y` (*SpinChainNNN2.init_lattice*), ??
`bc_y` (*TFIChain.init_lattice*), 404
`bc_y` (*TFIModel.init_lattice*), ??
`bc_y` (*ToricCode.init_lattice*), ??
`bc_y` (*XXZChain2.init_lattice*), 415
`conserve` (*BoseHubbardModel*), ??
`explicit_plus_hc` (*CouplingMPOModel*), ??
`filling` (*BoseHubbardModel*), ??
`L` (*multiple definitions*), 437
`L` (*FermionChain.init_lattice*), 437
`L` (*FermionModel.init_lattice*), ??
`L` (*BosonicHaldaneModel.init_lattice*), ??
`L` (*FermionicHaldaneModel.init_lattice*), ??
`L` (*HofstadterBosons.init_lattice*), ??
`L` (*HofstadterFermions.init_lattice*), ??
`L` (*BoseHubbardChain.init_lattice*), 449
`L` (*BoseHubbardModel.init_lattice*), ??
`L` (*FermiHubbardChain.init_lattice*), 459
`L` (*FermiHubbardModel.init_lattice*), ??
`L` (*CouplingMPOModel.init_lattice*), ??
`L` (*SpinChain.init_lattice*), 425
`L` (*SpinModel.init_lattice*), ??
`L` (*SpinChainNNN.init_lattice*), ??
`L` (*SpinChainNNN2.init_lattice*), ??
`L` (*TFIChain.init_lattice*), 403
`L` (*TFIModel.init_lattice*), ??
`L` (*ToricCode.init_lattice*), ??
`L` (*XXZChain2.init_lattice*), 415

lattice (multiple definitions), 437
 lattice (FermionChain.init_lattice), 437
 lattice (FermionModel.init_lattice), ??
 lattice (BosonicHaldaneModel.init_lattice), ??
 lattice (FermionicHaldaneModel.init_lattice), ??
 lattice (HofstadterBosons.init_lattice), ??
 lattice (HofstadterFermions.init_lattice), ??
 lattice (BoseHubbardChain.init_lattice), 449
 lattice (BoseHubbardModel.init_lattice), ??
 lattice (FermiHubbardChain.init_lattice), 459
 lattice (FermiHubbardModel.init_lattice), ??
 lattice (CouplingMPOModel.init_lattice), ??
 lattice (SpinChain.init_lattice), 425
 lattice (SpinModel.init_lattice), ??
 lattice (SpinChainNNN.init_lattice), ??
 lattice (SpinChainNNN2.init_lattice), ??
 lattice (TFIChain.init_lattice), 403
 lattice (TFIModel.init_lattice), ??
 lattice (ToricCode.init_lattice), ??
 lattice (XXZChain2.init_lattice), 415
 Lx (multiple definitions), 437
 Lx (FermionChain.init_lattice), 437
 Lx (FermionModel.init_lattice), ??
 Lx (BosonicHaldaneModel.init_lattice), ??
 Lx (FermionicHaldaneModel.init_lattice), ??
 Lx (HofstadterBosons.init_lattice), ??
 Lx (HofstadterFermions.init_lattice), ??
 Lx (BoseHubbardChain.init_lattice), 449
 Lx (BoseHubbardModel.init_lattice), ??
 Lx (FermiHubbardChain.init_lattice), 459
 Lx (FermiHubbardModel.init_lattice), ??
 Lx (CouplingMPOModel.init_lattice), ??
 Lx (SpinChain.init_lattice), 425
 Lx (SpinModel.init_lattice), ??
 Lx (SpinChainNNN.init_lattice), ??
 Lx (SpinChainNNN2.init_lattice), ??
 Lx (TFIChain.init_lattice), 403
 Lx (TFIModel.init_lattice), ??
 Lx (ToricCode.init_lattice), ??
 Lx (XXZChain2.init_lattice), 415
 Ly (multiple definitions), 438
 Ly (FermionChain.init_lattice), 438
 Ly (FermionModel.init_lattice), ??
 Ly (BosonicHaldaneModel.init_lattice), ??
 Ly (FermionicHaldaneModel.init_lattice), ??
 Ly (HofstadterBosons.init_lattice), ??
 Ly (HofstadterFermions.init_lattice), ??
 Ly (BoseHubbardChain.init_lattice), 449
 Ly (BoseHubbardModel.init_lattice), ??
 Ly (FermiHubbardChain.init_lattice), 459
 Ly (FermiHubbardModel.init_lattice), ??
 Ly (CouplingMPOModel.init_lattice), ??
 Ly (SpinChain.init_lattice), 425
 Ly (SpinModel.init_lattice), ??

Ly (SpinChainNNN.init_lattice), ??
 Ly (SpinChainNNN2.init_lattice), ??
 Ly (TFIChain.init_lattice), 404
 Ly (TFIModel.init_lattice), ??
 Ly (ToricCode.init_lattice), ??
 Ly (XXZChain2.init_lattice), 415
 mu (BoseHubbardModel), ??
 n_max (BoseHubbardModel), ??
 order (multiple definitions), 437
 order (FermionChain.init_lattice), 437
 order (FermionModel.init_lattice), ??
 order (BosonicHaldaneModel.init_lattice), ??
 order (FermionicHaldaneModel.init_lattice), ??
 order (HofstadterBosons.init_lattice), ??
 order (HofstadterFermions.init_lattice), ??
 order (BoseHubbardChain.init_lattice), 449
 order (BoseHubbardModel.init_lattice), ??
 order (FermiHubbardChain.init_lattice), 459
 order (FermiHubbardModel.init_lattice), ??
 order (CouplingMPOModel.init_lattice), ??
 order (SpinChain.init_lattice), 425
 order (SpinModel.init_lattice), ??
 order (SpinChainNNN.init_lattice), ??
 order (SpinChainNNN2.init_lattice), ??
 order (TFIChain.init_lattice), 403
 order (TFIModel.init_lattice), ??
 order (ToricCode.init_lattice), ??
 order (XXZChain2.init_lattice), 415
 sort_mpo_legs (CouplingMPOModel), ??
 t (BoseHubbardModel), ??
 U (BoseHubbardModel), ??
 V (BoseHubbardModel), ??
 verbose (Config), ??

BosonicHaldaneModel

bc_MPS (multiple definitions), 437
 bc_MPS (FermionChain.init_lattice), 437
 bc_MPS (FermionModel.init_lattice), ??
 bc_MPS (BosonicHaldaneModel.init_lattice), ??
 bc_MPS (FermionicHaldaneModel.init_lattice), ??
 bc_MPS (HofstadterBosons.init_lattice), ??
 bc_MPS (HofstadterFermions.init_lattice), ??
 bc_MPS (BoseHubbardChain.init_lattice), 449
 bc_MPS (BoseHubbardModel.init_lattice), ??
 bc_MPS (FermiHubbardChain.init_lattice), 459
 bc_MPS (FermiHubbardModel.init_lattice), ??
 bc_MPS (CouplingMPOModel.init_lattice), ??
 bc_MPS (SpinChain.init_lattice), 425
 bc_MPS (SpinModel.init_lattice), ??
 bc_MPS (SpinChainNNN.init_lattice), ??
 bc_MPS (SpinChainNNN2.init_lattice), ??
 bc_MPS (TFIChain.init_lattice), 403
 bc_MPS (TFIModel.init_lattice), ??
 bc_MPS (ToricCode.init_lattice), ??

bc_MPS (XXZChain2.init_lattice), 415
 bc_x (multiple definitions), 438
 bc_x (FermionChain.init_lattice), 438
 bc_x (FermionModel.init_lattice), ??
 bc_x (BosonicHaldaneModel.init_lattice), ??
 bc_x (FermionicHaldaneModel.init_lattice), ??
 bc_x (HofstadterBosons.init_lattice), ??
 bc_x (HofstadterFermions.init_lattice), ??
 bc_x (BoseHubbardChain.init_lattice), 449
 bc_x (BoseHubbardModel.init_lattice), ??
 bc_x (FermiHubbardChain.init_lattice), 459
 bc_x (FermiHubbardModel.init_lattice), ??
 bc_x (CouplingMPOModel.init_lattice), ??
 bc_x (SpinChain.init_lattice), 426
 bc_x (SpinModel.init_lattice), ??
 bc_x (SpinChainNNN.init_lattice), ??
 bc_x (SpinChainNNN2.init_lattice), ??
 bc_x (TFIChain.init_lattice), 404
 bc_x (TFIModel.init_lattice), ??
 bc_x (ToricCode.init_lattice), ??
 bc_x (XXZChain2.init_lattice), 415
 bc_y (multiple definitions), 438
 bc_y (FermionChain.init_lattice), 438
 bc_y (FermionModel.init_lattice), ??
 bc_y (BosonicHaldaneModel.init_lattice), ??
 bc_y (FermionicHaldaneModel.init_lattice), ??
 bc_y (HofstadterBosons.init_lattice), ??
 bc_y (HofstadterFermions.init_lattice), ??
 bc_y (BoseHubbardChain.init_lattice), 449
 bc_y (BoseHubbardModel.init_lattice), ??
 bc_y (FermiHubbardChain.init_lattice), 459
 bc_y (FermiHubbardModel.init_lattice), ??
 bc_y (CouplingMPOModel.init_lattice), ??
 bc_y (SpinChain.init_lattice), 425
 bc_y (SpinModel.init_lattice), ??
 bc_y (SpinChainNNN.init_lattice), ??
 bc_y (SpinChainNNN2.init_lattice), ??
 bc_y (TFIChain.init_lattice), 404
 bc_y (TFIModel.init_lattice), ??
 bc_y (ToricCode.init_lattice), ??
 bc_y (XXZChain2.init_lattice), 415
 conserve (BosonicHaldaneModel), ??
 explicit_plus_hc (CouplingMPOModel), ??
 L (multiple definitions), 437
 L (FermionChain.init_lattice), 437
 L (FermionModel.init_lattice), ??
 L (BosonicHaldaneModel.init_lattice), ??
 L (FermionicHaldaneModel.init_lattice), ??
 L (HofstadterBosons.init_lattice), ??
 L (HofstadterFermions.init_lattice), ??
 L (BoseHubbardChain.init_lattice), 449
 L (BoseHubbardModel.init_lattice), ??
 L (FermiHubbardChain.init_lattice), 459
 L (FermiHubbardModel.init_lattice), ??
 L (CouplingMPOModel.init_lattice), ??
 L (SpinChain.init_lattice), 425
 L (SpinModel.init_lattice), ??
 L (SpinChainNNN.init_lattice), ??
 L (SpinChainNNN2.init_lattice), ??
 L (TFIChain.init_lattice), 403
 L (TFIModel.init_lattice), ??
 L (ToricCode.init_lattice), ??
 L (XXZChain2.init_lattice), 415
 Ly (multiple definitions), 438
 Ly (FermionChain.init_lattice), 438
 Ly (FermionModel.init_lattice), ??
 Ly (BosonicHaldaneModel.init_lattice), ??
 Ly (FermionicHaldaneModel.init_lattice), ??
 L (CouplingMPOModel.init_lattice), ??
 L (SpinChain.init_lattice), 425
 L (SpinModel.init_lattice), ??
 L (SpinChainNNN.init_lattice), ??
 L (SpinChainNNN2.init_lattice), ??
 L (TFIChain.init_lattice), 403
 L (TFIModel.init_lattice), ??
 L (ToricCode.init_lattice), ??
 L (XXZChain2.init_lattice), 415
 lattice (multiple definitions), 437
 lattice (FermionChain.init_lattice), 437
 lattice (FermionModel.init_lattice), ??
 lattice (BosonicHaldaneModel.init_lattice), ??
 lattice (FermionicHaldaneModel.init_lattice), ??
 lattice (HofstadterBosons.init_lattice), ??
 lattice (HofstadterFermions.init_lattice), ??
 lattice (BoseHubbardChain.init_lattice), 449
 lattice (BoseHubbardModel.init_lattice), ??
 lattice (FermiHubbardChain.init_lattice), 459
 lattice (FermiHubbardModel.init_lattice), ??
 lattice (CouplingMPOModel.init_lattice), ??
 lattice (SpinChain.init_lattice), 425
 lattice (SpinModel.init_lattice), ??
 lattice (SpinChainNNN.init_lattice), ??
 lattice (SpinChainNNN2.init_lattice), ??
 lattice (TFIChain.init_lattice), 403
 lattice (TFIModel.init_lattice), ??
 lattice (ToricCode.init_lattice), ??
 lattice (XXZChain2.init_lattice), 415
 Lx (multiple definitions), 437
 Lx (FermionChain.init_lattice), 437
 Lx (FermionModel.init_lattice), ??
 Lx (BosonicHaldaneModel.init_lattice), ??
 Lx (FermionicHaldaneModel.init_lattice), ??
 Lx (HofstadterBosons.init_lattice), ??
 Lx (HofstadterFermions.init_lattice), ??
 Lx (BoseHubbardChain.init_lattice), 449
 Lx (BoseHubbardModel.init_lattice), ??
 Lx (FermiHubbardChain.init_lattice), 459
 Lx (FermiHubbardModel.init_lattice), ??
 Lx (CouplingMPOModel.init_lattice), ??
 Lx (SpinChain.init_lattice), 425
 Lx (SpinModel.init_lattice), ??
 Lx (SpinChainNNN.init_lattice), ??
 Lx (SpinChainNNN2.init_lattice), ??
 Lx (TFIChain.init_lattice), 403
 Lx (TFIModel.init_lattice), ??
 Lx (ToricCode.init_lattice), ??
 Lx (XXZChain2.init_lattice), 415
 Ly (multiple definitions), 438
 Ly (FermionChain.init_lattice), 438
 Ly (FermionModel.init_lattice), ??
 Ly (BosonicHaldaneModel.init_lattice), ??
 Ly (FermionicHaldaneModel.init_lattice), ??

Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*BosonicHaldaneModel*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 t1 (*BosonicHaldaneModel*), ??
 t2 (*BosonicHaldaneModel*), ??
 V (*BosonicHaldaneModel*), ??
 verbose (*Config*), ??

Config

verbose (*Config*), ??

CouplingMPOModel

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449

bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 explicit_plus_hc (*CouplingMPOModel*), ??
 L (*multiple definitions*), 437

L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (multiple definitions), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (multiple definitions), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??

Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (multiple definitions), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 order (multiple definitions), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

DMRG

active_sites (*run*), ??
 chi_list (multiple definitions), ??
 chi_list (*DMRGEngine.reset_stats*), ??
 chi_list (*EngineCombine.reset_stats*), 154
 chi_list (*EngineFracture.reset_stats*), 162

`chi_list (SingleSiteDMRGEngine.reset_stats), ??`
`chi_list (TwoSiteDMRGEngine.reset_stats), ??`
`combine (Sweep), ??`
`diag_method (multiple definitions), ??`
`diag_method (DMRGEngine.run), ??`
`diag_method (DMRGEngine.diag), ??`
`diag_method (EngineCombine.diag), 151`
`diag_method (EngineCombine.run), 155`
`diag_method (EngineFracture.diag), 159`
`diag_method (EngineFracture.run), 163`
`diag_method (SingleSiteDMRGEngine.diag), ??`
`diag_method (SingleSiteDMRGEngine.run), ??`
`diag_method (TwoSiteDMRGEngine.diag), ??`
`diag_method (TwoSiteDMRGEngine.run), ??`
`E_tol_max (multiple definitions), ??`
`E_tol_max (DMRGEngine.run), ??`
`E_tol_max (EngineCombine.run), 155`
`E_tol_max (EngineFracture.run), 163`
`E_tol_max (SingleSiteDMRGEngine.run), ??`
`E_tol_max (TwoSiteDMRGEngine.run), ??`
`E_tol_min (multiple definitions), ??`
`E_tol_min (DMRGEngine.run), ??`
`E_tol_min (EngineCombine.run), 155`
`E_tol_min (EngineFracture.run), 163`
`E_tol_min (SingleSiteDMRGEngine.run), ??`
`E_tol_min (TwoSiteDMRGEngine.run), ??`
`E_tol_to_trunc (multiple definitions), ??`
`E_tol_to_trunc (DMRGEngine.run), ??`
`E_tol_to_trunc (EngineCombine.run), 155`
`E_tol_to_trunc (EngineFracture.run), 163`
`E_tol_to_trunc (SingleSiteDMRGEngine.run), ??`
`E_tol_to_trunc (TwoSiteDMRGEngine.run), ??`
`init_env_data (multiple definitions), ??`
`init_env_data (DMRGEngine.init_env), ??`
`init_env_data (EngineCombine.init_env), 153`
`init_env_data (EngineFracture.init_env), 160`
`init_env_data (SingleSiteDMRGEngine.init_env), ??`
`init_env_data (TwoSiteDMRGEngine.init_env), ??`
`init_env_data (Sweep.init_env), ??`
`lanczos_params (Sweep), ??`
`max_E_err (multiple definitions), ??`
`max_E_err (DMRGEngine.run), ??`
`max_E_err (EngineCombine.run), 155`
`max_E_err (EngineFracture.run), 163`
`max_E_err (SingleSiteDMRGEngine.run), ??`
`max_E_err (TwoSiteDMRGEngine.run), ??`
`max_hours (multiple definitions), ??`
`max_hours (DMRGEngine.run), ??`
`max_hours (EngineCombine.run), 155`
`max_hours (EngineFracture.run), 163`
`max_hours (SingleSiteDMRGEngine.run), ??`
`max_hours (TwoSiteDMRGEngine.run), ??`
`max_N_for_ED (multiple definitions), ??`
`max_N_for_ED (DMRGEngine.diag), ??`
`max_N_for_ED (EngineCombine.diag), 151`
`max_N_for_ED (EngineFracture.diag), 159`
`max_N_for_ED (SingleSiteDMRGEngine.diag), ??`
`max_N_for_ED (TwoSiteDMRGEngine.diag), ??`
`max_S_err (multiple definitions), ??`
`max_S_err (DMRGEngine.run), ??`
`max_S_err (EngineCombine.run), 155`
`max_S_err (EngineFracture.run), 163`
`max_S_err (SingleSiteDMRGEngine.run), ??`
`max_S_err (TwoSiteDMRGEngine.run), ??`
`max_sweeps (multiple definitions), ??`
`max_sweeps (DMRGEngine.run), ??`
`max_sweeps (EngineCombine.run), 155`
`max_sweeps (EngineFracture.run), 163`
`max_sweeps (SingleSiteDMRGEngine.run), ??`
`max_sweeps (TwoSiteDMRGEngine.run), ??`
`min_sweeps (multiple definitions), ??`
`min_sweeps (DMRGEngine.run), ??`
`min_sweeps (EngineCombine.run), 155`
`min_sweeps (EngineFracture.run), 163`
`min_sweeps (SingleSiteDMRGEngine.run), ??`
`min_sweeps (TwoSiteDMRGEngine.run), ??`
`mixer (multiple definitions), ??`
`mixer (SingleSiteDMRGEngine.mixer_activate), ??`
`mixer (EngineCombine.mixer_activate), 153`
`mixer (EngineFracture.mixer_activate), 161`
`mixer (TwoSiteDMRGEngine.mixer_activate), ??`
`mixer_params (multiple definitions), ??`
`mixer_params (SingleSiteDMRGEngine.mixer_activate), ??`
`mixer_params (EngineCombine.mixer_activate), 153`
`mixer_params (EngineFracture.mixer_activate), 161`
`mixer_params (TwoSiteDMRGEngine.mixer_activate), ??`
`N_sweeps_check (multiple definitions), ??`
`N_sweeps_check (DMRGEngine.run), ??`
`N_sweeps_check (EngineCombine.run), 155`
`N_sweeps_check (EngineFracture.run), 163`
`N_sweeps_check (SingleSiteDMRGEngine.run), ??`
`N_sweeps_check (TwoSiteDMRGEngine.run), ??`
`norm_tol (multiple definitions), ??`
`norm_tol (DMRGEngine.run), ??`
`norm_tol (EngineCombine.run), 155`
`norm_tol (EngineFracture.run), 163`
`norm_tol (SingleSiteDMRGEngine.run), ??`
`norm_tol (TwoSiteDMRGEngine.run), ??`
`norm_tol_iter (multiple definitions), ??`
`norm_tol_iter (DMRGEngine.run), ??`
`norm_tol_iter (EngineCombine.run), 156`
`norm_tol_iter (EngineFracture.run), 163`
`norm_tol_iter (SingleSiteDMRGEngine.run), ??`
`norm_tol_iter (TwoSiteDMRGEngine.run), ??`
`orthogonal_to (multiple definitions), ??`

orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 P_tol_max (*multiple definitions*), ??
 P_tol_max (*DMRGEngine.run*), ??
 P_tol_max (*EngineCombine.run*), 156
 P_tol_max (*EngineFracture.run*), 163
 P_tol_max (*SingleSiteDMRGEngine.run*), ??
 P_tol_max (*TwoSiteDMRGEngine.run*), ??
 P_tol_min (*multiple definitions*), ??
 P_tol_min (*DMRGEngine.run*), ??
 P_tol_min (*EngineCombine.run*), 156
 P_tol_min (*EngineFracture.run*), 163
 P_tol_min (*SingleSiteDMRGEngine.run*), ??
 P_tol_min (*TwoSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*multiple definitions*), ??
 P_tol_to_trunc (*DMRGEngine.run*), ??
 P_tol_to_trunc (*EngineCombine.run*), 156
 P_tol_to_trunc (*EngineFracture.run*), 163
 P_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*DMRGEngine.reset_stats*), ??
 sweep_0 (*EngineCombine.reset_stats*), 155
 sweep_0 (*EngineFracture.reset_stats*), 162
 sweep_0 (*SingleSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*TwoSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*Sweep*), ??
 update_env (*multiple definitions*), ??
 update_env (*DMRGEngine.run*), ??
 update_env (*EngineCombine.run*), 156
 update_env (*EngineFracture.run*), 163
 update_env (*SingleSiteDMRGEngine.run*), ??
 update_env (*TwoSiteDMRGEngine.run*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

DMRGEngine

chi_list (*multiple definitions*), ??
 chi_list (*DMRGEngine.reset_stats*), ??
 chi_list (*EngineCombine.reset_stats*), 154
 chi_list (*EngineFracture.reset_stats*), 162
 chi_list (*SingleSiteDMRGEngine.reset_stats*), ??
 chi_list (*TwoSiteDMRGEngine.reset_stats*), ??
 combine (*Sweep*), ??
 diag_method (*multiple definitions*), ??
 diag_method (*DMRGEngine.run*), ??
 diag_method (*DMRGEngine.diag*), ??
 diag_method (*EngineCombine.diag*), 151
 diag_method (*EngineCombine.run*), 155
 diag_method (*EngineFracture.diag*), 159
 diag_method (*EngineFracture.run*), 163
 diag_method (*SingleSiteDMRGEngine.diag*), ??
 diag_method (*SingleSiteDMRGEngine.run*), ??
 diag_method (*TwoSiteDMRGEngine.diag*), ??
 diag_method (*TwoSiteDMRGEngine.run*), ??
 E_tol_max (*multiple definitions*), ??
 E_tol_max (*DMRGEngine.run*), ??
 E_tol_max (*EngineCombine.run*), 155
 E_tol_max (*EngineFracture.run*), 163
 E_tol_max (*SingleSiteDMRGEngine.run*), ??
 E_tol_max (*TwoSiteDMRGEngine.run*), ??
 E_tol_min (*multiple definitions*), ??
 E_tol_min (*DMRGEngine.run*), ??
 E_tol_min (*EngineCombine.run*), 155
 E_tol_min (*EngineFracture.run*), 163
 E_tol_min (*SingleSiteDMRGEngine.run*), ??
 E_tol_min (*TwoSiteDMRGEngine.run*), ??
 E_tol_to_trunc (*multiple definitions*), ??
 E_tol_to_trunc (*DMRGEngine.run*), ??
 E_tol_to_trunc (*EngineCombine.run*), 155
 E_tol_to_trunc (*EngineFracture.run*), 163
 E_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 E_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??
 init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160
 init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 max_E_err (*multiple definitions*), ??
 max_E_err (*DMRGEngine.run*), ??
 max_E_err (*EngineCombine.run*), 155
 max_E_err (*EngineFracture.run*), 163
 max_E_err (*SingleSiteDMRGEngine.run*), ??
 max_E_err (*TwoSiteDMRGEngine.run*), ??
 max_hours (*multiple definitions*), ??
 max_hours (*DMRGEngine.run*), ??

max_hours (*EngineCombine.run*), 155
 max_hours (*EngineFracture.run*), 163
 max_hours (*SingleSiteDMRGEngine.run*), ??
 max_hours (*TwoSiteDMRGEngine.run*), ??
 max_N_for_ED (*multiple definitions*), ??
 max_N_for_ED (*DMRGEngine.diag*), ??
 max_N_for_ED (*EngineCombine.diag*), 151
 max_N_for_ED (*EngineFracture.diag*), 159
 max_N_for_ED (*SingleSiteDMRGEngine.diag*), ??
 max_N_for_ED (*TwoSiteDMRGEngine.diag*), ??
 max_S_err (*multiple definitions*), ??
 max_S_err (*DMRGEngine.run*), ??
 max_S_err (*EngineCombine.run*), 155
 max_S_err (*EngineFracture.run*), 163
 max_S_err (*SingleSiteDMRGEngine.run*), ??
 max_S_err (*TwoSiteDMRGEngine.run*), ??
 max_sweeps (*multiple definitions*), ??
 max_sweeps (*DMRGEngine.run*), ??
 max_sweeps (*EngineCombine.run*), 155
 max_sweeps (*EngineFracture.run*), 163
 max_sweeps (*SingleSiteDMRGEngine.run*), ??
 max_sweeps (*TwoSiteDMRGEngine.run*), ??
 min_sweeps (*multiple definitions*), ??
 min_sweeps (*DMRGEngine.run*), ??
 min_sweeps (*EngineCombine.run*), 155
 min_sweeps (*EngineFracture.run*), 163
 min_sweeps (*SingleSiteDMRGEngine.run*), ??
 min_sweeps (*TwoSiteDMRGEngine.run*), ??
 N_sweeps_check (*multiple definitions*), ??
 N_sweeps_check (*DMRGEngine.run*), ??
 N_sweeps_check (*EngineCombine.run*), 155
 N_sweeps_check (*EngineFracture.run*), 163
 N_sweeps_check (*SingleSiteDMRGEngine.run*), ??
 N_sweeps_check (*TwoSiteDMRGEngine.run*), ??
 norm_tol (*multiple definitions*), ??
 norm_tol (*DMRGEngine.run*), ??
 norm_tol (*EngineCombine.run*), 155
 norm_tol (*EngineFracture.run*), 163
 norm_tol (*SingleSiteDMRGEngine.run*), ??
 norm_tol (*TwoSiteDMRGEngine.run*), ??
 norm_tol_iter (*multiple definitions*), ??
 norm_tol_iter (*DMRGEngine.run*), ??
 norm_tol_iter (*EngineCombine.run*), 156
 norm_tol_iter (*EngineFracture.run*), 163
 norm_tol_iter (*SingleSiteDMRGEngine.run*), ??
 norm_tol_iter (*TwoSiteDMRGEngine.run*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??

P_tol_max (*multiple definitions*), ??
 P_tol_max (*DMRGEngine.run*), ??
 P_tol_max (*EngineCombine.run*), 156
 P_tol_max (*EngineFracture.run*), 163
 P_tol_max (*SingleSiteDMRGEngine.run*), ??
 P_tol_max (*TwoSiteDMRGEngine.run*), ??
 P_tol_min (*multiple definitions*), ??
 P_tol_min (*DMRGEngine.run*), ??
 P_tol_min (*EngineCombine.run*), 156
 P_tol_min (*EngineFracture.run*), 163
 P_tol_min (*SingleSiteDMRGEngine.run*), ??
 P_tol_min (*TwoSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*multiple definitions*), ??
 P_tol_to_trunc (*DMRGEngine.run*), ??
 P_tol_to_trunc (*EngineCombine.run*), 156
 P_tol_to_trunc (*EngineFracture.run*), 163
 P_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*DMRGEngine.reset_stats*), ??
 sweep_0 (*EngineCombine.reset_stats*), 155
 sweep_0 (*EngineFracture.reset_stats*), 162
 sweep_0 (*SingleSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*TwoSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*Sweep*), ??
 update_env (*multiple definitions*), ??
 update_env (*DMRGEngine.run*), ??
 update_env (*EngineCombine.run*), 156
 update_env (*EngineFracture.run*), 163
 update_env (*SingleSiteDMRGEngine.run*), ??
 update_env (*TwoSiteDMRGEngine.run*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

ExpMPOEvolution

start_time (*ExpMPOEvolution*), ??
 start_trunc_err (*ExpMPOEvolution*), ??
 trunc_params (*ExpMPOEvolution*), ??
 verbose (*Config*), ??

FermiHubbardModel

bc_MPS (*multiple definitions*), 437

bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (multiple definitions), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (multiple definitions), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 403
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 L (multiple definitions), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (multiple definitions), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (multiple definitions), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??

Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*FermiHubbardModel*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??

order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 t (*FermiHubbardModel*), ??
 U (*FermiHubbardModel*), ??
 verbose (*Config*), ??

FermionicHaldaneModel

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??

bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*FermionicHaldaneModel*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*FermionicHaldaneModel*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??

order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 t1 (*FermionicHaldaneModel*), ??
 t2 (*FermionicHaldaneModel*), ??
 V (*FermionicHaldaneModel*), ??
 verbose (*Config*), ??

FermionModel

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??

bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*FermionModel*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 J (*FermionModel*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459

lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*FermionModel*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??

order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 V (*FermionModel*), ??
 verbose (*Config*), ??

HofstadterBosons

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??

bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*HofstadterBosons*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 filling (*HofstadterBosons*), ??
 gauge (*HofstadterBosons*), ??
 Jx (*HofstadterBosons*), ??
 Jy (*HofstadterBosons*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), ??
 Lx (*HofstadterBosons*), ??
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), ??
 Ly (*HofstadterBosons*), ??
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??

Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*HofstadterBosons*), ??
 mx (*HofstadterBosons*), ??
 my (*HofstadterBosons*), ??
 Nmax (*HofstadterBosons*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 phi (*HofstadterBosons*), ??
 phi_ext (*HofstadterBosons*), ??
 sort_mpo_legs (*CouplingMPOModel*), ??
 U (*HofstadterBosons*), ??
 verbose (*Config*), ??

HofstadterFermions

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??

bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*HofstadterFermions*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 filling (*HofstadterFermions*), ??
 gauge (*HofstadterFermions*), ??
 Jx (*HofstadterFermions*), ??
 Jy (*HofstadterFermions*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??

L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (multiple definitions), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (multiple definitions), ??
 Lx (*HofstadterFermions*), ??
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (multiple definitions), ??
 Ly (*HofstadterFermions*), ??
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 mu (*HofstadterFermions*), ??
 mx (*HofstadterFermions*), ??
 my (*HofstadterFermions*), ??
 order (multiple definitions), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 phi (*HofstadterFermions*), ??
 phi_ext (*HofstadterFermions*), ??
 sort_mpo_legs (*CouplingMPOModel*), ??
 v (*HofstadterFermions*), ??
 verbose (*Config*), ??

Lanczos

cutoff (*LanczosGroundState*), ??
 E_shift (*LanczosGroundState*), ??
 E_tol (*LanczosGroundState*), ??
 min_gap (*LanczosGroundState*), ??
 N_cache (*LanczosGroundState*), ??
 N_max (*LanczosGroundState*), ??
 N_min (*LanczosGroundState*), ??
 P_tol (*LanczosGroundState*), ??
 reortho (*LanczosGroundState*), ??
 verbose (*Config*), ??

LanczosEvolution

cutoff (*LanczosGroundState*), ??
 E_shift (*LanczosGroundState*), ??
 E_tol (*multiple definitions*), ??
 E_tol (*LanczosEvolution*), ??
 E_tol (*LanczosGroundState*), ??
 min_gap (*multiple definitions*), ??
 min_gap (*LanczosEvolution*), ??
 min_gap (*LanczosGroundState*), ??
 N_cache (*LanczosGroundState*), ??
 N_max (*LanczosGroundState*), ??
 N_min (*LanczosGroundState*), ??
 P_tol (*LanczosGroundState*), ??
 reortho (*LanczosGroundState*), ??
 verbose (*Config*), ??

Mixer

amplitude (*Mixer*), ??
 decay (*Mixer*), ??
 disable_after (*Mixer*), ??
 verbose (*multiple definitions*), ??
 verbose (*Mixer*), ??
 verbose (*Config*), ??

MpoEvolution

approximation (*ExpMPOEvolution.run*), ??
 dt (*ExpMPOEvolution.run*), ??
 N_steps (*ExpMPOEvolution.run*), ??
 order (*ExpMPOEvolution.run*), ??

MPS_compress

combine (*Sweep*), ??
 compression_method (*multiple definitions*), ??
 compression_method (*MPS.compress*), ??
 compression_method (*PurificationMPS.compress*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??
 init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160

init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 N_sweeps (*VariationalCompression*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*multiple definitions*), ??
 trunc_params (*MPS.compress*), ??
 trunc_params (*PurificationMPS.compress*), ??
 trunc_params (*VariationalCompression*), ??
 trunc_params (*Sweep*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

RandomUnitaryEvolution

delta_tau_list (*multiple definitions*), 181
 delta_tau_list (*PurificationTEBD.run_GS*), 181
 delta_tau_list (*PurificationTEBD2.run_GS*), 186
 delta_tau_list (*Engine.run_GS*), ??
 delta_tau_list (*RandomUnitaryEvolution.run_GS*), ??
 dt (*multiple definitions*), 181
 dt (*PurificationTEBD.run*), 181
 dt (*PurificationTEBD2.run*), 186
 dt (*Engine.run*), ??
 N_steps (*multiple definitions*), ??
 N_steps (*RandomUnitaryEvolution*), ??
 N_steps (*PurificationTEBD.run*), 181
 N_steps (*PurificationTEBD.run_GS*), 181
 N_steps (*PurificationTEBD2.run*), 186
 N_steps (*PurificationTEBD2.run_GS*), 186
 N_steps (*Engine.run*), ??
 N_steps (*Engine.run_GS*), ??

N_steps (RandomUnitaryEvolution.run_GS), ??
order (multiple definitions), 181
order (PurificationTEBD.run), 181
order (PurificationTEBD.run_GS), 181
order (PurificationTEBD2.run), 186
order (PurificationTEBD2.run_GS), 186
order (Engine.run), ??
order (Engine.run_GS), ??
order (RandomUnitaryEvolution.run_GS), ??
start_time (Engine), ??
start_trunc_err (Engine), ??
trunc_params (multiple definitions), ??
trunc_params (RandomUnitaryEvolution), ??
trunc_params (Engine), ??
verbose (Config), ??

SingleSiteDMRGEngine

chi_list (multiple definitions), ??
chi_list (DMRGEngine.reset_stats), ??
chi_list (EngineCombine.reset_stats), 154
chi_list (EngineFracture.reset_stats), 162
chi_list (SingleSiteDMRGEngine.reset_stats), ??
chi_list (TwoSiteDMRGEngine.reset_stats), ??
combine (Sweep), ??
diag_method (multiple definitions), ??
diag_method (DMRGEngine.run), ??
diag_method (DMRGEngine.diag), ??
diag_method (EngineCombine.diag), 151
diag_method (EngineCombine.run), 155
diag_method (EngineFracture.diag), 159
diag_method (EngineFracture.run), 163
diag_method (SingleSiteDMRGEngine.diag), ??
diag_method (SingleSiteDMRGEngine.run), ??
diag_method (TwoSiteDMRGEngine.diag), ??
diag_method (TwoSiteDMRGEngine.run), ??
E_tol_max (multiple definitions), ??
E_tol_max (DMRGEngine.run), ??
E_tol_max (EngineCombine.run), 155
E_tol_max (EngineFracture.run), 163
E_tol_max (SingleSiteDMRGEngine.run), ??
E_tol_max (TwoSiteDMRGEngine.run), ??
E_tol_min (multiple definitions), ??
E_tol_min (DMRGEngine.run), ??
E_tol_min (EngineCombine.run), 155
E_tol_min (EngineFracture.run), 163
E_tol_min (SingleSiteDMRGEngine.run), ??
E_tol_min (TwoSiteDMRGEngine.run), ??
E_tol_to_trunc (multiple definitions), ??
E_tol_to_trunc (DMRGEngine.run), ??
E_tol_to_trunc (EngineCombine.run), 155
E_tol_to_trunc (EngineFracture.run), 163
E_tol_to_trunc (SingleSiteDMRGEngine.run), ??
E_tol_to_trunc (TwoSiteDMRGEngine.run), ??
init_env_data (multiple definitions), ??

init_env_data (DMRGEngine.init_env), ??
init_env_data (EngineCombine.init_env), 153
init_env_data (EngineFracture.init_env), 160
init_env_data (SingleSiteDMRGEngine.init_env), ??
init_env_data (TwoSiteDMRGEngine.init_env), ??
init_env_data (Sweep.init_env), ??
lanczos_params (Sweep), ??
max_E_err (multiple definitions), ??
max_E_err (DMRGEngine.run), ??
max_E_err (EngineCombine.run), 155
max_E_err (EngineFracture.run), 163
max_E_err (SingleSiteDMRGEngine.run), ??
max_E_err (TwoSiteDMRGEngine.run), ??
max_hours (multiple definitions), ??
max_hours (DMRGEngine.run), ??
max_hours (EngineCombine.run), 155
max_hours (EngineFracture.run), 163
max_hours (SingleSiteDMRGEngine.run), ??
max_hours (TwoSiteDMRGEngine.run), ??
max_N_for_ED (multiple definitions), ??
max_N_for_ED (DMRGEngine.diag), ??
max_N_for_ED (EngineCombine.diag), 151
max_N_for_ED (EngineFracture.diag), 159
max_N_for_ED (SingleSiteDMRGEngine.diag), ??
max_N_for_ED (TwoSiteDMRGEngine.diag), ??
max_S_err (multiple definitions), ??
max_S_err (DMRGEngine.run), ??
max_S_err (EngineCombine.run), 155
max_S_err (EngineFracture.run), 163
max_S_err (SingleSiteDMRGEngine.run), ??
max_S_err (TwoSiteDMRGEngine.run), ??
max_sweeps (multiple definitions), ??
max_sweeps (DMRGEngine.run), ??
max_sweeps (EngineCombine.run), 155
max_sweeps (EngineFracture.run), 163
max_sweeps (SingleSiteDMRGEngine.run), ??
max_sweeps (TwoSiteDMRGEngine.run), ??
min_sweeps (multiple definitions), ??
min_sweeps (DMRGEngine.run), ??
min_sweeps (EngineCombine.run), 155
min_sweeps (EngineFracture.run), 163
min_sweeps (SingleSiteDMRGEngine.run), ??
min_sweeps (TwoSiteDMRGEngine.run), ??
mixer (SingleSiteDMRGEngine.mixer_activate), ??
mixer_params (SingleSiteDMRGEngine.mixer_activate), ??
N_sweeps_check (multiple definitions), ??
N_sweeps_check (DMRGEngine.run), ??
N_sweeps_check (EngineCombine.run), 155
N_sweeps_check (EngineFracture.run), 163
N_sweeps_check (SingleSiteDMRGEngine.run), ??
N_sweeps_check (TwoSiteDMRGEngine.run), ??
norm_tol (multiple definitions), ??

norm_tol (*DMRGEngine.run*), ??
 norm_tol (*EngineCombine.run*), 155
 norm_tol (*EngineFracture.run*), 163
 norm_tol (*SingleSiteDMRGEngine.run*), ??
 norm_tol (*TwoSiteDMRGEngine.run*), ??
 norm_tol_iter (*multiple definitions*), ??
 norm_tol_iter (*DMRGEngine.run*), ??
 norm_tol_iter (*EngineCombine.run*), 156
 norm_tol_iter (*EngineFracture.run*), 163
 norm_tol_iter (*SingleSiteDMRGEngine.run*), ??
 norm_tol_iter (*TwoSiteDMRGEngine.run*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 P_tol_max (*multiple definitions*), ??
 P_tol_max (*DMRGEngine.run*), ??
 P_tol_max (*EngineCombine.run*), 156
 P_tol_max (*EngineFracture.run*), 163
 P_tol_max (*SingleSiteDMRGEngine.run*), ??
 P_tol_max (*TwoSiteDMRGEngine.run*), ??
 P_tol_min (*multiple definitions*), ??
 P_tol_min (*DMRGEngine.run*), ??
 P_tol_min (*EngineCombine.run*), 156
 P_tol_min (*EngineFracture.run*), 163
 P_tol_min (*SingleSiteDMRGEngine.run*), ??
 P_tol_min (*TwoSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*multiple definitions*), ??
 P_tol_to_trunc (*DMRGEngine.run*), ??
 P_tol_to_trunc (*EngineCombine.run*), 156
 P_tol_to_trunc (*EngineFracture.run*), 163
 P_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*DMRGEngine.reset_stats*), ??
 sweep_0 (*EngineCombine.reset_stats*), 155
 sweep_0 (*EngineFracture.reset_stats*), 162
 sweep_0 (*SingleSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*TwoSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177

trunc_params (*Sweep*), ??
 update_env (*multiple definitions*), ??
 update_env (*DMRGEngine.run*), ??
 update_env (*EngineCombine.run*), 156
 update_env (*EngineFracture.run*), 163
 update_env (*SingleSiteDMRGEngine.run*), ??
 update_env (*TwoSiteDMRGEngine.run*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

SpinChainNNN

bc_MPS (*multiple definitions*), ??
 bc_MPS (*SpinChainNNN*), ??
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438

bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*SpinChainNNN*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 hx (*SpinChainNNN*), ??
 hy (*SpinChainNNN*), ??
 hz (*SpinChainNNN*), ??
 Jx (*SpinChainNNN*), ??
 Jxp (*SpinChainNNN*), ??
 Jy (*SpinChainNNN*), ??
 Jyp (*SpinChainNNN*), ??
 Jz (*SpinChainNNN*), ??
 Jzp (*SpinChainNNN*), ??
 L (multiple definitions), ??
 L (*SpinChainNNN*), ??
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (multiple definitions), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??

lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (multiple definitions), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (multiple definitions), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404

Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 order (multiple definitions), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 S (*SpinChainNNN*), ??
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

SpinChainNNN2

bc_MPS (multiple definitions), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (multiple definitions), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??

bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (multiple definitions), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*SpinChainNNN2*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 hx (*SpinChainNNN2*), ??
 hy (*SpinChainNNN2*), ??
 hz (*SpinChainNNN2*), ??
 Jx (*SpinChainNNN2*), ??
 Jxp (*SpinChainNNN2*), ??
 Jy (*SpinChainNNN2*), ??
 Jyp (*SpinChainNNN2*), ??
 Jz (*SpinChainNNN2*), ??
 Jzp (*SpinChainNNN2*), ??
 L (multiple definitions), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??

L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (multiple definitions), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (multiple definitions), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (multiple definitions), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??

Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 order (multiple definitions), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 S (*SpinChainNNN2*), ??
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

SpinModel

bc_MPS (multiple definitions), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??

bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*SpinModel*), ??
 D (*SpinModel*), ??
 E (*SpinModel*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 hx (*SpinModel*), ??
 hy (*SpinModel*), ??
 hz (*SpinModel*), ??
 Jx (*SpinModel*), ??
 Jy (*SpinModel*), ??
 Jz (*SpinModel*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459

Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 muJ (*SpinModel*), ??
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 S (*SpinModel*), ??
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

Sweep

combine (*Sweep*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??
 init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160
 init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*Sweep*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

TDVP

active_sites (*Engine*), ??
 dt (*Engine*), ??
 Lanczos (*Engine*), ??
 N_steps (*Engine*), ??
 start_time (*Engine*), ??
 trunc_params (*Engine*), ??
 verbose (*Config*), ??

TEBD

delta_tau_list (*multiple definitions*), 181
 delta_tau_list (*PurificationTEBD.run_GS*), 181
 delta_tau_list (*PurificationTEBD2.run_GS*), 186
 delta_tau_list (*Engine.run_GS*), ??
 delta_tau_list (*RandomUnitaryEvolution.run_GS*), ??
 dt (*multiple definitions*), 181

dt (*PurificationTEBD.run*), 181
 dt (*PurificationTEBD2.run*), 186
 dt (*Engine.run*), ??
 N_steps (*multiple definitions*), 181
 N_steps (*PurificationTEBD.run*), 181
 N_steps (*PurificationTEBD.run_GS*), 181
 N_steps (*PurificationTEBD2.run*), 186
 N_steps (*PurificationTEBD2.run_GS*), 186
 N_steps (*Engine.run*), ??
 N_steps (*Engine.run_GS*), ??
 N_steps (*RandomUnitaryEvolution.run_GS*), ??
 order (*multiple definitions*), 181
 order (*PurificationTEBD.run*), 181
 order (*PurificationTEBD.run_GS*), 181
 order (*PurificationTEBD2.run*), 186
 order (*PurificationTEBD2.run_GS*), 186
 order (*Engine.run*), ??
 order (*Engine.run_GS*), ??
 order (*RandomUnitaryEvolution.run_GS*), ??
 start_time (*Engine*), ??
 start_trunc_err (*Engine*), ??
 trunc_params (*Engine*), ??
 verbose (*Config*), ??

TFIModel

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??

bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*TFIModel*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 g (*TFIModel*), ??
 J (*TFIModel*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??

L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425

Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 order (*multiple definitions*), 437
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

ToricCode

bc_MPS (*multiple definitions*), 437
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), ??
 bc_x (*ToricCode*), ??
 bc_x (*FermionChain.init_lattice*), 438

bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??
 bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), ??
 bc_y (*ToricCode*), ??
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 conserve (*ToricCode*), ??
 explicit_plus_hc (*CouplingMPOModel*), ??
 Jc (*ToricCode*), ??
 Jp (*ToricCode*), ??
 L (*multiple definitions*), 437
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), ??
 Ly (*ToricCode*), ??
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), ??
 Lx (*ToricCode*), ??
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), ??
 Ly (*ToricCode*), ??
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??

Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??
 Ly (*SpinChainNNN2.init_lattice*), ??
 Ly (*TFIChain.init_lattice*), 404
 Ly (*TFIModel.init_lattice*), ??
 Ly (*ToricCode.init_lattice*), ??
 Ly (*XXZChain2.init_lattice*), 415
 order (*multiple definitions*), ??
 order (*ToricCode*), ??
 order (*FermionChain.init_lattice*), 437
 order (*FermionModel.init_lattice*), ??
 order (*BosonicHaldaneModel.init_lattice*), ??
 order (*FermionicHaldaneModel.init_lattice*), ??
 order (*HofstadterBosons.init_lattice*), ??
 order (*HofstadterFermions.init_lattice*), ??
 order (*BoseHubbardChain.init_lattice*), 449
 order (*BoseHubbardModel.init_lattice*), ??
 order (*FermiHubbardChain.init_lattice*), 459
 order (*FermiHubbardModel.init_lattice*), ??
 order (*CouplingMPOModel.init_lattice*), ??
 order (*SpinChain.init_lattice*), 425
 order (*SpinModel.init_lattice*), ??
 order (*SpinChainNNN.init_lattice*), ??
 order (*SpinChainNNN2.init_lattice*), ??
 order (*TFIChain.init_lattice*), 403
 order (*TFIModel.init_lattice*), ??
 order (*ToricCode.init_lattice*), ??
 order (*XXZChain2.init_lattice*), 415
 sort_mpo_legs (*CouplingMPOModel*), ??
 verbose (*Config*), ??

truncation

chi_max (*truncate*), ??
 chi_min (*truncate*), ??
 degeneracy_tol (*truncate*), ??
 svd_min (*truncate*), ??
 trunc_cut (*truncate*), ??
 verbose (*Config*), ??

TwoSiteDMRGEngine

chi_list (*multiple definitions*), ??
 chi_list (*DMRGEngine.reset_stats*), ??
 chi_list (*EngineCombine.reset_stats*), 154
 chi_list (*EngineFracture.reset_stats*), 162

chi_list (*SingleSiteDMRGEngine.reset_stats*), ??
 chi_list (*TwoSiteDMRGEngine.reset_stats*), ??
 combine (*Sweep*), ??
 diag_method (*multiple definitions*), ??
 diag_method (*DMRGEngine.run*), ??
 diag_method (*DMRGEngine.diag*), ??
 diag_method (*EngineCombine.diag*), 151
 diag_method (*EngineCombine.run*), 155
 diag_method (*EngineFracture.diag*), 159
 diag_method (*EngineFracture.run*), 163
 diag_method (*SingleSiteDMRGEngine.diag*), ??
 diag_method (*SingleSiteDMRGEngine.run*), ??
 diag_method (*TwoSiteDMRGEngine.diag*), ??
 diag_method (*TwoSiteDMRGEngine.run*), ??
 E_tol_max (*multiple definitions*), ??
 E_tol_max (*DMRGEngine.run*), ??
 E_tol_max (*EngineCombine.run*), 155
 E_tol_max (*EngineFracture.run*), 163
 E_tol_max (*SingleSiteDMRGEngine.run*), ??
 E_tol_max (*TwoSiteDMRGEngine.run*), ??
 E_tol_min (*multiple definitions*), ??
 E_tol_min (*DMRGEngine.run*), ??
 E_tol_min (*EngineCombine.run*), 155
 E_tol_min (*EngineFracture.run*), 163
 E_tol_min (*SingleSiteDMRGEngine.run*), ??
 E_tol_min (*TwoSiteDMRGEngine.run*), ??
 E_tol_to_trunc (*multiple definitions*), ??
 E_tol_to_trunc (*DMRGEngine.run*), ??
 E_tol_to_trunc (*EngineCombine.run*), 155
 E_tol_to_trunc (*EngineFracture.run*), 163
 E_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 E_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??
 init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160
 init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 max_E_err (*multiple definitions*), ??
 max_E_err (*DMRGEngine.run*), ??
 max_E_err (*EngineCombine.run*), 155
 max_E_err (*EngineFracture.run*), 163
 max_E_err (*SingleSiteDMRGEngine.run*), ??
 max_E_err (*TwoSiteDMRGEngine.run*), ??
 max_hours (*multiple definitions*), ??
 max_hours (*DMRGEngine.run*), ??
 max_hours (*EngineCombine.run*), 155
 max_hours (*EngineFracture.run*), 163
 max_hours (*SingleSiteDMRGEngine.run*), ??
 max_hours (*TwoSiteDMRGEngine.run*), ??
 max_N_for_ED (*multiple definitions*), ??

max_N_for_ED (*DMRGEngine.diag*), ??
 max_N_for_ED (*EngineCombine.diag*), 151
 max_N_for_ED (*EngineFracture.diag*), 159
 max_N_for_ED (*SingleSiteDMRGEngine.diag*), ??
 max_N_for_ED (*TwoSiteDMRGEngine.diag*), ??
 max_S_err (*multiple definitions*), ??
 max_S_err (*DMRGEngine.run*), ??
 max_S_err (*EngineCombine.run*), 155
 max_S_err (*EngineFracture.run*), 163
 max_S_err (*SingleSiteDMRGEngine.run*), ??
 max_S_err (*TwoSiteDMRGEngine.run*), ??
 max_sweeps (*multiple definitions*), ??
 max_sweeps (*DMRGEngine.run*), ??
 max_sweeps (*EngineCombine.run*), 155
 max_sweeps (*EngineFracture.run*), 163
 max_sweeps (*SingleSiteDMRGEngine.run*), ??
 max_sweeps (*TwoSiteDMRGEngine.run*), ??
 min_sweeps (*multiple definitions*), ??
 min_sweeps (*DMRGEngine.run*), ??
 min_sweeps (*EngineCombine.run*), 155
 min_sweeps (*EngineFracture.run*), 163
 min_sweeps (*SingleSiteDMRGEngine.run*), ??
 min_sweeps (*TwoSiteDMRGEngine.run*), ??
 mixer (*multiple definitions*), 153
 mixer (*EngineCombine.mixer_activate*), 153
 mixer (*EngineFracture.mixer_activate*), 161
 mixer (*TwoSiteDMRGEngine.mixer_activate*), ??
 mixer_params (*multiple definitions*), 153
 mixer_params (*EngineCombine.mixer_activate*), 153
 mixer_params (*EngineFracture.mixer_activate*), 161
 mixer_params (*TwoSiteDMRGEngine.mixer_activate*), ??
 N_sweeps_check (*multiple definitions*), ??
 N_sweeps_check (*DMRGEngine.run*), ??
 N_sweeps_check (*EngineCombine.run*), 155
 N_sweeps_check (*EngineFracture.run*), 163
 N_sweeps_check (*SingleSiteDMRGEngine.run*), ??
 N_sweeps_check (*TwoSiteDMRGEngine.run*), ??
 norm_tol (*multiple definitions*), ??
 norm_tol (*DMRGEngine.run*), ??
 norm_tol (*EngineCombine.run*), 155
 norm_tol (*EngineFracture.run*), 163
 norm_tol (*SingleSiteDMRGEngine.run*), ??
 norm_tol (*TwoSiteDMRGEngine.run*), ??
 norm_tol_iter (*multiple definitions*), ??
 norm_tol_iter (*DMRGEngine.run*), ??
 norm_tol_iter (*EngineCombine.run*), 156
 norm_tol_iter (*EngineFracture.run*), 163
 norm_tol_iter (*SingleSiteDMRGEngine.run*), ??
 norm_tol_iter (*TwoSiteDMRGEngine.run*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 P_tol_max (*multiple definitions*), ??
 P_tol_max (*DMRGEngine.run*), ??
 P_tol_max (*EngineCombine.run*), 156
 P_tol_max (*EngineFracture.run*), 163
 P_tol_max (*SingleSiteDMRGEngine.run*), ??
 P_tol_max (*TwoSiteDMRGEngine.run*), ??
 P_tol_min (*multiple definitions*), ??
 P_tol_min (*DMRGEngine.run*), ??
 P_tol_min (*EngineCombine.run*), 156
 P_tol_min (*EngineFracture.run*), 163
 P_tol_min (*SingleSiteDMRGEngine.run*), ??
 P_tol_min (*TwoSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*multiple definitions*), ??
 P_tol_to_trunc (*DMRGEngine.run*), ??
 P_tol_to_trunc (*EngineCombine.run*), 156
 P_tol_to_trunc (*EngineFracture.run*), 163
 P_tol_to_trunc (*SingleSiteDMRGEngine.run*), ??
 P_tol_to_trunc (*TwoSiteDMRGEngine.run*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*DMRGEngine.reset_stats*), ??
 sweep_0 (*EngineCombine.reset_stats*), 155
 sweep_0 (*EngineFracture.reset_stats*), 162
 sweep_0 (*SingleSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*TwoSiteDMRGEngine.reset_stats*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*Sweep*), ??
 update_env (*multiple definitions*), ??
 update_env (*DMRGEngine.run*), ??
 update_env (*EngineCombine.run*), 156
 update_env (*EngineFracture.run*), 163
 update_env (*SingleSiteDMRGEngine.run*), ??
 update_env (*TwoSiteDMRGEngine.run*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

VariationalApplyMPO

combine (*Sweep*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??

init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160
 init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 N_sweeps (*VariationalCompression*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??
 orthogonal_to (*Sweep.init_env*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*multiple definitions*), ??
 trunc_params (*VariationalCompression*), ??
 trunc_params (*Sweep*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

VariationalCompression

combine (*Sweep*), ??
 init_env_data (*multiple definitions*), ??
 init_env_data (*DMRGEngine.init_env*), ??
 init_env_data (*EngineCombine.init_env*), 153
 init_env_data (*EngineFracture.init_env*), 160
 init_env_data (*SingleSiteDMRGEngine.init_env*), ??
 init_env_data (*TwoSiteDMRGEngine.init_env*), ??
 init_env_data (*Sweep.init_env*), ??
 lanczos_params (*Sweep*), ??
 N_sweeps (*VariationalCompression*), ??
 orthogonal_to (*multiple definitions*), ??
 orthogonal_to (*DMRGEngine.init_env*), ??
 orthogonal_to (*EngineCombine.init_env*), 153
 orthogonal_to (*EngineFracture.init_env*), 160
 orthogonal_to (*SingleSiteDMRGEngine.init_env*), ??
 orthogonal_to (*TwoSiteDMRGEngine.init_env*), ??

orthogonal_to (*Sweep.init_env*), ??
 start_env (*multiple definitions*), ??
 start_env (*DMRGEngine.init_env*), ??
 start_env (*EngineCombine.init_env*), 153
 start_env (*EngineFracture.init_env*), 160
 start_env (*SingleSiteDMRGEngine.init_env*), ??
 start_env (*TwoSiteDMRGEngine.init_env*), ??
 start_env (*Sweep.init_env*), ??
 sweep_0 (*multiple definitions*), ??
 sweep_0 (*Sweep.reset_stats*), ??
 sweep_0 (*VariationalApplyMPO.reset_stats*), ??
 sweep_0 (*VariationalCompression.reset_stats*), ??
 sweep_0 (*PurificationApplyMPO.reset_stats*), 177
 trunc_params (*multiple definitions*), ??
 trunc_params (*VariationalCompression*), ??
 trunc_params (*Sweep*), ??
 verbose (*multiple definitions*), ??
 verbose (*Sweep*), ??
 verbose (*Config*), ??

XXZChain

bc_MPS (*multiple definitions*), ??
 bc_MPS (*XXZChain*), ??
 bc_MPS (*FermionChain.init_lattice*), 437
 bc_MPS (*FermionModel.init_lattice*), ??
 bc_MPS (*BosonicHaldaneModel.init_lattice*), ??
 bc_MPS (*FermionicHaldaneModel.init_lattice*), ??
 bc_MPS (*HofstadterBosons.init_lattice*), ??
 bc_MPS (*HofstadterFermions.init_lattice*), ??
 bc_MPS (*BoseHubbardChain.init_lattice*), 449
 bc_MPS (*BoseHubbardModel.init_lattice*), ??
 bc_MPS (*FermiHubbardChain.init_lattice*), 459
 bc_MPS (*FermiHubbardModel.init_lattice*), ??
 bc_MPS (*CouplingMPOModel.init_lattice*), ??
 bc_MPS (*SpinChain.init_lattice*), 425
 bc_MPS (*SpinModel.init_lattice*), ??
 bc_MPS (*SpinChainNNN.init_lattice*), ??
 bc_MPS (*SpinChainNNN2.init_lattice*), ??
 bc_MPS (*TFIChain.init_lattice*), 403
 bc_MPS (*TFIModel.init_lattice*), ??
 bc_MPS (*ToricCode.init_lattice*), ??
 bc_MPS (*XXZChain2.init_lattice*), 415
 bc_x (*multiple definitions*), 438
 bc_x (*FermionChain.init_lattice*), 438
 bc_x (*FermionModel.init_lattice*), ??
 bc_x (*BosonicHaldaneModel.init_lattice*), ??
 bc_x (*FermionicHaldaneModel.init_lattice*), ??
 bc_x (*HofstadterBosons.init_lattice*), ??
 bc_x (*HofstadterFermions.init_lattice*), ??
 bc_x (*BoseHubbardChain.init_lattice*), 449
 bc_x (*BoseHubbardModel.init_lattice*), ??
 bc_x (*FermiHubbardChain.init_lattice*), 459
 bc_x (*FermiHubbardModel.init_lattice*), ??
 bc_x (*CouplingMPOModel.init_lattice*), ??

bc_x (*SpinChain.init_lattice*), 426
 bc_x (*SpinModel.init_lattice*), ??
 bc_x (*SpinChainNNN.init_lattice*), ??
 bc_x (*SpinChainNNN2.init_lattice*), ??
 bc_x (*TFIChain.init_lattice*), 404
 bc_x (*TFIModel.init_lattice*), ??
 bc_x (*ToricCode.init_lattice*), ??
 bc_x (*XXZChain2.init_lattice*), 415
 bc_y (*multiple definitions*), 438
 bc_y (*FermionChain.init_lattice*), 438
 bc_y (*FermionModel.init_lattice*), ??
 bc_y (*BosonicHaldaneModel.init_lattice*), ??
 bc_y (*FermionicHaldaneModel.init_lattice*), ??
 bc_y (*HofstadterBosons.init_lattice*), ??
 bc_y (*HofstadterFermions.init_lattice*), ??
 bc_y (*BoseHubbardChain.init_lattice*), 449
 bc_y (*BoseHubbardModel.init_lattice*), ??
 bc_y (*FermiHubbardChain.init_lattice*), 459
 bc_y (*FermiHubbardModel.init_lattice*), ??
 bc_y (*CouplingMPOModel.init_lattice*), ??
 bc_y (*SpinChain.init_lattice*), 425
 bc_y (*SpinModel.init_lattice*), ??
 bc_y (*SpinChainNNN.init_lattice*), ??
 bc_y (*SpinChainNNN2.init_lattice*), ??
 bc_y (*TFIChain.init_lattice*), 404
 bc_y (*TFIModel.init_lattice*), ??
 bc_y (*ToricCode.init_lattice*), ??
 bc_y (*XXZChain2.init_lattice*), 415
 explicit_plus_hc (*CouplingMPOModel*), ??
 hz (*XXZChain*), ??
 Jxx (*XXZChain*), ??
 Jz (*XXZChain*), ??
 L (*multiple definitions*), ??
 L (*XXZChain*), ??
 L (*FermionChain.init_lattice*), 437
 L (*FermionModel.init_lattice*), ??
 L (*BosonicHaldaneModel.init_lattice*), ??
 L (*FermionicHaldaneModel.init_lattice*), ??
 L (*HofstadterBosons.init_lattice*), ??
 L (*HofstadterFermions.init_lattice*), ??
 L (*BoseHubbardChain.init_lattice*), 449
 L (*BoseHubbardModel.init_lattice*), ??
 L (*FermiHubbardChain.init_lattice*), 459
 L (*FermiHubbardModel.init_lattice*), ??
 L (*CouplingMPOModel.init_lattice*), ??
 L (*SpinChain.init_lattice*), 425
 L (*SpinModel.init_lattice*), ??
 L (*SpinChainNNN.init_lattice*), ??
 L (*SpinChainNNN2.init_lattice*), ??
 L (*TFIChain.init_lattice*), 403
 L (*TFIModel.init_lattice*), ??
 L (*ToricCode.init_lattice*), ??
 L (*XXZChain2.init_lattice*), 415
 lattice (*multiple definitions*), 437
 lattice (*FermionChain.init_lattice*), 437
 lattice (*FermionModel.init_lattice*), ??
 lattice (*BosonicHaldaneModel.init_lattice*), ??
 lattice (*FermionicHaldaneModel.init_lattice*), ??
 lattice (*HofstadterBosons.init_lattice*), ??
 lattice (*HofstadterFermions.init_lattice*), ??
 lattice (*BoseHubbardChain.init_lattice*), 449
 lattice (*BoseHubbardModel.init_lattice*), ??
 lattice (*FermiHubbardChain.init_lattice*), 459
 lattice (*FermiHubbardModel.init_lattice*), ??
 lattice (*CouplingMPOModel.init_lattice*), ??
 lattice (*SpinChain.init_lattice*), 425
 lattice (*SpinModel.init_lattice*), ??
 lattice (*SpinChainNNN.init_lattice*), ??
 lattice (*SpinChainNNN2.init_lattice*), ??
 lattice (*TFIChain.init_lattice*), 403
 lattice (*TFIModel.init_lattice*), ??
 lattice (*ToricCode.init_lattice*), ??
 lattice (*XXZChain2.init_lattice*), 415
 Lx (*multiple definitions*), 437
 Lx (*FermionChain.init_lattice*), 437
 Lx (*FermionModel.init_lattice*), ??
 Lx (*BosonicHaldaneModel.init_lattice*), ??
 Lx (*FermionicHaldaneModel.init_lattice*), ??
 Lx (*HofstadterBosons.init_lattice*), ??
 Lx (*HofstadterFermions.init_lattice*), ??
 Lx (*BoseHubbardChain.init_lattice*), 449
 Lx (*BoseHubbardModel.init_lattice*), ??
 Lx (*FermiHubbardChain.init_lattice*), 459
 Lx (*FermiHubbardModel.init_lattice*), ??
 Lx (*CouplingMPOModel.init_lattice*), ??
 Lx (*SpinChain.init_lattice*), 425
 Lx (*SpinModel.init_lattice*), ??
 Lx (*SpinChainNNN.init_lattice*), ??
 Lx (*SpinChainNNN2.init_lattice*), ??
 Lx (*TFIChain.init_lattice*), 403
 Lx (*TFIModel.init_lattice*), ??
 Lx (*ToricCode.init_lattice*), ??
 Lx (*XXZChain2.init_lattice*), 415
 Ly (*multiple definitions*), 438
 Ly (*FermionChain.init_lattice*), 438
 Ly (*FermionModel.init_lattice*), ??
 Ly (*BosonicHaldaneModel.init_lattice*), ??
 Ly (*FermionicHaldaneModel.init_lattice*), ??
 Ly (*HofstadterBosons.init_lattice*), ??
 Ly (*HofstadterFermions.init_lattice*), ??
 Ly (*BoseHubbardChain.init_lattice*), 449
 Ly (*BoseHubbardModel.init_lattice*), ??
 Ly (*FermiHubbardChain.init_lattice*), 459
 Ly (*FermiHubbardModel.init_lattice*), ??
 Ly (*CouplingMPOModel.init_lattice*), ??
 Ly (*SpinChain.init_lattice*), 425
 Ly (*SpinModel.init_lattice*), ??
 Ly (*SpinChainNNN.init_lattice*), ??

Ly (*SpinChainNNN2.init_lattice*), ??
Ly (*TFIChain.init_lattice*), [404](#)
Ly (*TFIModel.init_lattice*), ??
Ly (*ToricCode.init_lattice*), ??
Ly (*XXZChain2.init_lattice*), [415](#)
order (*multiple definitions*), [437](#)
order (*FermionChain.init_lattice*), [437](#)
order (*FermionModel.init_lattice*), ??
order (*BosonicHaldaneModel.init_lattice*), ??
order (*FermionicHaldaneModel.init_lattice*), ??
order (*HofstadterBosons.init_lattice*), ??
order (*HofstadterFermions.init_lattice*), ??
order (*BoseHubbardChain.init_lattice*), [449](#)
order (*BoseHubbardModel.init_lattice*), ??
order (*FermiHubbardChain.init_lattice*), [459](#)
order (*FermiHubbardModel.init_lattice*), ??
order (*CouplingMPOModel.init_lattice*), ??
order (*SpinChain.init_lattice*), [425](#)
order (*SpinModel.init_lattice*), ??
order (*SpinChainNNN.init_lattice*), ??
order (*SpinChainNNN2.init_lattice*), ??
order (*TFIChain.init_lattice*), [403](#)
order (*TFIModel.init_lattice*), ??
order (*ToricCode.init_lattice*), ??
order (*XXZChain2.init_lattice*), [415](#)
sort_mpo_legs (*CouplingMPOModel*), ??
verbose (*Config*), ??

zip_up

m_temp (*MPO.apply_zipup*), ??
trunc_params (*MPO.apply_zipup*), ??
trunc_weight (*MPO.apply_zipup*), ??
verbose (*Config*), ??

Symbols

- `_LP` (*tenpy.networks.mps.MPSEnvironment* attribute), 510
 - `_LP_age` (*tenpy.networks.mps.MPSEnvironment* attribute), 510
 - `_RP` (*tenpy.networks.mps.MPSEnvironment* attribute), 510
 - `_RP_age` (*tenpy.networks.mps.MPSEnvironment* attribute), 510
 - `__full_version__` (in module *tenpy*), 131
 - `__version__` (in module *tenpy*), 131
 - `_bra_N` (*tenpy.networks.mps.TransferMatrix* attribute), 515
 - `_data` (*tenpy.linalg.np_conserved.Array* attribute), 200
 - `_disent_iterations` (*tenpy.algorithms.purification.PurificationTEBD* attribute), 179
 - `_finite` (*tenpy.networks.mps.MPSEnvironment* attribute), 510
 - `_grid_legs` (*tenpy.networks.mpo.MPOGraph* attribute), 526
 - `_guess_U_disent` (*tenpy.algorithms.purification.PurificationTEBD* attribute), 179
 - `_ket_M` (*tenpy.networks.mps.TransferMatrix* attribute), 515
 - `_labels` (*tenpy.linalg.np_conserved.Array* attribute), 200
 - `_labels_p` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_labels_pconj` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_labels_split` (*tenpy.linalg.sparse.FlatLinearOperator* attribute), 263
 - `_mask` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_mask` (*tenpy.linalg.charges.ChargeInfo* attribute), 231
 - `_mask` (*tenpy.linalg.sparse.FlatLinearOperator* attribute), 263
 - `_mod_masked` (*tenpy.linalg.charges.ChargeInfo* attribute), 231
 - `_mps2lat_vals_idx` (*tenpy.models.lattice.Lattice* attribute), 324
 - `_mps2lat_vals_idx_fix_u` (*tenpy.models.lattice.Lattice* attribute), 324
 - `_mps_fix_u` (*tenpy.models.lattice.Lattice* attribute), 324
 - `_npc_matvec_multileg` (*tenpy.linalg.sparse.FlatLinearOperator* attribute), 263
 - `_old_level` (*tenpy.tools.optimization.temporary_level* attribute), 585
 - `_order` (*tenpy.models.lattice.Lattice* attribute), 324
 - `_perm` (*tenpy.linalg.charges.LegPipe* attribute), 244
 - `_perm` (*tenpy.models.lattice.Lattice* attribute), 324
 - `_pipe` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_pipe_conj` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_qdata` (*tenpy.linalg.np_conserved.Array* attribute), 200
 - `_qdata_sorted` (*tenpy.linalg.np_conserved.Array* attribute), 200
 - `_sites` (*tenpy.algorithms.exact_diag.ExactDiag* attribute), 194
 - `_strides` (*tenpy.linalg.charges.LegPipe* attribute), 244
 - `_strides` (*tenpy.models.lattice.Lattice* attribute), 324
- ## A
- `acts_on` (*tenpy.algorithms.mps_common.EffectiveH* attribute), 140
 - `acts_on` (*tenpy.algorithms.mps_common.OneSiteH* attribute), 142
 - `acts_on` (*tenpy.algorithms.mps_common.TwoSiteH* attribute), 144
 - `acts_on` (*tenpy.linalg.sparse.NpcLinearOperator* attribute), 268
 - `add()` (*tenpy.linalg.charges.ChargeInfo* class method), 232
 - `add()` (*tenpy.networks.mpo.MPOGraph* method), 527
 - `add_charge()` (*tenpy.linalg.np_conserved.Array* method), 206
 - `add_coupling()` (*tenpy.models.fermions_spinless.FermionChain* method), 430
 - `add_coupling()` (*tenpy.models.hubbard.BoseHubbardChain* method), 430

method), 442
 add_coupling() (*tenpy.models.hubbard.FermiHubbardChain* *method*), 452
 add_coupling() (*tenpy.models.model.CouplingModel* *method*), 371
 add_coupling() (*tenpy.models.model.MultiCouplingModel* *method*), 384
 add_coupling() (*tenpy.models.spins.SpinChain* *method*), 418
 add_coupling() (*tenpy.models.tf_ising.TFChain* *method*), 396
 add_coupling() (*tenpy.models.xxz_chain.XXZChain2* *method*), 408
 add_coupling_term() (*tenpy.models.fermions_spinless.FermionChain* *method*), 432
 add_coupling_term() (*tenpy.models.hubbard.BoseHubbardChain* *method*), 443
 add_coupling_term() (*tenpy.models.hubbard.FermiHubbardChain* *method*), 453
 add_coupling_term() (*tenpy.models.model.CouplingModel* *method*), 373
 add_coupling_term() (*tenpy.models.model.MultiCouplingModel* *method*), 385
 add_coupling_term() (*tenpy.models.spins.SpinChain* *method*), 420
 add_coupling_term() (*tenpy.models.tf_ising.TFChain* *method*), 398
 add_coupling_term() (*tenpy.models.xxz_chain.XXZChain2* *method*), 409
 add_coupling_term() (*tenpy.networks.terms.CouplingTerms* *method*), 532
 add_coupling_term() (*tenpy.networks.terms.MultiCouplingTerms* *method*), 537
 add_leg() (*tenpy.linalg.np_conserved.Array* *method*), 205
 add_local_term() (*tenpy.models.fermions_spinless.FermionChain* *method*), 433
 add_local_term() (*tenpy.models.hubbard.BoseHubbardChain* *method*), 444
 add_local_term() (*tenpy.models.hubbard.FermiHubbardChain* *method*), 454
 add_local_term() (*tenpy.models.model.CouplingModel* *method*), 370
 add_local_term() (*tenpy.models.model.MultiCouplingModel* *method*), 386
 add_local_term() (*tenpy.models.spins.SpinChain* *method*), 421
 add_local_term() (*tenpy.models.tf_ising.TFChain* *method*), 399
 add_local_term() (*tenpy.models.xxz_chain.XXZChain2* *method*), 410
 add_missing_IdL_IdR() (*tenpy.networks.mpo.MPOGraph* *method*), 528
 add_multi_coupling() (*tenpy.models.model.MultiCouplingModel* *method*), 382
 add_multi_coupling_term() (*tenpy.models.model.MultiCouplingModel* *method*), 383
 add_multi_coupling_term() (*tenpy.networks.terms.MultiCouplingTerms* *method*), 536
 add_onsite() (*tenpy.models.fermions_spinless.FermionChain* *method*), 433
 add_onsite() (*tenpy.models.hubbard.BoseHubbardChain* *method*), 444
 add_onsite() (*tenpy.models.hubbard.FermiHubbardChain* *method*), 454
 add_onsite() (*tenpy.models.model.CouplingModel* *method*), 371
 add_onsite() (*tenpy.models.model.MultiCouplingModel* *method*), 386
 add_onsite() (*tenpy.models.spins.SpinChain* *method*), 421
 add_onsite() (*tenpy.models.tf_ising.TFChain* *method*), 399
 add_onsite() (*tenpy.models.xxz_chain.XXZChain2* *method*), 410
 add_onsite_term() (*tenpy.models.fermions_spinless.FermionChain* *method*), 434
 add_onsite_term() (*tenpy.models.hubbard.BoseHubbardChain* *method*), 445
 add_onsite_term() (*tenpy.models.hubbard.FermiHubbardChain* *method*), 455
 add_onsite_term() (*tenpy.models.model.CouplingModel* *method*), 371
 add_onsite_term() (*tenpy.models.model.MultiCouplingModel* *method*), 387
 add_onsite_term() (*tenpy.models.spins.SpinChain* *method*), 421
 add_onsite_term() (*tenpy.models.tf_ising.TFChain* *method*), 399

- 399
- `add_onsite_term()`
(*tenpy.models.xxz_chain.XXZChain2* method), 411
- `add_onsite_term()`
(*tenpy.networks.terms.OnsiteTerms* method), 540
- `add_op()` (*tenpy.networks.site.BosonSite* method), 476
- `add_op()` (*tenpy.networks.site.FermionSite* method), 481
- `add_op()` (*tenpy.networks.site.GroupedSite* method), 485
- `add_op()` (*tenpy.networks.site.Site* method), 491
- `add_op()` (*tenpy.networks.site.SpinHalfFermionSite* method), 495
- `add_op()` (*tenpy.networks.site.SpinHalfSite* method), 499
- `add_op()` (*tenpy.networks.site.SpinSite* method), 503
- `add_string()` (*tenpy.networks.mpo.MPOGraph* method), 527
- `add_to_graph()` (*tenpy.networks.terms.CouplingTerms* method), 533
- `add_to_graph()` (*tenpy.networks.terms.MultiCouplingTerms* method), 537
- `add_to_graph()` (*tenpy.networks.terms.OnsiteTerms* method), 540
- `add_to_nn_bond_Arrays()`
(*tenpy.networks.terms.OnsiteTerms* method), 541
- `add_trivial_leg()`
(*tenpy.linalg.np_conserved.Array* method), 205
- `add_with_None_0()` (in module *tenpy.tools.misc*), 566
- `adjoint()` (*tenpy.algorithms.mps_common.EffectiveH* method), 140
- `adjoint()` (*tenpy.algorithms.mps_common.OneSiteH* method), 143
- `adjoint()` (*tenpy.algorithms.mps_common.TwoSiteH* method), 145
- `adjoint()` (*tenpy.algorithms.purification.PurificationTwoSiteU* method), 189
- `adjoint()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 258
- `adjoint()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 265
- `adjoint()` (*tenpy.linalg.sparse.NpcLinearOperator* method), 268
- `adjoint()` (*tenpy.linalg.sparse.NpcLinearOperatorWrapper* method), 269
- `adjoint()` (*tenpy.linalg.sparse.OrthogonalNpcLinearOperator* method), 270
- `adjoint()` (*tenpy.linalg.sparse.ShiftNpcLinearOperator* method), 271
- `adjoint()` (*tenpy.linalg.sparse.SumNpcLinearOperator* method), 272
- `adjoint()` (*tenpy.networks.mps.TransferMatrix* method), 516
- `alg_decay()` (in module *tenpy.tools.fit*), 576
- `alg_decay_fit()` (in module *tenpy.tools.fit*), 577
- `alg_decay_fit_res()` (in module *tenpy.tools.fit*), 577
- `alg_decay_fits()` (in module *tenpy.tools.fit*), 577
- `all_coupling_terms()`
(*tenpy.models.fermions_spinless.FermionChain* method), 434
- `all_coupling_terms()`
(*tenpy.models.hubbard.BoseHubbardChain* method), 445
- `all_coupling_terms()`
(*tenpy.models.hubbard.FermiHubbardChain* method), 455
- `all_coupling_terms()`
(*tenpy.models.model.CouplingModel* method), 374
- `all_coupling_terms()`
(*tenpy.models.model.MultiCouplingModel* method), 387
- `all_coupling_terms()`
(*tenpy.models.spins.SpinChain* method), 422
- `all_coupling_terms()`
(*tenpy.models.tf_ising.TFICChain* method), 400
- `all_coupling_terms()`
(*tenpy.models.xxz_chain.XXZChain2* method), 411
- `all_onsite_terms()`
(*tenpy.models.fermions_spinless.FermionChain* method), 434
- `all_onsite_terms()`
(*tenpy.models.hubbard.BoseHubbardChain* method), 445
- `all_onsite_terms()`
(*tenpy.models.hubbard.FermiHubbardChain* method), 455
- `all_onsite_terms()`
(*tenpy.models.model.CouplingModel* method), 371
- `all_onsite_terms()`
(*tenpy.models.model.MultiCouplingModel* method), 387
- `all_onsite_terms()`
(*tenpy.models.spins.SpinChain* method), 422
- `all_onsite_terms()`
(*tenpy.models.tf_ising.TFICChain* method), 400

`all_onsite_terms()` (*tenpy.models.xxz_chain.XXZChain2 method*), 411
`any_nonzero()` (*in module tenpy.tools.misc*), 566
`anynan()` (*in module tenpy.tools.misc*), 566
`argsort()` (*in module tenpy.tools.misc*), 567
`Array` (*class in tenpy.linalg.np_conserved*), 199
`as_completely_blocked()` (*tenpy.linalg.np_conserved.Array method*), 210
`asConfig()` (*in module tenpy.tools.params*), 563
`astype()` (*tenpy.linalg.np_conserved.Array method*), 210
`atleast_2d_pad()` (*in module tenpy.tools.misc*), 567
`ATTR_CLASS` (*in module tenpy.tools.hdf5_io*), 560
`ATTR_FORMAT` (*in module tenpy.tools.hdf5_io*), 560
`ATTR_LEN` (*in module tenpy.tools.hdf5_io*), 560
`ATTR_MODULE` (*in module tenpy.tools.hdf5_io*), 560
`ATTR_TYPE` (*in module tenpy.tools.hdf5_io*), 560

B

`basis` (*tenpy.models.lattice.Lattice attribute*), 324
`bc` (*tenpy.models.lattice.Lattice attribute*), 323
`bc` (*tenpy.networks.mpo.MPOGraph attribute*), 526
`bc_MPS` (*tenpy.models.lattice.Lattice attribute*), 324
`bc_shift` (*tenpy.models.lattice.Lattice attribute*), 324
`binary_blockwise()` (*tenpy.linalg.np_conserved.Array method*), 213
`block_number` (*tenpy.linalg.charges.LegCharge attribute*), 235
`bond_energies()` (*tenpy.models.fermions_spinless.FermionChain method*), 434
`bond_energies()` (*tenpy.models.hubbard.BoseHubbardChain method*), 445
`bond_energies()` (*tenpy.models.hubbard.FermiHubbardChain method*), 455
`bond_energies()` (*tenpy.models.model.NearestNeighborModel method*), 392
`bond_energies()` (*tenpy.models.spins.SpinChain method*), 422
`bond_energies()` (*tenpy.models.tf_ising.TFICChain method*), 400
`bond_energies()` (*tenpy.models.xxz_chain.XXZChain2 method*), 411
`BoseHubbardChain` (*class in tenpy.models.hubbard*), 441
`BosonSite` (*class in tenpy.networks.site*), 476
`bottleneck` (*in module tenpy.tools.optimization*), 589
`boundary_conditions()` (*tenpy.models.lattice.Chain property*), 279
`boundary_conditions()` (*tenpy.models.lattice.Honeycomb property*), 286
`boundary_conditions()` (*tenpy.models.lattice.IrregularLattice property*), 297
`boundary_conditions()` (*tenpy.models.lattice.Kagome property*), 304
`boundary_conditions()` (*tenpy.models.lattice.Ladder property*), 314
`boundary_conditions()` (*tenpy.models.lattice.Lattice property*), 326
`boundary_conditions()` (*tenpy.models.lattice.SimpleLattice property*), 333
`boundary_conditions()` (*tenpy.models.lattice.Square property*), 341
`boundary_conditions()` (*tenpy.models.lattice.Triangular property*), 351
`boundary_conditions()` (*tenpy.models.lattice.TrivialLattice property*), 358
`boundary_conditions()` (*tenpy.models.toric_code.DualSquare property*), 467
`box()` (*in module tenpy.linalg.random_matrix*), 255
`build_full_H_from_bonds()` (*tenpy.algorithms.exact_diag.ExactDiag method*), 195
`build_full_H_from_mpo()` (*tenpy.algorithms.exact_diag.ExactDiag method*), 195
`build_initial_state()` (*in module tenpy.networks.mps*), 517
`build_initial_state()` (*in module tenpy.tools.misc*), 568
`build_MPO()` (*tenpy.networks.mpo.MPOGraph method*), 528
`bunch()` (*tenpy.linalg.charges.LegCharge method*), 240
`bunch()` (*tenpy.linalg.charges.LegPipe method*), 245
`bunched` (*tenpy.linalg.charges.LegCharge attribute*), 235

C

`calc_H_bond()` (*tenpy.models.fermions_spinless.FermionChain method*), 434
`calc_H_bond()` (*tenpy.models.hubbard.BoseHubbardChain method*), 445
`calc_H_bond()` (*tenpy.models.hubbard.FermiHubbardChain method*), 455
`calc_H_bond()` (*tenpy.models.model.CouplingModel method*), 374
`calc_H_bond()` (*tenpy.models.model.MultiCouplingModel method*), 387

`calc_H_bond()` (*tenpy.models.spins.SpinChain* *method*), 422
`calc_H_bond()` (*tenpy.models.tf_ising.TFChain* *method*), 400
`calc_H_bond()` (*tenpy.models.xxz_chain.XXZChain2* *method*), 411
`calc_H_bond_from_MPO()` (*tenpy.models.fermions_spinless.FermionChain* *method*), 435
`calc_H_bond_from_MPO()` (*tenpy.models.hubbard.BoseHubbardChain* *method*), 446
`calc_H_bond_from_MPO()` (*tenpy.models.hubbard.FermiHubbardChain* *method*), 456
`calc_H_bond_from_MPO()` (*tenpy.models.model.MPOModel* *method*), 378
`calc_H_bond_from_MPO()` (*tenpy.models.spins.SpinChain* *method*), 422
`calc_H_bond_from_MPO()` (*tenpy.models.tf_ising.TFChain* *method*), 401
`calc_H_bond_from_MPO()` (*tenpy.models.xxz_chain.XXZChain2* *method*), 412
`calc_H_MPO()` (*tenpy.models.fermions_spinless.FermionChain* *method*), 434
`calc_H_MPO()` (*tenpy.models.hubbard.BoseHubbardChain* *method*), 445
`calc_H_MPO()` (*tenpy.models.hubbard.FermiHubbardChain* *method*), 455
`calc_H_MPO()` (*tenpy.models.model.CouplingModel* *method*), 374
`calc_H_MPO()` (*tenpy.models.model.MultiCouplingModel* *method*), 387
`calc_H_MPO()` (*tenpy.models.spins.SpinChain* *method*), 422
`calc_H_MPO()` (*tenpy.models.tf_ising.TFChain* *method*), 400
`calc_H_MPO()` (*tenpy.models.xxz_chain.XXZChain2* *method*), 411
`calc_H_MPO_from_bond()` (*tenpy.models.fermions_spinless.FermionChain* *method*), 434
`calc_H_MPO_from_bond()` (*tenpy.models.hubbard.BoseHubbardChain* *method*), 445
`calc_H_MPO_from_bond()` (*tenpy.models.hubbard.FermiHubbardChain* *method*), 455
`calc_H_MPO_from_bond()` (*tenpy.models.model.NearestNeighborModel* *method*), 392
`calc_H_MPO_from_bond()` (*tenpy.models.spins.SpinChain* *method*), 422
`calc_H_MPO_from_bond()` (*tenpy.models.tf_ising.TFChain* *method*), 400
`calc_H_MPO_from_bond()` (*tenpy.models.xxz_chain.XXZChain2* *method*), 411
`calc_H_onsite()` (*tenpy.models.fermions_spinless.FermionChain* *method*), 435
`calc_H_onsite()` (*tenpy.models.hubbard.BoseHubbardChain* *method*), 446
`calc_H_onsite()` (*tenpy.models.hubbard.FermiHubbardChain* *method*), 456
`calc_H_onsite()` (*tenpy.models.model.CouplingModel* *method*), 374
`calc_H_onsite()` (*tenpy.models.model.MultiCouplingModel* *method*), 387
`calc_H_onsite()` (*tenpy.models.spins.SpinChain* *method*), 423
`calc_H_onsite()` (*tenpy.models.tf_ising.TFChain* *method*), 401
`calc_H_onsite()` (*tenpy.models.xxz_chain.XXZChain2* *method*), 412
`calc_U()` (*tenpy.algorithms.purification.PurificationTEBD* *method*), 179
`calc_U()` (*tenpy.algorithms.purification.PurificationTEBD2* *method*), 185
`Chain` (*class in tenpy.models.lattice*), 278
`change()` (*tenpy.linalg.charges.ChargeInfo* *class* *method*), 232
`change_charge()` (*tenpy.linalg.np_conserved.Array* *method*), 207
`change_charge()` (*tenpy.networks.site.BosonSite* *method*), 477
`change_charge()` (*tenpy.networks.site.FermionSite* *method*), 481
`change_charge()` (*tenpy.networks.site.GroupedSite* *method*), 485
`change_charge()` (*tenpy.networks.site.Site* *method*), 490
`change_charge()` (*tenpy.networks.site.SpinHalfFermionSite* *method*), 495
`change_charge()` (*tenpy.networks.site.SpinHalfSite* *method*), 499
`change_charge()` (*tenpy.networks.site.SpinSite* *method*), 503
`charge_sector` (*tenpy.algorithms.exact_diag.ExactDiag* *attribute*), 194
`charge_sector()` (*tenpy.linalg.sparse.FlatHermitianOperator* *property*), 258
`charge_sector()` (*tenpy.linalg.sparse.FlatLinearOperator* *property*), 258

- property), 264
- charge_sectors() (tenpy.linalg.charges.LegCharge method), 241
- charge_sectors() (tenpy.linalg.charges.LegPipe method), 246
- ChargeInfo (class in tenpy.linalg.charges), 231
- charges (tenpy.linalg.charges.LegCharge attribute), 235
- check_valid() (tenpy.linalg.charges.ChargeInfo method), 233
- chi_list() (in module tenpy.algorithms.dmr), 169
- chi_list() (in module tenpy.tools.misc), 568
- chinfo (tenpy.algorithms.exact_diag.ExactDiag attribute), 193
- chinfo (tenpy.linalg.charges.LegCharge attribute), 235
- chinfo (tenpy.linalg.np_conserved.Array attribute), 200
- chinfo (tenpy.networks.mpo.MPOGraph attribute), 526
- COE() (in module tenpy.linalg.random_matrix), 253
- combine (tenpy.algorithms.mps_common.EffectiveH attribute), 140
- combine (tenpy.algorithms.mps_common.TwoSiteH attribute), 144
- combine_Heff() (tenpy.algorithms.mps_common.OneSiteH method), 142
- combine_Heff() (tenpy.algorithms.mps_common.TwoSiteH method), 145
- combine_Heff() (tenpy.algorithms.purification.PurificationTwoSiteH method), 189
- combine_legs() (tenpy.linalg.np_conserved.Array method), 208
- combine_theta() (tenpy.algorithms.mps_common.EffectiveH method), 140
- combine_theta() (tenpy.algorithms.mps_common.OneSiteH method), 142
- combine_theta() (tenpy.algorithms.mps_common.TwoSiteH method), 145
- combine_theta() (tenpy.algorithms.purification.PurificationTwoSiteH method), 189
- complex_conj() (tenpy.linalg.np_conserved.Array method), 213
- concatenate() (in module tenpy.linalg.np_conserved), 215
- conj() (tenpy.linalg.charges.LegCharge method), 238
- conj() (tenpy.linalg.charges.LegPipe method), 245
- conj() (tenpy.linalg.np_conserved.Array method), 212
- cons_N (tenpy.networks.site.SpinHalfFermionSite attribute), 495
- cons_Sz (tenpy.networks.site.SpinHalfFermionSite attribute), 495
- conserve (tenpy.networks.site.BosonSite attribute), 476
- conserve (tenpy.networks.site.FermionSite attribute), 480
- conserve (tenpy.networks.site.SpinHalfSite attribute), 499
- conserve (tenpy.networks.site.SpinSite attribute), 503
- contract() (in module tenpy.algorithms.network_contractor), 190
- copy() (tenpy.algorithms.truncation.TruncationError method), 134
- copy() (tenpy.linalg.charges.LegCharge method), 236
- copy() (tenpy.linalg.charges.LegPipe method), 245
- copy() (tenpy.linalg.np_conserved.Array method), 200
- count_neighbors() (tenpy.models.lattice.Chain method), 279
- count_neighbors() (tenpy.models.lattice.Honeycomb method), 286
- count_neighbors() (tenpy.models.lattice.IrregularLattice method), 297
- count_neighbors() (tenpy.models.lattice.Kagome method), 305
- count_neighbors() (tenpy.models.lattice.Ladder method), 314
- count_neighbors() (tenpy.models.lattice.Lattice method), 329
- count_neighbors() (tenpy.models.lattice.SimpleLattice method), 333
- count_neighbors() (tenpy.models.lattice.Square method), 341
- count_neighbors() (tenpy.models.lattice.Triangular method), 351
- count_neighbors() (tenpy.models.lattice.TrivialLattice method), 358
- count_neighbors() (tenpy.models.toric_code.DualSquare method), 367
- coupling_shape() (tenpy.models.lattice.Chain method), 279
- coupling_shape() (tenpy.models.lattice.Honeycomb method), 288
- coupling_shape() (tenpy.models.lattice.IrregularLattice method), 298
- coupling_shape() (tenpy.models.lattice.Kagome method), 305
- coupling_shape() (tenpy.models.lattice.Ladder method), 314
- coupling_shape() (tenpy.models.lattice.Lattice method), 329
- coupling_shape() (tenpy.models.lattice.SimpleLattice method), 334
- coupling_shape() (tenpy.models.lattice.Square method), 343

`coupling_shape()` (*tenpy.models.lattice.Triangular method*), 351
`coupling_shape()` (*tenpy.models.lattice.TrivialLattice method*), 359
`coupling_shape()` (*tenpy.models.toric_code.DualSquare method*), 467
`coupling_strength_add_ext_flux()` (*tenpy.models.fermions_spinless.FermionChain method*), 435
`coupling_strength_add_ext_flux()` (*tenpy.models.hubbard.BoseHubbardChain method*), 446
`coupling_strength_add_ext_flux()` (*tenpy.models.hubbard.FermiHubbardChain method*), 456
`coupling_strength_add_ext_flux()` (*tenpy.models.model.CouplingModel method*), 374
`coupling_strength_add_ext_flux()` (*tenpy.models.model.MultiCouplingModel method*), 388
`coupling_strength_add_ext_flux()` (*tenpy.models.spins.SpinChain method*), 423
`coupling_strength_add_ext_flux()` (*tenpy.models.tf_ising.TFChain method*), 401
`coupling_strength_add_ext_flux()` (*tenpy.models.xxz_chain.XXZChain2 method*), 412
`coupling_term_handle_JW()` (*tenpy.networks.terms.CouplingTerms method*), 533
`coupling_term_handle_JW()` (*tenpy.networks.terms.MultiCouplingTerms method*), 538
`coupling_terms` (*tenpy.models.model.CouplingModel attribute*), 370
`coupling_terms` (*tenpy.networks.terms.CouplingTerms attribute*), 532
`coupling_terms` (*tenpy.networks.terms.MultiCouplingTerms attribute*), 536
`CouplingModel` (*class in tenpy.models.model*), 369
`CouplingTerms` (*class in tenpy.networks.terms*), 532
`CRE()` (*in module tenpy.linalg.random_matrix*), 253
`create_group_for_obj()` (*tenpy.tools.hdf5_io.Hdf5Saver method*), 555
`CUE()` (*in module tenpy.linalg.random_matrix*), 253

D
`del_LP()` (*tenpy.networks.mpo.MPOEnvironment method*), 523
`del_LP()` (*tenpy.networks.mps.MPSEnvironment method*), 511
`del_RP()` (*tenpy.networks.mpo.MPOEnvironment method*), 523
`del_RP()` (*tenpy.networks.mps.MPSEnvironment method*), 511
`DensityMatrixMixer` (*class in tenpy.algorithms.dmrgh*), 147
`detect_grid_outer_legcharge()` (*in module tenpy.linalg.np_conserved*), 215
`detect_legcharge()` (*in module tenpy.linalg.np_conserved*), 216
`detect_qtotal()` (*in module tenpy.linalg.np_conserved*), 216
`diag()` (*in module tenpy.linalg.np_conserved*), 217
`diag()` (*tenpy.algorithms.dmrgh.EngineCombine method*), 151
`diag()` (*tenpy.algorithms.dmrgh.EngineFracture method*), 159
`dim()` (*tenpy.models.lattice.IrregularLattice property*), 298
`dim()` (*tenpy.models.lattice.Lattice property*), 325
`dim()` (*tenpy.models.lattice.SimpleLattice property*), 334
`dim()` (*tenpy.models.lattice.TrivialLattice property*), 359
`dim()` (*tenpy.models.toric_code.DualSquare property*), 467
`dim()` (*tenpy.networks.site.BosonSite property*), 477
`dim()` (*tenpy.networks.site.FermionSite property*), 481
`dim()` (*tenpy.networks.site.GroupedSite property*), 486
`dim()` (*tenpy.networks.site.Site property*), 490
`dim()` (*tenpy.networks.site.SpinHalfFermionSite property*), 496
`dim()` (*tenpy.networks.site.SpinHalfSite property*), 500
`dim()` (*tenpy.networks.site.SpinSite property*), 504
`disent_iterations()` (*tenpy.algorithms.purification.PurificationTEBD property*), 179
`disent_iterations()` (*tenpy.algorithms.purification.PurificationTEBD2 property*), 185
`disentangle()` (*tenpy.algorithms.purification.PurificationTEBD method*), 180
`disentangle()` (*tenpy.algorithms.purification.PurificationTEBD2 method*), 185
`disentangle_global()` (*tenpy.algorithms.purification.PurificationTEBD method*), 181
`disentangle_global()` (*tenpy.algorithms.purification.PurificationTEBD2 method*), 185
`disentangle_global_nsite()` (*tenpy.algorithms.purification.PurificationTEBD*

method), 181
 disentangle_global_nsite() (*tenpy.algorithms.purification.PurificationTEBD2 method*), 185
 disentangle_nsite() (*tenpy.algorithms.purification.PurificationTEBD method*), 181
 disentangle_nsite() (*tenpy.algorithms.purification.PurificationTEBD2 method*), 185
 dispatch_load (*tenpy.tools.hdf5_io.Hdf5Loader attribute*), 552
 dispatch_save (*tenpy.tools.hdf5_io.Hdf5Saver attribute*), 554
 dot() (*tenpy.linalg.sparse.FlatHermitianOperator method*), 258
 dot() (*tenpy.linalg.sparse.FlatLinearOperator method*), 265
 drop() (*tenpy.linalg.charges.ChargeInfo class method*), 232
 drop_charge() (*tenpy.linalg.np_conserved.Array method*), 207
 dtype (*tenpy.algorithms.mps_common.EffectiveH attribute*), 140
 dtype (*tenpy.linalg.np_conserved.Array attribute*), 200
 dtype (*tenpy.linalg.sparse.FlatLinearOperator attribute*), 263
 dtype (*tenpy.linalg.sparse.NpcLinearOperator attribute*), 267
 dtype (*tenpy.networks.mps.MPSEnvironment attribute*), 510
 DualSquare (*class in tenpy.models.toric_code*), 465

E

E (*tenpy.algorithms.exact_diag.ExactDiag attribute*), 194
 EffectiveH (*class in tenpy.algorithms.mps_common*), 139
 EffectiveH (*tenpy.algorithms.dmrgh.EngineCombine attribute*), 151
 EffectiveH (*tenpy.algorithms.dmrgh.EngineFracture attribute*), 159
 EffectiveH (*tenpy.algorithms.purification.PurificationApplyMPO attribute*), 176
 eig() (*in module tenpy.linalg.np_conserved*), 217
 eigenvectors() (*tenpy.networks.mps.TransferMatrix method*), 516
 eigh() (*in module tenpy.linalg.np_conserved*), 218
 eigvals() (*in module tenpy.linalg.np_conserved*), 218
 eigvalsh() (*in module tenpy.linalg.np_conserved*), 219
 EngineCombine (*class in tenpy.algorithms.dmrgh*), 151
 EngineFracture (*class in tenpy.algorithms.dmrgh*), 159

enlarge_mps_unit_cell() (*tenpy.models.fermions_spinless.FermionChain method*), 436
 enlarge_mps_unit_cell() (*tenpy.models.hubbard.BoseHubbardChain method*), 447
 enlarge_mps_unit_cell() (*tenpy.models.hubbard.FermiHubbardChain method*), 457
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Chain method*), 279
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Honeycomb method*), 288
 enlarge_mps_unit_cell() (*tenpy.models.lattice.IrregularLattice method*), 298
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Kagome method*), 306
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Ladder method*), 314
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Lattice method*), 326
 enlarge_mps_unit_cell() (*tenpy.models.lattice.SimpleLattice method*), 334
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Square method*), 343
 enlarge_mps_unit_cell() (*tenpy.models.lattice.Triangular method*), 351
 enlarge_mps_unit_cell() (*tenpy.models.lattice.TrivialLattice method*), 359
 enlarge_mps_unit_cell() (*tenpy.models.model.CouplingModel method*), 375
 enlarge_mps_unit_cell() (*tenpy.models.model.Model method*), 379
 enlarge_mps_unit_cell() (*tenpy.models.model.MPOModel method*), 377
 enlarge_mps_unit_cell() (*tenpy.models.model.MultiCouplingModel method*), 389
 enlarge_mps_unit_cell() (*tenpy.models.model.NearestNeighborModel method*), 392
 enlarge_mps_unit_cell() (*tenpy.models.spins.SpinChain method*), 424
 enlarge_mps_unit_cell() (*tenpy.models.tf_ising.TFChain method*), 402

`enlarge_mps_unit_cell()`
 (*tenpy.models.toric_code.DualSquare* method), 467
`enlarge_mps_unit_cell()`
 (*tenpy.models.xxz_chain.XXZChain2* method), 413
`entropy()` (in module *tenpy.tools.math*), 572
`environment_sweeps()`
 (*tenpy.algorithms.dmrg.EngineCombine* method), 152
`environment_sweeps()`
 (*tenpy.algorithms.dmrg.EngineFracture* method), 160
`environment_sweeps()`
 (*tenpy.algorithms.purification.PurificationApplyMPO* method), 176
`eps` (*tenpy.algorithms.truncation.TruncationError* attribute), 134
`ExactDiag` (class in *tenpy.algorithms.exact_diag*), 193
`exp_H()` (*tenpy.algorithms.exact_diag.ExactDiag* method), 195
`expectation_value()`
 (*tenpy.networks.mpo.MPOEnvironment* method), 523
`expectation_value()`
 (*tenpy.networks.mps.MPSEnvironment* method), 512
`explicit_plus_hc` (*tenpy.models.model.CouplingModel* attribute), 370
`expm()` (in module *tenpy.linalg.np_conserved*), 219
`extend()` (*tenpy.linalg.charges.LegCharge* method), 241
`extend()` (*tenpy.linalg.charges.LegPipe* method), 246
`extend()` (*tenpy.linalg.np_conserved.Array* method), 206
`eye_like()` (in module *tenpy.linalg.np_conserved*), 220

F

`FermiHubbardChain` (class in *tenpy.models.hubbard*), 451
`FermionChain` (class in *tenpy.models.fermions_spinless*), 430
`FermionSite` (class in *tenpy.networks.site*), 480
`filling` (*tenpy.networks.site.BosonSite* attribute), 476
`filling` (*tenpy.networks.site.FermionSite* attribute), 481
`filling` (*tenpy.networks.site.SpinHalfFermionSite* attribute), 495
`find_class()` (*tenpy.tools.hdf5_io.Hdf5Loader* static method), 552
`fit_with_sum_of_exp()` (in module *tenpy.tools.fit*), 577
`flat_linop` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`flat_to_npc()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 259
`flat_to_npc()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 264
`flat_to_npc_all_sectors()`
 (*tenpy.linalg.sparse.FlatHermitianOperator* method), 259
`flat_to_npc_all_sectors()`
 (*tenpy.linalg.sparse.FlatLinearOperator* method), 264
`flat_to_npc_None_sector()`
 (*tenpy.linalg.sparse.FlatHermitianOperator* method), 259
`flat_to_npc_None_sector()`
 (*tenpy.linalg.sparse.FlatLinearOperator* method), 264
`FlatHermitianOperator` (class in *tenpy.linalg.sparse*), 258
`FlatLinearOperator` (class in *tenpy.linalg.sparse*), 262
`flip_charges_qconj()`
 (*tenpy.linalg.charges.LegCharge* method), 238
`flip_charges_qconj()`
 (*tenpy.linalg.charges.LegPipe* method), 246
`form` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`format_selection` (*tenpy.tools.hdf5_io.Hdf5Saver* attribute), 555
`from_add_charge()`
 (*tenpy.linalg.charges.LegCharge* class method), 237
`from_add_charge()` (*tenpy.linalg.charges.LegPipe* class method), 246
`from_change_charge()`
 (*tenpy.linalg.charges.LegCharge* class method), 237
`from_change_charge()`
 (*tenpy.linalg.charges.LegPipe* class method), 247
`from_drop_charge()`
 (*tenpy.linalg.charges.LegCharge* class method), 237
`from_drop_charge()` (*tenpy.linalg.charges.LegPipe* class method), 247
`from_func()` (*tenpy.linalg.np_conserved.Array* class method), 202
`from_func_square()`
 (*tenpy.linalg.np_conserved.Array* class method), 203
`from_guess_with_pipe()`
 (*tenpy.linalg.sparse.FlatHermitianOperator*


```

        class method), 259
from_guess_with_pipe()
    (tenpy.linalg.sparse.FlatLinearOperator
    class method), 263
from_H_mpo() (tenpy.algorithms.exact_diag.ExactDiag
    class method), 194
from_hdf5() (tenpy.linalg.charges.ChargeInfo class
    method), 232
from_hdf5() (tenpy.linalg.charges.LegCharge class
    method), 236
from_hdf5() (tenpy.linalg.charges.LegPipe class
    method), 245
from_hdf5() (tenpy.linalg.np_conserved.Array class
    method), 201
from_hdf5() (tenpy.models.fermions_spinless.FermionChain
    class method), 436
from_hdf5() (tenpy.models.hubbard.BoseHubbardChain
    class method), 448
from_hdf5() (tenpy.models.hubbard.FermiHubbardChain
    class method), 458
from_hdf5() (tenpy.models.lattice.Chain class
    method), 280
from_hdf5() (tenpy.models.lattice.Honeycomb class
    method), 288
from_hdf5() (tenpy.models.lattice.IrregularLattice
    class method), 297
from_hdf5() (tenpy.models.lattice.Kagome class
    method), 306
from_hdf5() (tenpy.models.lattice.Ladder class
    method), 314
from_hdf5() (tenpy.models.lattice.Lattice class
    method), 325
from_hdf5() (tenpy.models.lattice.SimpleLattice
    class method), 334
from_hdf5() (tenpy.models.lattice.Square class
    method), 343
from_hdf5() (tenpy.models.lattice.Triangular class
    method), 351
from_hdf5() (tenpy.models.lattice.TrivialLattice class
    method), 359
from_hdf5() (tenpy.models.model.CouplingModel
    class method), 375
from_hdf5() (tenpy.models.model.Model class
    method), 380
from_hdf5() (tenpy.models.model.MPOModel class
    method), 378
from_hdf5() (tenpy.models.model.MultiCouplingModel
    class method), 389
from_hdf5() (tenpy.models.model.NearestNeighborModel
    class method), 392
from_hdf5() (tenpy.models.spins.SpinChain class
    method), 424
from_hdf5() (tenpy.models.tf_ising.TFChain class
    method), 402
from_hdf5() (tenpy.models.toric_code.DualSquare
    class method), 467
from_hdf5() (tenpy.models.xxz_chain.XXZChain2
    class method), 414
from_hdf5() (tenpy.networks.site.BosonSite class
    method), 477
from_hdf5() (tenpy.networks.site.FermionSite class
    method), 481
from_hdf5() (tenpy.networks.site.GroupedSite class
    method), 486
from_hdf5() (tenpy.networks.site.Site class method),
    492
from_hdf5() (tenpy.networks.site.SpinHalfFermionSite
    class method), 496
from_hdf5() (tenpy.networks.site.SpinHalfSite class
    method), 500
from_hdf5() (tenpy.networks.site.SpinSite class
    method), 504
from_hdf5() (tenpy.networks.terms.CouplingTerms
    class method), 534
from_hdf5() (tenpy.networks.terms.MultiCouplingTerms
    class method), 538
from_hdf5() (tenpy.networks.terms.OnsiteTerms
    class method), 541
from_hdf5() (tenpy.networks.terms.TermList class
    method), 543
from_hdf5() (tenpy.tools.hdf5_io.Hdf5Exportable
    class method), 549
from_MPOModel() (tenpy.models.fermions_spinless.FermionChain
    class method), 436
from_MPOModel() (tenpy.models.hubbard.BoseHubbardChain
    class method), 447
from_MPOModel() (tenpy.models.hubbard.FermiHubbardChain
    class method), 457
from_MPOModel() (tenpy.models.model.NearestNeighborModel
    class method), 391
from_MPOModel() (tenpy.models.spins.SpinChain
    class method), 424
from_MPOModel() (tenpy.models.tf_ising.TFChain
    class method), 402
from_MPOModel() (tenpy.models.xxz_chain.XXZChain2
    class method), 413
from_ndarray() (tenpy.linalg.np_conserved.Array
    class method), 202
from_ndarray_trivial()
    (tenpy.linalg.np_conserved.Array class
    method), 201
from_norm() (tenpy.algorithms.truncation.TruncationError
    class method), 134
from_NpcArray() (tenpy.linalg.sparse.FlatHermitianOperator
    class method), 259
from_NpcArray() (tenpy.linalg.sparse.FlatLinearOperator
    class method), 263
from_qdict() (tenpy.linalg.charges.LegCharge class

```

method), 237
 from_qdict() (tenpy.linalg.charges.LegPipe class method), 247
 from_qflat() (tenpy.linalg.charges.LegCharge class method), 236
 from_qflat() (tenpy.linalg.charges.LegPipe class method), 247
 from_qind() (tenpy.linalg.charges.LegCharge class method), 237
 from_qind() (tenpy.linalg.charges.LegPipe class method), 248
 from_S() (tenpy.algorithms.truncation.TruncationError class method), 134
 from_term_list() (tenpy.networks.mpo.MPOGraph class method), 527
 from_terms() (tenpy.networks.mpo.MPOGraph class method), 526
 from_trivial() (tenpy.linalg.charges.LegCharge class method), 236
 from_trivial() (tenpy.linalg.charges.LegPipe class method), 248
 full_contraction() (tenpy.networks.mpo.MPOEnvironment method), 523
 full_contraction() (tenpy.networks.mps.MPSEnvironment method), 512
 full_diag_effH() (in module tenpy.algorithms.dmrgh), 169
 full_diagonalization() (tenpy.algorithms.exact_diag.ExactDiag method), 195
 full_H (tenpy.algorithms.exact_diag.ExactDiag attribute), 194
 full_to_mps() (tenpy.algorithms.exact_diag.ExactDiag method), 195
 full_version (in module tenpy.version), 589

G

gauge_hopping() (in module tenpy.models.hofstadter), 461
 gauge_total_charge() (tenpy.linalg.np_conserved.Array method), 206
 gcd() (in module tenpy.tools.math), 573
 gcd_array() (in module tenpy.tools.math), 573
 get_attr() (tenpy.tools.hdf5_io.Hdf5Loader static method), 552
 get_block() (tenpy.linalg.np_conserved.Array method), 205
 get_block_sizes() (tenpy.linalg.charges.LegCharge method), 239
 get_block_sizes() (tenpy.linalg.charges.LegPipe method), 248
 get_charge() (tenpy.linalg.charges.LegCharge method), 240
 get_charge() (tenpy.linalg.charges.LegPipe method), 248
 get_hc_op_name() (tenpy.networks.site.BosonSite method), 477
 get_hc_op_name() (tenpy.networks.site.FermionSite method), 481
 get_hc_op_name() (tenpy.networks.site.GroupedSite method), 486
 get_hc_op_name() (tenpy.networks.site.Site method), 491
 get_hc_op_name() (tenpy.networks.site.SpinHalfFermionSite method), 496
 get_hc_op_name() (tenpy.networks.site.SpinHalfSite method), 500
 get_hc_op_name() (tenpy.networks.site.SpinSite method), 504
 get_initialization_data() (tenpy.networks.mpo.MPOEnvironment method), 524
 get_initialization_data() (tenpy.networks.mps.MPSEnvironment method), 511
 get_lattice() (in module tenpy.models.lattice), 365
 get_leg() (tenpy.linalg.np_conserved.Array method), 204
 get_leg_index() (tenpy.linalg.np_conserved.Array method), 203
 get_leg_indices() (tenpy.linalg.np_conserved.Array method), 204
 get_leg_labels() (tenpy.linalg.np_conserved.Array method), 204
 get_level() (in module tenpy.tools.optimization), 586
 get_LP() (tenpy.networks.mpo.MPOEnvironment method), 522
 get_LP() (tenpy.networks.mps.MPSEnvironment method), 510
 get_LP_age() (tenpy.networks.mpo.MPOEnvironment method), 524
 get_LP_age() (tenpy.networks.mps.MPSEnvironment method), 511
 get_op() (tenpy.networks.site.BosonSite method), 477
 get_op() (tenpy.networks.site.FermionSite method), 482
 get_op() (tenpy.networks.site.GroupedSite method), 486
 get_op() (tenpy.networks.site.Site method), 491
 get_op() (tenpy.networks.site.SpinHalfFermionSite method), 496

- `get_op()` (*tenpy.networks.site.SpinHalfSite* method), 500
`get_op()` (*tenpy.networks.site.SpinSite* method), 504
`get_order()` (in module *tenpy.models.lattice*), 366
`get_order_grouped()` (in module *tenpy.models.lattice*), 366
`get_parameter()` (in module *tenpy.tools.params*), 563
`get_qindex()` (*tenpy.linalg.charges.LegCharge* method), 239
`get_qindex()` (*tenpy.linalg.charges.LegPipe* method), 248
`get_qindex_of_charges()` (*tenpy.linalg.charges.LegCharge* method), 240
`get_qindex_of_charges()` (*tenpy.linalg.charges.LegPipe* method), 248
`get_RP()` (*tenpy.networks.mpo.MPOEnvironment* method), 522
`get_RP()` (*tenpy.networks.mps.MPSEnvironment* method), 511
`get_RP_age()` (*tenpy.networks.mpo.MPOEnvironment* method), 524
`get_RP_age()` (*tenpy.networks.mps.MPSEnvironment* method), 511
`get_slice()` (*tenpy.linalg.charges.LegCharge* method), 239
`get_slice()` (*tenpy.linalg.charges.LegPipe* method), 248
`get_sweep_schedule()` (*tenpy.algorithms.dmrgh.EngineCombine* method), 152
`get_sweep_schedule()` (*tenpy.algorithms.dmrgh.EngineFracture* method), 160
`get_sweep_schedule()` (*tenpy.algorithms.purification.PurificationApplyMPO* method), 176
`get_xL()` (*tenpy.algorithms.dmrgh.DensityMatrixMixer* method), 149
`get_xR()` (*tenpy.algorithms.dmrgh.DensityMatrixMixer* method), 149
`git_revision` (in module *tenpy.version*), 589
`GOE()` (in module *tenpy.linalg.random_matrix*), 254
`gram_schmidt()` (in module *tenpy.linalg.lanczos*), 274
`graph` (*tenpy.networks.mpo.MPOGraph* attribute), 526
`grid_concat()` (in module *tenpy.linalg.np_conserved*), 220
`grid_insert_ops()` (in module *tenpy.networks.mpo*), 529
`grid_outer()` (in module *tenpy.linalg.np_conserved*), 221
`groundstate()` (*tenpy.algorithms.exact_diag.ExactDiag* method), 195
`group_sites()` (in module *tenpy.networks.site*), 506
`group_sites()` (*tenpy.models.fermions_spinless.FermionChain* method), 437
`group_sites()` (*tenpy.models.hubbard.BoseHubbardChain* method), 448
`group_sites()` (*tenpy.models.hubbard.FermiHubbardChain* method), 458
`group_sites()` (*tenpy.models.model.CouplingModel* method), 376
`group_sites()` (*tenpy.models.model.Model* method), 380
`group_sites()` (*tenpy.models.model.MPOModel* method), 378
`group_sites()` (*tenpy.models.model.MultiCouplingModel* method), 389
`group_sites()` (*tenpy.models.model.NearestNeighborModel* method), 392
`group_sites()` (*tenpy.models.spins.SpinChain* method), 425
`group_sites()` (*tenpy.models.tf_ising.TFIChain* method), 403
`group_sites()` (*tenpy.models.xxz_chain.XXZChain2* method), 414
`GroupedSite` (class in *tenpy.networks.site*), 484
`GUE()` (in module *tenpy.linalg.random_matrix*), 254
- ## H
- `H` (*tenpy.networks.mpo.MPOEnvironment* attribute), 521
`H()` (*tenpy.linalg.sparse.FlatHermitianOperator* property), 258
`H()` (*tenpy.linalg.sparse.FlatLinearOperator* property), 265
`H0_mixed` (class in *tenpy.algorithms.tdvp*), 171
`H1_mixed` (class in *tenpy.algorithms.tdvp*), 172
`H2_mixed` (class in *tenpy.algorithms.tdvp*), 173
`h5group` (*tenpy.tools.hdf5_io.Hdf5Loader* attribute), 552
`h5group` (*tenpy.tools.hdf5_io.Hdf5Saver* attribute), 554
`H_bond` (*tenpy.models.model.NearestNeighborModel* attribute), 391
`H_MPO` (*tenpy.models.model.MPOModel* attribute), 377
`has_edge()` (*tenpy.networks.mpo.MPOGraph* method), 528
`has_label()` (*tenpy.linalg.np_conserved.Array* method), 204
`have_cython_functions` (in module *tenpy.tools.optimization*), 589
`hc_ops` (*tenpy.networks.site.Site* attribute), 490
`Hdf5Exportable` (class in *tenpy.tools.hdf5_io*), 548
`Hdf5ExportError`, 557
`Hdf5FormatError`, 557
`Hdf5Ignored` (class in *tenpy.tools.hdf5_io*), 550
`Hdf5ImportError`, 557

Hdf5Loader (class in *tenpy.tools.hdf5_io*), 551
Hdf5Saver (class in *tenpy.tools.hdf5_io*), 554
Honeycomb (class in *tenpy.models.lattice*), 286

I

iadd_prefactor_other() (tenpy.linalg.np_conserved.Array method), 213
ibinary_blockwise() (tenpy.linalg.np_conserved.Array method), 213
iconj() (tenpy.linalg.np_conserved.Array method), 212
idrop_labels() (tenpy.linalg.np_conserved.Array method), 204
ignore_unknown(tenpy.tools.hdf5_io.Hdf5Loader attribute), 552
ind_len(tenpy.linalg.charges.LegCharge attribute), 235
init_env() (tenpy.algorithms.dmrng.EngineCombine method), 152
init_env() (tenpy.algorithms.dmrng.EngineFracture method), 160
init_env() (tenpy.algorithms.purification.PurificationApp method), 176
init_lattice() (tenpy.models.fermions_spinless.FermionChain method), 437
init_lattice() (tenpy.models.hubbard.BoseHubbardChain method), 448
init_lattice() (tenpy.models.hubbard.FermiHubbardChain method), 458
init_lattice() (tenpy.models.spins.SpinChain method), 425
init_lattice() (tenpy.models.tf_ising.TFChain method), 403
init_lattice() (tenpy.models.xx_z_chain.XXZChain2 method), 414
init_LP() (tenpy.networks.mpo.MPOEnvironment method), 521
init_LP() (tenpy.networks.mps.MPSEnvironment method), 510
init_RP() (tenpy.networks.mpo.MPOEnvironment method), 522
init_RP() (tenpy.networks.mps.MPSEnvironment method), 510
init_sites() (tenpy.models.fermions_spinless.FermionChain method), 438
init_sites() (tenpy.models.hubbard.BoseHubbardChain method), 449
init_sites() (tenpy.models.hubbard.FermiHubbardChain method), 459
init_sites() (tenpy.models.spins.SpinChain method), 426
init_sites() (tenpy.models.tf_ising.TFChain method), 404
init_sites() (tenpy.models.xx_z_chain.XXZChain2 method), 407
init_terms() (tenpy.models.fermions_spinless.FermionChain method), 438
init_terms() (tenpy.models.hubbard.BoseHubbardChain method), 449
init_terms() (tenpy.models.hubbard.FermiHubbardChain method), 459
init_terms() (tenpy.models.spins.SpinChain method), 426
init_terms() (tenpy.models.tf_ising.TFChain method), 404
init_terms() (tenpy.models.xx_z_chain.XXZChain2 method), 408
initial_guess() (tenpy.networks.mps.TransferMatrix method), 516
inner() (in module tenpy.linalg.np_conserved), 222
inverse_permutation() (in module tenpy.tools.misc), 568
iproject() (tenpy.linalg.np_conserved.Array method), 210
is_mpo_zeros() (tenpy.linalg.np_conserved.Array method), 210
is_replace_label() (tenpy.linalg.np_conserved.Array method), 204
is_replace_labels() (tenpy.linalg.np_conserved.Array method), 204
IrregularLattice (class in tenpy.models.lattice), 295
is_blocked() (tenpy.linalg.charges.LegCharge method), 238
is_blocked() (tenpy.linalg.charges.LegPipe method), 248
is_bunched() (tenpy.linalg.charges.LegCharge method), 238
is_bunched() (tenpy.linalg.charges.LegPipe method), 248
is_completely_blocked() (tenpy.linalg.np_conserved.Array method), 207
is_non_string_iterable() (in module tenpy.tools.string), 579
is_sorted() (tenpy.linalg.charges.LegCharge method), 238
is_sorted() (tenpy.linalg.charges.LegPipe method), 248
iscale_axis() (tenpy.linalg.np_conserved.Array method), 211
iscale_prefactor() (tenpy.linalg.np_conserved.Array method), 213

`iset_leg_labels()`
 (*tenpy.linalg.np_conserved.Array* *method*),
 204
`isort_qdata()` (*tenpy.linalg.np_conserved.Array*
 method), 208
`iswapaxes()` (*tenpy.linalg.np_conserved.Array*
 method), 211
`itranspose()` (*tenpy.linalg.np_conserved.Array*
 method), 211
`iunary_blockwise()`
 (*tenpy.linalg.np_conserved.Array* *method*),
 212

J

`JW_exponent` (*tenpy.networks.site.Site* attribute), 490

K

`Kagome` (*class in tenpy.models.lattice*), 304
`kronckerproduct()`
 (*tenpy.networks.site.GroupedSite* *method*),
 485

L

`L` (*tenpy.networks.mps.MPSEnvironment* attribute), 509
`L` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`L` (*tenpy.networks.terms.CouplingTerms* attribute), 532
`L` (*tenpy.networks.terms.MultiCouplingTerms* attribute),
 536
`L` (*tenpy.networks.terms.OnsiteTerms* attribute), 540
`L()` (*tenpy.networks.mpo.MPOGraph* property), 527
`label_split` (*tenpy.networks.mps.TransferMatrix* at-
 tribute), 515
`labels` (*tenpy.networks.site.GroupedSite* attribute), 485
`Ladder` (*class in tenpy.models.lattice*), 313
`lanczos()` (*in module tenpy.linalg.lanczos*), 274
`lanczos_arpack()` (*in module tenpy.linalg.lanczos*),
 274
`lat` (*tenpy.models.model.Model* attribute), 379
`lat2mps_idx()` (*tenpy.models.lattice.Chain* method),
 280
`lat2mps_idx()` (*tenpy.models.lattice.Honeycomb*
 method), 288
`lat2mps_idx()` (*tenpy.models.lattice.IrregularLattice*
 method), 298
`lat2mps_idx()` (*tenpy.models.lattice.Kagome*
 method), 306
`lat2mps_idx()` (*tenpy.models.lattice.Ladder*
 method), 315
`lat2mps_idx()` (*tenpy.models.lattice.Lattice*
 method), 326
`lat2mps_idx()` (*tenpy.models.lattice.SimpleLattice*
 method), 334
`lat2mps_idx()` (*tenpy.models.lattice.Square*
 method), 343

`lat2mps_idx()` (*tenpy.models.lattice.Triangular*
 method), 352
`lat2mps_idx()` (*tenpy.models.lattice.TrivialLattice*
 method), 359
`lat2mps_idx()` (*tenpy.models.toric_code.DualSquare*
 method), 467
`Lattice` (*class in tenpy.models.lattice*), 322
`lcm()` (*in module tenpy.tools.math*), 573
`leg` (*tenpy.linalg.sparse.FlatLinearOperator* attribute),
 263
`leg` (*tenpy.networks.site.Site* attribute), 489
`LegCharge` (*class in tenpy.linalg.charges*), 234
`LegPipe` (*class in tenpy.linalg.charges*), 243
`legs` (*tenpy.linalg.charges.LegPipe* attribute), 243
`legs` (*tenpy.linalg.np_conserved.Array* attribute), 200
`length` (*tenpy.algorithms.mps_common.EffectiveH* at-
 tribute), 140
`length` (*tenpy.algorithms.mps_common.OneSiteH* at-
 tribute), 142
`length` (*tenpy.algorithms.mps_common.TwoSiteH* at-
 tribute), 144
`LeviCivita3` (*in module tenpy.tools.math*), 576
`lexsort()` (*in module tenpy.tools.misc*), 569
`LHeff` (*tenpy.algorithms.mps_common.TwoSiteH*
 attribute), 144
`lin_fit_res()` (*in module tenpy.tools.fit*), 578
`linear_fit()` (*in module tenpy.tools.fit*), 578
`list_to_dict_list()` (*in* *module*
 tenpy.tools.misc), 569
`load()` (*in module tenpy.tools.hdf5_io*), 558
`load()` (*tenpy.tools.hdf5_io.Hdf5Loader* method), 552
`load_dataset()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 552
`load_dict()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 553
`load_dtype()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 553
`load_from_hdf5()` (*in module tenpy.tools.hdf5_io*),
 558
`load_general_dict()`
 (*tenpy.tools.hdf5_io.Hdf5Loader* *method*),
 553
`load_hdf5exportable()`
 (*tenpy.tools.hdf5_io.Hdf5Loader* *method*),
 553
`load_ignored()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 553
`load_list()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 552
`load_none()` (*tenpy.tools.hdf5_io.Hdf5Loader*
 method), 552
`load_omp_library()` (*in* *module*
 tenpy.tools.process), 581
`load_range()` (*tenpy.tools.hdf5_io.Hdf5Loader*

- method), 553
- load_set() (tenpy.tools.hdf5_io.Hdf5Loader method), 553
- load_simple_dict() (tenpy.tools.hdf5_io.Hdf5Loader method), 553
- load_tuple() (tenpy.tools.hdf5_io.Hdf5Loader method), 553
- Lp (tenpy.algorithms.tdvp.H0_mixed attribute), 171
- Lp (tenpy.algorithms.tdvp.H1_mixed attribute), 172
- Lp (tenpy.algorithms.tdvp.H2_mixed attribute), 173
- Ls (tenpy.models.lattice.Lattice attribute), 323
- ## M
- make_eff_H() (tenpy.algorithms.dmrq.EngineCombine method), 153
- make_eff_H() (tenpy.algorithms.dmrq.EngineFracture method), 161
- make_eff_H() (tenpy.algorithms.purification.PurificationApplyMPO method), 177
- make_pipe() (tenpy.linalg.np_conserved.Array method), 208
- make_valid() (tenpy.linalg.charges.ChargeInfo method), 233
- make_W_II() (in module tenpy.networks.mpo), 529
- map_incoming_flat() (tenpy.linalg.charges.LegPipe method), 246
- matmat() (tenpy.linalg.sparse.FlatHermitianOperator method), 260
- matmat() (tenpy.linalg.sparse.FlatLinearOperator method), 265
- matvec() (tenpy.algorithms.exact_diag.ExactDiag method), 195
- matvec() (tenpy.algorithms.mps_common.EffectiveH method), 140
- matvec() (tenpy.algorithms.mps_common.OneSiteH method), 142
- matvec() (tenpy.algorithms.mps_common.TwoSiteH method), 145
- matvec() (tenpy.algorithms.purification.PurificationTwoSite method), 189
- matvec() (tenpy.linalg.np_conserved.Array method), 213
- matvec() (tenpy.linalg.sparse.FlatHermitianOperator method), 260
- matvec() (tenpy.linalg.sparse.FlatLinearOperator method), 266
- matvec() (tenpy.linalg.sparse.NpcLinearOperator method), 268
- matvec() (tenpy.networks.mps.TransferMatrix method), 515
- matvec_count (tenpy.linalg.sparse.FlatLinearOperator attribute), 263
- matvec_to_array() (in module tenpy.tools.math), 573
- max_range (tenpy.networks.mpo.MPOGraph attribute), 526
- max_range() (tenpy.networks.terms.CouplingTerms method), 532
- max_range() (tenpy.networks.terms.MultiCouplingTerms method), 537
- max_size (tenpy.algorithms.exact_diag.ExactDiag attribute), 194
- memo_load (tenpy.tools.hdf5_io.Hdf5Loader attribute), 552
- memo_save (tenpy.tools.hdf5_io.Hdf5Saver attribute), 555
- memorize_load() (tenpy.tools.hdf5_io.Hdf5Loader method), 552
- memorize_save() (tenpy.tools.hdf5_io.Hdf5Saver method), 555
- message() (in module tenpy.tools.process), 581
- mix_rho_L() (tenpy.algorithms.dmrq.DensityMatrixMixer method), 148
- mix_rho_R() (tenpy.algorithms.dmrq.DensityMatrixMixer method), 148
- mixed_svd() (tenpy.algorithms.dmrq.EngineCombine method), 153
- mixed_svd() (tenpy.algorithms.dmrq.EngineFracture method), 161
- mixer_activate() (tenpy.algorithms.dmrq.EngineCombine method), 153
- mixer_activate() (tenpy.algorithms.dmrq.EngineFracture method), 161
- mixer_cleanup() (tenpy.algorithms.dmrq.EngineCombine method), 153
- mixer_cleanup() (tenpy.algorithms.dmrq.EngineFracture method), 161
- mkl_get_nthreads() (in module tenpy.tools.process), 582
- mkl_set_nthreads() (in module tenpy.tools.process), 582
- Model (tenpy.linalg.charges.ChargeInfo property), 233
- Model (class in tenpy.models.model), 379
- model (tenpy.algorithms.exact_diag.ExactDiag attribute), 193
- module
- tenpy, 131
 - tenpy.algorithms, 132
 - tenpy.algorithms.dmrq, 170
 - tenpy.algorithms.exact_diag, 196
 - tenpy.algorithms.mpo_evolution, 190
 - tenpy.algorithms.mps_common, 145
 - tenpy.algorithms.network_contractor, 192
 - tenpy.algorithms.purification, 189
 - tenpy.algorithms.tdvp, 174

tenpy.algorithms.tebd, 137
 tenpy.algorithms.truncation, 136
 tenpy.linalg, 196
 tenpy.linalg.charges, 250
 tenpy.linalg.lanczos, 275
 tenpy.linalg.np_conserved, 227
 tenpy.linalg.random_matrix, 255
 tenpy.linalg.sparse, 273
 tenpy.linalg.svd_robust, 252
 tenpy.models, 275
 tenpy.models.fermions_spinless, 439
 tenpy.models.haldane, 463
 tenpy.models.hofstadter, 462
 tenpy.models.hubbard, 460
 tenpy.models.lattice, 367
 tenpy.models.model, 393
 tenpy.models.spins, 427
 tenpy.models.spins_nnn, 428
 tenpy.models.tf_ising, 405
 tenpy.models.toric_code, 473
 tenpy.models.xx_z_chain, 416
 tenpy.networks, 473
 tenpy.networks.mpo, 530
 tenpy.networks.mps, 518
 tenpy.networks.purification_mps, 545
 tenpy.networks.site, 507
 tenpy.networks.terms, 544
 tenpy.tools, 547
 tenpy.tools.fit, 579
 tenpy.tools.hdf5_io, 560
 tenpy.tools.math, 576
 tenpy.tools.misc, 572
 tenpy.tools.optimization, 588
 tenpy.tools.params, 565
 tenpy.tools.process, 583
 tenpy.tools.string, 580
 tenpy.version, 589
 move_right (*tenpy.algorithms.mps_common.EffectiveH*
attribute), 140
 MPOEnvironment (*class in tenpy.networks.mpo*), 520
 MPOGraph (*class in tenpy.networks.mpo*), 525
 MPOModel (*class in tenpy.models.model*), 377
 mps2lat_idx() (*tenpy.models.lattice.Chain method*),
 280
 mps2lat_idx() (*tenpy.models.lattice.Honeycomb*
method), 288
 mps2lat_idx() (*tenpy.models.lattice.IrregularLattice*
method), 298
 mps2lat_idx() (*tenpy.models.lattice.Kagome*
method), 306
 mps2lat_idx() (*tenpy.models.lattice.Ladder*
method), 315
 mps2lat_idx() (*tenpy.models.lattice.Lattice*
method), 326
 mps2lat_idx() (*tenpy.models.lattice.SimpleLattice*
method), 335
 mps2lat_idx() (*tenpy.models.lattice.Square*
method), 343
 mps2lat_idx() (*tenpy.models.lattice.Triangular*
method), 352
 mps2lat_idx() (*tenpy.models.lattice.TrivialLattice*
method), 359
 mps2lat_idx() (*tenpy.models.toric_code.DualSquare*
method), 468
 mps2lat_values() (*tenpy.models.lattice.Chain*
method), 280
 mps2lat_values() (*tenpy.models.lattice.Honeycomb*
method), 289
 mps2lat_values() (*tenpy.models.lattice.IrregularLattice*
method), 299
 mps2lat_values() (*tenpy.models.lattice.Kagome*
method), 306
 mps2lat_values() (*tenpy.models.lattice.Ladder*
method), 315
 mps2lat_values() (*tenpy.models.lattice.Lattice*
method), 327
 mps2lat_values() (*tenpy.models.lattice.SimpleLattice*
method), 333
 mps2lat_values() (*tenpy.models.lattice.Square*
method), 344
 mps2lat_values() (*tenpy.models.lattice.Triangular*
method), 352
 mps2lat_values() (*tenpy.models.lattice.TrivialLattice*
method), 360
 mps2lat_values() (*tenpy.models.toric_code.DualSquare*
method), 468
 mps2lat_values_masked() (*tenpy.models.lattice.Chain method*), 280
 mps2lat_values_masked() (*tenpy.models.lattice.Honeycomb method*),
 290
 mps2lat_values_masked() (*tenpy.models.lattice.IrregularLattice method*),
 300
 mps2lat_values_masked() (*tenpy.models.lattice.Kagome method*), 307
 mps2lat_values_masked() (*tenpy.models.lattice.Ladder method*), 316
 mps2lat_values_masked() (*tenpy.models.lattice.Lattice method*), 328
 mps2lat_values_masked() (*tenpy.models.lattice.SimpleLattice method*),
 335
 mps2lat_values_masked() (*tenpy.models.lattice.Square method*), 344
 mps2lat_values_masked() (*tenpy.models.lattice.Triangular method*),
 352

```

mps2lat_values_masked() (tenpy.models.toric_code.DualSquare method), 470
    (tenpy.models.lattice.TrivialLattice method), 361
mps2lat_values_masked() (tenpy.models.toric_code.DualSquare method), 469
mps_idx_fix_u() (tenpy.models.lattice.Chain method), 281
mps_idx_fix_u() (tenpy.models.lattice.Honeycomb method), 290
mps_idx_fix_u() (tenpy.models.lattice.IrregularLattice method), 297
mps_idx_fix_u() (tenpy.models.lattice.Kagome method), 308
mps_idx_fix_u() (tenpy.models.lattice.Ladder method), 316
mps_idx_fix_u() (tenpy.models.lattice.Lattice method), 327
mps_idx_fix_u() (tenpy.models.lattice.SimpleLattice method), 335
mps_idx_fix_u() (tenpy.models.lattice.Square method), 344
mps_idx_fix_u() (tenpy.models.lattice.Triangular method), 352
mps_idx_fix_u() (tenpy.models.lattice.TrivialLattice method), 361
mps_idx_fix_u() (tenpy.models.toric_code.DualSquare method), 469
mps_lat_idx_fix_u() (tenpy.models.lattice.Chain method), 281
mps_lat_idx_fix_u() (tenpy.models.lattice.Honeycomb method), 290
mps_lat_idx_fix_u() (tenpy.models.lattice.IrregularLattice method), 300
mps_lat_idx_fix_u() (tenpy.models.lattice.Kagome method), 308
mps_lat_idx_fix_u() (tenpy.models.lattice.Ladder method), 317
mps_lat_idx_fix_u() (tenpy.models.lattice.Lattice method), 327
mps_lat_idx_fix_u() (tenpy.models.lattice.SimpleLattice method), 335
mps_lat_idx_fix_u() (tenpy.models.lattice.Square method), 344
mps_lat_idx_fix_u() (tenpy.models.lattice.Triangular method), 353
mps_lat_idx_fix_u() (tenpy.models.lattice.TrivialLattice method), 361
mps_lat_idx_fix_u() (tenpy.models.toric_code.DualSquare method), 470
mps_sites() (tenpy.models.lattice.Chain method), 281
mps_sites() (tenpy.models.lattice.Honeycomb method), 290
mps_sites() (tenpy.models.lattice.IrregularLattice method), 300
mps_sites() (tenpy.models.lattice.Kagome method), 308
mps_sites() (tenpy.models.lattice.Ladder method), 317
mps_sites() (tenpy.models.lattice.Lattice method), 326
mps_sites() (tenpy.models.lattice.SimpleLattice method), 336
mps_sites() (tenpy.models.lattice.Square method), 344
mps_sites() (tenpy.models.lattice.Triangular method), 353
mps_sites() (tenpy.models.lattice.TrivialLattice method), 361
mps_sites() (tenpy.models.toric_code.DualSquare method), 470
mps_to_full() (tenpy.algorithms.exact_diag.ExactDiag method), 195
MPSEnvironment (class in tenpy.networks.mps), 508
multi_coupling_shape() (tenpy.models.lattice.Chain method), 281
multi_coupling_shape() (tenpy.models.lattice.Honeycomb method), 291
multi_coupling_shape() (tenpy.models.lattice.IrregularLattice method), 300
multi_coupling_shape() (tenpy.models.lattice.Kagome method), 308
multi_coupling_shape() (tenpy.models.lattice.Ladder method), 317
multi_coupling_shape() (tenpy.models.lattice.Lattice method), 330
multi_coupling_shape() (tenpy.models.lattice.SimpleLattice method), 336
multi_coupling_shape() (tenpy.models.lattice.Square method), 345
multi_coupling_shape() (tenpy.models.lattice.Triangular method), 353
multi_coupling_shape() (tenpy.models.lattice.TrivialLattice method), 362
multi_coupling_shape() (tenpy.models.toric_code.DualSquare method),

```


- 470
- `multi_coupling_term_handle_JW()` (*tenpy.networks.terms.MultiCouplingTerms* method), 536
- `multi_sites_combine_charges()` (in module *tenpy.networks.site*), 506
- `MultiCouplingModel` (class in *tenpy.models.model*), 382
- `MultiCouplingTerms` (class in *tenpy.networks.terms*), 536
- `multiply_op_names()` (*tenpy.networks.site.BosonSite* method), 477
- `multiply_op_names()` (*tenpy.networks.site.FermionSite* method), 482
- `multiply_op_names()` (*tenpy.networks.site.GroupedSite* method), 486
- `multiply_op_names()` (*tenpy.networks.site.Site* method), 492
- `multiply_op_names()` (*tenpy.networks.site.SpinHalfFermionSite* method), 496
- `multiply_op_names()` (*tenpy.networks.site.SpinHalfSite* method), 500
- `multiply_op_names()` (*tenpy.networks.site.SpinSite* method), 504
- ## N
- `N` (*tenpy.algorithms.mps_common.EffectiveH* attribute), 140
- `N_cells` (*tenpy.models.lattice.Lattice* attribute), 323
- `N_rings` (*tenpy.models.lattice.Lattice* attribute), 323
- `N_sites` (*tenpy.models.lattice.Lattice* attribute), 323
- `n_sites` (*tenpy.networks.site.GroupedSite* attribute), 485
- `N_sites_per_ring` (*tenpy.models.lattice.Lattice* attribute), 323
- `name` (*tenpy.tools.hdf5_io.Hdf5Ignored* attribute), 550
- `names` (*tenpy.linalg.charges.ChargeInfo* attribute), 231
- `ncon()` (in module *tenpy.algorithms.network_contractor*), 191
- `ndim()` (*tenpy.linalg.np_conserved.Array* property), 203
- `NearestNeighborModel` (class in *tenpy.models.model*), 391
- `need_JW_string` (*tenpy.networks.site.Site* attribute), 489
- `nlegs` (*tenpy.linalg.charges.LegPipe* attribute), 243
- `norm()` (in module *tenpy.linalg.np_conserved*), 222
- `norm()` (*tenpy.linalg.np_conserved.Array* method), 213
- `npc_matvec` (*tenpy.linalg.sparse.FlatLinearOperator* attribute), 263
- `npc_to_flat()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 260
- `npc_to_flat()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 264
- `npc_to_flat_all_sectors()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 260
- `npc_to_flat_all_sectors()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 265
- `NpcLinearOperator` (class in *tenpy.linalg.sparse*), 267
- `NpcLinearOperatorWrapper` (class in *tenpy.linalg.sparse*), 269
- `number_nearest_neighbors()` (*tenpy.models.lattice.Chain* method), 281
- `number_nearest_neighbors()` (*tenpy.models.lattice.Honeycomb* method), 291
- `number_nearest_neighbors()` (*tenpy.models.lattice.IrregularLattice* method), 300
- `number_nearest_neighbors()` (*tenpy.models.lattice.Kagome* method), 308
- `number_nearest_neighbors()` (*tenpy.models.lattice.Ladder* method), 317
- `number_nearest_neighbors()` (*tenpy.models.lattice.Lattice* method), 329
- `number_nearest_neighbors()` (*tenpy.models.lattice.SimpleLattice* method), 336
- `number_nearest_neighbors()` (*tenpy.models.lattice.Square* method), 345
- `number_nearest_neighbors()` (*tenpy.models.lattice.Triangular* method), 353
- `number_nearest_neighbors()` (*tenpy.models.lattice.TrivialLattice* method), 362
- `number_nearest_neighbors()` (*tenpy.models.toric_code.DualSquare* method), 470
- `number_next_nearest_neighbors()` (*tenpy.models.lattice.Chain* method), 281
- `number_next_nearest_neighbors()` (*tenpy.models.lattice.Honeycomb* method), 291
- `number_next_nearest_neighbors()` (*tenpy.models.lattice.IrregularLattice* method), 301
- `number_next_nearest_neighbors()` (*tenpy.models.lattice.Kagome* method), 309

`number_next_nearest_neighbors()` (*tenpy.models.lattice.Ladder method*), 317
`number_next_nearest_neighbors()` (*tenpy.models.lattice.Lattice method*), 329
`number_next_nearest_neighbors()` (*tenpy.models.lattice.SimpleLattice method*), 336
`number_next_nearest_neighbors()` (*tenpy.models.lattice.Square method*), 345
`number_next_nearest_neighbors()` (*tenpy.models.lattice.Triangular method*), 353
`number_next_nearest_neighbors()` (*tenpy.models.lattice.TrivialLattice method*), 362
`number_next_nearest_neighbors()` (*tenpy.models.toric_code.DualSquare method*), 470

O

`O_close_1()` (*in module tenpy.linalg.random_matrix*), 254
`omp_get_nthreads()` (*in module tenpy.tools.process*), 582
`omp_set_nthreads()` (*in module tenpy.tools.process*), 582
`ones()` (*in module tenpy.linalg.np_conserved*), 223
`OneSiteH` (*class in tenpy.algorithms.mps_common*), 141
`onsite_ops()` (*tenpy.networks.site.BosonSite property*), 478
`onsite_ops()` (*tenpy.networks.site.FermionSite property*), 482
`onsite_ops()` (*tenpy.networks.site.GroupedSite property*), 486
`onsite_ops()` (*tenpy.networks.site.Site property*), 490
`onsite_ops()` (*tenpy.networks.site.SpinHalfFermionSite property*), 496
`onsite_ops()` (*tenpy.networks.site.SpinHalfSite property*), 500
`onsite_ops()` (*tenpy.networks.site.SpinSite property*), 504
`onsite_terms` (*tenpy.models.model.CouplingModel attribute*), 370
`onsite_terms` (*tenpy.networks.terms.OnsiteTerms attribute*), 540
`OnsiteTerms` (*class in tenpy.networks.terms*), 540
`op_needs_JW()` (*tenpy.networks.site.BosonSite method*), 478
`op_needs_JW()` (*tenpy.networks.site.FermionSite method*), 482
`op_needs_JW()` (*tenpy.networks.site.GroupedSite method*), 486
`op_needs_JW()` (*tenpy.networks.site.Site method*), 492
`op_needs_JW()` (*tenpy.networks.site.SpinHalfFermionSite method*), 497
`op_needs_JW()` (*tenpy.networks.site.SpinHalfSite method*), 501
`op_needs_JW()` (*tenpy.networks.site.SpinSite method*), 505
`opnames` (*tenpy.networks.site.Site attribute*), 489
`ops` (*tenpy.networks.site.Site attribute*), 489
`OptimizationFlag` (*class in tenpy.tools.optimization*), 584
`optimize()` (*in module tenpy.tools.optimization*), 586
`order()` (*tenpy.models.lattice.Chain property*), 282
`order()` (*tenpy.models.lattice.Honeycomb property*), 291
`order()` (*tenpy.models.lattice.IrregularLattice property*), 297
`order()` (*tenpy.models.lattice.Kagome property*), 309
`order()` (*tenpy.models.lattice.Ladder property*), 317
`order()` (*tenpy.models.lattice.Lattice property*), 325
`order()` (*tenpy.models.lattice.SimpleLattice property*), 336
`order()` (*tenpy.models.lattice.Square property*), 345
`order()` (*tenpy.models.lattice.Triangular property*), 353
`order()` (*tenpy.models.lattice.TrivialLattice property*), 362
`order()` (*tenpy.models.toric_code.DualSquare property*), 470
`order_combine()` (*tenpy.networks.terms.TermList method*), 543
`order_combine_term()` (*in module tenpy.networks.terms*), 544
`ordering()` (*tenpy.models.lattice.Chain method*), 279
`ordering()` (*tenpy.models.lattice.Honeycomb method*), 286
`ordering()` (*tenpy.models.lattice.IrregularLattice method*), 297
`ordering()` (*tenpy.models.lattice.Kagome method*), 309
`ordering()` (*tenpy.models.lattice.Ladder method*), 317
`ordering()` (*tenpy.models.lattice.Lattice method*), 325
`ordering()` (*tenpy.models.lattice.SimpleLattice method*), 336
`ordering()` (*tenpy.models.lattice.Square method*), 345
`ordering()` (*tenpy.models.lattice.Triangular method*), 353
`ordering()` (*tenpy.models.lattice.TrivialLattice method*), 362
`ordering()` (*tenpy.models.toric_code.DualSquare method*), 465
`orig_operator` (*tenpy.linalg.sparse.NpcLinearOperatorWrapper*

- `attribute`), 269
`OrthogonalNpcLinearOperator` (class in `tenpy.linalg.sparse`), 270
`outer()` (in module `tenpy.linalg.np_conserved`), 223
`outer_conj()` (`tenpy.linalg.charges.LegPipe` method), 245
`outer_product` (in module `tenpy.algorithms.network_contractor`), 192
`ov` (`tenpy.algorithms.truncation.TruncationError` attribute), 134
`ov_err()` (`tenpy.algorithms.truncation.TruncationError` property), 134
- ## P
- `pad()` (in module `tenpy.tools.misc`), 569
`pairs` (`tenpy.models.lattice.Lattice` attribute), 324
`perm` (`tenpy.networks.site.Site` attribute), 489
`perm_flat_from_perm_qind()` (`tenpy.linalg.charges.LegCharge` method), 241
`perm_flat_from_perm_qind()` (`tenpy.linalg.charges.LegPipe` method), 249
`perm_qind_from_perm_flat()` (`tenpy.linalg.charges.LegCharge` method), 241
`perm_qind_from_perm_flat()` (`tenpy.linalg.charges.LegPipe` method), 249
`perm_sign()` (in module `tenpy.tools.math`), 574
`permute()` (`tenpy.linalg.np_conserved.Array` method), 211
`perturb_svd()` (`tenpy.algorithms.dmrgh.DensityMatrixMixer` method), 147
`perturb_svd()` (`tenpy.algorithms.dmrgh.SingleSiteMixer` method), 166
`perturb_svd()` (`tenpy.algorithms.dmrgh.TwoSiteMixer` method), 168
`pinv()` (in module `tenpy.linalg.np_conserved`), 224
`pipe` (`tenpy.networks.mps.TransferMatrix` attribute), 515
`plot_alg_decay_fit()` (in module `tenpy.tools.fit`), 578
`plot_basis()` (`tenpy.models.lattice.Chain` method), 282
`plot_basis()` (`tenpy.models.lattice.Honeycomb` method), 291
`plot_basis()` (`tenpy.models.lattice.IrregularLattice` method), 301
`plot_basis()` (`tenpy.models.lattice.Kagome` method), 309
`plot_basis()` (`tenpy.models.lattice.Ladder` method), 318
`plot_basis()` (`tenpy.models.lattice.Lattice` method), 331
`plot_basis()` (`tenpy.models.lattice.SimpleLattice` method), 337
`plot_basis()` (`tenpy.models.lattice.Square` method), 346
`plot_basis()` (`tenpy.models.lattice.Triangular` method), 354
`plot_basis()` (`tenpy.models.lattice.TrivialLattice` method), 363
`plot_basis()` (`tenpy.models.toric_code.DualSquare` method), 470
`plot_bc_identified()` (`tenpy.models.lattice.Chain` method), 282
`plot_bc_identified()` (`tenpy.models.lattice.Honeycomb` method), 291
`plot_bc_identified()` (`tenpy.models.lattice.IrregularLattice` method), 301
`plot_bc_identified()` (`tenpy.models.lattice.Kagome` method), 309
`plot_bc_identified()` (`tenpy.models.lattice.Ladder` method), 318
`plot_bc_identified()` (`tenpy.models.lattice.Lattice` method), 331
`plot_bc_identified()` (`tenpy.models.lattice.SimpleLattice` method), 337
`plot_bc_identified()` (`tenpy.models.lattice.Square` method), 346
`plot_bc_identified()` (`tenpy.models.lattice.Triangular` method), 354
`plot_bc_identified()` (`tenpy.models.lattice.TrivialLattice` method), 363
`plot_bc_identified()` (`tenpy.models.toric_code.DualSquare` method), 470
`plot_coupling()` (`tenpy.models.lattice.Chain` method), 282
`plot_coupling()` (`tenpy.models.lattice.Honeycomb` method), 291
`plot_coupling()` (`tenpy.models.lattice.IrregularLattice` method), 301
`plot_coupling()` (`tenpy.models.lattice.Kagome` method), 310
`plot_coupling()` (`tenpy.models.lattice.Ladder` method), 318
`plot_coupling()` (`tenpy.models.lattice.Lattice` method), 331
`plot_coupling()` (`tenpy.models.lattice.SimpleLattice` method), 337
`plot_coupling()` (`tenpy.models.lattice.Square` method), 346

`plot_coupling()` (*tenpy.models.lattice.Triangular method*), 354
`plot_coupling()` (*tenpy.models.lattice.TrivialLattice method*), 363
`plot_coupling()` (*tenpy.models.toric_code.DualSquare method*), 471
`plot_coupling_terms()` (*tenpy.networks.terms.CouplingTerms method*), 533
`plot_coupling_terms()` (*tenpy.networks.terms.MultiCouplingTerms method*), 538
`plot_order()` (*tenpy.models.lattice.Chain method*), 282
`plot_order()` (*tenpy.models.lattice.Honeycomb method*), 292
`plot_order()` (*tenpy.models.lattice.IrregularLattice method*), 301
`plot_order()` (*tenpy.models.lattice.Kagome method*), 310
`plot_order()` (*tenpy.models.lattice.Ladder method*), 319
`plot_order()` (*tenpy.models.lattice.Lattice method*), 330
`plot_order()` (*tenpy.models.lattice.SimpleLattice method*), 337
`plot_order()` (*tenpy.models.lattice.Square method*), 346
`plot_order()` (*tenpy.models.lattice.Triangular method*), 355
`plot_order()` (*tenpy.models.lattice.TrivialLattice method*), 363
`plot_order()` (*tenpy.models.toric_code.DualSquare method*), 471
`plot_sites()` (*tenpy.models.lattice.Chain method*), 283
`plot_sites()` (*tenpy.models.lattice.Honeycomb method*), 292
`plot_sites()` (*tenpy.models.lattice.IrregularLattice method*), 302
`plot_sites()` (*tenpy.models.lattice.Kagome method*), 310
`plot_sites()` (*tenpy.models.lattice.Ladder method*), 319
`plot_sites()` (*tenpy.models.lattice.Lattice method*), 330
`plot_sites()` (*tenpy.models.lattice.SimpleLattice method*), 338
`plot_sites()` (*tenpy.models.lattice.Square method*), 347
`plot_sites()` (*tenpy.models.lattice.Triangular method*), 355
`plot_sites()` (*tenpy.models.lattice.TrivialLattice method*), 364
`plot_sites()` (*tenpy.models.toric_code.DualSquare method*), 471
`plot_stats()` (*in module tenpy.linalg.lanczos*), 275
`plot_sweep_stats()` (*tenpy.algorithms.dmrq.EngineCombine method*), 154
`plot_sweep_stats()` (*tenpy.algorithms.dmrq.EngineFracture method*), 161
`plot_update_stats()` (*tenpy.algorithms.dmrq.EngineCombine method*), 154
`plot_update_stats()` (*tenpy.algorithms.dmrq.EngineFracture method*), 162
`position()` (*tenpy.models.lattice.Chain method*), 283
`position()` (*tenpy.models.lattice.Honeycomb method*), 292
`position()` (*tenpy.models.lattice.IrregularLattice method*), 302
`position()` (*tenpy.models.lattice.Kagome method*), 310
`position()` (*tenpy.models.lattice.Ladder method*), 319
`position()` (*tenpy.models.lattice.Lattice method*), 326
`position()` (*tenpy.models.lattice.SimpleLattice method*), 338
`position()` (*tenpy.models.lattice.Square method*), 347
`position()` (*tenpy.models.lattice.Triangular method*), 355
`position()` (*tenpy.models.lattice.TrivialLattice method*), 364
`position()` (*tenpy.models.toric_code.DualSquare method*), 471
`possible_charge_sectors` (*tenpy.linalg.sparse.FlatLinearOperator attribute*), 263
`possible_couplings()` (*tenpy.models.lattice.Chain method*), 283
`possible_couplings()` (*tenpy.models.lattice.Honeycomb method*), 292
`possible_couplings()` (*tenpy.models.lattice.IrregularLattice method*), 302
`possible_couplings()` (*tenpy.models.lattice.Kagome method*), 311
`possible_couplings()` (*tenpy.models.lattice.Ladder method*), 319
`possible_couplings()` (*tenpy.models.lattice.Lattice method*), 329
`possible_couplings()` (*tenpy.models.lattice.SimpleLattice method*), 338

`possible_couplings()` (*tenpy.models.lattice.Square* method), 347
`possible_couplings()` (*tenpy.models.lattice.Triangular* method), 355
`possible_couplings()` (*tenpy.models.lattice.TrivialLattice* method), 364
`possible_couplings()` (*tenpy.models.toric_code.DualSquare* method), 472
`possible_multi_couplings()` (*tenpy.models.lattice.Chain* method), 283
`possible_multi_couplings()` (*tenpy.models.lattice.Honeycomb* method), 293
`possible_multi_couplings()` (*tenpy.models.lattice.IrregularLattice* method), 302
`possible_multi_couplings()` (*tenpy.models.lattice.Kagome* method), 311
`possible_multi_couplings()` (*tenpy.models.lattice.Ladder* method), 320
`possible_multi_couplings()` (*tenpy.models.lattice.Lattice* method), 330
`possible_multi_couplings()` (*tenpy.models.lattice.SimpleLattice* method), 338
`possible_multi_couplings()` (*tenpy.models.lattice.Square* method), 347
`possible_multi_couplings()` (*tenpy.models.lattice.Triangular* method), 356
`possible_multi_couplings()` (*tenpy.models.lattice.TrivialLattice* method), 364
`possible_multi_couplings()` (*tenpy.models.toric_code.DualSquare* method), 472
`post_update_local()` (*tenpy.algorithms.dmrg.EngineCombine* method), 154
`post_update_local()` (*tenpy.algorithms.dmrg.EngineFracture* method), 162
`post_update_local()` (*tenpy.algorithms.purification.PurificationApplyMPO* method), 177
`prepare_svd()` (*tenpy.algorithms.dmrg.EngineCombine* method), 154
`prepare_svd()` (*tenpy.algorithms.dmrg.EngineFracture* method), 162
`prepare_update()` (*tenpy.algorithms.dmrg.EngineCombine* method), 154
`prepare_update()` (*tenpy.algorithms.dmrg.EngineFracture* method), 162
`prepare_update()` (*tenpy.algorithms.purification.PurificationApplyMPO* method), 177
`project()` (*tenpy.linalg.charges.LegCharge* method), 240
`project()` (*tenpy.linalg.charges.LegPipe* method), 245
`PurificationApplyMPO` (class in *tenpy.algorithms.purification*), 176
`PurificationTEBD` (class in *tenpy.algorithms.purification*), 179
`PurificationTEBD2` (class in *tenpy.algorithms.purification*), 184
`PurificationTwoSiteU` (class in *tenpy.algorithms.purification*), 189
 Python Enhancement Proposals
 PEP 257, 126
 PEP 8, 126

Q

`q_map` (*tenpy.linalg.charges.LegPipe* attribute), 244
`q_map_slices` (*tenpy.linalg.charges.LegPipe* attribute), 244
`qconj` (*tenpy.linalg.charges.LegCharge* attribute), 235
`QCUTOFF` (in module *tenpy.linalg.np_conserved*), 228
`qnumber()` (*tenpy.linalg.charges.ChargeInfo* property), 233
`qr()` (in module *tenpy.linalg.np_conserved*), 224
`qr_li()` (in module *tenpy.tools.math*), 574
`qttotal` (*tenpy.linalg.np_conserved.Array* attribute), 200
`qttotal` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`QTYPE` (in module *tenpy.linalg.charges*), 250
`QTYPE` (in module *tenpy.linalg.np_conserved*), 228

R

`rank` (*tenpy.linalg.np_conserved.Array* attribute), 200
`regular_lattice` (*tenpy.models.lattice.IrregularLattice* attribute), 296
`released` (in module *tenpy.version*), 589
`remove_op()` (*tenpy.networks.site.BosonSite* method), 478
`remove_op()` (*tenpy.networks.site.FermionSite* method), 482
`remove_op()` (*tenpy.networks.site.GroupedSite* method), 487
`remove_op()` (*tenpy.networks.site.Site* method), 491
`remove_op()` (*tenpy.networks.site.SpinHalfFermionSite* method), 497
`remove_op()` (*tenpy.networks.site.SpinHalfSite* method), 501
`remove_op()` (*tenpy.networks.site.SpinSite* method), 505

`remove_zeros()` (*tenpy.networks.terms.CouplingTerms* method), 534
`remove_zeros()` (*tenpy.networks.terms.MultiCouplingTerms* method), 537
`remove_zeros()` (*tenpy.networks.terms.OnsiteTerms* method), 541
`rename_op()` (*tenpy.networks.site.BosonSite* method), 478
`rename_op()` (*tenpy.networks.site.FermionSite* method), 482
`rename_op()` (*tenpy.networks.site.GroupedSite* method), 487
`rename_op()` (*tenpy.networks.site.Site* method), 491
`rename_op()` (*tenpy.networks.site.SpinHalfFermionSite* method), 497
`rename_op()` (*tenpy.networks.site.SpinHalfSite* method), 501
`rename_op()` (*tenpy.networks.site.SpinSite* method), 505
`replace_label()` (*tenpy.linalg.np_conserved.Array* method), 204
`replace_labels()` (*tenpy.linalg.np_conserved.Array* method), 204
`REPR_ARRAY` (in module *tenpy.tools.hdf5_io*), 560
`REPR_BOOL` (in module *tenpy.tools.hdf5_io*), 561
`REPR_COMPLEX` (in module *tenpy.tools.hdf5_io*), 560
`REPR_DICT_GENERAL` (in module *tenpy.tools.hdf5_io*), 561
`REPR_DICT_SIMPLE` (in module *tenpy.tools.hdf5_io*), 561
`REPR_DTYPE` (in module *tenpy.tools.hdf5_io*), 561
`REPR_FLOAT` (in module *tenpy.tools.hdf5_io*), 560
`REPR_FLOAT32` (in module *tenpy.tools.hdf5_io*), 561
`REPR_FLOAT64` (in module *tenpy.tools.hdf5_io*), 561
`REPR_HDF5EXPORTABLE` (in module *tenpy.tools.hdf5_io*), 560
`REPR_IGNORED` (in module *tenpy.tools.hdf5_io*), 561
`REPR_INT` (in module *tenpy.tools.hdf5_io*), 560
`REPR_INT32` (in module *tenpy.tools.hdf5_io*), 561
`REPR_INT64` (in module *tenpy.tools.hdf5_io*), 560
`REPR_LIST` (in module *tenpy.tools.hdf5_io*), 561
`REPR_NONE` (in module *tenpy.tools.hdf5_io*), 561
`REPR_RANGE` (in module *tenpy.tools.hdf5_io*), 561
`REPR_SET` (in module *tenpy.tools.hdf5_io*), 561
`REPR_STR` (in module *tenpy.tools.hdf5_io*), 560
`REPR_TUPLE` (in module *tenpy.tools.hdf5_io*), 561
`reset_stats()` (*tenpy.algorithms.dmrgh.EngineCombine* method), 154
`reset_stats()` (*tenpy.algorithms.dmrgh.EngineFracture* method), 162
`reset_stats()` (*tenpy.algorithms.purification.PurificationApplyMPO* method), 177
`RHeff` (*tenpy.algorithms.mps_common.TwoSiteH* attribute), 144
`rmatmat()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 260
`rmatmat()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 266
`rmatvec()` (*tenpy.linalg.sparse.FlatHermitianOperator* method), 261
`rmatvec()` (*tenpy.linalg.sparse.FlatLinearOperator* method), 266
`Rp` (*tenpy.algorithms.tdvp.H0_mixed* attribute), 171
`Rp` (*tenpy.algorithms.tdvp.H1_mixed* attribute), 172
`Rp` (*tenpy.algorithms.tdvp.H2_mixed* attribute), 173
`rq_li()` (in module *tenpy.tools.math*), 574
`run()` (*tenpy.algorithms.dmrgh.EngineCombine* method), 155
`run()` (*tenpy.algorithms.dmrgh.EngineFracture* method), 162
`run()` (*tenpy.algorithms.purification.PurificationApplyMPO* method), 177
`run()` (*tenpy.algorithms.purification.PurificationTEBD* method), 181
`run()` (*tenpy.algorithms.purification.PurificationTEBD2* method), 185
`run_GS()` (*tenpy.algorithms.purification.PurificationTEBD* method), 181
`run_GS()` (*tenpy.algorithms.purification.PurificationTEBD2* method), 186
`run_imaginary()` (*tenpy.algorithms.purification.PurificationTEBD* method), 179
`run_imaginary()` (*tenpy.algorithms.purification.PurificationTEBD2* method), 186

S

`S` (*tenpy.networks.site.SpinSite* attribute), 503
`save()` (in module *tenpy.tools.hdf5_io*), 558
`save()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 555
`save_dataset()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_dict()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_dict_content()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_dtype()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_hdf5()` (*tenpy.linalg.charges.ChargeInfo* method), 232
`save_hdf5()` (*tenpy.linalg.charges.LegCharge* method), 236
`save_hdf5()` (*tenpy.linalg.charges.LegPipe* method), 245
`save_hdf5()` (*tenpy.linalg.np_conserved.Array* method), 201
`save_hdf5()` (*tenpy.models.fermions_spinless.FermionChain* method), 438

`save_hdf5()` (*tenpy.models.hubbard.BoseHubbardChain* method), 449
`save_hdf5()` (*tenpy.models.hubbard.FermiHubbardChain* method), 459
`save_hdf5()` (*tenpy.models.lattice.Chain* method), 284
`save_hdf5()` (*tenpy.models.lattice.Honeycomb* method), 293
`save_hdf5()` (*tenpy.models.lattice.IrregularLattice* method), 296
`save_hdf5()` (*tenpy.models.lattice.Kagome* method), 311
`save_hdf5()` (*tenpy.models.lattice.Ladder* method), 320
`save_hdf5()` (*tenpy.models.lattice.Lattice* method), 325
`save_hdf5()` (*tenpy.models.lattice.SimpleLattice* method), 339
`save_hdf5()` (*tenpy.models.lattice.Square* method), 348
`save_hdf5()` (*tenpy.models.lattice.Triangular* method), 356
`save_hdf5()` (*tenpy.models.lattice.TrivialLattice* method), 365
`save_hdf5()` (*tenpy.models.model.CouplingModel* method), 376
`save_hdf5()` (*tenpy.models.model.Model* method), 380
`save_hdf5()` (*tenpy.models.model.MPOModel* method), 378
`save_hdf5()` (*tenpy.models.model.MultiCouplingModel* method), 389
`save_hdf5()` (*tenpy.models.model.NearestNeighborModel* method), 393
`save_hdf5()` (*tenpy.models.spins.SpinChain* method), 426
`save_hdf5()` (*tenpy.models.tf_ising.TFChain* method), 404
`save_hdf5()` (*tenpy.models.toric_code.DualSquare* method), 472
`save_hdf5()` (*tenpy.models.xxz_chain.XXZChain2* method), 415
`save_hdf5()` (*tenpy.networks.site.BosonSite* method), 478
`save_hdf5()` (*tenpy.networks.site.FermionSite* method), 482
`save_hdf5()` (*tenpy.networks.site.GroupedSite* method), 487
`save_hdf5()` (*tenpy.networks.site.Site* method), 492
`save_hdf5()` (*tenpy.networks.site.SpinHalfFermionSite* method), 497
`save_hdf5()` (*tenpy.networks.site.SpinHalfSite* method), 501
`save_hdf5()` (*tenpy.networks.site.SpinSite* method), 505
`save_hdf5()` (*tenpy.networks.terms.CouplingTerms* method), 534
`save_hdf5()` (*tenpy.networks.terms.MultiCouplingTerms* method), 539
`save_hdf5()` (*tenpy.networks.terms.OnsiteTerms* method), 541
`save_hdf5()` (*tenpy.networks.terms.TermList* method), 543
`save_hdf5()` (*tenpy.tools.hdf5_io.Hdf5Exportable* method), 549
`save_ignored()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_iterable()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_iterable_content()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_none()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_range()` (*tenpy.tools.hdf5_io.Hdf5Saver* method), 556
`save_to_hdf5()` (in module *tenpy.tools.hdf5_io*), 559
`scale_axis()` (*tenpy.linalg.np_conserved.Array* method), 212
`set_B()` (*tenpy.algorithms.dmrgh.EngineCombine* method), 156
`set_B()` (*tenpy.algorithms.dmrgh.EngineFracture* method), 164
`set_level()` (in module *tenpy.tools.optimization*), 587
`set_LP()` (*tenpy.networks.mpo.MPOEnvironment* method), 524
`set_LP()` (*tenpy.networks.mps.MPSEnvironment* method), 511
`set_RP()` (*tenpy.networks.mpo.MPOEnvironment* method), 524
`set_RP()` (*tenpy.networks.mps.MPSEnvironment* method), 511
`setup_executable()` (in module *tenpy.tools.misc*), 570
`shape` (*tenpy.linalg.np_conserved.Array* attribute), 200
`shape` (*tenpy.linalg.sparse.FlatLinearOperator* attribute), 263
`shape` (*tenpy.models.lattice.Lattice* attribute), 323
`shift_bra` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`shift_ket` (*tenpy.networks.mps.TransferMatrix* attribute), 515
`ShiftNpcLinearOperator` (class in *tenpy.linalg.sparse*), 271
`short_version` (in module *tenpy.version*), 589
`show_config()` (in module *tenpy*), 131
`SimpleLattice` (class in *tenpy.models.lattice*), 333

SingleSiteMixer (class in *tenpy.algorithms.dmr*), 165
 Site (class in *tenpy.networks.site*), 489
 site() (*tenpy.models.lattice.Chain* method), 284
 site() (*tenpy.models.lattice.Honeycomb* method), 293
 site() (*tenpy.models.lattice.IrregularLattice* method), 302
 site() (*tenpy.models.lattice.Kagome* method), 311
 site() (*tenpy.models.lattice.Ladder* method), 320
 site() (*tenpy.models.lattice.Lattice* method), 326
 site() (*tenpy.models.lattice.SimpleLattice* method), 339
 site() (*tenpy.models.lattice.Square* method), 348
 site() (*tenpy.models.lattice.Triangular* method), 356
 site() (*tenpy.models.lattice.TrivialLattice* method), 365
 site() (*tenpy.models.toric_code.DualSquare* method), 472
 sites (*tenpy.networks.mpo.MPOGraph* attribute), 526
 sites (*tenpy.networks.site.GroupedSite* attribute), 485
 size() (*tenpy.linalg.np_conserved.Array* property), 203
 slices (*tenpy.linalg.charges.LegCharge* attribute), 235
 sort() (*tenpy.linalg.charges.LegCharge* method), 240
 sort() (*tenpy.linalg.charges.LegPipe* method), 245
 sort_legcharge() (*tenpy.linalg.np_conserved.Array* method), 207
 sorted (*tenpy.linalg.charges.LegCharge* attribute), 235
 sparse_diag() (*tenpy.algorithms.exact_diag.ExactDiag* method), 195
 sparse_stats() (*tenpy.linalg.np_conserved.Array* method), 205
 speigs() (in module *tenpy.linalg.np_conserved*), 225
 speigs() (in module *tenpy.tools.math*), 575
 speigsh() (in module *tenpy.tools.math*), 575
 SpinChain (class in *tenpy.models.spins*), 418
 SpinHalfFermionSite (class in *tenpy.networks.site*), 494
 SpinHalfSite (class in *tenpy.networks.site*), 499
 SpinSite (class in *tenpy.networks.site*), 503
 split_legs() (*tenpy.linalg.np_conserved.Array* method), 209
 Square (class in *tenpy.models.lattice*), 341
 squeeze() (*tenpy.linalg.np_conserved.Array* method), 210
 standard_normal_complex() (in module *tenpy.linalg.random_matrix*), 255
 state_index() (*tenpy.networks.site.BosonSite* method), 478
 state_index() (*tenpy.networks.site.FermionSite* method), 483
 state_index() (*tenpy.networks.site.GroupedSite* method), 487
 state_index() (*tenpy.networks.site.Site* method), 491
 state_index() (*tenpy.networks.site.SpinHalfFermionSite* method), 497
 state_index() (*tenpy.networks.site.SpinHalfSite* method), 501
 state_index() (*tenpy.networks.site.SpinSite* method), 505
 state_indices() (*tenpy.networks.site.BosonSite* method), 478
 state_indices() (*tenpy.networks.site.FermionSite* method), 483
 state_indices() (*tenpy.networks.site.GroupedSite* method), 487
 state_indices() (*tenpy.networks.site.Site* method), 491
 state_indices() (*tenpy.networks.site.SpinHalfFermionSite* method), 497
 state_indices() (*tenpy.networks.site.SpinHalfSite* method), 501
 state_indices() (*tenpy.networks.site.SpinSite* method), 505
 state_labels (*tenpy.networks.site.Site* attribute), 489
 states (*tenpy.networks.mpo.MPOGraph* attribute), 526
 stored_blocks() (*tenpy.linalg.np_conserved.Array* property), 203
 strengths (*tenpy.networks.terms.TermList* attribute), 543
 subqshape (*tenpy.linalg.charges.LegPipe* attribute), 244
 subshape (*tenpy.linalg.charges.LegPipe* attribute), 243
 subspace_expand() (*tenpy.algorithms.dmr.SingleSiteMixer* method), 166
 subspace_expand() (*tenpy.algorithms.dmr.TwoSiteMixer* method), 168
 sum_of_exp() (in module *tenpy.tools.fit*), 579
 SumNpcLinearOperator (class in *tenpy.linalg.sparse*), 272
 suzuki_trotter_decomposition() (*tenpy.algorithms.purification.PurificationTEBD* static method), 181
 suzuki_trotter_decomposition() (*tenpy.algorithms.purification.PurificationTEBD2* static method), 186
 suzuki_trotter_time_steps() (*tenpy.algorithms.purification.PurificationTEBD* static method), 182
 suzuki_trotter_time_steps() (*tenpy.algorithms.purification.PurificationTEBD2* static method), 186
 svd() (in module *tenpy.linalg.np_conserved*), 225
 svd() (in module *tenpy.linalg.svd_robust*), 251
 svd_gesvd() (in module *tenpy.linalg.svd_robust*), 251

`svd_theta()` (in module `tenpy.algorithms.truncation`), 135

`sweep()` (`tenpy.algorithms.dmrq.EngineCombine` method), 156

`sweep()` (`tenpy.algorithms.dmrq.EngineFracture` method), 164

`sweep()` (`tenpy.algorithms.purification.PurificationApplyMPO` method), 177

T

`T()` (`tenpy.linalg.sparse.FlatHermitianOperator` property), 258

`T()` (`tenpy.linalg.sparse.FlatLinearOperator` property), 265

`take_slice()` (`tenpy.linalg.np_conserved.Array` method), 205

`temporary_level` (class in `tenpy.tools.optimization`), 585

`temporary_level` (`tenpy.tools.optimization.temporary_level` attribute), 585

`tenpy`
module, 131

`tenpy.algorithms`
module, 132

`tenpy.algorithms.dmrq`
module, 170

`tenpy.algorithms.exact_diag`
module, 196

`tenpy.algorithms.mpo_evolution`
module, 190

`tenpy.algorithms.mps_common`
module, 145

`tenpy.algorithms.network_contractor`
module, 192

`tenpy.algorithms.purification`
module, 189

`tenpy.algorithms.tdvp`
module, 174

`tenpy.algorithms.tebd`
module, 137

`tenpy.algorithms.truncation`
module, 136

`tenpy.linalg`
module, 196

`tenpy.linalg.charges`
module, 250

`tenpy.linalg.lanczos`
module, 275

`tenpy.linalg.np_conserved`
module, 227

`tenpy.linalg.random_matrix`
module, 255

`tenpy.linalg.sparse`
module, 273

`tenpy.linalg.svd_robust`
module, 252

`tenpy.models`
module, 275

`tenpy.models.fermions_spinless`
module, 439

`tenpy.models.haldane`
module, 463

`tenpy.models.hofstadter`
module, 462

`tenpy.models.hubbard`
module, 460

`tenpy.models.lattice`
module, 367

`tenpy.models.model`
module, 393

`tenpy.models.spins`
module, 427

`tenpy.models.spins_nnn`
module, 428

`tenpy.models.tf_ising`
module, 405

`tenpy.models.toric_code`
module, 473

`tenpy.models.xx_z_chain`
module, 416

`tenpy.networks`
module, 473

`tenpy.networks.mpo`
module, 530

`tenpy.networks.mps`
module, 518

`tenpy.networks.purification_mps`
module, 545

`tenpy.networks.site`
module, 507

`tenpy.networks.terms`
module, 544

`tenpy.tools`
module, 547

`tenpy.tools.fit`
module, 579

`tenpy.tools.hdf5_io`
module, 560

`tenpy.tools.math`
module, 576

`tenpy.tools.misc`
module, 572

`tenpy.tools.optimization`
module, 588

`tenpy.tools.params`
module, 565

`tenpy.tools.process`
module, 583

```

tenpy.tools.string
    module, 580
tenpy.version
    module, 589
tensordot() (in module tenpy.linalg.np_conserved),
    226
TermList (class in tenpy.networks.terms), 542
terms (tenpy.networks.terms.TermList attribute), 543
test_contractible()
    (tenpy.linalg.charges.LegCharge method),
    238
test_contractible()
    (tenpy.linalg.charges.LegPipe method), 249
test_equal() (tenpy.linalg.charges.LegCharge
    method), 239
test_equal() (tenpy.linalg.charges.LegPipe
    method), 249
test_sanity() (tenpy.linalg.charges.ChargeInfo
    method), 233
test_sanity() (tenpy.linalg.charges.LegCharge
    method), 238
test_sanity() (tenpy.linalg.charges.LegPipe
    method), 245
test_sanity() (tenpy.linalg.np_conserved.Array
    method), 200
test_sanity() (tenpy.models.fermions_spinless.FermionChain
    method), 438
test_sanity() (tenpy.models.hubbard.BoseHubbardChain
    method), 450
test_sanity() (tenpy.models.hubbard.FermiHubbardChain
    method), 460
test_sanity() (tenpy.models.lattice.Chain method),
    284
test_sanity() (tenpy.models.lattice.Honeycomb
    method), 293
test_sanity() (tenpy.models.lattice.IrregularLattice
    method), 303
test_sanity() (tenpy.models.lattice.Kagome
    method), 312
test_sanity() (tenpy.models.lattice.Ladder
    method), 320
test_sanity() (tenpy.models.lattice.Lattice
    method), 324
test_sanity() (tenpy.models.lattice.SimpleLattice
    method), 339
test_sanity() (tenpy.models.lattice.Square
    method), 348
test_sanity() (tenpy.models.lattice.Triangular
    method), 356
test_sanity() (tenpy.models.lattice.TrivialLattice
    method), 365
test_sanity() (tenpy.models.model.CouplingModel
    method), 370
test_sanity() (tenpy.models.model.MultiCouplingModel
    method), 389
test_sanity() (tenpy.models.spins.SpinChain
    method), 426
test_sanity() (tenpy.models.tf_ising.TFICChain
    method), 404
test_sanity() (tenpy.models.toric_code.DualSquare
    method), 473
test_sanity() (tenpy.models.xxz_chain.XXZChain2
    method), 415
test_sanity() (tenpy.networks.mpo.MPOEnvironment
    method), 521
test_sanity() (tenpy.networks.mpo.MPOGraph
    method), 527
test_sanity() (tenpy.networks.mps.MPSEnvironment
    method), 510
test_sanity() (tenpy.networks.site.BosonSite
    method), 478
test_sanity() (tenpy.networks.site.FermionSite
    method), 483
test_sanity() (tenpy.networks.site.GroupedSite
    method), 487
test_sanity() (tenpy.networks.site.Site method),
    490
test_sanity() (tenpy.networks.site.SpinHalfFermionSite
    method), 497
test_sanity() (tenpy.networks.site.SpinHalfSite
    method), 501
test_sanity() (tenpy.networks.site.SpinSite
    method), 505
TFICChain (class in tenpy.models.tf_ising), 396
to_array() (in module tenpy.tools.misc), 570
to_Arrays() (tenpy.networks.terms.OnsiteTerms
    method), 540
to_iterable() (in module tenpy.tools.misc), 571
to_iterable_arrays() (in module
    tenpy.linalg.np_conserved), 227
to_iterable_of_len() (in module
    tenpy.tools.misc), 571
to_LegCharge() (tenpy.linalg.charges.LegPipe
    method), 245
to_mathematica_lists() (in module
    tenpy.tools.string), 580
to_matrix() (tenpy.algorithms.mps_common.EffectiveH
    method), 140
to_matrix() (tenpy.algorithms.mps_common.OneSiteH
    method), 143
to_matrix() (tenpy.algorithms.mps_common.TwoSiteH
    method), 145
to_matrix() (tenpy.algorithms.purification.PurificationTwoSiteU
    method), 189
to_matrix() (tenpy.linalg.sparse.NpcLinearOperator
    method), 268
to_matrix() (tenpy.linalg.sparse.NpcLinearOperatorWrapper
    method), 269

```

`to_matrix()` (*tenpy.linalg.sparse.OrthogonalNpcLinearOperator* `method`), 270
`to_matrix()` (*tenpy.linalg.sparse.ShiftNpcLinearOperator* `method`), 271
`to_matrix()` (*tenpy.linalg.sparse.SumNpcLinearOperator* `method`), 272
`to_matrix()` (*tenpy.networks.mps.TransferMatrix* `method`), 516
`to_ndarray()` (*tenpy.linalg.np_conserved.Array* `method`), 205
`to_nn_bond_Arrays()` (*tenpy.networks.terms.CouplingTerms* `method`), 533
`to_nn_bond_Arrays()` (*tenpy.networks.terms.MultiCouplingTerms* `method`), 539
`to_OnsiteTerms_CouplingTerms()` (*tenpy.networks.terms.TermList* `method`), 543
`to_OptimizationFlag()` (*in module tenpy.tools.optimization*), 587
`to_qdict()` (*tenpy.linalg.charges.LegCharge* `method`), 238
`to_qdict()` (*tenpy.linalg.charges.LegPipe* `method`), 250
`to_qflat()` (*tenpy.linalg.charges.LegCharge* `method`), 238
`to_qflat()` (*tenpy.linalg.charges.LegPipe* `method`), 250
`to_TermList()` (*tenpy.networks.terms.CouplingTerms* `method`), 534
`to_TermList()` (*tenpy.networks.terms.MultiCouplingTerms* `method`), 537
`to_TermList()` (*tenpy.networks.terms.OnsiteTerms* `method`), 541
`trace()` (*in module tenpy.linalg.np_conserved*), 227
`TransferMatrix` (*class in tenpy.networks.mps*), 514
`transpose` (*tenpy.networks.mps.TransferMatrix* `attribute`), 515
`transpose()` (*tenpy.linalg.np_conserved.Array* `method`), 211
`transpose()` (*tenpy.linalg.sparse.FlatHermitianOperator* `method`), 261
`transpose()` (*tenpy.linalg.sparse.FlatLinearOperator* `method`), 267
`transpose_list_list()` (*in module tenpy.tools.misc*), 571
`Triangular` (*class in tenpy.models.lattice*), 350
`trivial_like_NNModel()` (*tenpy.models.fermions_spinless.FermionChain* `method`), 438
`trivial_like_NNModel()` (*tenpy.models.hubbard.BoseHubbardChain* `method`), 450
`trivial_like_NNModel()` (*tenpy.models.hubbard.FermiHubbardChain* `method`), 460
`trivial_like_NNModel()` (*tenpy.models.model.NearestNeighborModel* `method`), 392
`trivial_like_NNModel()` (*tenpy.models.spins.SpinChain* `method`), 426
`trivial_like_NNModel()` (*tenpy.models.tf_ising.TFChain* `method`), 404
`trivial_like_NNModel()` (*tenpy.models.xxz_chain.XXZChain2* `method`), 415
`TrivialLattice` (*class in tenpy.models.lattice*), 358
`trunc_err_bonds()` (*tenpy.algorithms.purification.PurificationTEBD* `property`), 182
`trunc_err_bonds()` (*tenpy.algorithms.purification.PurificationTEBD2* `property`), 187
`TruncationError` (*class in tenpy.algorithms.truncation*), 134
`TwoSiteH` (*class in tenpy.algorithms.mps_common*), 144
`TwoSiteMixer` (*class in tenpy.algorithms.dmrg*), 167
`TYPES_FOR_HDF5_DATASETS` (*in module tenpy.tools.hdf5_io*), 561

U

`un_close_1()` (*in module tenpy.linalg.random_matrix*), 255
`unary_blockwise()` (*tenpy.linalg.np_conserved.Array* `method`), 212
`unit_cell` (*tenpy.models.lattice.Lattice* `attribute`), 323
`unit_cell_positions` (*tenpy.models.lattice.Lattice* `attribute`), 324
`unused_parameters()` (*in module tenpy.tools.params*), 564
`unwrapped()` (*tenpy.linalg.sparse.NpcLinearOperatorWrapper* `method`), 269
`unwrapped()` (*tenpy.linalg.sparse.OrthogonalNpcLinearOperator* `method`), 270
`unwrapped()` (*tenpy.linalg.sparse.ShiftNpcLinearOperator* `method`), 271
`unwrapped()` (*tenpy.linalg.sparse.SumNpcLinearOperator* `method`), 272
`update()` (*tenpy.algorithms.purification.PurificationTEBD* `method`), 182
`update()` (*tenpy.algorithms.purification.PurificationTEBD2* `method`), 184
`update_amplitude()`

(*tenpy.algorithms.dmrp.DensityMatrixMixer*
method), 149
 update_amplitude() (*tenpy.algorithms.dmrp.SingleSiteMixer*
method), 166
 update_amplitude() (*tenpy.algorithms.dmrp.TwoSiteMixer* *method*),
 168
 update_bond() (*tenpy.algorithms.purification.PurificationTEBD*
method), 179
 update_bond() (*tenpy.algorithms.purification.PurificationTEBD2*
method), 187
 update_bond_imag() (*tenpy.algorithms.purification.PurificationTEBD*
method), 180
 update_bond_imag() (*tenpy.algorithms.purification.PurificationTEBD2*
method), 187
 update_imag() (*tenpy.algorithms.purification.PurificationTEBD*
method), 182
 update_imag() (*tenpy.algorithms.purification.PurificationTEBD2*
method), 187
 update_local() (*tenpy.algorithms.dmrp.EngineCombine*
method), 157
 update_local() (*tenpy.algorithms.dmrp.EngineFracture*
method), 164
 update_local() (*tenpy.algorithms.purification.PurificationTEBD*
method), 176
 update_LP() (*tenpy.algorithms.dmrp.EngineCombine*
method), 156
 update_LP() (*tenpy.algorithms.dmrp.EngineFracture*
method), 164
 update_RP() (*tenpy.algorithms.dmrp.EngineCombine*
method), 156
 update_RP() (*tenpy.algorithms.dmrp.EngineFracture*
method), 164
 update_step() (*tenpy.algorithms.purification.PurificationTEBD*
method), 182
 update_step() (*tenpy.algorithms.purification.PurificationTEBD2*
method), 184
 use_cython() (*in module tenpy.tools.optimization*),
 587
 used_disentangler
 (*tenpy.algorithms.purification.PurificationTEBD*
attribute), 179

V

V (*tenpy.algorithms.exact_diag.ExactDiag* *attribute*), 194
 valid_hdf5_path_component() (*in module*
tenpy.tools.hdf5_io), 559
 valid_opname() (*tenpy.networks.site.BosonSite*
method), 479
 valid_opname() (*tenpy.networks.site.FermionSite*
method), 483
 valid_opname() (*tenpy.networks.site.GroupedSite*
method), 487
 valid_opname() (*tenpy.networks.site.Site* *method*),
 492
 valid_opname() (*tenpy.networks.site.SpinHalfFermionSite*
method), 497
 valid_opname() (*tenpy.networks.site.SpinHalfSite*
method), 501
 valid_opname() (*tenpy.networks.site.SpinSite*
method), 505
 valid_opname() (*tenpy.linalg.sparse.FlatLinearOperator*
attribute), 263
 version (*in module tenpy.version*), 589
 version_summary (*in module tenpy.version*), 589
 vert_join() (*in module tenpy.tools.string*), 580

W

W (*tenpy.algorithms.tdvp.H1_mixed* *attribute*), 172
 W0 (*tenpy.algorithms.tdvp.H2_mixed* *attribute*), 173
 W1 (*tenpy.algorithms.tdvp.H2_mixed* *attribute*), 173

X

XXZChain2 (*class in tenpy.models.xxz_chain*), 407

Z

zero_if_close() (*in module tenpy.tools.misc*), 571
 zeros() (*in module tenpy.linalg.np_conserved*), 227
 zeros_like() (*tenpy.linalg.np_conserved.Array*
method), 203